



MADE EASY

India's Best Institute for IES, GATE & PSUs

GATE 2021

ELECTRICAL ENGINEERING

Questions & Solutions

Exam held on 07/02/2021



Scroll
down
to view

MADE EASY Delhi : 44-A/1, Kalu Sarai, New Delhi - 110016 | **Ph :** 011-45124612, 9958995830
• Delhi • Hyderabad • Noida • Bhopal • Jaipur • Lucknow • Indore • Pune • Bhubaneswar • Kolkata • Patna

www.madeeasy.in

If you find any discrepancy in question or solution, kindly write us at : info@madeeasy.in mentioning stream, date of exam and session.

SECTION - A

GENERAL APTITUDE

Q.1 Seven cars P, Q, R, S, T, U and V are parked in a row not necessarily in that order. The cars T and U should be parked next to each other. The cars S and V also should be parked next to each other, whereas P and Q cannot be parked next to each other. Q and S must be parked next to each other. R is parked to the immediate right of V. T is parked to the left of U.

Based on the above statements, the only INCORRECT option given below is:

- (a) There are two cars parked in between Q and V.
- (b) Q and R are not parked together.
- (c) V is the only car parked in between S and R
- (d) Car P is parked at the extreme end.

Ans. (a)

\therefore S and V must be parked together and Q and S also must be parked together.

These two condition possible parkings are:

Q S V – – –

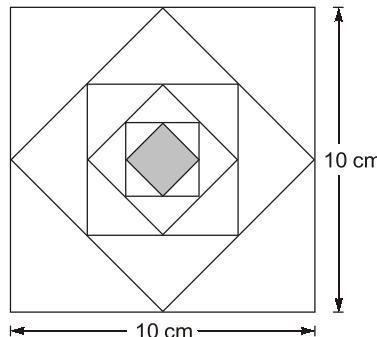
V S Q – – –

We can observe that in all cases only one car can be parked in between Q and V which is car S.

Hence option (a) is incorrect.

End of Solution

Q.2



In the figure shown above, each inside square is formed by joining the midpoints of the sides of the next larger square. The area of the smallest square (Shaded) as shown, in cm^2 is

- | | |
|------------|-----------|
| (a) 3.125 | (b) 12.50 |
| (c) 1.5625 | (d) 6.25 |

Ans. (a)

Side of outer first square = 10 cm

Side of outer second square = $\frac{10}{\sqrt{2}}$ cm

like wise,

$$\text{Side of outer third square} = \left(\frac{10}{(\sqrt{2})^2} \right)$$

Hence,

$$\text{side of smallest square} = \frac{10}{(\sqrt{2})^5}$$

$$\text{Area of smallest square} = \left(\frac{10}{(\sqrt{2})^5} \right)^2 = \frac{100}{2^5} = 3.125$$

End of Solution

Q.3 Which one of the following numbers is exactly divisible by $(11^{13} + 1)$?

- | | |
|-------------------|-------------------|
| (a) $11^{33} + 1$ | (b) $11^{52} - 1$ |
| (c) $11^{26} + 1$ | (d) $11^{39} + 1$ |

Ans. (b)

Consider expression $\frac{x^n - a^n}{x + a}$.

Now assuming similar expression $11^{52} - 1 = (11^{13})^4 - (1)^4$

$$\begin{aligned} \frac{(11^{13})^4 - (1)^4}{11^3 + 1} &= \frac{((11^{13})^2 - (1)^2)((11^{13})^2 + (1)^2)}{11^3 + 1} \\ &= [(11^{13} - 1)][(11^{13})^2 + (1)^2] \end{aligned}$$

Hence, $11^{52} - 1$ is divisible by $11^{13} + 1$.

End of Solution

Q.4 The people _____ were at the demonstration were from all section of society.

- | | |
|-----------|-----------|
| (a) whose | (b) who |
| (c) whom | (d) which |

Ans. (b)

We cannot use 'which' for people, 'who' is the only word which acts as a subject for the verb.

End of Solution

Q.5 Let X be a continuous random variable denoting the temperature measured. The range of temperature is $(0, 100)$ degree Celsius and let the probability density function of X be $f(x) = 0.01$ for $0 \leq X \leq 100$. The mean of X is _____ .

- | | |
|----------|----------|
| (a) 5.0 | (b) 50.0 |
| (c) 25.0 | (d) 2.5 |

Ans. (b)

n is a continuous random variable for continuous random variable

$$\therefore f(x) = \begin{cases} \frac{1}{\beta - \alpha} & \alpha \leq x \leq \beta \\ 0 & \text{otherwise} \end{cases}$$

From here, $\alpha = 0, \beta = 100$

For continuous probability function mean

$$= \frac{\alpha + \beta}{2} = \frac{0 + 100}{2} = 50$$

Alternate Solution:

Given: pdf $f(x) = 10^{-2}, 0 < x < 100$

$$\begin{aligned} E(x) &= \int_0^{100} xf(x)dx = \int_0^{100} x10^{-2}dx \\ &= \left[\frac{1}{100} \frac{x^2}{2} \right]_0^{100} = \frac{100}{2} = 50 \end{aligned}$$

End of Solution

Q.6 For a regular polygon having 10 sides, the interior angle between the sides of the polygon, in degrees, is :

- | | |
|---------|---------|
| (a) 396 | (b) 144 |
| (c) 324 | (d) 216 |

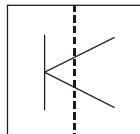
Ans. (b)

Sum of the interior angle = $(n - 2) \times 180 = 1440$

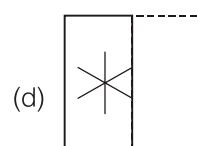
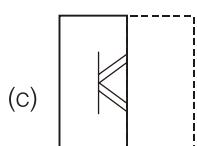
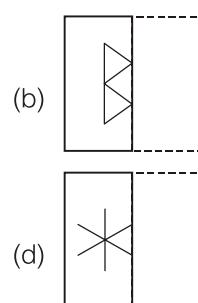
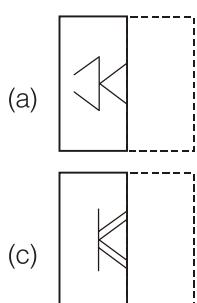
The interior angle between two sides of polygon is $\frac{1440}{10} = 144$.

End of Solution

Q.7

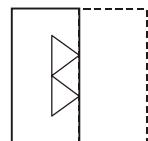


A transparent square sheet above is folded along the dotted line. The folded sheet will look like _____.



Ans. (b)

Upon rotation, we get the below figure.

**End of Solution**

- Q.8** The importance of sleep is often overlooked by students when they are preparing for exams. Research has consistently shown that sleep deprivation greatly reduces the ability to recall the material learned. Hence, cutting down on sleep to study longer hours can be counterproductive.

Which one of the following statements is the CORRECT inference from the above passage?

- (a) Sleeping well alone is enough to prepare for an exam. Studying has lesser benefit.
- (b) To do well in an exam, adequate sleep must be part of the preparation.
- (c) Students are efficient and are not wrong in thinking that sleep is a waste of time.
- (d) If a student is extremely well prepared for an exam, he needs little or no sleep.

Ans. (b)

First statement is ridiculous, third and fourth are contradictory to what is given in the passage.

End of Solution

- Q.9** Oasis is to sand as island is to _____ .

Which one of the following options maintains a similar logical relation in the above sentence?

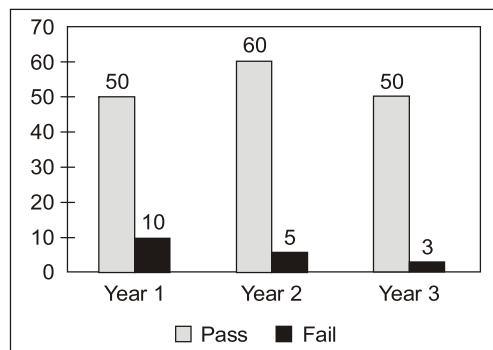
- | | |
|--------------|-----------|
| (a) Mountain | (b) Water |
| (c) Land | (d) Stone |

Ans. (b)

Oasis is surrounded by sand as Island is surrounded by water.

End of Solution

- Q.10**



The number of students passing or failing in an exam for a particular subject is presented in the bar chart above. Students who pass the exam cannot appear for the exam again. Students who fail the exam in the first attempt must appear for the exam in the following year. Students always pass the exam in their second attempt.

The number of students who took the exam for the first time in the year 2 and the year 3 respectively, are _____ .

Ans. (d)

Total number of student in the year-2

$$= 60 + 5 = 65$$

Students who failed in the year and appeared in year-2 = 10

So the students who appeared first time in year-2 = $65 - 10 = 55$

Similarly, Total number of students in year-3 = 53

Students who failed in the year-2 and appeared in year-3 = 5

So, the students who appeared first time in year-3

$$= 53 - 5 = 48$$

End of Solution





MADE EASY

India's Best Institute for IES, GATE & PSUs*

Under the leadership of
Mr. B. Singh
Chairman & Managing Director



- Well Planned Curriculum
- Systematic Subject Sequence
- Comprehensive Study Materials

ADMISSION OPEN

**ESE + GATE
2022**

**GATE
2022**

- ✓ Classes by India's highly proficient and experienced top faculties.
- ✓ Similar teaching pedagogy in online and offline courses.
- ✓ Concept practice through workbooks and updated theory books.
- ✓ Thoroughly revised, updated study materials as per latest exam pattern.
- ✓ Systematic subject sequence and time bound completion of syllabus.
- ✓ Assessment of performance through subject-wise tests.
- ✓ Professionally managed, interactive classrooms and well equipped infrastructure.

LIVE CLASSES at MADE EASY Prime

Medium : Hindi + English

Morning Batch from 18th Feb, 2021
Time: 8.30 AM - 11.30 AM

Medium : English

Evening Batch from 25th Feb, 2021
Time: 5.30 PM - 8.30 PM

Scan to download app



android



iOS

8851176822, 9958995830
www.madeeasyprime.com

OFFLINE CLASSES

Regular Batches

First Batch
from 22nd Feb, 2021

Second Batch
from 1st Mar, 2021

Third Batch
from 18th Mar, 2021

Weekend Batches

Commencing
from 21st Feb, 2021

MADE EASY Delhi

011-45124612, 9958995830
www.madeeasy.in

**Easy EMI
options available**

Avail 10 % Discount till 28th Feb, 2021
on ESE & GATE long term Online/Offline Courses

COVID 19 Security Features

- Spacious classrooms that enable social distancing.
- Institute is fully sanitized and hygienic.

Corporate Office: 44-A/1, Kalu Sarai, Sarvapriya Vihar, Near Hauz Khas Metro Station, New Delhi-110016

MADE EASY Centres: Delhi | Hyderabad | Noida | Jaipur | Lucknow | Bhopal | Bhubaneswar | Pune | Indore | Patna | Kolkata

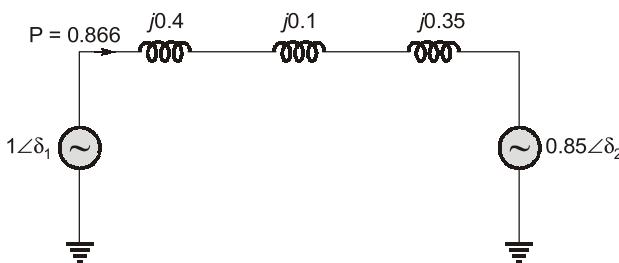
Admission open at all MADE EASY centres • For details, visit: www.madeeasy.in

SECTION - B
TECHNICAL

- Q.1** An alternator with internal voltage of $1\angle\delta_1$ p.u. and synchronous reactance of 0.4 p.u. is connected by a transmission line of reactance 0.1 p.u. to a synchronous motor having synchronous reactance 0.35 p.u. and internal voltage of $0.85\angle\delta_2$ p.u. If the real power supplied by the alternator is 0.866 p.u., then $(\delta_1 - \delta_2)$ is _____ degrees. (Round off to 2 decimal places)

(Machines are of non-salient type. Neglect resistances)

Ans. 60 (59.50 to 60.50)



Given real power in (p.u.), $P = 0.866$

$$P = \frac{EV \sin(\delta_1 - \delta_2)}{X_{eq}} = \left| \frac{1 \times 0.85}{0.4 + 0.1 + 0.35} \right| \sin(\delta_1 - \delta_2)$$

$$(\delta_1 - \delta_2) = 60^\circ$$

End of Solution

- Q.2** Let $f(t)$ be an even function, i.e. $f(-t) = f(t)$ for all t . Let the Fourier transform of $f(t)$ be

defined as $F(\omega) = \int_{-\infty}^{\infty} f(t)e^{-j\omega t} dt$. Suppose $\frac{dF(\omega)}{d\omega} = -\omega F(\omega)$ for all ω , and $F(0) = 1$. Then

- | | |
|----------------|----------------|
| (a) $f(0) = 0$ | (b) $f(0) = 1$ |
| (c) $f(0) > 1$ | (d) $f(0) < 1$ |

Ans. (d)

$$f(t) \rightleftharpoons F(\omega) = \int_{-\infty}^{\infty} f(t)e^{-j\omega t} dt$$

The following informations are given about $f(t) \rightleftharpoons F(\omega)$.

- (i) $f(t) = f(-t)$
- (ii) $F(\omega)|_{\omega=0} = 1$
- (iii) $\frac{dF(\omega)}{d\omega} = -\omega F(\omega)$

$$\text{From (iii), } \frac{dF(\omega)}{d\omega} + \omega F(\omega) = 0$$

By solving the above linear differential equations, (by mathematics)

$$\ln F(\omega) = -\frac{\omega^2}{2}$$

$$\Rightarrow F(\omega) = K \cdot e^{-\omega^2/2} \quad (\text{iv})$$

$$\text{Put } \omega = 0, \quad F(0) = K$$

$$\Rightarrow 1 = K \text{ (from info. (ii))}$$

$$\text{From (iv), } F(\omega) = e^{-\omega^2/2}$$

$$\text{As we know, } e^{-at^2}, a > 0 \Rightarrow \sqrt{\frac{\pi}{a}} e^{-\omega^2/4a}$$

$$\text{At } a = \frac{1}{2}, \quad e^{-t^2/2} \Rightarrow \sqrt{\frac{\pi}{1/2}} \cdot e^{-\omega^2/2}$$

$$f(t) = \frac{1}{\sqrt{2\pi}} e^{-t^2/2} \Rightarrow e^{-\omega^2/2} = F(\omega)$$

$$\text{Thus, } f(t) = \frac{1}{\sqrt{2\pi}} e^{-t^2/2}$$

$$\text{At } t = 0, \quad f(0) = \frac{1}{\sqrt{2\pi}} < 1$$

End of Solution

- Q.3** Suppose the circle $x^2 + y^2 = 1$ and $(x-1)^2 + (y-1)^2 = r^2$ intersect each other orthogonally at the point (u, v) . Then $u + v = \underline{\hspace{2cm}}$.

Ans. (1)

If two curves cut orthogonally then product of slopes = -1

$$x^2 + y^2 = 1$$

$$2x + 2y \frac{dy}{dx} = 0$$

$$(M_1)_{u,v} = \frac{dy}{dx} = \frac{-x}{y} = \frac{-u}{v}$$

$$(x-1)^2 + (y-1)^2 = r^2$$

$$(M_2)_{u,v} = \left(\frac{dy}{dx} \right) = \left(\frac{-2(x-1)}{2(y-1)} \right)_{(u,v)} = \frac{1-u}{v-1}$$

$$\therefore M_1 M_2 = -1$$

$$\frac{-u}{v} \times \frac{1-u}{v-1} = -1$$

$$-u + u^2 = -v^2 + v$$

$$u^2 + v^2 = v + u$$

$$x^2 + y^2 = 1$$

$$\therefore u + v = 1$$

End of Solution

- Q.4** A 1 μC point charge is held at the origin of a Cartesian coordinate system. If a second point charge of 10 μC is moved from (0, 10, 0) to (5, 5, 5) and subsequently to (5, 0, 0), then the total work done is _____ mJ. (Round off to 2 decimal places.)

Take $\frac{1}{4\pi\epsilon_0} = 9 \times 10^9$ in SI units. All coordinates are in meters.

Ans. 9.00 (8.80 to 9.20)

$$Q = 1 \mu\text{C} \quad P(r, \theta, \phi) \quad \vec{E} = \frac{Q}{4\pi \epsilon_0 r^2} \hat{a}_r = \frac{10^{-6}(9 \times 10^9)}{r^2} \hat{a}_r = \frac{9 \times 10^3}{r^2} \hat{a}_r$$

In this case work done is independent of type of path but depends on initial and final point.

x	y	z	r	θ	ϕ		
(0,	10,	0)	\rightarrow	(10,	90°,	90°)	
x	y	z	r	θ	ϕ	Initial point	
(5,	5,	5)	\rightarrow	($5\sqrt{3}$,	54.73°,	45°)	Intermediate point
x	y	z	r	θ	ϕ		
(5,	0,	0)	\rightarrow	(5,	90°,	0°)	Final point

Work done (by external source) in moving Q-charge (10 μC) in the presence of electric field \vec{E} is

$$W = -Q \int_{\text{initial point}}^{\text{final point}} \vec{E} \cdot d\vec{l} = -(10 \times 10^{-6}) \int_{r=10}^{r=5} \frac{9 \times 10^3}{r^2} \hat{a}_r \cdot dr \hat{a}_r$$

$$W = -10 \times 10^{-6} (9 \times 10^3) \left(-\frac{1}{r} \right)_{r=10}^5$$

$$= 9 \times 10^{-2} \left[\frac{1}{5} - \frac{1}{10} \right] = 9 \times 10^{-2} \left[\frac{10-5}{50} \right] = 9 \times 10^{-2} (10^{-1})$$

$$W = 9 \text{ mJ}$$

End of Solution

- Q.5** Consider a power system consisting of N number of buses. Buses in this power system are categorized into slack bus, PV buses and PQ buses for load flow study. The number of PQ buses is N_L . The balanced Newton-Raphson method is used to carry out load flow study in polar form. H , S , M , and R are sub-matrices of the Jacobian matrix J as shown below:

$$\begin{bmatrix} \Delta P \\ \Delta Q \end{bmatrix} = J \begin{bmatrix} \Delta \delta \\ \Delta V \end{bmatrix}, \text{ where } J = \begin{bmatrix} H & S \\ M & R \end{bmatrix}$$

The dimensions of the sub-matrix is

- | | |
|------------------------------------|------------------------------------|
| (a) $N_L \times (N - 1 + N_L)$ | (b) $N_L \times (N - 1)$ |
| (c) $(N - 1) \times (N - 1 + N_L)$ | (d) $(N - 1) \times (N - 1 - N_L)$ |

Ans. (b)

$$\begin{bmatrix} \Delta P \\ \Delta Q \end{bmatrix} = J \begin{bmatrix} \Delta \delta \\ \Delta V \end{bmatrix} \text{ where } J = \begin{bmatrix} H & S \\ M & R \end{bmatrix}$$

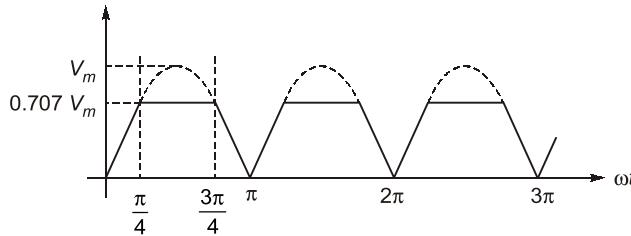
For size of M

 Row = No. of unknown variables of Q = N_L

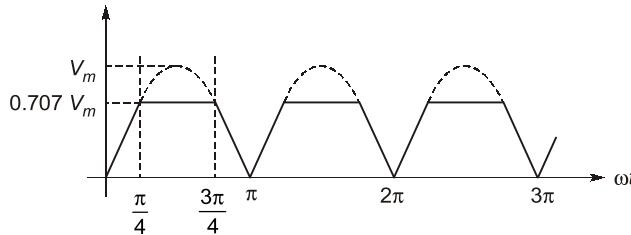
 Column = No. of variable which has δ = $N_L + (N - 1 - N_L) = N - 1$

 So, size of $M = N_L \times (N - 1)$
End of Solution

- Q.6** The waveform shown in solid line is obtained by clipping a full-wave rectified sinusoid (shown dashed). The ratio of the RMS value of the full-wave rectified waveform to the RMS value of the clipped waveform is _____.
 (Round off to 2 decimal places.)



Ans. 1.21 (1.19 to 1.24)



We know,

$$\text{RMS value of full wave rectified sine wave} = \frac{V_m}{\sqrt{2}} = 0.707 V_m$$

For clipped wave form

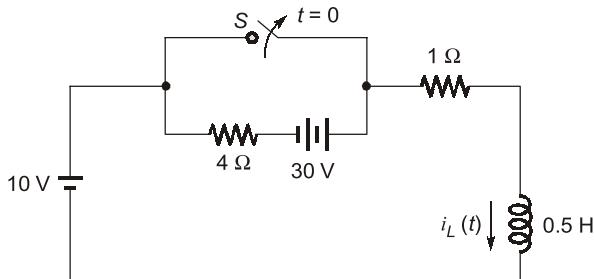
 As $0 \rightarrow \frac{\pi}{4}$ and $\frac{3\pi}{4} \rightarrow \pi$ wave form are identical

$$\begin{aligned} \text{rms value of clipped wave} &= \sqrt{\frac{1}{\pi} \left[2 \int_0^{\pi/4} V_m^2 \sin^2 \omega t + \int_{\pi/4}^{3\pi/4} (0.707 V_m)^2 d\omega t \right]} \\ &= \sqrt{\frac{1}{\pi} \left(\int_0^{\pi/4} \frac{2V_m^2}{2} [1 - \cos 2\omega t] d\omega t + \frac{1}{2} V_m^2 \times \frac{\pi}{2} \right)^{1/2}} \end{aligned}$$

$$\begin{aligned}
 &= \left[\frac{1}{\pi} \left[V_m^2 \left(\frac{\pi}{4} - \frac{1}{2} \sin \frac{\pi}{2} \right) + \frac{V_m^2}{4} \pi \right] \right]^{1/2} \\
 &= \left[\frac{V_m^2}{\pi} \left[\frac{\pi}{4} - \frac{1}{2} \right] + \frac{V_m^2}{4} \right]^{1/2} = 0.5838 V_m \\
 \text{Ratio} &= \frac{0.707}{0.5838} = 1.21
 \end{aligned}$$

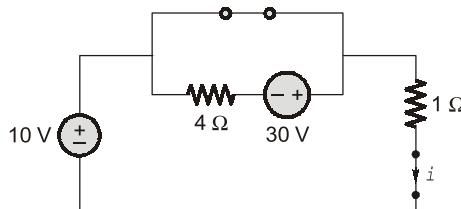
End of Solution

- Q.7** In the circuit, switch 'S' is in the closed position for a very long time. If the switch is opened at time $t = 0$, then $i_L(t)$ in amperes, for $t \geq 0$ is

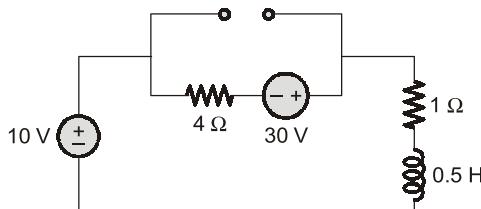


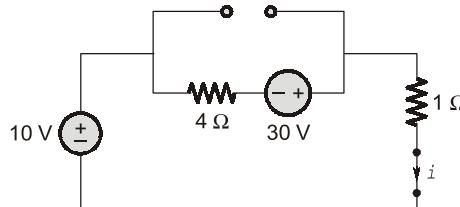
- (a) 10
 (c) $8 + 2e^{-10t}$
 (b) $8e^{-10t}$
 (d) $10(1 - e^{-2t})$

Ans. (c)

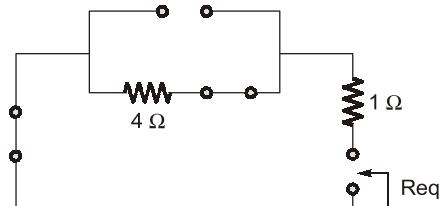
 At $t = 0^-$


$$i_L(0^-) = \frac{10}{1} = 10 \text{ A}$$

 For $t > 0$


At $t = \infty$


$$i(\infty) = \frac{40}{5} = 8 \text{ A}$$

 $R_{eq} :$


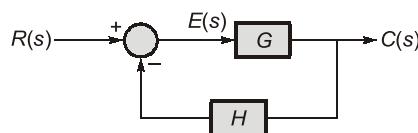
$$R_{eq} = 5 \Omega$$

$$\tau = \frac{L}{R_{eq}} = \frac{0.5}{5} = 0.1 \text{ sec}$$

$$i(t) = 8 + [10 - 8]e^{-t/0.1} \\ = 8 + 2e^{-10t} \text{ A}$$

End of Solution

Q.8 For the closed-loop system shown, the transfer function $\frac{E(s)}{R(s)}$ is



(a) $\frac{1}{1+G}$

(b) $\frac{1}{1+GH}$

(c) $\frac{GH}{1+GH}$

(d) $\frac{G}{1+GH}$

Ans. (b)

$$\begin{aligned} \frac{E(s)}{R(s)} &= \frac{R(s) - H \times C(s)}{R(s)} = 1 - H \times \frac{C(s)}{R(s)} \\ &= 1 - \frac{HG}{1+GH} = \frac{1+GH - GH}{1+GH} \\ &= \frac{1}{1+GH} \end{aligned}$$

End of Solution

- Q.9** In the open interval $(0, 1)$, the polynomial $p(x) = x^4 - 4x^3 + 2$ has
- three real roots
 - two real roots
 - one real root
 - no real roots

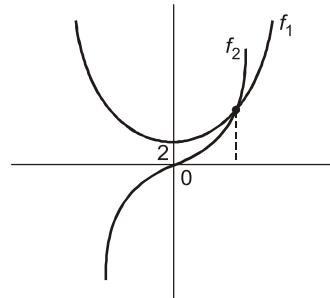
Ans. (c)

$$x^4 + 2 = 4x^3$$

$$f_1(x) = x^4 + 2$$

$$f_2(x) = 4x^3$$

It is clear that point of intersection of these graphs is solution (or) root of $p(x) = 0$



According to intermediate value theorem
 $P(0)$ and $P(1)$ are having opposite signs
 \therefore a root of $p(x) = 0$ in $(0, 1)$
 and also from graph, there is only one point of intersection
 Hence exactly one real root exists in $(0, 1)$

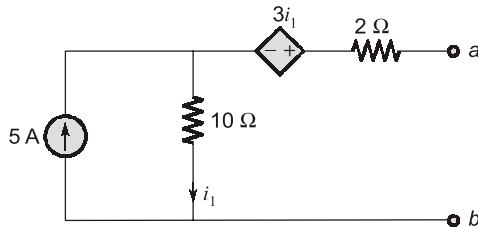
End of Solution

- Q.10** Inductance is measured by
- Maxwell bridge
 - Wien bridge
 - Schering bridge
 - Kelvin bridge

Ans. (a)

End of Solution

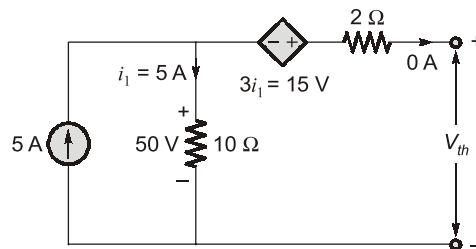
- Q.11** For the network shown, the equivalent Thevenin voltage and Thevenin impedance as seen across terminals 'ab' is



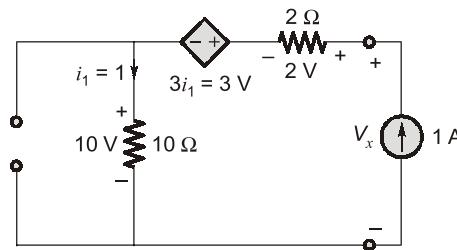
- 10 V in series with 12Ω
- 35 V in series with 2Ω
- 50 V in series with 2Ω
- 65 V in series with 15Ω

Ans. (d)

Given circuit can be resolved as shown below,



$$V_{TH} = 15 + 50 = 65 \text{ V}$$

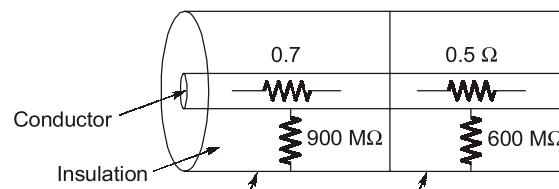


$$V_x = 2 + 3 + 10 = 15 \text{ V}$$

$$R_{TH} = \frac{V_x}{1} = 15 \Omega$$

End of Solution

- Q.12** Two single-core power cables have total conductor resistances of 0.7Ω and 0.5Ω , respectively, and their insulation resistances (between core and sheath) are $600 \text{ M}\Omega$ and $900 \text{ M}\Omega$, respectively. When the two cables are joined in series, the ratio of insulation resistance to conductor resistance is _____ $\times 10^6$.

Ans. (300)


$$(R_{eq})_{conductor} = 0.7 + 0.5 = 1.2 \Omega$$

$$(R_{eq})_{in} = \frac{1}{(R_{eq})_{in}} = \frac{1}{(R_{in})_1} + \frac{1}{(R_{in})_2} = \frac{1}{900 \times 10^6} + \frac{1}{600 \times 10^6}$$

$$(R_{eq})_{in} = 360 \times 10^6 \Omega$$

$$\frac{(R_{eq})_{in}}{(R_{eq})_{conductor}} = \frac{360 \times 10^6}{1.2} = 300 \times 10^6.$$

End of Solution

ESE2021

G.S & Engineering Aptitude **Online Classes**



Features:

- Full coverage of the syllabus to train the aspirants for every possible question.
- Classes will be conducted by experienced faculties.
- The course is designed keeping in mind the latest trends of the ESE paper.
- Lectures will help students to grasp the subject from the grass-root level.
- Emphasis will be given on objective questions solving approach according to the standard of exam.
- Lectures will be delivered in online recorded mode, thereby helping aspirants to access from anywhere and from any device using our user-friendly interface.
- This course will cover 8 GS subjects. Note: Engineering Mathematics and Reasoning Aptitude will not be covered in this course.

Streams: CE, ME, EE & E&T	Duration: 200 Hours	Fee: ₹12000 +GST
--	--------------------------------	-----------------------------

Course will be active till the date of examination

Download **MADE EASY Prime** app



android



iOS



Helpline

8851176822, 9958995830

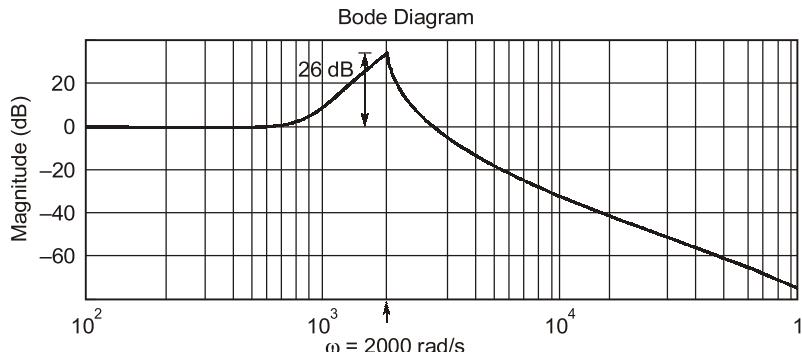
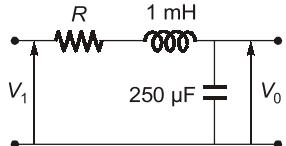


info@madeeasyprime.com



www.madeeasyprime.com

- Q.13** The Bode magnitude plot for the transfer function $\frac{V_0(s)}{V_i(s)}$ of the circuit is as shown. The value of R is _____ Ω . (Round off 2 decimal places)



Ans. 0.10 (0.09 to 0.11)

From response plot

$$M_r = 26 \text{ dB} = 20$$

$$\therefore \frac{1}{2\xi\sqrt{1-\xi^2}} = 20$$

$$\therefore \xi = 0.025$$

From electrical network

$$\chi = \frac{R}{2}\sqrt{\frac{C}{L}} = 0.025$$

$$\therefore R = 0.10 \Omega$$

End of Solution

- Q.14** Consider a continuous-time signal $x(t)$ defined by $x(t) = 0$ for $|t| > 1$, and $x(t) = 1 - |t|$ for $|t| \leq 1$. Let the Fourier transform of $x(t)$ be defined as $X(\omega) = \int_{-\infty}^{\infty} x(t) e^{-j\omega t} dt$. The maximum magnitude of $X(\omega)$ is _____ .

Ans. (1)

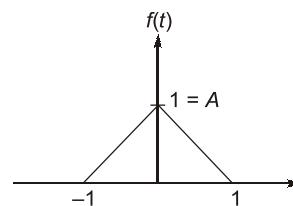
$$\text{Fourier transform, } F(\omega) = A\tau Sa^2\left(\frac{\omega\tau}{2}\right)$$

As $A = 1$, $\tau = 1$,

$$F(\omega) = Sa^2\left(\frac{\omega}{2}\right)$$

$$F(\omega)|_{\text{peak}} = F(0) = Sa^2(0) = 1$$

\therefore Peak value of sampling function occurs at $\omega = 0$,
 Peak value = 1



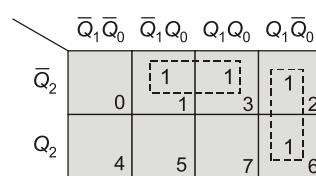
End of Solution

- Q.15** A counter is constructed with three D flip-flops. The input-output pairs are named (D_0 , Q_0), (D_1 , Q_1) and (D_2 , Q_2), where the subscript 0 denotes the least significant bit. The output sequence is desired to be the Gray-code sequence 000, 001, 011, 010, 110, 111, 101 and 100, repeating periodically. Note that the bits are listed in the $Q_2 Q_1 Q_0$ format. The combinational logic expression for D_1 is

- (a) $Q_2 Q_1 + \bar{Q}_2 \bar{Q}_1$ (b) $Q_2 Q_1 Q_0$
 (c) $\bar{Q}_2 Q_0 + Q_1 \bar{Q}_0$ (d) $Q_2 Q_0 + Q_1 \bar{Q}_0$

Ans. (c)

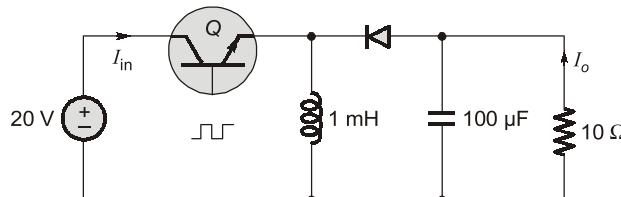
Present state			Next state			D_2	D_1	D_0
Q_2	Q_1	Q_0	Q_2^+	Q_1^+	Q_0^+			
0	0	0	0	0	1	0		
0	0	1	0	1	1	1		
0	1	1	0	1	0	1		
0	1	0	1	1	0	1		
1	1	0	1	1	1	1		
1	1	1	1	0	1	0		
1	0	1	1	0	0	0		
1	0	0	0	0	0	0		



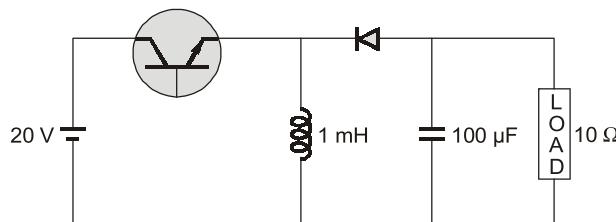
$$D_1 = \bar{Q}_2 Q_0 + Q_1 \bar{Q}_0$$

End of Solution

- Q.16** Consider the buck-boost converter shown. Switch Q is operating at 25 kHz and 0.75 duty-cycle. Assume diode and switch to be ideal. Under steady-state condition, the average current flowing through the inductor is _____ A.



Ans. (24)



$$\alpha = 0.75, f = 25 \text{ kHz}$$

Assume continuous conduction:

$$V_o = \frac{\alpha V_s}{1 - \alpha} = \frac{0.75 \times 20}{1 - 0.75}$$

$$V_o = 60 \text{ V}$$

$$I_0 = \frac{V_0}{R} = \frac{60}{10} = 6 \text{ A}$$

$$I_L = \frac{I_0}{1-\alpha} = \frac{6}{1-0.75} = 24 \text{ A}$$

$$\Delta I_L = \frac{\alpha V_s}{f_L} = \frac{0.75 \times 60}{25 \times 10^3 \times (1 \times 10^{-3})} = 1.8 \text{ A}$$

$$I_{L \min} = I_L - \frac{\Delta I_L}{2} = 24 - \frac{1.8}{2} = 24 - 0.9$$

$$(I_{L \min} = 23.1 \text{ A}) > 0$$

∴ Continuous conduction assumption is correct.

$$I_L = 24 \text{ A}$$

End of Solution

- Q.17** A belt-driven DC shunt generator running at 300 RPM delivers 100 kW to a 200 V DC grid. It continues to run as a motor when the belt breaks, taking 10 kW from the DC grid. The armature resistance is 0.025 Ω , field resistance is 50 Ω , and brush drop is 2 V. Ignoring armature reaction, the speed of the motor is _____ RPM. (Round off 2 decimal places)

Ans. 275.18 (274.00 to 276.00)

$$I_L = \frac{100 \times 10^3}{200} = 500 \text{ A}$$

$$I_{sh} = \frac{200}{50} = 4 \text{ A}$$

$$I_a = 504 \text{ A}$$

$$E_q = V + I_a R_a + \text{Brush drop} \\ = 200 + 504 (0.025) + 2 \text{ V} \\ = 214.6 \text{ V}$$

In motoring case: $VI = 10 \text{ kW}$, $V = 200 \text{ V}$

$$\therefore I = \frac{10000}{200} = 50 \text{ A}$$

$$I_f = 4 \text{ A}, I_a = I_L - I_f \\ = 46 \text{ A}$$

$$E_b = V - I_a R_a - \text{Brush Drop} \\ = 200 - 46 (0.025) - 2 = 196.85 \text{ V}$$

$$\frac{N_m}{N_g} = \frac{E_b}{E_g}$$

$$N_m = \frac{E_b}{E_g} \times N_g$$

$$\therefore N_m = \frac{196.85}{214.6} \times 300 = 275.18 \text{ rpm}$$

End of Solution

Q.18 Let $p(z) = z^3 + (1 + j)z^2 + (2 + j)z + 3$, where z is a complex number. Which one of the following is true?

- (a) The complex roots of the equation $p(z) = 0$ come in conjugate pairs.
- (b) All the roots cannot be real.
- (c) The sum of the roots of $p(z) = 0$ is real number
- (d) Conjugate $\{p(z)\} = p(\text{conjugate}(z))$ for all z

Ans. (b)

Since sum of the roots is a complex number

\Rightarrow absent one root is complex

So all the roots cannot be real.

End of Solution

Q.19 A signal generator having a source resistance of 50Ω is set to generate a 1 kHz sinewave. Open circuit terminal voltage is 10 V peak-to-peak. Connecting a capacitor across the terminals reduces the voltage to 8 V peak-to-peak. The value of this capacitor is _____ μF . (Round off to 2 decimal places).

Ans. 2.38 (2.30 to 2.45)

$$\frac{V_o(j\omega)}{V_i(j\omega)} = \frac{1}{1+j\omega RC}$$

$$\frac{8}{10} \angle \theta = \frac{1}{1+j\omega RC}$$

$$1 + j\omega RC = 1.25 \angle \theta$$

$$\omega RC = \sqrt{1.25^2 - 1^2}$$

$$\omega RC = 0.75$$

$$C = \frac{0.75}{2000\pi \times 50} = 2.38 \mu\text{F}$$

End of Solution

Q.20 The power input to a 500 V, 50 Hz, 6-pole, 3-phase induction motor running at 975 RPM is 40 kW. The total stator losses are 1 kW. If the total friction and windage losses are 2.025 kW, then the efficiency is _____ %.

Ans. (90)

$$P_{i/p} = 40 \text{ kW}, \text{ stator loss} = 1 \text{ kW}, F \text{ and } W = 2.025 \text{ kW}$$

$$\text{Stator o/p} = 40 - 1 = 39 \text{ kW}$$

$$\text{Slip} = \frac{1000 - 975}{1000} = 0.025$$

$$\text{Rotor o/p} = \text{Rotor i/p} \times (1 - s)$$

$$= 39 (1 - 0.025) = 38.025 \text{ kW}$$

$$\text{Motor o/p} = 38.025 - 2.025 = 36 \text{ kW}$$

$$\eta = \frac{\text{Motor output}}{\text{Motor input}} = \frac{36}{40} \times 100 = 90\%$$

End of Solution

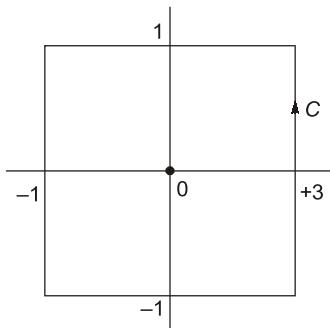
Q.21 Let $(-1 - j)$, $(3 - j)$, $(3 + j)$ and $(-1 + j)$ be the vertices of rectangle C in the complex plane. Assuming that C is traversed in counter-clockwise direction, the value of the

contour integral $\oint_C \frac{dz}{z^2(z-4)}$ is

- | | |
|----------------------|-----------------------|
| (a) 0 | (b) $\frac{-j\pi}{8}$ |
| (c) $\frac{j\pi}{2}$ | (d) $\frac{j\pi}{16}$ |

Ans. (b)

$$\oint_C \frac{dz}{z^2(z-4)}$$



Singularities are given by $z^2(z-4) = 0$

$$\Rightarrow z = 0, 4$$

$z = 0$ is pole of order $m = 2$ lies inside contour 'c'

$z = 4$ is pole of order $m = 1$ lies outside 'c'

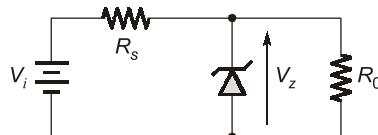
$$\begin{aligned} \text{Res}_0 &= \frac{1}{(2-1)!} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left[(z-0)^2 \frac{1}{z^2(z-4)} \right] \\ &= \frac{-1}{(0.4)^2} = \frac{-1}{16} \end{aligned}$$

By CRT

$$\begin{aligned} \oint_C f(z) dz &= 2\pi i \text{Res}_0 = 2\pi i \left[\frac{-1}{16} \right] \\ &= \frac{-\pi i}{8} \end{aligned}$$

End of Solution

- Q.22** In the circuit shown, a 5 V Zener diode is used to regulate the voltage across load R_0 . The input is an unregulated DC voltage with a minimum value of 6 V and a maximum value of 8 V. The value of R_s is 6 Ω . The Zener diode has a maximum rated power dissipation of 2.5 W. Assuming the Zener diode to be ideal, the minimum value of R_0 is _____ Ω .



Ans. (30)

To calculate $R_{0 \text{ min}}$, we must find $I_{L \text{ max}}$

$$I_{s \text{ min}} = I_z \text{ min} + I_{L \text{ max}}$$

$$\frac{V_{i \text{ min}} - V_z}{R_s} = I_z \text{ min} + I_{L \text{ max}}$$

For ideal zener diode, $I_z \text{ min} = 0$

$$\frac{V_{i \text{ min}} - V_z}{R_s} = I_{L \text{ max}}$$

$$\frac{6 - 5}{6} = I_{L \text{ max}}$$

$$I_{L \text{ max}} = \frac{1}{6} \text{ A}$$

$$R_{0 \text{ min}} = \frac{V_z}{I_{L \text{ max}}} = \frac{5}{1/6} = 30 \Omega$$

End of Solution

- Q.23** One coulomb of point charge moving with a uniform velocity $10\hat{x}$ m/s enters the region $x \geq 0$ having a magnetic flux density.

$$\vec{B} = (10y\hat{x} + 10x\hat{y} + 10\hat{z}) \text{ T}$$

The magnitude of force on the charge at $x = 0^+$ is _____ N.

(\hat{x} , \hat{y} and \hat{z} are unit vectors along x -axis, y -axis and z -axis, respectively)

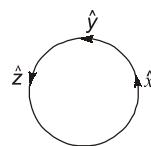
Ans. (100)

Force on a charge moving with \vec{v} velocity due to magnetic field is

$$\begin{aligned}\vec{F} &= Q(\vec{v} \times \vec{B}) \\ &= [10\hat{x} \times (10y\hat{x} + 10x\hat{y} + 10\hat{z})] \\ &= 10(10x)\hat{z} + 10(10)(-\hat{y}) \\ &= 100x\hat{z} - 100\hat{y}\end{aligned}$$

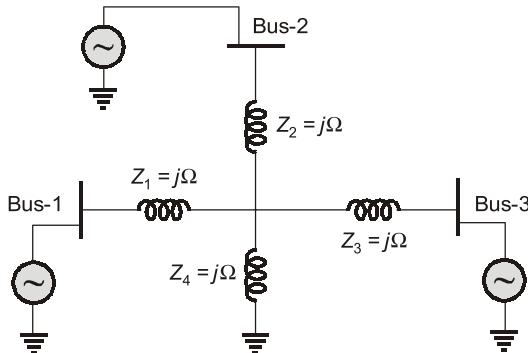
$$\vec{F}|_{x=0^+} = -100\hat{y}$$

$$|\vec{F}| = \sqrt{(-100)^2} = 100 \text{ Newton}$$



End of Solution

- Q.24** A 3 Bus network is shown. Consider generators as ideal voltage sources. If rows 1, 2 and 3 of the Y_{Bus} matrix correspond to Bus 1, 2 and 3 respectively, then Y_{Bus} of the network is



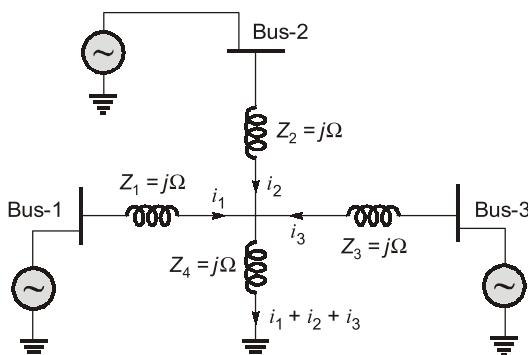
$$(a) \begin{bmatrix} -\frac{1}{2}j & \frac{1}{4}j & \frac{1}{4}j \\ \frac{1}{4}j & -\frac{1}{2}j & \frac{1}{4}j \\ \frac{1}{4}j & \frac{1}{4}j & -\frac{1}{2}j \end{bmatrix}$$

$$(b) \begin{bmatrix} -\frac{3}{4}j & \frac{1}{4}j & \frac{1}{4}j \\ \frac{1}{4}j & -\frac{3}{4}j & \frac{1}{4}j \\ \frac{1}{4}j & \frac{1}{4}j & -\frac{3}{4}j \end{bmatrix}$$

$$(c) \begin{bmatrix} -4j & j & j \\ j & -4j & j \\ j & j & -4j \end{bmatrix}$$

$$(d) \begin{bmatrix} -4j & 2j & 2j \\ 2j & -4j & 2j \\ 2j & 2j & -4j \end{bmatrix}$$

Ans. (b)



$$V_1 = j1i_1 + j1(i_1 + i_2 + i_3)$$

$$V_1 = 2ji_1 + ji_2 + ji_3$$

and

$$V_2 = ji_1 + 2ji_2 + ji_3$$

$$V_3 = ji_1 + ji_2 + 2ji_3$$

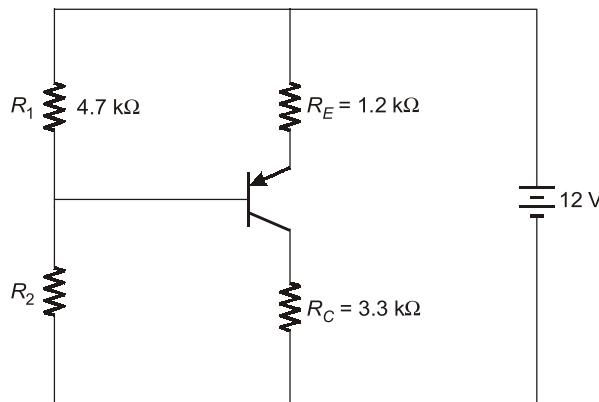
$$\therefore \begin{bmatrix} V_1 \\ V_2 \\ V_3 \end{bmatrix} = \begin{bmatrix} 2j & j & j \\ j & 2j & j \\ j & j & 2j \end{bmatrix} \begin{bmatrix} i_1 \\ i_2 \\ i_3 \end{bmatrix}$$

$$Z_{\text{bus}} = \begin{bmatrix} 2j & j & j \\ j & 2j & j \\ j & j & 2j \end{bmatrix}$$

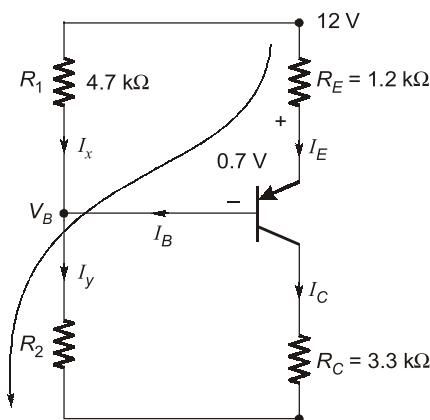
$$Y_{\text{bus}} = \begin{bmatrix} -3j & j & j \\ 4 & 4 & 4 \\ j & -3j & j \\ 4 & 4 & 4 \\ j & j & -3j \\ 4 & 4 & 4 \end{bmatrix}$$

End of Solution

- Q.25** In the BJT circuit shown, beta of the PNP transistor is 100. Assume $V_{BE} = -0.7$ V. The voltage across R_C will be 5 V when R_2 is _____ kΩ. (Round off 2 decimal places).



Ans. 17.06 (16.50 to 17.50)



$$I_C = \frac{5V}{3.3k} = 1.515 \text{ mA}$$

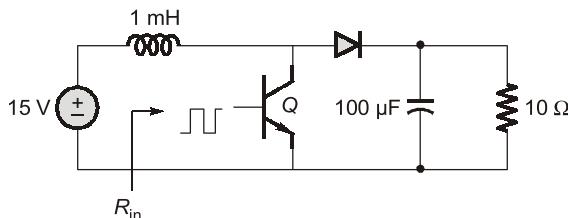
$$I_E = 1.53 \text{ mA}$$

$$I_B = 0.0151 \text{ mA}$$

$$\begin{aligned}
 -12 + 1.2k \times 1.53 m + 0.7 + V_B &= 0 \\
 V_B &= 9.464 \text{ V} \\
 I_x &= \frac{12 - V_B}{4.7k} = \frac{12 - 9.464}{4.7k} = 0.539 \text{ mA} \\
 I_x + I_B &= I_y \\
 \Rightarrow I_y &= 0.5396 + 0.0151 \\
 I_y &= 0.5546 \text{ mA} \\
 V_B &= 0.5546 \text{ m} \times R_2 = 9.464 \\
 R_2 &= 17.06 \text{ k}\Omega
 \end{aligned}$$

End of Solution

- Q.26** Consider the boost converter shown. Switch Q is operating at 25 kHz with a duty cycle of 0.6. Assume the diode and switch to be ideal. Under steady-state condition, the average resistance R_{in} as seen by the source is _____ Ω .
 (Round off to 2 decimal places.)



Ans. 1.60 (1.50 to 1.70)

Checking for continuous conduction mode

$$\Delta I_L = \frac{\alpha V_S}{fL} = \frac{0.6 \times 15}{25 \times 10^3 \times 1 \times 10^{-3}} = 0.36A$$

$$\frac{\Delta I_L}{2} = 0.18A$$

$$\begin{aligned}
 I_{L,\min} &= I_L - \frac{\Delta I_L}{2} = I_S - \frac{\Delta I_L}{2} \\
 &= (9.375 - 0.18) = 9.195 > 0
 \end{aligned}$$

As it is continuous conduction

$$V_0 = \frac{V_S}{1-\alpha} = \frac{15}{1-0.6} = 37.5V$$

$$I_0 = \frac{V_0}{R} = \frac{37.5}{10} = 3.75V$$

$$\frac{V_0}{V_S} = \frac{I_S}{I_o} = \frac{1}{1-\alpha}$$

$$I_S = \frac{I_o}{1-\alpha} = \frac{3.75}{1-0.6} = 9.375A$$

$$R_{in} = \frac{V_S}{I_S} = \frac{15}{9.375} = 1.6\Omega$$

End of Solution



MADE EASY

India's Best Institute for IES, GATE & PSUs

ESE 2021 Preliminary Examination Online Test Series

34 Tests

2206 Questions

Combined Package of
ESE 2020 + ESE 2021 (Pre)
also available : 68 Tests

Streams: CE, ME, EE , E&T

- Quality questions as per standard and pattern of ESE.
- Includes tests of Paper-I (GS & Engg. Aptitude) and Paper-II (Technical)
- Fully explained and well illustrated solutions.
- Due care taken for accuracy.
- Comprehensive performance analysis report.



ESE 2021 Prelims Offline Test Series

Starting from 15th April, 2021

More details will be uploaded shortly at our website

Technical Queries Helpline : ☎ 9818098817, 011-45124612

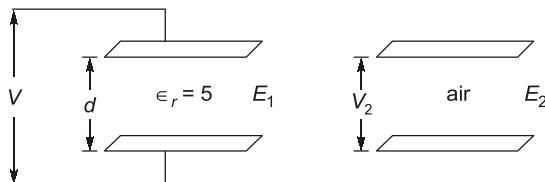
Enroll now



www.onlinetestseriesmadeeasy.in

- Q.27** Consider a large parallel plate capacitor. The gap 'd' between the two plates is filled entirely with a dielectric slab of relative permittivity 5. The plates are initially charged to a potential difference of V volts and then disconnected from the source. If the dielectric slab is pulled out completely, then the ratio of the new electric field E_2 in the gap to the original electric field E_1 is _____.

Ans. (5)



If voltage source is removed then in both cases charge Q is constant.

Case-1: ($Q_1 = Q$; $V_1 = V$)

$$Q_1 = C_1 V_1$$

$$Q = \frac{\epsilon_0 (5)A}{d} V_1$$

$$Q = 5 \left(\frac{\epsilon_0 A}{d} \right) V_1 \quad \dots(i)$$

Case-2: ($Q_2 = Q$; V_2)

$$Q_2 = C_2 V_2$$

$$Q = \frac{\epsilon_0 (1)A}{d} V_2$$

$$Q = \left(\frac{\epsilon_0 A}{d} \right) V_2 \quad \dots(ii)$$

Equation (i) is equal to equation (ii)

$$\Rightarrow 5 \left(\frac{\epsilon_0 A}{d} \right) V_1 = \left(\frac{\epsilon_0 A}{d} \right) V_2$$

$$\Rightarrow 5V_1 = V_2$$

$$\frac{V_2}{V_1} = 5 \quad \dots(iii)$$

$$E_1 = \frac{V_1}{d}; E_2 = \frac{V_2}{d}$$

$$\frac{E_2}{E_1} = \frac{V_2/d}{V_1/d}$$

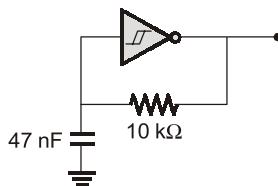
$$\Rightarrow \frac{E_2}{E_1} = \frac{V_2}{V_1} \quad \dots(iv)$$

Put equation (iii) in equation (iv),

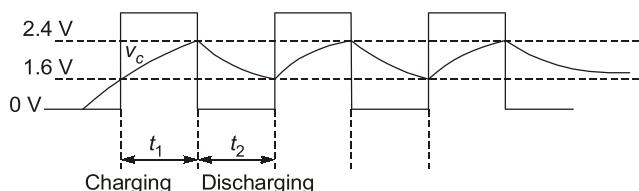
$$\Rightarrow \frac{E_2}{E_1} = 5$$

End of Solution

- Q.28** A CMOS Schmitt-trigger inverter has a low output level of 0 V and a high output level of 5 V. It has input thresholds of 1.6 V and 2.4 V. The input capacitance and output resistance of the Schmitt-trigger are negligible. The frequency of the oscillator shown is _____ Hz. (Round off to 2 decimal places.)



Ans. 3157.56 (3100.00 to 3200.00)



Charging,

$$v_c(t) = v_{c \text{ final}} + [v_{\text{initial}} - v_{c \text{ final}}] e^{-t/RC}$$

$$v_c(t) = 5 + (1.6 - 5)e^{-t/RC}$$

$$= 5 - 3.4 e^{-t/RC}$$

$t = t_1$,

$$v_c(t) = 2.4 \text{ V}$$

$$2.4 = 5 - 3.4 e^{-t/RC}$$

$$3.4e^{-t_1/RC} = 2.6$$

$$t_1 = \ln\left(\frac{3.4}{2.6}\right)RC = 0.268 \times RC$$

Discharging,

$$v_c(t) = 0 + (2.4 - 0) e^{-t/RC}$$

$$= 2.4e^{-t/RC}$$

$t = t_2$,

$$v_c(t_a) = 1.6 \text{ V}$$

$$1.6 = 2.4e^{-t_2/RC}$$

$$t_2 = \ln\left(\frac{2.4}{1.6}\right)RC = 0.405 \times RC$$

$$T = t_1 + t_2 = (0.268 + 0.405)RC$$

$$T = 0.673 RC$$

$$f = \frac{1}{0.673RC} = \frac{1}{0.673 \times 10^4 \times 47 \times 10^{-9}}$$

$$f = 3157.46 \text{ Hz}$$

End of Solution

Q.29 The state space representation of a first-order system is given as

$$\dot{x} = -x + u$$

$$y = x$$

where, x is the state variable, u is the control input and y is the controlled output. Let $u = -Kx$ be the control law, where K is the controller gain. To place a closed-loop pole at -2 , the value of K is _____.

Ans. (1)

$$\dot{x} = -x - Kx = x(-K - I)$$

Characteristic equation,

$$|sI + KI + I| = 0$$

$$|(s+1+K)I| = 0$$

$$\therefore s + 1 + K = 0$$

$$s = -1 - K$$

$$-2 = -1 - K$$

$$K = 1$$

End of Solution

Q.30 An 8-pole, 50 Hz. three-phase, slip-ring induction motor has an effective rotor resistance of 0.08Ω per phase. Its speed at maximum torque is 650 RPM. The additional resistance per phase that must be inserted in the rotor to achieve maximum torque at start is _____ Ω . (Round off to 2 decimal places.)

Neglect magnetizing current and stator leakage impedance. Consider equivalent circuit parameters referred to stator.

Ans. 0.52 (0.50 to 0.54)

$$N_{\max} = 650 \text{ rpm}, P = 8, 50 \text{ Hz}$$

$$s_m = \frac{750 - 650}{750} = 0.1333$$

$$s_m = \frac{R_2}{X_2}$$

$$\therefore X_2 = \frac{R_2}{s_m} = \frac{0.08}{0.133} = 0.601 \Omega$$

$$R_2 = 0.08 \Omega, X_2 = 0.601 \Omega$$

Condition for maximum T_{st}

$$\Rightarrow R_2 = X_2$$

$$\therefore R_2 + R_{ext} = X_2$$

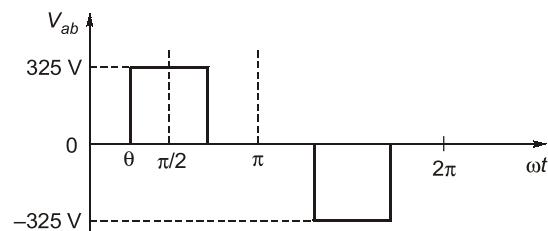
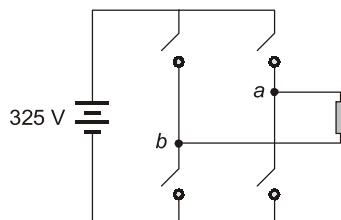
$$\therefore R_{ext} = 0.601 - 0.08 = 0.521 \Omega$$

End of Solution

- Q.31** A single-phase full-bridge inverter fed by a 325 V DC produces a symmetric quasi-square waveform across 'ab' as shown. To achieve a modulation index of 0.8, the angle θ expressed in degrees should be _____.

(Round off to 2 decimal places.)

(Modulation index is defined as the ratio of the peak of the fundamental component of V_{ab} to the applied DC value.)



Ans. 51.10 (50.00 to 52.00)

$$\widehat{V_{01}} = m_a V_S = 0.8 \times 325 = 260 \text{ V}$$

$$\widehat{V_{01}} = \frac{4V_S}{\pi} \sin d = 260$$

$$\frac{4(325)}{\pi} \sin d = 260$$

$$\sin d = \frac{260 \times \pi}{4 \times 325} = 0.628$$

$$d = 38.9$$

$$\therefore \theta = \frac{\pi}{2} - d = 90^\circ - 38.9 = 51.1$$

End of Solution

- Q.32** Let p and q be real numbers such that $p^2 + q^2 = 1$. The eigenvalues of the matrix $\begin{bmatrix} p & q \\ q & -p \end{bmatrix}$

are

- | | |
|--------------------|----------------|
| (a) pq and $-pq$ | (b) 1 and 1 |
| (c) j and $-j$ | (d) 1 and -1 |

Ans. (d)

Characteristic equation of A

$$|A_{2x2} - \lambda J| = (-1)^2 \lambda^2 + (-1)^1 \text{Tr}(A)\lambda + |A| = 0$$

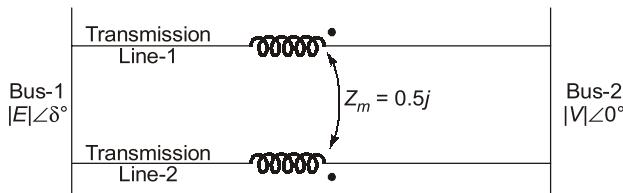
$$\lambda^2 - (p-p)\lambda + (-p^2 - q^2) = 0$$

$$\Rightarrow \lambda^2 - 1 = 0$$

$$\Rightarrow \lambda = \pm 1$$

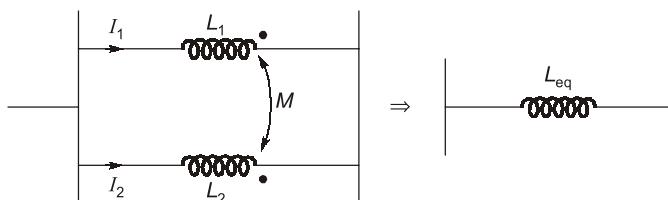
End of Solution

- Q.33** In the figure shown, self-impedances of the two transmission lines are $1.5j$ p.u each, and $Z_m = 0.5j$ p.u is the mutual impedance. Bus voltages shown in the figure are in p.u. Given that $\delta > 0$, the maximum steady-state real power that can be transferred in p.u from Bus-1 to Bus-2 is



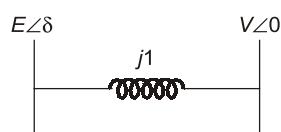
- (a) $\frac{|E||V|}{2}$ (b) $\frac{3|E||V|}{2}$
 (c) $|E||V|$ (d) $2|E||V|$

Ans. (c)



$$L_{eq} = \frac{L_1 L_2 - M^2}{(L_1 + L_2 - 2M)}$$

$$X_{eq} = \frac{1.5 \times 1.5 - 0.5^2}{1.5 + 1.5 - 2 \times 0.5} = 1 \text{ p.u.}$$

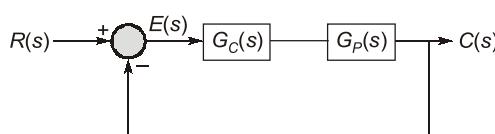


$$P_{max} = \frac{|E||V|}{1}$$

$$P_{max} = |E||V|$$

End of Solution

- Q.34** Consider a closed-loop system as shown. $G_p(s) = \frac{14.4}{s(1+0.1s)}$ is the plant transfer function and $G_c(s) = 1$ is the compensator. For a unit-step input, the output response has damped oscillations. The damped natural frequency is _____ rad/s. (Round off to 2 decimal places.)



Ans. 10.90 (10.80 to 11.00)

$$q(s) = s^2 + 10s + 144 = 0$$

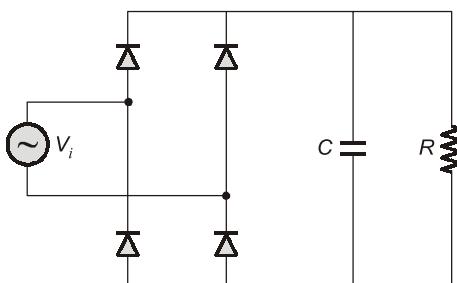
$$\omega_n = 12; \xi = \frac{5}{12}$$

$$\omega_d = \omega_n \sqrt{1 - \xi^2}$$

$$= 12 \sqrt{\frac{119}{144}} = 10.90$$

End of Solution

- Q.35** In the circuit shown, the input V_i is a sinusoidal AC voltage having an RMS value of 230 V \pm 20%. The worst-case peak-inverse voltage seen across any diode is _____ V. (Round off to 2 decimal places.)



Ans. 390.32 (385.00 to 395.00)

$$(V_D)_{\text{peak}} \text{ for worst case} = (230 + 20\%) \times \sqrt{2}$$

$$= \left(230 + 230 \times \frac{20}{100} \right) \times \sqrt{2} = 390.32 \text{ V}$$

End of Solution

- Q.36** Which one of the following vector functions represents a magnetic field \vec{B} ?

(\hat{x} , \hat{y} and \hat{z} are unit vectors along x -axis, y -axis and z -axis, respectively)

$$(a) 10x\hat{X} + 20y\hat{Y} - 30z\hat{Z} \quad (b) 10x\hat{X} - 30z\hat{Y} + 20y\hat{Z}$$

$$(c) 10z\hat{X} + 20y\hat{Y} - 30x\hat{Z} \quad (d) 10y\hat{X} + 20x\hat{Y} - 10z\hat{Z}$$

Ans. (a)

If \vec{B} is magnetic flux density then $\nabla \cdot \vec{B} = 0$

$$\nabla \cdot \vec{B} = \frac{\partial B_x}{\partial x} + \frac{\partial B_y}{\partial y} + \frac{\partial B_z}{\partial z}$$

$$\frac{\partial}{\partial x}(10x) + \frac{\partial}{\partial y}(20y) + \frac{\partial}{\partial z}(-30z) = \vec{\nabla} \cdot \vec{B}$$

$$\vec{\nabla} \cdot \vec{B} = 10 + 20 - 30 = 0$$

End of Solution

Q.37 Consider the table given:

Constructional feature	Machine type	Mitigation
(P) Damper bars	(S) Induction motor	(X) Hunting
(Q) Skewed rotor slots	(T) Transformer	(Y) Magnetic locking
(R) Compensating winding	(U) Synchronous machine	(Z) Armature reaction
	(V) DC machine	

The correct combination that relates the constructional feature, machine type and mitigation is

Ans. (c)

End of Solution

Q.38 Let A be a 10×10 matrix such that A^5 is null matrix, and let I be the 10×10 identity matrix. The determinant of $A + I$ is _____.

Ans. (1)

$$\begin{aligned}
 & \text{Given:} & A^5 &= 0 \\
 & & Ax &= \lambda x \\
 \Rightarrow & & A^5x &= \lambda^5 x \quad (\because x \neq 0) \\
 \Rightarrow & & \lambda^5 &= 0 \\
 \Rightarrow & & \lambda &= 0
 \end{aligned}$$

Eigen values of $A + I$ given $\lambda + 1$

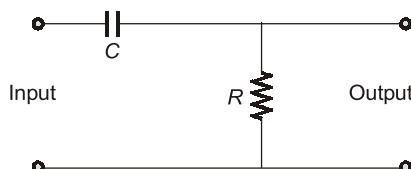
\therefore Eigen values of $I_4 = 1$

Hence $|A+I| \equiv$ Product of eigen values $\equiv 1 \times 1 \times 1 \times \dots$ 10 times

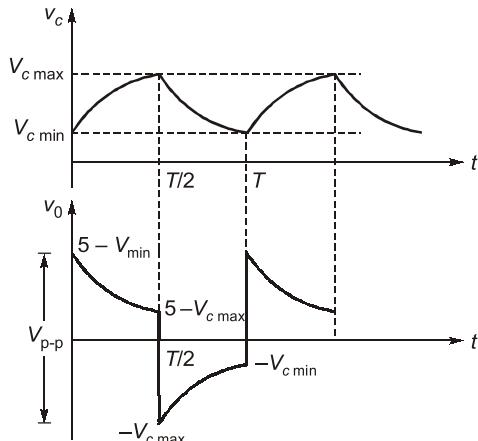
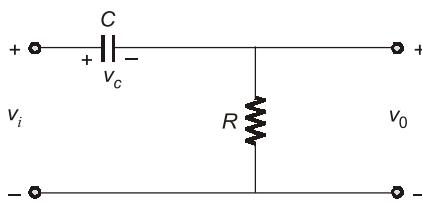
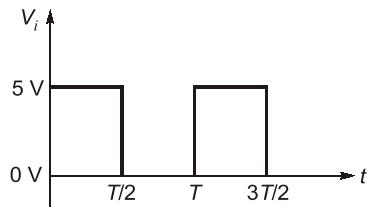
- 1

End of Solution

Q.39 A 100 Hz square wave, switching between 0 V and 5 V, is applied to a CR high-pass filter circuit as shown. The output voltage waveform across the resistor is 6.2 V peak-to-peak. If the resistance R is 820Ω , then the value C is ____ μF .
(Round off to 2 decimal places.)



Ans. 12.46 (12.00 to 13.00)



For 1st half cycle,

$$V_0 = V_i - V_c$$

For 2nd half cycle,

$$V_0 = -V_c$$

$$V_{p-p} = (5 - V_{c \min}) - (-V_{c \max})$$

$$6.2 = 5 + V_{c \max} - V_{c \min}$$

$$\Rightarrow V_{c \max} - V_{c \min} = 1.2 \quad \dots(\alpha)$$

For first half cycle i.e. $0 < t < \frac{T}{2}$

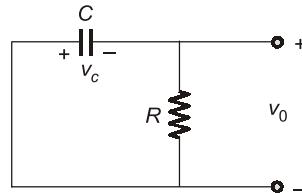
$$\begin{aligned} V_c(0^+) &= V_c(0) = V_c(0^-) = V_{c \min} \\ V_c(\infty) &= 5 \text{ V} \end{aligned}$$

$$\therefore V_c(t) = V_c(\infty) + [V_c(0^+) - V_c(\infty)] e^{-t/\tau}$$

$$V_c(t) = 5 + [V_{c \min} - 5] e^{-t/2\tau} = V_{c \max}$$

$$\Rightarrow V_{c \max} = 5[1 - e^{-T/2\tau}] + V_{c \min} e^{-T/2\tau} \quad \dots(i)$$

For $\frac{T}{2} < t < T$



$$v_c(t) = V_{c\max} \left(\frac{T}{2} \right) e^{-(t-T/2)\tau}$$

$$\therefore v_c(t) = V_{c\max} e^{-(t-T/2)\tau}$$

$$\text{at } t = T, \quad V_c = V_{c\min}$$

$$\Rightarrow V_{c\min} = V_{c\max} e^{-T/2\tau} \quad \dots(\text{ii})$$

$$\text{As } V_{c\max} - V_{c\min} = 1.2 \quad [\text{From (a)}]$$

$$\therefore V_{c\max} - V_{c\max} e^{-T/2\tau} = 1.2$$

$$V_{c\max} = \frac{1.2}{1 - e^{-T/2\tau}} \quad \dots(\text{iii})$$

$$\Rightarrow V_{c\max} = \frac{1.2}{1 - e^{-T/2\tau}} = 5[1 - e^{-T/2\tau}] + V_{c\min} e^{-2\tau}$$

From (ii),

$$V_{c\max} = 5[1 - e^{-T/2\tau}] + (V_{c\max} e^{-T/2\tau}) e^{-T/2\tau}$$

$$V_{c\max} = 5[1 - e^{-T/2\tau}] + V_{c\max} e^{-T/\tau}$$

$$\Rightarrow V_{c\max} [1 - e^{-T/\tau}] = 5[1 - e^{-T/2\tau}]$$

$$V_{c\max} = \frac{5[1 - e^{-T/2\tau}]}{[1 + e^{-T/2\tau}][1 - e^{-T/2\tau}]}$$

Using equation (iii),

$$\frac{1.2}{1 - e^{-T/2\tau}} = \frac{5}{1 + e^{-T/2\tau}}$$

$$\Rightarrow 1.2 + 1.2 e^{-T/2\tau} = 5 - 5 e^{-T/2\tau}$$

$$\Rightarrow 6.2 e^{-T/2\tau} = 3.8$$

$$e^{-T/2\tau} = \frac{3.8}{6.2} = 0.6129$$

$$\frac{T}{2\tau} = 0.4895$$

as $T = \frac{1}{f} = \frac{1}{100}$ sec

and $\tau = RC = 820$ C

$$\Rightarrow \frac{1}{(100)(2)(820)C} = 0.4895$$

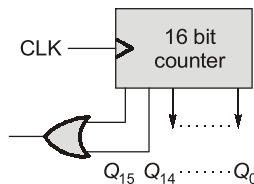
$$\therefore C = 12.46 \mu\text{F}$$

End of Solution

- Q.40** A 16-bit synchronous binary up-counter is clocked with a frequency f_{CLK} . The two most significant bits are OR-ed together to form an output Y. Measurements show that Y is periodic, and the duration for which Y remains high in each period is 24 ms. The clock frequency f_{CLK} is _____ MHz.

(Round off to 2 decimal places.)

Ans. 2.05 (2.00 to 2.10)



$y = 1$ for 24 m sec

	Q_{15}	Q_{14}	Q_0
$y = 1$ Starts at	0100	0000	0000
$y = 1$ Ends at	1111	1111	1111	1111

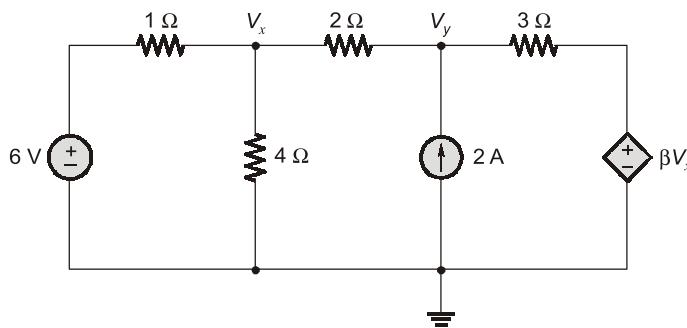
Total number of states for which $y = 1$ is $2^{16} - 2^{14}$

Time is $(2^{16} - 2^{14})T = 24$ msec

$$f = \frac{1}{T} = 2.05 \text{ MHz}$$

End of Solution

- Q.41** In the given circuit, for voltage V_y to be zero, the value of β should be _____.
 (Round off to 2 decimal places).



Ans. (-3.25) (-3.30 to -3.20)

$$\frac{V_x - 6}{1} + \frac{V_x}{4} + \frac{V_x - V_y}{2} = 0$$

$$4V_x - 24 + V_x + 2V_x - 2V_y = 0$$

$$7V_x - 2V_y = 24$$

If $V_y = 0$

$$\Rightarrow 7V_x = 24$$

$$\Rightarrow V_x = \frac{24}{7}$$

$$\frac{V_y - V_x}{2} + \frac{V_y - \beta V_x}{3} = 2$$

$$3V_y - 3V_x + 2V_y - 2\beta V_x = 12$$

$$5V_y - (3 + 2\beta)V_x = 12$$

$$V_y = 0$$

$$-(3 + 2\beta)\frac{24}{7} = 12$$

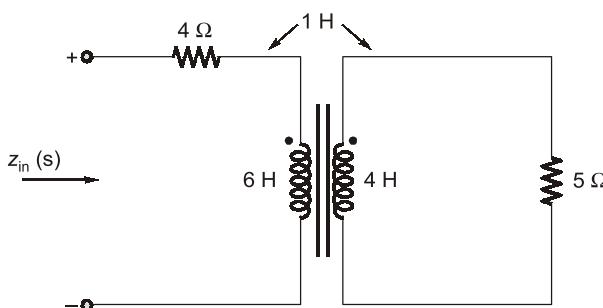
$$(3 + 2\beta) = \frac{-7}{2}$$

$$2\beta = \frac{-7}{2} - 3 = \frac{-7 - 6}{2} = \frac{-13}{2}$$

$$\beta = \frac{-13}{4} = -3.25$$

End of Solution

Q.42 The input impedance $Z_{in}(s)$, for the network shown in



(a) $7s + 4$

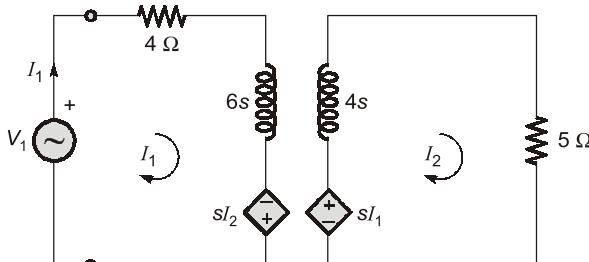
(b) $\frac{23s^2 + 46s + 20}{4s + 5}$

(c) $\frac{25s^2 + 46s + 20}{4s + 5}$

(d) $6s + 4$

Ans. (b)

Circuit in s-domain,



$$-sI_1 + (4s + 5)I_2 = 0$$

$$\Rightarrow I_2 = \frac{s}{4s+5} I_1$$

$$V_1 = (4 + 6s)I_1 - \frac{s^2}{4s+5} I_1$$

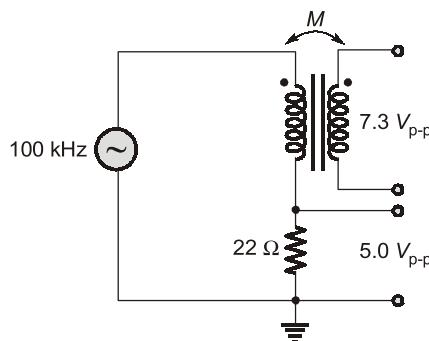
$$\frac{V_1}{I_1} = \frac{(4 + 6s)(4s + 5) - s^2}{4s + 5}$$

$$= \frac{24s^2 + 30s + 16s + 20 - s^2}{4s + 5}$$

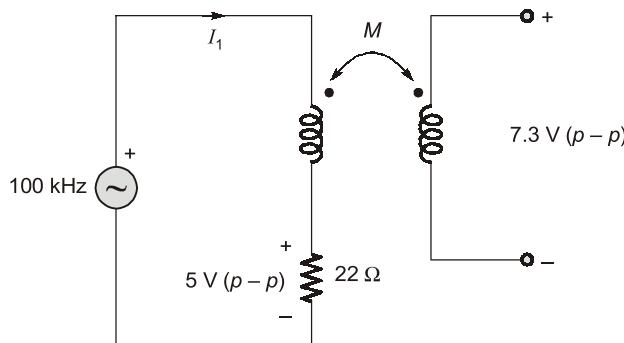
$$Z_{in} = \frac{23s^2 + 46s + 20}{4s + 5}$$

End of Solution

- Q.43** An air-core radio-frequency transformer as shown has a primary winding and a secondary winding. The mutual inductance M between the windings of the transformer is _____ μH , (Round off to 2 decimal places.)



Ans. 51.10 (50.00 to 52.00)



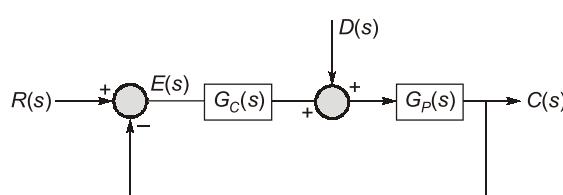
$$I_1 = \frac{5}{22} (p-p)$$

$$V_o = j\omega MI_1 = 7.3 = (2\pi \times 10 \times 10^3) \times M \times \left(\frac{5}{22}\right)$$

$$M = 51.10 \mu\text{H}$$

End of Solution

Q.44 In the given figure, plant $G_p(s) = \frac{2.2}{(1+0.1s)(1+0.4s)(1+1.2s)}$ and compensator $G_c(s) = K \left(\frac{1+T_1s}{1+T_2s} \right)$. The external disturbance input is $D(s)$. It is desired that when the disturbance is a unit step, the steady-state error should not exceed 0.1 unit. The minimum value of K is _____ . (Round off to 2 decimal places)



Ans. -10.45 (-11.00 to -10.00)

$$e_{ss} = \lim_{s \rightarrow 0} \left[\frac{sR}{1+G_C G_P} - \frac{sD G_P}{1+G_C G_P} \right]$$

$$R(s) = 0; D(s) = \frac{1}{s}$$

$$\therefore e_{ss} = \frac{2.2}{1+2.2K} = 0.1$$

$$\therefore K_{\min} = -10.45$$

End of Solution



ESE 2021

Mains Exam Conventional Batches

Mode: Live/Online & Offline

Batches commencing from
1st Week of April, 2021

**Duration
75 days**

Total 275-300
Teaching hours

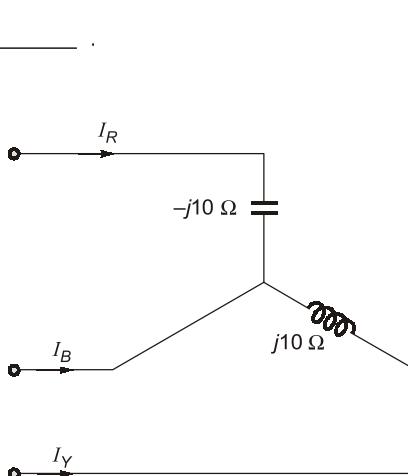
Streams:
CE, ME, EE, E&T

**More Details will
be updated shortly
at our website**

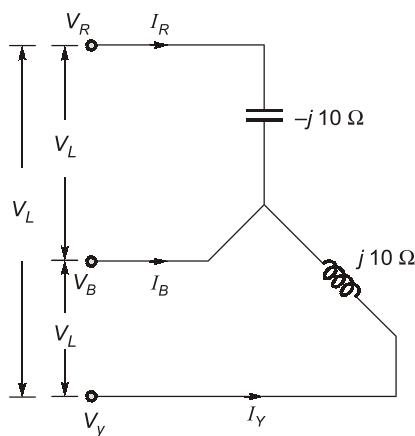


www.madeeasy.in

Q.45 A three-phase balanced voltage is applied to the load shown. The phase sequence is RYB. The ratio $\frac{|I_B|}{|I_R|}$ is _____.



Ans. (1)



$$I_R = \frac{V_{RB}}{-j10} = \frac{V_L \angle -60^\circ}{-j10} = \frac{V_L}{10} \angle 30^\circ$$

$$I_Y = \frac{V_{YB}}{j10} = \frac{V_L \angle -120^\circ}{-j10} = \frac{V_L}{10} \angle 150^\circ$$

and

$$I_B = -(I_R + I_Y) = \frac{V_L}{10} \angle -90^\circ$$

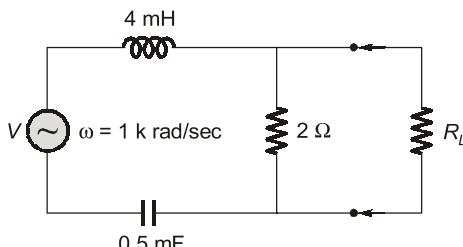
∴

$$\frac{|I_B|}{|I_R|} = 1$$

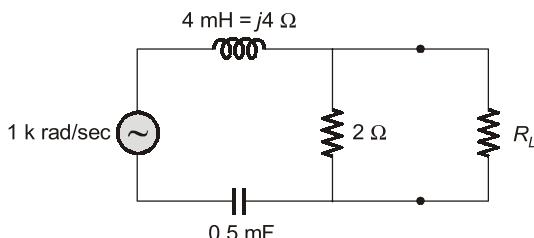
End of Solution

Q.46 In the given circuit, for maximum power to be delivered to R_L , its value should be Ω .

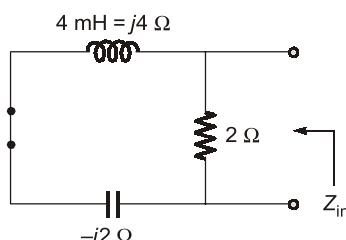
(Round off to 2 decimal places)



Ans. 1.41 (1.40 to 1.42)



$$= \frac{-j}{\omega C} = \frac{-j}{1000 \times 0.5 \times 10^{-3}} = -j2\Omega$$



$$Z_{in} = 2 \| j2 = \frac{j4}{2+j2} = \frac{j2}{1+j1}$$

For maximum power transfer,

$$R_L = |Z_{TH}| = \frac{2}{\sqrt{2}} = \sqrt{2} = 1.414 \Omega$$

End of Solution

Q.47 In a single-phase transformer, the total iron loss is 2500 W at nominal voltage of 440 V and frequency 50 Hz. The total iron loss is 850 W at 220 V and 25 Hz. Then, at nominal voltage and frequency, the hysteresis loss and eddy current loss respectively are

Ans. (b)

$$W_{i1} = 2500 \text{ W at } 440 \text{ V, } 50 \text{ Hz}$$

$$W_{i2} = 850 \text{ W at } 220 \text{ V, } 25 \text{ Hz}$$

$$W_{i3} = R_{e3} + P_{h3} \text{ at } 440 \text{ V, } 50 \text{ Hz}$$

$$R_{e3} = ?, \quad P_{h3} = ?, \quad \frac{V}{f} = \text{constant}$$

$$\Rightarrow 2500 = Af + Bf^2 \quad \left\{ \frac{400}{50} = \frac{220}{25} = \text{Constant} \right\}$$

$$\text{or, } \frac{2500}{f} = A + Bf$$

$$\text{or, } \frac{2500}{50} = A + B(50) \quad \dots(i)$$

$$\text{and } \frac{850}{25} = A + B(25) \quad \dots(ii)$$

Solving (i) and (ii), we get

$$25B = \frac{2500}{50} - \frac{850}{25} = \frac{2500 - 1700}{50}$$

$$= \frac{800}{50} = 16$$

$$B = \frac{16}{25}$$

$$\text{and from (i), } A = 50 - \frac{16}{25} \times 50 = 50 - 32 = 18$$

So, at 50 Hz

$$P_h = Af = 18 \times 50 = 900 \text{ W}$$

$$P_e = B^2 = \left(\frac{16}{25}\right) \times (50)^2 = 1600 \text{ W}$$

End of Solution
Q.48 The causal signal with z-transform $z^2(z - a)$ is ($u[n]$ is the unit step signal)

- | | |
|-----------------------|-----------------------|
| (a) $n^{-1} a^n u[n]$ | (b) $(n + 1)a^n u[n]$ |
| (c) $n^2 a^n u[n]$ | (d) $a^{2n} u[n]$ |

Ans. (b)

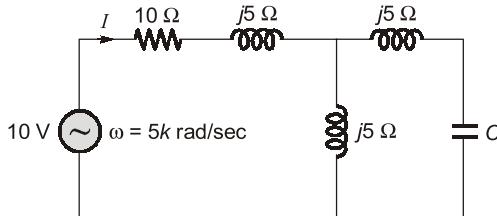
As we know,

$$n.a^n u(n) \Leftrightarrow \frac{az}{(z-a)^2}$$

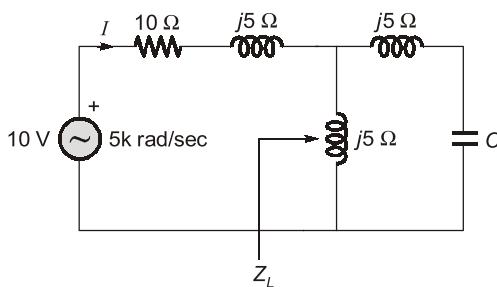
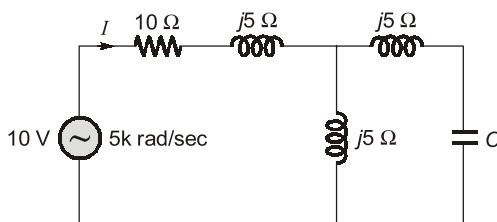
$$\frac{1}{a} \cdot n.a^n u(n) \Leftrightarrow \frac{z}{(z-a)^2}$$

$$f(n) = n.a^{n-1} u(n) \Leftrightarrow \frac{z}{(z-a)^2} = F(z)$$

Q.51 In the given circuit, the value of capacitor C that makes current $I = 0$ is _____ μF .



Ans. 20.00 (19.90 to 20.10)



$$Z_L = (j5) \parallel (j5 - jX_c)$$

$$\frac{(j5)(j5 - jX_c)}{j5 + j5 - jX_c} = \infty$$

$$\sqrt{5} + \sqrt{5} - jX_c = 0$$

$$\Rightarrow \quad jX_c = j10 \\ \Rightarrow \quad X_c = 10 \Omega$$

$$X_c = \frac{1}{\omega C} = 10$$

$$\Rightarrow \quad C = \frac{1}{10 \times 5 \times 10^3}$$

$$C = \frac{1}{5 \times 10^4} \times \frac{10^2}{10^2} = \frac{10^2}{5 \times 10^6} = 20 \mu\text{F}$$

End of Solution

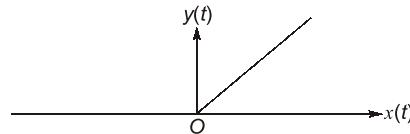
Q.52 If the input $x(t)$ and output $y(t)$ of a system are related as $y(t) = \max(0, x(t))$, then the system is

- | | |
|---------------------------------|-----------------------------------|
| (a) non-linear and time variant | (b) linear and time-variant |
| (c) linear and time-invariant | (d) non-linear and time-invariant |

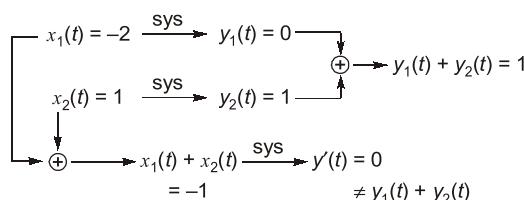
Ans. (d)

$$y(t) = \max(0, x(t))$$

$$= \begin{cases} 0, & x(t) < 0 \\ x(t), & x(t) > 0 \end{cases}$$


Linearity check :

 at input $x_1(t) = -2$, output $y_1(t) = 0$

 at input $x_2(t) = 1$, output $y_2(t) = 1$

∴ system is non-linear because it violates law of additivity.
Check for time-invariance :

Delayed O/P :

$$y(t - t_o) = \begin{cases} x(t - t_o), & x(t - t_o) > 0 \\ 0, & x(t - t_o) < 0 \end{cases}$$

 O/P of system when input is $x(t - t_o) = f(t)$

$$y_1(t) = \begin{cases} f(t), & f(t) > 0 \\ 0, & f(t) < 0 \end{cases} = \begin{cases} x(t - t_o), & x(t - t_o) > 0 \\ 0, & x(t - t_o) < 0 \end{cases}$$

Therefore, system is time-invariant.

End of Solution
Q.53 Two generators have cost functions F_1 and F_2 . Their incremental-cost characteristics are

$$\frac{dF_1}{dP_1} = 40 + 0.2P_1 ; \quad \frac{dF_2}{dP_2} = 32 + 0.4P_2$$

 They need to deliver a combined load of 260 MW. Ignoring the network losses, for economic operation, the generation P_1 and P_2 (in MW) are

- | | |
|----------------------------|----------------------------|
| (a) $P_1 = 160, P_2 = 100$ | (b) $P_1 = P_2 = 130$ |
| (c) $P_1 = 120, P_2 = 140$ | (d) $P_1 = 140, P_2 = 120$ |

Ans. (a)

$$IC_1 = IC_2$$

$$40 + 0.2P_1 = 32 + 0.4P_2$$

$$0.4P_2 - 0.2P_1 = 8 \quad \dots(i)$$

$$P_2 + P_1 = 260 \quad \dots(ii)$$

Solving equation (i) and (ii),

$$P_1 = 160 \text{ MW}; \quad P_2 = 100 \text{ MW}$$

End of Solution

Q.54 Suppose the probability that a coin toss shows "head" is p , where $0 < p < 1$. The coin is tossed repeatedly until the first "head" appears. The expected number of tosses required is

- (a) $\frac{(1-p)}{p}$
- (b) $\frac{1}{p}$
- (c) $\frac{1}{p^2}$
- (d) $\frac{p}{(1-p)}$

Ans. (b)

$$P(H) = p, \text{ let } x = \text{Number of tosses}$$

x	1	2	3	4	5...
$P(x)$	p	$(1-p)p$	$(1-p)^2p$		

$$\begin{aligned} E(x) &= \sum x_i P(x) = p + 2(1-p)p + 3(p)(1-p)^2 + \dots \\ &= p[1 + 2(1-p) + 3(1-p)^2 + \dots] \\ &= p[1 - (1-p)]^{-2} = \frac{1}{p} \end{aligned}$$

End of Solution

Q.55 Two discrete-time linear time-invariant systems with impulse response $h_1[n] = \delta[n-1] + \delta[n+1]$ and $h_2[n] = \delta[n] + \delta[n-1]$ are connected in cascade, where $\delta[n]$ is the Kronecker delta. The impulse response of the cascaded system is

- (a) $\delta[n-2] + \delta[n+1]$
- (b) $\delta[n-2] + \delta[n-1] + \delta[n] + \delta[n+1]$
- (c) $\delta[n-1] \delta[n] + \delta[n+1] \delta[n-1]$
- (d) $\delta[n] \delta[n-1] + \delta[n-2] \delta[n+1]$

Ans. (b)

$$\begin{aligned} h(n) &= \text{Resultant impulse response} \\ &= h_1(n) * h_2(n) \end{aligned}$$

By applying z-transform

$$\begin{aligned} H(z) &= H_1(z)H_2(z) \\ &= (z + z^{-1})(1 + z^{-1}) \\ &= z + z^{-1} + 1 + z^{-2} \end{aligned}$$

By applying inverse ZT,

$$h(n) = \delta(n+1) + \delta(n-1) + \delta(n) + \delta(n-2)$$

End of Solution





MADE EASY

India's Best Institute for IES, GATE & PSUs

POSTAL PACKAGE



- CSE
- ESE
- GATE
- PSUs
- SSC-JE
- RRB-JE
- MPSC
- OPSC
- BPSC
- Other State Engineering Services Exams

“ Postal Study Package is the distance learning program designed to meet the needs of the college going students, working professionals and those who are unable to join the classroom courses. The study material is compact, yet comprehensive & effective and easy to understand. MADE EASY has made all efforts to provide an error free material introducing smart and shortcut techniques for better understanding. ”

Salient Features of Postal Study Package

- 🌐 Full Emphasis on both technical and non-technical aspects (Including GS, Aptitude, Reasoning and Engineering Mathematics).
- 📋 Subjectwise Theory and practice sets.
- 📄 Previous year questions along with solutions.
- 📚 Revised and updated study material.
- ⭐ Proven track record of making students succeed.

Note :

1. The study material is usually sent in 2 or more packages.
2. Current Affairs for ESE will be sent 1 month prior to examination.

For book list, fee structure & online purchasing, visit : www.madeeasy.in

One can also buy by walk-in at any MADE EASY centre across India. Material will be dispatched to his/her address.

Dispatch procedure: After receiving the online order/demand draft we ship the material within a week, however delivery timing may vary depending on the destination (location).

Address : Corporate Office: 44-A/1, Kalu Sarai, Sarvapriya Vihar, Near Hauz Khas Metro Station, New Delhi-110016

Ph: 011-45124645, 08860378004

E-mail: postalstudycourse@madeeasy.in