

2019

**RANK IMPROVEMENT  
WORKBOOK**

**Mechanical Engineering**

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**Theory of Machines**

Answer Key of Objective & Conventional Questions



**MADE EASY**  
Publications

# 1

## Mechanisms and Machines

### LEVEL 1 Objective Questions

1. (c)
2. (c)
3. (a)
4. (a)
5. (c)
6. (a)
7. (d)
8. (d)
9. (d)
10. (a)
11. (c)
12. (d)
13. (d)

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### LEVEL 2 Objective Questions

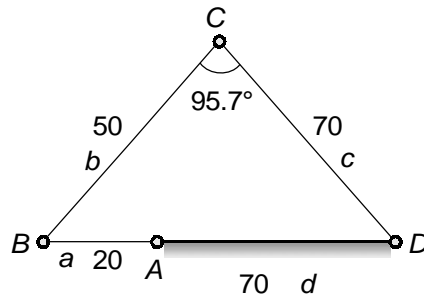
14. (6)
15. (1)
16. (c)
17. (1)
19. (c)
20. (c)
21. (b)
22. (a)
23. (b)
24. (b)
25. (1)
26. (a)
27. (180)

■■■■

**LEVEL 3** Conventional Questions

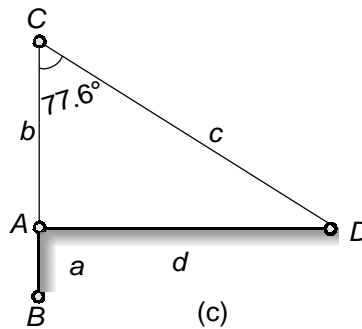
**Solution : 28**

In this mechanism



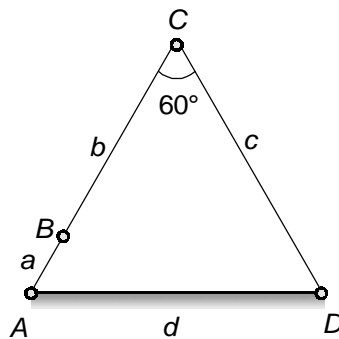
(a)

$$\mu = 95.7^\circ$$



(c)

$$\mu = 45.6^\circ$$



(d)

$$\mu = 60^\circ$$

And the input angle,  $\theta = 60^\circ$

**Solution : 29**

The mechanism has three sub-chains:

- (i)  $ABC$ , a slider-crank chain
- (ii)  $ABDE$ , a four-bar chain
- (iii)  $AEFG$ , a four-bar chain

( $DEF$  is a locked chain as it has only three links.)

- As the length  $BC$  is more than the length  $AB$  plus the offset of 2 units,  $AB$  acts as a crank and can revolve about  $A$ .

- In the chain  $ABDE$ ,

Length of the longest link = 8, Length of the shortest link = 4, Length of the other links = 8 and 6

Since  $8 + 4 < 8 + 6$ , it belongs to the class-I mechanism. In this case as the shortest link is fixed, it is a double-crank mechanism and thus  $EF$  and  $AG$  can revolve fully.

- In the chain  $AEFG$ ,

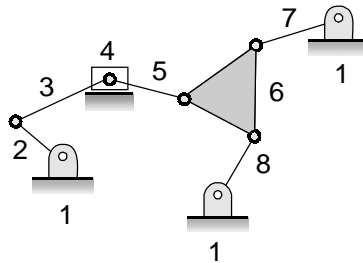
Length of the longest link = 8, Length of the shortest link = 4, Length of the other links = 6 and 6

Since  $8 + 4 = 6 + 6$ , it belongs to the class-I mechanism. In this case as the shortest link is fixed, it is a double-crank mechanism and thus  $EF$  and  $AG$  can revolve fully.

As  $DEF$  is a locked chain with three links, the link  $EF$  revolves with the revolving of  $ED$ . With the revolving of  $ED$ ,  $AG$  also revolves.

**Solution : 30**

- (a) The mechanism has a sliding pair. Therefore, its degree of freedom must be found from Gruebler's criterion. Total number of links = 8



(At the slider, one sliding pair and two turning pairs)

$$\begin{aligned} F &= 3(N - 1) - 2P_1 - P_2 \\ &= 3(8 - 1) - 2 \times 10 - 0 = 1 \end{aligned}$$

Thus, it is a mechanism with a single degree of freedom.

- (b) The system has a redundant degree of freedom as the rod of the mechanism can slide without causing any movement in the rest of the mechanism.

$$\begin{aligned} \therefore \text{Effective degree of freedom} &= 3(N - 1) - 2P_1 - P_2 - F_r \\ &= 3(4 - 1) - 2 \times 4 - 0 - 1 = 0 \end{aligned}$$

As the effective degree of freedom is zero, it is a locked system.



# 2

## Velocity & Acceleration Analysis

### LEVEL 1 Objective Questions

1. (b)
2. (0.33)
3. (d)
4. (c)
5. (b)
6. (d)
7. (0)
8. (b)
9. (1)
10. (b)
11. (c)

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### LEVEL 2 Objective Questions

12. (67) (66.5 to 67.5)
13. (a)
14. (301.59)
15. (2.74)
16. (a)
17. (3)
18. (1000)
19. (45)
20. (2.69)
21. (8.386)
22. (a)

■■■■

## LEVEL 3 Conventional Questions

**Solution : 23**

$$v_d = gd = 0.56 \text{ m/s}$$

$$\omega_{bq} = 5.63 \text{ rad/s}$$

$$\omega_{ba} = 6.3 \text{ rad/s}$$

counter-clockwise

counter-clockwise

Velocity of rubbing at the crank pin

$$B = 0.0268 \text{ m/s}$$

**Solution : 24**

$$v_s = 0.276 \text{ m/s}$$

$$v_{pq} = 0.177 \text{ m/s}$$

$$\omega_{rs} = 0.279 \text{ rad/s clockwise}$$

**Solution : 25**

$$v_d = 2.28 \text{ m/s}$$

**Solution : 26**

$$\alpha_{cd} = 33.25 \text{ rad/s}^2$$

**Solution : 27**

$$a_{A/O} = 3.507 \times 10^3 \text{ mm/s}^2$$

$$V_B = 2.3 \times 4 = 9.2 \text{ m/s}$$

$$a_B = 2.6 \times 10^5 \text{ m/s}^2$$

$$\alpha = 6666.67 \text{ rad/s}^2$$

$$a_G = 2800 \text{ m/s}^2$$

Acceleration of mid point

**Solution : 28**By measurement  $V_R = \text{vector } O_1r = 1.61 \text{ m/s}$ 

$$\omega_{DO_2} = 1.112 \text{ rad/s anticlockwise about } O_2$$

**Solution : 29**

Length of crank = 25 cm

$$V = 4.1887 \text{ m/s}$$



**LEVEL 1** Objective Questions

1. (c)

2. (c)

3. (c)

4. (a)

5. (a)

6. (c)

7. (c)

8. (c)

9. (c)

11. (c)

12. (b)

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**LEVEL 2** Objective Questions

13. (2.37)

14. (720)

15. (0.628)

16. (1.95)

17. (d)

18. (b)

19. (d)

20. (d)

21. (c)

22. (a)

23. (c)

24. (b)

25. (a)

26. (b)

27. (b)

28. (a)

29. (d)

■■■■

**LEVEL 3** Conventional Questions

**Solution : 30**

During descent

$$V_{\max} = 226.3 \text{ mm/s}$$

$$f_{\max} = 3.413 \text{ m/s}^2$$

$$V_{\max} = 216 \text{ mm/s}$$

$$f_{\max} = f = 0$$

**Solution : 31**

During descent

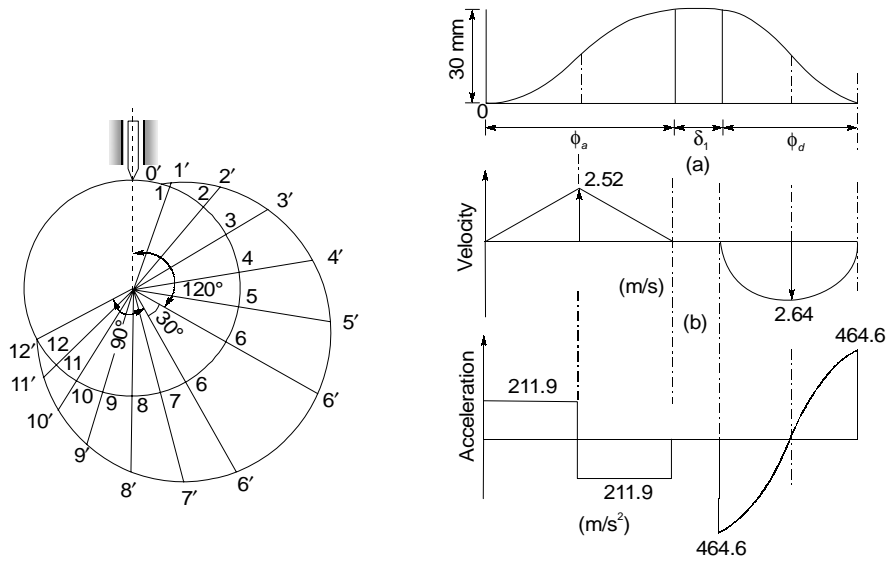
$$V_{\max} = 824.7 \text{ mm/s}$$

$$V_{\max} = 549.8 \text{ mm/s}$$

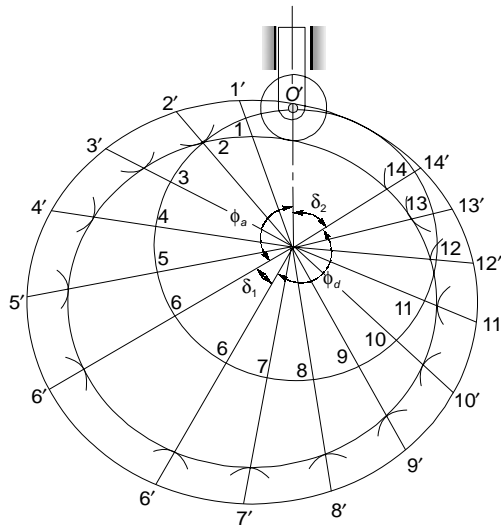
$$f_{\max} = 38862 \text{ mm/s}^2 = 38.882 \text{ m/s}^2$$

$$f_{\max} = 17272 \text{ mm/s}^2 \text{ or } 17.272 \text{ m/s}^2$$

**Solution : 32**



**Solution : 33**





$$V_{\max} = 360 \text{ m/s}$$

$$f_{\max} = 4320 \text{ mm/s}^2 \text{ or } 4.32 \text{ m/s}^2$$

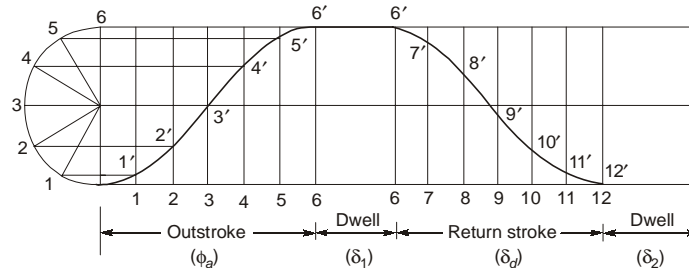
**Solution : 34**

$$\ddot{x} = 40 \omega^2 \cos \theta$$

$$N = 609.9 \text{ rpm}$$

**Solution : 35**

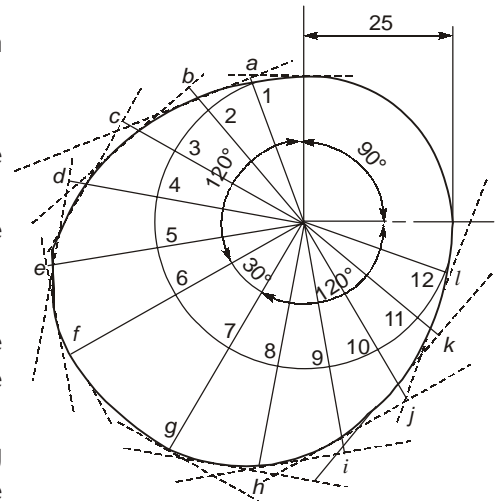
The displacement diagram for the given flat reciprocating follower movement will be as:



Given:  $\phi_a = 120^\circ$ ,  $h(\text{lift}) = 20 \text{ mm}$ ,  $\delta_1 = 30^\circ$ ,  $\phi_d = 120^\circ$ ,  $\delta_2 = 90^\circ$   
Motion is SHM both during outward and inward stroke, minimum radius of cam ( $r_c$ ) = 25 mm.

Construction:

1. First draw the displacement diagram now construct the cam profile as follows
2. Draw a circle with radius ( $r_c = 25 \text{ mm}$ )
3. Take angles ( $\phi_a$ ,  $\delta_1$ ,  $\phi_d$  and  $\delta_2$ ) in the counter clockwise direction if the cam rotation is assumed clockwise
4. Divide  $\phi_a$  and  $\phi_d$  into same number of parts as in the displacement diagram. (Example take 6 equal parts)
5. Draw radial lines (0-1, 0-2, 0-3,, etc. ....)
6. On the radial lines produced, take distances equal to the lift of the follower beyond the circumference of the circle with radius  $r_c$ , i.e., 1 - 1', 2 - 2', 3 - 3', etc.
7. Draw the follower in all the positions by drawing perpendiculars to the radial lines at 1', 2', 3', etc. In all the positions, the axis of the follower passes through centre O
8. Draw a curve tangential to the flat faces of the follower representing the cam profile.



**Solution : 36**

Radial component of cam force is given by;

$$F_r = 61 \text{ N}$$

$$\text{Torque} = 0.651 \text{ N.m}$$

**Solution : 37**

In this motion:

$$(V_0)_{\max} = 1.2 \text{ m/s}$$

$$a = 72 \text{ m/s}^2$$



# 4

## Gear and Gear Train

### LEVEL 1 Objective Questions

1. (c)
2. (7.48)
3. (91)
4. (360)
5. (a)
6. (c)
7. (b)
8. (d)
9. (d)
10. (d)
11. (c)
12. (39207.076)

### LEVEL 2 Objective Questions

13. (c)
14. (c)
15. (b)
16. (a)
17. (b)
18. (b)
19. (b)

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20. (a)
21. (a)
22. (c)
23. (0.86)
24. (10.29)
25. (9.04)
26. (c)
27. (b)
28. (a)
29. (c)
30. (b)
31. (c)
32. (b)
33. (b)
34. (a)
35. (d)
36. (c)
37. (d)
38. (70)
39. (d)
40. (18)
41. (c)



**LEVEL 3** Conventional Questions

**Solution : 42**

$$\text{Velocity of sliding} = 57049 \text{ mm/min} = 950.8 \text{ mm/s}$$

$$\text{Maximum velocity of sliding} = 1017.1 \text{ mm/s}$$

**Solution : 43**

$$\text{Addendum of the wheel} = 8.3 \text{ mm}$$

$$r_a^2 = 30271$$

$$\text{Addendum of the pinion} = 14 \text{ mm}$$

$$\text{Arc of contact} = 58.2 \text{ mm}$$

**Solution : 44**

$$\text{Length of arc of contact} = 30.788 \text{ mm}$$

$$n = 1.6334$$

$$\text{Angle of action by the pinion, } \theta_p = 0.54 \text{ radian}$$

$$\theta_p = 30.95^\circ$$

(a)  $= 0.388$

(b)  $= 0.348$

(c)  $= 0$

**Solution : 45**

$$T = 49.44$$

$$n = 1.78$$

**Solution : 46**

$$\text{Addendum, } a = 0.8010 \text{ m}$$

$$\text{Stubbing required} = 19.9\% \text{ or } 20\%$$

**Solution : 47**

$$T_F = 72$$

$$T_S = 18$$

$$\text{Speed of } P, N_p = -166.67 \text{ rpm}$$

Therefore, speed of planet Gear  $P$  is 166.67 rpm in opposite direction to  $S$  and  $A$ .

**Solution : 48**

$$\text{Speed of output shaft} = -50 \text{ rpm (clockwise)}$$

$$\text{Speed of output shaft} = 39.5 \text{ rpm (clockwise)}$$



# 5

## Flywheel and Governors

### LEVEL 1 Objective Questions

1. (c)
2. (d)
3. (d)
4. (d)
5. (243.17)
6. (0.04)
7. (0.38)
8. (d)
9. (a)
10. (d)
11. (206.04)
12. (b)
13. (a)
14. (a)
15. (c)
16. (d)
17. (a)

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### LEVEL 2 Objective Questions

18. (d)
19. (323.6)
20. (991.735)
21. (183.33)
22. (22360)
23. (0.38)
24. (d)
25. (b)
26. (0.51)
27. (31.98)
28. (0.0444)
29. (51.3)
30. (31.4)(30 to 33)
31. (b)
32. (c)
33. (c)
34. (c)
35. (a)
36. (d)



**LEVEL 3** Conventional Questions

**Solution : 37**

$$m = 1217.4 \text{ kg}$$

**Solution : 38**

$$I = 293.3 \text{ kg.m}^2$$

**Solution : 39**

$$\text{Power of motor} = 4276.5 \text{ Watt} = 4.28 \text{ kW}$$

**Solution : 40**

$$\begin{aligned} \text{Motor power} &= 0.3 \text{ kW} \\ M &= 988.68 \text{ kg} \end{aligned}$$

**Solution : 41**

$$\begin{aligned} N &= 167 \text{ rpm} \\ \text{Range of speed} &= 4.163 \text{ rpm} \end{aligned}$$

**Solution : 42**

$$\begin{aligned} m &= 5.2 \text{ kg} \\ s &= 32.72 \text{ N/mm} \\ \text{compression of the spring} &= 33.2 \text{ mm} \end{aligned}$$

**Solution : 43**

$$I = 1394.58 \text{ kg-m}^2$$

**Solution : 44**

$$K = 0.678\%$$

**Solution : 45**

$$N = 430.43 \text{ rpm}$$

**Solution : 46**

$$\begin{aligned} \text{Power of engine} &= 261.8 \text{ kW} \\ I &= 785.166 \text{ kg-m}^2 \\ \alpha &= 2.547 \text{ rad/sec}^2 \end{aligned}$$

**Solution : 47**

$$\begin{aligned} \text{Initial compression, } S_1 &= 10.03 \text{ cm} \\ x_1 &= 11.65 \text{ cm} \end{aligned}$$



# 6

## Balancing and Gyroscope

### LEVEL 1 Objective Questions

1. (c)
2. (d)
3. (b)
4. (a)
5. (d)
6. (c)
7. (a)
8. (a)
9. (b)

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### LEVEL 2 Objective Questions

10. (d)
11. (c)
12. (a)
13. (a)
14. (a)
15. (a)
16. (a)

■■■■

**LEVEL 3** Conventional Questions

**Solution : 17**

$$v = 151 \text{ km/h}$$

**Solution : 18**

$$m_{c1} = 3.13 \text{ kg at } 253^\circ$$

$$m_{c1} = 3.14 \text{ kg}$$

**Solution : 19**

$$m_a = 17.37 \text{ kg}$$

$$\theta_a = 294.6^\circ \text{ or } 294^\circ 36'$$

$$l_d = -309 \text{ mm}$$

$$l_b = -376 \text{ mm}$$

$$l_c = -126 \text{ mm}$$

**Solution : 20**

$$m_4 = 178.7 \text{ kg}$$

$$\theta_4 = 248.2^\circ$$

$$m_1 = 178.7 \text{ kg} = m_4$$

$$\theta_1 = 201.8^\circ$$

$$\text{Swaying couple} = 3030.3 \text{ N.m}$$

$$\text{Variation in tractive force} = 10100 \text{ N}$$

$$\text{Balance mass for reciprocating parts only} = 74.46 \text{ kg}$$

$$\text{Maximum pressure on rails} = 45326 \text{ N}$$

$$\text{Minimum pressure on rails} = 23344 \text{ N}$$

$$\text{Velocity of wheels} = 88.36 \text{ km/h}$$

**Solution : 21**

$$m_3 = 448 \text{ kg}$$

$$m_2 = 438 \text{ kg}$$

**Solution : 22**

$$R_1 = 4431.8 \text{ N}$$

$$R_2 = 8223.8 \text{ N}$$

$$R_3 = 2567.2 \text{ N}$$

$$R_4 = 6359.2 \text{ N}$$

$$R_1 = 8158.2 \text{ N}$$

$$R_2 = 4366.2 \text{ N}$$

$$R_3 = 6426.8 \text{ N}$$

$$R_4 = 2632.8 \text{ N}$$

**Solution : 23**

Reaction at bearing,  $B = 98.6 \text{ N}$

Reaction at bearing,  $A = 59.4 \text{ N}$

**Solution : 24**

$$m_A = 9.67 \text{ kg}, m_D = 7.89 \text{ kg}$$

Angular position of the mass at  $D = 252.7^\circ$  (w.r.t.  $B$ )

**Solution : 25**

$$m = 92.8 \text{ kg}$$

$$\theta = 201.48^\circ$$

**Solution : 26**

$$\text{Resultant} = 8224.6 \text{ N}$$

$$M = 40 \text{ kg}$$





**LEVEL 1** Objective Questions

1. (d)

2. (d)

3. (d)

4. (a)

5. (a)

6. (3)

7. (b)

8. (d)

9. (d)

10. (d)

11. (b)

12.. (a)

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**LEVEL 2** Objective Questions

13. (b)

14. (a)

15. (1.11)

16. (c)

17. (b)

18. (2.28)

19. (0.56)

20. (26.74)

21. (1.9052)

22. (a)

23. (0.667)

24. (1)

25. (8)

26. (2)

27. (0.05)

■■■■

**LEVEL 3** Conventional Questions
**Solution : 28**

$$\frac{1}{2} a l p \times 2 \ddot{x} + a p g \times 2 x \dot{x} = 0$$

$$\ddot{x} + \frac{2g}{l} x = 0$$

**Solution : 29**

$$A = 0.00298 \text{ m} = 2.98 \text{ mm}$$

**Solution : 30**

$$f_n = 2.85 \text{ Hz}$$

**Solution : 31**

$$\delta = 0.693$$

$$C = 45.809 \text{ Nm/rad}$$

$$\text{periodic time of oscillation} = 1.503 \times 10^{-3} \text{ sec}$$

$$f_n = 669.2 \text{ Hz}$$

**Solution : 32**

$$\omega_d = \sqrt{\frac{k_1 l_1^2 + m g l}{m l^2} - \left( \frac{C l_2}{2 m l^2} \right)^2}$$

**Solution : 33**

$$N_c = 2598 \text{ r.p.m}$$

**Solution : 34**

$$C = 400.824 \text{ N/m/s}$$

$$\frac{f_d}{f_n} = 0.99$$

$$T_d = 0.32 \text{ sec}$$

**Solution : 35**

$$\delta = 0.405$$

$$\text{Damping coefficient, } C = 32.745 \text{ N.m.s/rad}$$

$$\omega_d = 4233.72 \text{ rad/s}$$

$$T_d = 1.484 \times 10^{-3} \text{ s}$$

**Solution : 36**

$$F_T = 38.6 \text{ N}$$

$$F_T = 367 \text{ N}$$

Amplitude of the forced vibration of the machine at resonance = 8.7 mm

**Solution : 37**

$$C = 2970 \text{ N-m/rad}$$

**Solution : 38**

$$A = 130 \text{ mm}$$

$$\phi = 42.4897^\circ$$

**Solution : 39**

$$k = 1.607 \text{ N/mm}$$

