



MADE EASY

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Important Questions
for **GATE 2022**

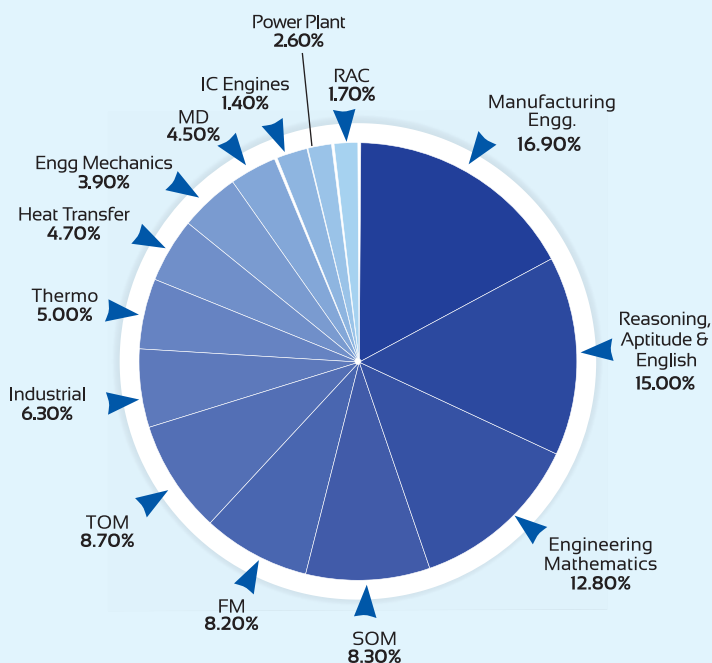
**MECHANICAL
ENGINEERING**

Day 8 of 8

Q.176 - Q.200 (Out of 200 Questions)

**Power Plant +
Engineering Materials +
Strength of Materials**

SUBJECT-WISE WEIGHTAGE ANALYSIS OF GATE SYLLABUS



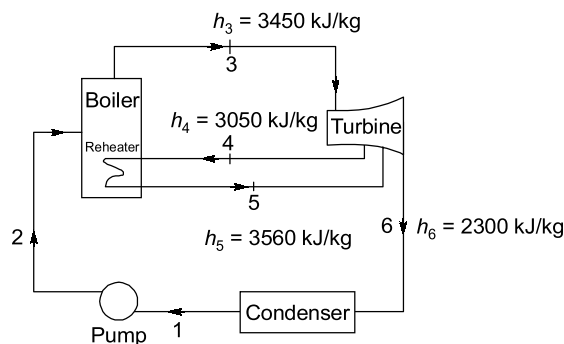
Subject	Average % (last 5 yrs)
Manufacturing Engineering	16.90%
Reasoning, Aptitude & English	15.00%
Engineering Mathematics	12.80%
Strength of Materials	8.30%
Theory of Machines	8.70%
Fluid Mechanics & Hydraulic Machines	8.20%
Industrial Engineering	6.30%
Thermodynamics	5.00%
Heat Transfer	4.70%
Engineering Mechanics	3.90%
Machine Design	4.50%
Internal Combustion Engines	1.40%
Power Plant Engineering	2.60%
Refrigeration & Air Conditioning	1.70%
Total	100%

Power Plant + Engineering Materials + Strength of Materials

Q.176 A steam power plant operates on a theoretical reheat cycle as shown below. Steam enters high pressure turbine at 150 bar and 550°C ($h_3 = 3450$ kJ/kg) and expands upto 40 bar ($h_4 = 3050$ kJ/kg). It is reheated at constant pressure to 550°C ($h_5 = 3560$ kJ/kg) and expands through the low pressure turbine to a condenser at 0.1 bar ($h_6 = 2300$ kJ/kg).

Also given, h_{f1} (at 0.1 bar) = 191.8 kJ/kg.

Thermal efficiency (in %) and steam rate (kg/kWh) of the plant neglecting pump work are, respectively



- (a) 44.05 and 4.34 (b) 48.10 and 5.12
(c) 42.10 and 3.10 (d) 44.05 and 2.17

Q.177 In order to control the temperature of steam in a steam generator, a spray type desuperheater is used. It is fed with water at 60°C. Steam at 90 bar and 500°C with flow rate 300 tons/hr enters the desuperheater. Neglect any pressure drop due to mixing and heat loss to the surrounding. Also given

$$h_g \text{ (at 90 bar and 500°C)} = 3386.1 \text{ kJ/kg}$$

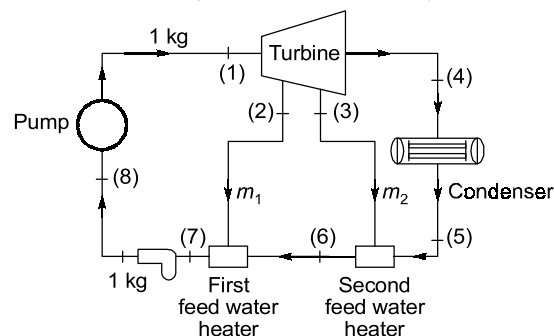
$$h_f \text{ (at 60°C)} = 251.11 \text{ kJ/kg}$$

$$h_g \text{ (at 90 bar and 450°C)} = 3256.6 \text{ kJ/kg}$$

Amount of water that must be sprayed to maintain steam at 450°C is _____ kg/s.

[Correct upto 1 decimal place]

Q.178 A steam power plant operates on regenerative steam cycle as shown in figure.



Given :

$$h_2 = 2679 \text{ kJ/kg}, h_3 = 2365 \text{ kJ/kg}, h_{f5} = 137.8 \text{ kJ/kg}, h_{f6} = 467.1 \text{ kJ/kg} \text{ and } h_{f7} = 762.6 \text{ kJ/kg}$$

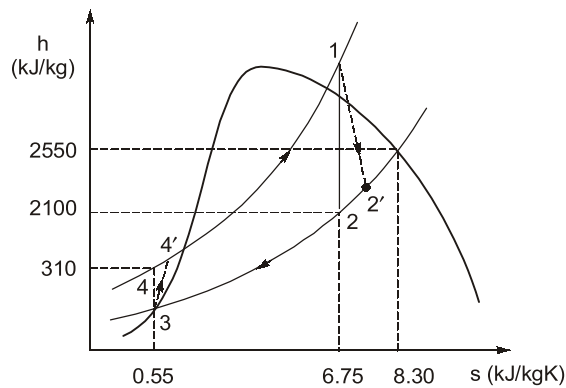
Total mass of steam ($m_1 + m_2$) extracted from the two points of the turbine is _____ kg.

[Correct upto 2 decimal places]

Q.179 In an ideal Brayton cycle with 100% efficient regeneration, argon gas is compressed from 100 kPa and 25°C to 400 kPa, and then heated to 1200°C before entering the turbine. The highest temperature that argon can be heated in the regenerator is _____ °C. [Correct upto two decimal places]

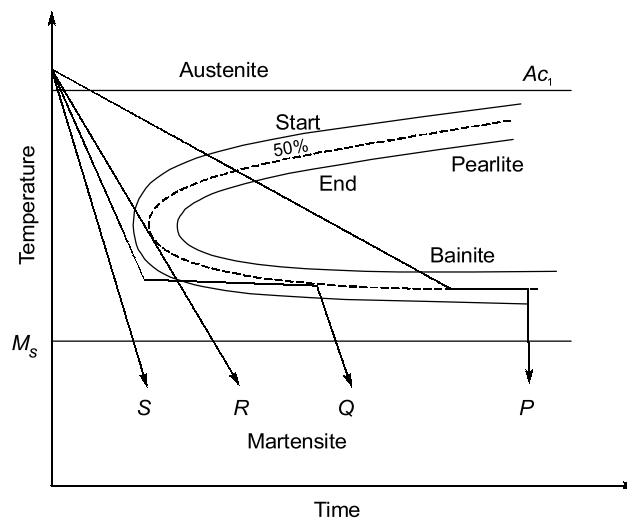
[Take $C_{p-\text{argon}} = 0.5203 \text{ kJ/kg-K}$, $C_{v-\text{argon}} = 0.3122 \text{ kJ/kg-K}$]

Q.180 The $h-s$ diagram for a Rankine cycle is given below



Assuming pump work of 15 kJ/kg, the friction loss in the pump is _____ percent. [Correct upto 1 decimal place]

Q.181 Which of the following cooling curves (shown in schematic) in an eutectoid steel will produce 50% bainitic structure?



- (a) P (b) Q
(c) R (d) S

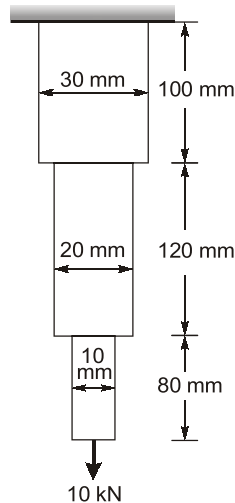
Q.182 In metals subjected to cold working, strain hardening effect is due to:

- (a) Twinning mechanism (b) Dislocation mechanism
(c) Fracture mechanism (d) Twisting mechanism

Q.183 The Mohr's circle for plane stress condition is a circle of radius R with its centre at $+\frac{R}{2}$ on σ -axis. The value of shear stress on the plane of pure shear stress will be _____ αR , where α is _____. [Correct upto 3 decimal places]

Q.184 What is the strain energy of the massless stepped bar as shown in the figure below?

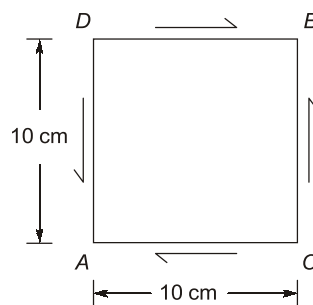
[Take $E = 200$ GPa]



- (a) 0.38 N-m
(c) 0.50 N-m

- (b) 0.42 N-m
(d) 0.56 N-m

Q.185 In a pure shear condition, the maximum value of shear stress is observed to be 20 MPa for an element shown, subjected to above condition. The change in length of diagonal AB is ___ μm . [Take $G = 80$ GPa] [Correct upto 2 decimal places]



Q.186 A cantilever of length 3 m carries two point loads of 2 kN at free end and 4 kN at the distance of 1 m from the free end. The deflection at the free end is _____ mm. [Correct upto 2 decimal places]

[Take $E = 2 \times 10^5$ N/mm² and $I = 10^8$ mm⁴]

Multiple Select Questions (MSQ)

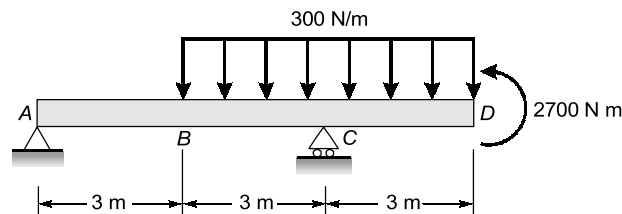
Q.197 Which of the following properties of solids is/are dependent on crystal imperfections?

- (a) Yield stress (b) Melting point
(c) Conductivity (d) Ductility

Q.198 Percentages of various alloying elements present in different materials for high speed steels are

- (a) 27% Cr, 3% Ni, 5% Mo, 0.25% C, 0.1% Pb
(b) 18% Cr, 8% Ni, 0.15% C, 0.2% Sn, 0.1% Pb
(c) 8% Mo, 4% Cr, 2% V, 6% W, 0.7% C
(d) 18% W, 4% Cr, 1% V, 5% Co, 0.7

Q.199 The shear force diagram changes its sign, for the given loading on beam *ABCD*, at



- (a) point *B* (b) point *C*
(c) mid point of *BC* (d) a distance of 1.67 m from point *B* towards *C*

Q.200 The modulus of rigidity and the bulk modulus of a material are found as 70 GPa and 150 GPa respectively. Then,

- (a) Elasticity modulus is 200 GPa (b) Poisson's ratio is 0.22
(c) Elasticity modulus is 182 GPa (d) Poisons ratio is 0.3



Detailed Explanations

176. (d)

$$Q_s = (h_3 - h_{f1}) + (h_5 - h_4) \quad [\text{Neglecting pump work, } h_{f1} = h_2]$$

$$= (3450 - 191.8) + (3560 - 3050)$$

$$= 3768.2 \text{ kJ/kg}$$

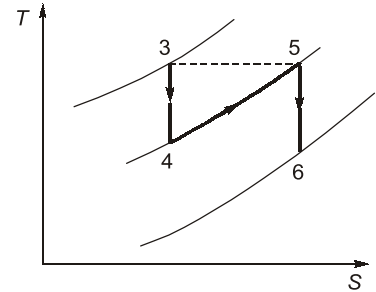
$$W = (h_3 - h_4) + (h_5 - h_6)$$

$$= (3450 - 3050) + (3560 - 2300)$$

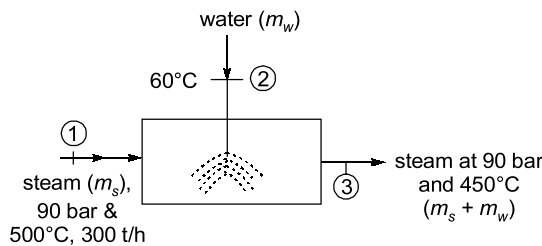
$$= 1660 \text{ kJ/kg}$$

$$\eta_{\text{cycle}} = \frac{W}{Q_s} = \frac{1660}{3768.2} = 44.05\%$$

$$\text{Steam rate} = \frac{3600}{W} = \frac{3600}{1660} = 2.17 \text{ kg/kWh}$$



177. 3.6 (3.5 to 3.6)



$$m_s h_1 + m_w h_2 = (m_s + m_w) h_3$$

$$m_w = \frac{m_s (h_1 - h_3)}{(h_3 - h_2)}$$

$$= \frac{300(3386.1 - 3256.6)}{(3256.6 - 251.11)} = 12.92 \text{ t/h}$$

$$= \frac{12.92 \times 1000}{3600} \text{ kg/s} = 3.588 \text{ kg/s} \approx 3.6 \text{ kg/s}$$

178. 0.26 (0.25 to 0.27)

Energy balance for first feedwater heater

$$m_1 \times h_2 + (1 - m_1) h_{f6} = h_{f7}$$

$$\Rightarrow m_1 \times 2679 + (1 - m_1) 467.1 = 762.6$$

$$\Rightarrow m_1 = 0.1336 \text{ kg}$$

Energy balance for second feed water heater :

$$m_2 h_3 + (1 - m_1 - m_2) h_{f5} = (1 - m_1) h_{f6}$$

$$\Rightarrow m_2 \times 2365 + (1 - 0.1336 - m_2) \times 137.8 = (1 - 0.1336) \times 467.1$$

⇒

$$m_2 = 0.1281 \text{ kg}$$

$$\text{Total mass} = m_1 + m_2 = 0.1336 + 0.1281 = 0.26 \text{ kg}$$

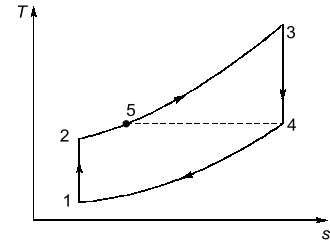
179. 572.88(572.60 to 572.90)

$$P_1 = 100 \text{ kPa} = P_4$$

$$P_3 = P_2 = 400 \text{ kPa}$$

$$\gamma = \frac{C_p}{C_v} = \frac{0.5203}{0.3122} = 1.667$$

$$T_1 = 298 \text{ K}, T_3 = 1473 \text{ K}$$



The maximum temperature to which argon can be heated in regenerator is equal to outlet temperature of turbine assuming 100% efficiency of regenerator.

$$\Rightarrow \frac{T_3}{T_4} = \left(\frac{P_3}{P_4} \right)^{(\gamma-1)/\gamma}$$

$$\Rightarrow \frac{1473}{T_4} = (4)^{0.667/1.667}$$

$$\Rightarrow T_4 = T_5 = 845.875 \text{ K} = 572.875^\circ\text{C} \approx 572.88^\circ$$

180. (33.3)(33 to 34)

$$s_1 = s_2$$

$$6.75 = 0.55 + x_2(8.30 - 0.55)$$

⇒

$$x_2 = 0.8$$

$$h_2 = h_f + x_2 h_{fg}$$

⇒

$$h_2 = h_3 + x_2 \{h_g - h_3\}$$

⇒

$$h_2 = h_3(1 - x_2) + x_2 h_g$$

⇒

$$2100 = h_3 \times 0.2 + 0.8 \times 2550$$

⇒

$$h_3 = 300 \text{ kJ/kg}$$

$$w_p = 15 \text{ kJ/kg} \quad [\text{Given}]$$

$$h_4' = h_3 + w_p = 315 \text{ kJ/kg}$$

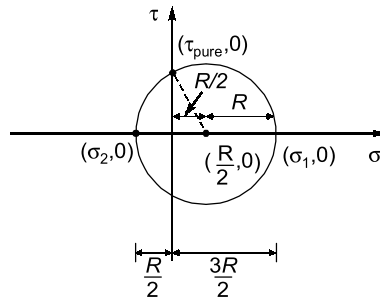
$$\eta_p = \frac{h_4 - h_3}{h_4' - h_3} = \frac{10}{15} \times 100 = 66.66\%$$

$$\text{Losses} = 33.33\%$$

181. (b)

182. (b)

183. 86.60 (0.866 to 0.866)



$$\Rightarrow \sigma_1 = \frac{3R}{2}, \sigma_2 = -\frac{R}{2}$$

$$\Rightarrow (\tau)_{\text{on plane of pure shear}} = \sqrt{-\sigma_1 \times \sigma_2}$$

$$= \sqrt{-\left(-\frac{R}{2} \times \frac{3R}{2}\right)} = 0.866 \times R$$

Thus, $\alpha = 0.866 \text{ MPa}$

Alternate solution:

From Mohr's circle

$$(\tau)_{\text{on plane of pure shear}} = \sqrt{R^2 - \left(\frac{R}{2}\right)^2}$$

$$= \sqrt{3} \frac{R}{2} = 0.866 R$$

184. (a)

$$\text{Total strain energy} = \frac{1}{2} P_1 \delta_1 + \frac{1}{2} P_2 \delta_2 + \frac{1}{2} P_3 \delta_3$$

$$= \frac{1}{2} \times P \times \frac{PL_1}{A_1 E} + \frac{1}{2} P \times \frac{PL_2}{A_2 E} + \frac{1}{2} \times P \times \frac{PL_3}{A_3 E}$$

$$= \frac{P^2}{2E} \left[\frac{L_1}{A_1} + \frac{L_2}{A_2} + \frac{L_3}{A_3} \right]$$

$$= \frac{(10 \times 1000)^2}{2 \times 200 \times 10^9} \left[\frac{100 \times 4 \times 1000}{\pi \times (30)^2} + \frac{120 \times 4 \times 1000}{\pi \times (20)^2} + \frac{80 \times 4 \times 1000}{\pi \times (10)^2} \right]$$

$$= 0.3855 \text{ N-m}$$

185. 17.67 (17.60 to 17.70)

$$y = \frac{\tau}{G} = \frac{20}{80 \times 10^3} = 0.25 \times 10^{-3}$$

$$(\epsilon)_{\text{at } \theta = 45^\circ} = \frac{y}{2} \sin 90^\circ = \frac{y}{2} = 0.125 \times 10^{-3}$$

$$\frac{\text{Change in length}}{\text{Original length}} = 0.125 \times 10^{-3}$$

$$\text{Change in length} = 0.125 \times 10^{-3} \times \sqrt{10^2 + 10^2} = 0.01767 \text{ mm} \approx 17.67 \mu\text{m}$$

186. 1.83 (1.80 to 1.86)

$$\text{Distance } AC = a = 2 \text{ m} = 2000 \text{ mm}$$

$$\therefore W_1 = 2 \text{ kN} = 2000 \text{ N}$$

$$W_2 = 4 \text{ kN} = 4000 \text{ N}$$

Let y_1 = Deflection at the free end due to load 2 kN alone

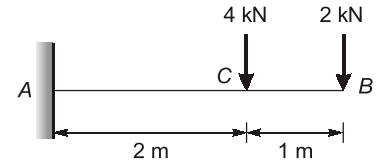
y_2 = Deflection at the free end due to load 4 kN alone

$$y_1 = \frac{W_1 L^3}{3EI} = \frac{2000 \times 3000^3}{3 \times 2 \times 10^5 \times 10^8} = 0.9 \text{ mm}$$

and

$$\begin{aligned} y_2 &= \frac{W_2 a^3}{3EI} + \frac{W_2 a^2}{2EI} (L - a) \\ &= \frac{4000 \times 2000^3}{3 \times 2 \times 10^5 \times 10^8} + \frac{4000 \times 2000^2}{2 \times 2 \times 10^5 \times 10^8} (3000 - 2000) \\ &= 0.53 + 0.4 = 0.93 \text{ mm} \end{aligned}$$

Total deflection at the free end = $y_1 + y_2 = 0.93 + 0.9 = 1.83 \text{ mm}$



187. 107.59 (105 to 109)

Expansion required for the rod to just fix itself between the walls.

$$= (2.43 - 2.4) = 0.03 \text{ m}$$

Increase in length, $\delta l = 0.03$

\therefore Temperature rise required

$$t_1 = \frac{0.03}{11.8 \times 10^{-5} \times 2.4} = 105.9 \text{ }^\circ\text{C}$$

Strain required for a stress of 21 MN/m².

$$\frac{\sigma}{E} = \frac{21 \times 10^6}{105 \times 10^9} = 200 \times 10^{-6}$$

Let the temperature rise required for this strain = t_2

$$\text{Strain} = \alpha t_2$$

$$t_2 = \frac{\text{Strain}}{\alpha}$$

$$t_2 = \frac{200 \times 10^{-6}}{11.8 \times 10^{-5}} = 1.694 \text{ }^\circ\text{C}$$

\therefore Total temperature rise required = $t_1 + t_2 = 105.9 + 1.694$

$$= 107.59^\circ\text{C} \approx 107.6^\circ\text{C}$$

188. (c)

Maximum bending stress at any section x - x .

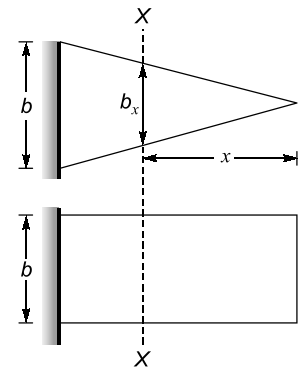
$$b_x = \frac{b}{l}x$$

$$I_x = \frac{b_x d^3}{12}$$

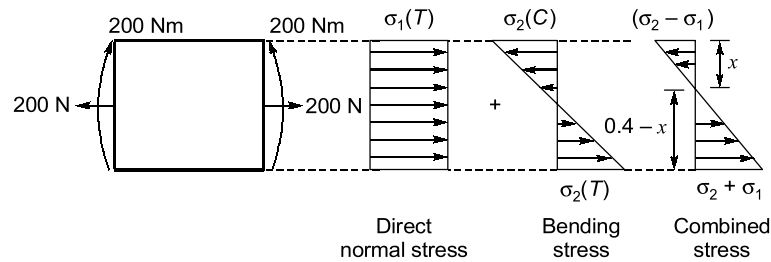
$$\therefore (\sigma_{\max})_x = \frac{M}{I_x} y_{\max} = \frac{wx^2 \cdot d}{\left(\frac{b_x d^3}{12}\right) \cdot \frac{d}{2}}$$

$$\therefore (\sigma_{\max})_x = \frac{3wx^2}{b_x d^2} = \frac{3wlx}{bd^2}$$

$$\therefore (\sigma_{\max})_x \propto x$$

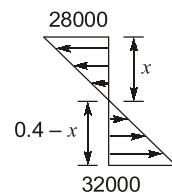


189. (b)



Direct normal stress $\sigma_1 = \frac{200}{0.4 \times 0.25} = 2000 \text{ N/m}^2$

$$\begin{aligned} \text{Bending stress } \sigma_2 &= \frac{M}{I} \cdot y_{\max} = \frac{200}{\left(\frac{0.25 \times 0.4^3}{12}\right)} \times 0.2 \\ &= 30000 \text{ N/m}^2 \end{aligned}$$



The distance from top surface at which normal stress is zero be x .

$$\frac{x}{28000} = \frac{0.4 - x}{32000}$$

$$\therefore x = (0.4 - x) \frac{7}{8}$$

$$\therefore x = 0.1866 \text{ m}$$

190. 9.1 (9.0 to 9.3)

According to maximum principal strain theory,

$$\frac{\sigma_1}{E} - \mu \frac{\sigma_2}{E} \leq \frac{\sigma_y / FOS}{E}$$

$$\therefore \sigma_1 - \mu \sigma_2 \leq \frac{\sigma_y}{FOS}$$

Here, $\sigma_1 = \sigma_h = \text{Circumferential stress} = \frac{pd}{2t}$

$$\sigma_2 = \sigma_L = \text{Longitudinal stress} = \frac{pd}{4t}$$

$$\therefore \frac{pd}{2t} - \frac{\mu pd}{4t} \leq \frac{\sigma_y}{FOS}$$

$$\therefore t \geq \frac{FOS \left[\frac{pd}{2} - \frac{\mu pd}{4} \right]}{\sigma_y}$$

$$t \geq \frac{2}{280} \left[\frac{6 \times 500}{2} - \frac{0.3 \times 6 \times 500}{4} \right]$$

$$t \geq 9.1071 \text{ mm}$$

191. 3(3 to 3)

$$\Sigma \text{Torque} = 0$$

$$T_R - (4 \times 4) + 4 = 0$$

$$T_R = 12 \text{ kNm}$$

Consider an element of length ' dx ' at any section $x - x$ at x distance from fixed end.

\therefore Angle of twist of element

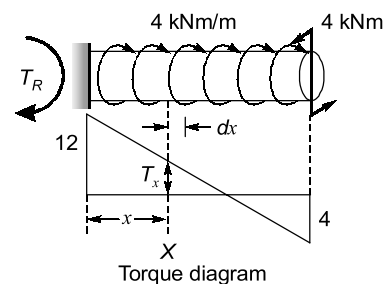
$$\begin{aligned} \theta_x &= \int_0^x \frac{T_x \cdot dx}{G \cdot I_p} = \int_0^x \frac{(12 - 4x) dx}{G I_p} \\ &= \frac{(12x - 2x^2)}{G I_p} \end{aligned}$$

For maximum angular twist

$$\frac{d\theta_x}{dx} = 0$$

$$\frac{12 - 4x}{G I_p} = 0$$

$$x = 3 \text{ m}$$



192. (c)

$$\begin{aligned} \Sigma F_V &= 0; & R_A + R_C &= 0 \\ \Sigma F_H &= 0; & H_A &= P \\ \Sigma M_C &= 0; & H_A L + R_A L &= 0 \\ R_A &= -H_A = -P \end{aligned}$$

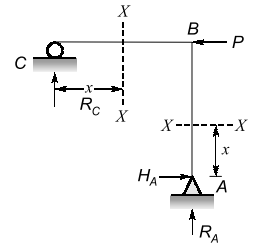
Now

$$\Delta_{BH} = \frac{\partial U}{\partial P} = \frac{\partial U_{BC}}{\partial P} + \frac{\partial U_{AB}}{\partial P}$$

$$\begin{aligned} U_{BC} &= \int_0^L \frac{Mx_{AB}^2}{2EI} dx = \int_0^L \frac{(R_C \cdot x)^2}{2EI} dx \\ &= \int_0^L \frac{P^2 x^2}{2EI} dx = \frac{P^2 L^3}{6EI} \end{aligned}$$

$$\begin{aligned} U_{AB} &= \int_0^L \frac{Mx_{AB}^2}{2EI} dx = \int_0^L \frac{(H_A \cdot x)^2}{2EI} dx \\ &= \int_0^L \frac{P^2 x^2}{2EI} dx = \frac{P^2 L^3}{6EI} \end{aligned}$$

$$\therefore \Delta_{BH} = \frac{\partial}{\partial P} \left(\frac{2P^2 L^3}{6EI} \right) = \frac{2PL^3}{3EI}$$

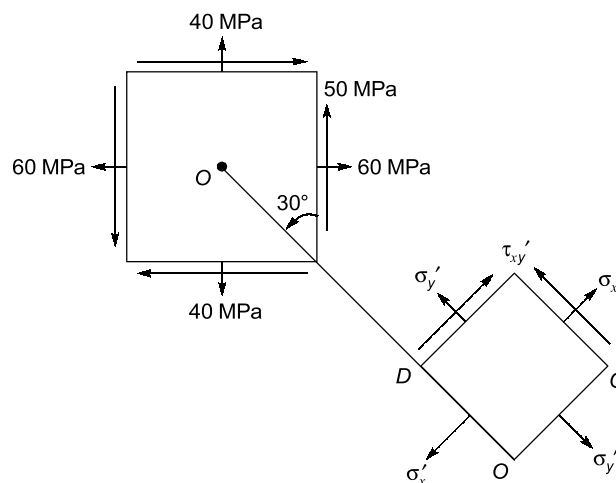


193. 0.272 (0.260 to 0.280)

$$\sigma_x = 60 \text{ MPa}$$

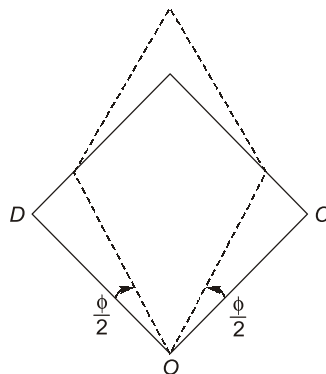
$$\sigma_y = 40 \text{ MPa}$$

$$\tau_{xy} = 50 \text{ MPa}$$



$$\begin{aligned}\tau'_{xy} &= -\left(\frac{\sigma_x - \sigma_y}{2}\right)\sin 2\theta + \tau_{xy} \cos 2\theta \\ &= -\left(\frac{60 - 40}{2}\right)\sin 60^\circ + 50 \cos 60^\circ \\ &= -5\sqrt{3} + 25 \\ &= 16.3397 \text{ MPa}\end{aligned}$$

Change in angle between OC and OD

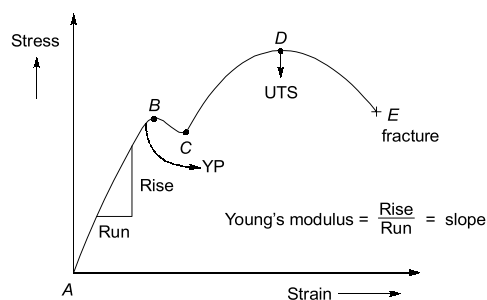


$$\phi = \frac{\tau'_{xy}}{G}$$

\therefore

$$\phi = \frac{16.3397}{60 \times 10^3} = 0.2723 \times 10^{-3}$$

194. (d)



Necking starts from ultimate tensile strength and ends at the point of failure of specimen.

195. (d)

When both ends are hinged, the buckling load is given by

$$P_{\text{critical}} = \frac{\pi^2 EI}{L^2}$$

$$\Rightarrow 200 = \frac{\pi^2 EI}{L^2}$$

When the lateral movement at the mid height is restrained, then buckling load

$$\begin{aligned} \text{Buckling load} &= \frac{\pi^2 EI}{L_1^2} \quad \left(\text{where, } L = \frac{L}{2} \right) \\ &= \frac{4\pi^2 EI}{L^2} \\ &= 4 \times 200 = 800 \text{ N} \end{aligned}$$

196. (9.50) (9.0 to 9.9)

Given: $b_1 = 100 \text{ mm}$, $b_2 = 75 \text{ mm}$, $t_f = 10 \text{ mm}$, $h = 360 \text{ mm}$

$$\text{Position of shear centre, } e = \frac{h^2 t_f (b_1^2 - b_2^2)}{4I_z}$$

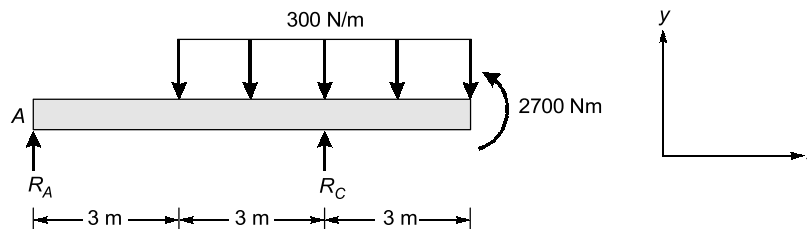
$$\begin{aligned} I_z &= I_{\text{web}} + 2I_{\text{flange}} \\ &= \frac{10 \times 350^3}{12} + 2 \left[\frac{175 \times 10^3}{12} + 175 \times 10 \left(\frac{350}{2} + 5 \right)^2 \right] \\ &= 1.492 \times 10^8 \text{ mm}^4 \end{aligned}$$

$$e = \frac{360^2 \times 10 \times (100^2 - 75^2)}{4 \times 1.492 \times 10^8} = 9.50 \text{ mm}$$

197. (a, c, d)

198. (c, d)

199. (b, c)



$$\sum M_A = 0$$

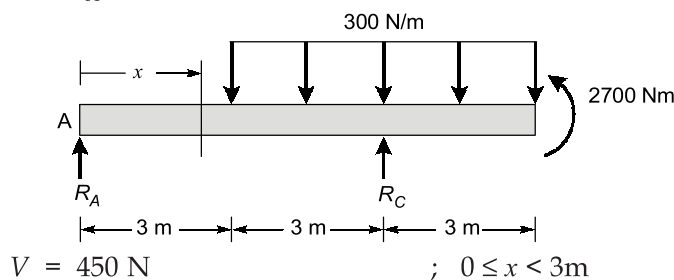
$$\Rightarrow 300(6)(3+3) - R_C(6) - 2700 = 0$$

$$\Rightarrow R_C = 1350 \text{ N}$$

$$\sum F_y = 0$$

$$\Rightarrow R_A + R_C = 300(6)$$

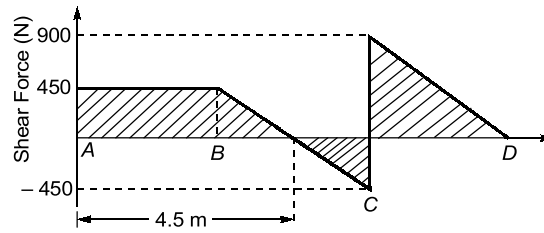
$$\Rightarrow R_A = 450 \text{ N}$$



$$V = 450 \text{ N} \quad ; \quad 0 \leq x < 3\text{m}$$

$$V = [450 - 300(x - 3)] \text{ N} \quad ; \quad 3 \text{ m} \leq x < 6 \text{ m}$$

$$V = [450 - 300(x - 3) + 1350] \text{ N} \quad ; \quad 6 \text{ m} \leq x < 9 \text{ m}$$



200. (c, d)

Given: $G = 70 \text{ GPa}$, $K = 150 \text{ GPa}$

$$E = 2G(1 + \mu) = 3K(1 - 2\mu)$$

$$\frac{3K}{2G} = \frac{(1 + \mu)}{(1 - 2\mu)}$$

$$\frac{3 \times 150}{2 \times 70} = \frac{(1 + \mu)}{(1 - 2\mu)}$$

$$450 - 900\mu = 140 + 140\mu$$

$$\mu = \frac{450 - 140}{900 + 140} = 0.298$$

$$E = 2G(1 + \mu) = 2 \times 70(1 + 0.3) \\ = 182 \text{ GPa}$$

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