

Fluid Mechanics and Machinery + Heat Transfer

Q.126 The Navier-Stoke's equation for an incompressible fluid with constant viscosity is

- (a) $-\vec{\nabla}P + \rho\vec{g} + \mu\vec{\nabla}^2\vec{V} = 0$ (b) $\rho\frac{D\vec{V}}{Dt} = \vec{\nabla}P + \mu\vec{\nabla}^2\vec{V}$
 (c) $\rho\frac{D\vec{V}}{Dt} = -\vec{\nabla}P + \rho\vec{g} + \mu\vec{\nabla}^2\vec{V}$ (d) $\rho\frac{D\vec{V}}{Dt} = -\vec{\nabla}P + \rho\vec{g} + \mu\vec{\nabla}^2\vec{V} + \vec{\nabla} \cdot \vec{V} = 0$

Q.127 The impeller of a centrifugal pump has an outer diameter of 30 cm and inner diameter of 15 cm. The pump runs at 1200 rpm. The impeller vanes are set at a blade angle of 30° at the outlet. If the velocity of flow is constant at 2.0 m/s. The head developed is

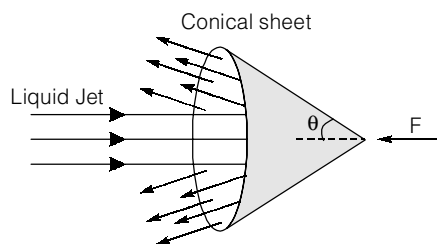
(Assume manometric efficiency = 0.85 and $g = 9.81 \text{ m/s}^2$)

- (a) 25.13 m (b) 23.6 m
 (c) 28.4 m (d) 29.8 m

Q.128 A double overhung 1.5 m diameter impulse turbine installation is to develop 3000 kW at 400 rpm under a net head of 300 m. If the overall efficiency is 0.90, then the diameter of the jet is _____ cm. (Take $C_v = 0.95$, unit weight of water = 9.79 kN/m^3) [Correct upto 1 decimal place]

Q.129 A double jet Pelton wheel has a specific speed of 15 (SI units) and is required to deliver a power of 1500 kW. The turbine is supplied through a pipeline from a reservoir whose level is 500 m above the nozzles. Allowing 5% for friction loss in the pipe, the rotational speed is _____ rpm. (Correct upto two decimal places)

Q.130 A liquid jet of velocity V_j and diameter D_j strikes a fixed cone and deflects back as a conical sheet with the same velocity as shown in figure below. The expression for restraining force may be given as $F = \frac{3}{2}(\rho A_j V_j^2)$. The cone angle (θ) is



- (a) 30° (b) 43°
 (c) 45° (d) 60°

Q.131 A fluid flow field is given by

$$V = x^2y\hat{i} + y^2z\hat{j} - (2xyz + yz^2)\hat{k}$$

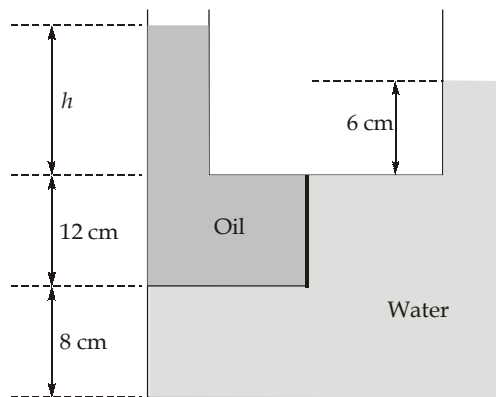
The x -component of acceleration at point (3, 2, 1) is _____ units.

Q.138 Which one of the following is correct with respect to dimensional analysis?

- (a) A dimension is a measure of a physical quantity (without numerical values)
- (b) A unit is a way to assign a number to the dimension
- (c) Both (a) and (b)
- (d) None of these

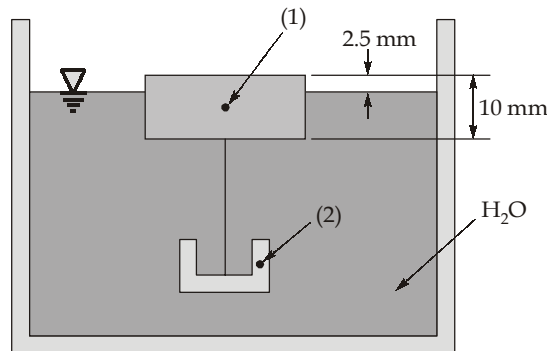
Q.139 As the tank shown below contains water and immiscible oil at 20 °C. Then the height h of the column is

[Assume the density of oil is 898 kg/m³]



- (a) 0.010 m
- (b) 0.017 m
- (c) 1.01 m
- (d) 0.080 m

Q.140 A metal part (object 2) is hanging by a thin cord from a floating wood block (object 1). The wood block has a specific gravity $S_1 = 0.3$ and dimensions of $50 \times 50 \times 10 \text{ mm}^3$. The metal part has a volume of 6600 mm^3 ($g = 9.8 \text{ m/s}^2$). The mass m_2 of the metal part is



- (a) 0.01282
- (b) 0.01540
- (c) 0.01372
- (d) 0.01785

Q.141 Consider conditions for which a fluid with a free stream velocity V flows over a surface with characteristic length L , providing an average convection heat transfer coefficient \bar{h} . The experimental measurements showed following results: When $V_1 = 25 \text{ m/s}$, $\bar{h}_1 = 60 \text{ W/m}^2\text{K}$ and when $V_2 = 15 \text{ m/s}$, $\bar{h}_2 = 30 \text{ W/m}^2\text{K}$. Assume that Nusselt number is of the form $\overline{Nu} = CRe^m Pr^n$, where C , m and n are constants. The value of convective heat transfer ($\text{W/m}^2\text{K}$) when $V = 40 \text{ m/s}$ is _____. (Correct upto two decimal places)

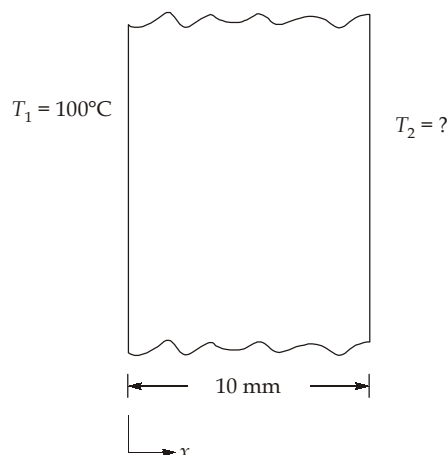
Important Questions

for

GATE 2022

ME

- Q.142** In a steam condenser, the steam condenses at a temperature of 60°C . The cooling water enters at 25°C and leaves at 45°C . The surface area of condenser tubes is 30 m^2 and the overall heat transfer coefficient for the heat exchanger is $2000\text{ W/m}^2\text{C}$. The heat of vaporization of water at 60°C is $h_{fg} = 2358\text{ kJ/kg}$. The rate of condensation of steam (in kg/s) in the condenser is
- (a) 0.2 (b) 0.4
(c) 0.6 (d) 0.8
- Q.143** In a counter flow, concentric tube heat exchanger, water flows through the inner tube having diameter 30 mm at 30°C . The hot oil enters the annulus having diameter 50 mm at 100°C and leaves at 60°C . The mass flow rate of the water and the oil are 0.5 kg/s and 0.7 kg/s , respectively. The specific heat of water and oil are 4200 J/kgK and 2400 J/kgK , respectively. If the overall heat transfer coefficient of the heat exchanger is $300\text{ W/m}^2\text{C}$, the length of the tube required to achieve the desired heat transfer is _____ m. (Correct upto two decimal places)
- Q.144** A drying oven is shaped like a long equilateral-triangular duct. The width of each side is 1.5 m and heat is supplied from the base surface ($\epsilon = 0.9$) at a rate of 1000 W/m while the side surfaces ($\epsilon = 0.4$) are maintained at 400 K . Neglecting any end effects, the temperature of the base surface is _____ K. (Correct upto one decimal place)
- Q.145** An infinitely long copper ($k = 400\text{ W/mK}$) rod of length L and diameter D is attached at one end to a heated wall and transfers heat \dot{q}_1 by convection to a cold fluid. If an aluminium ($k = 250\text{ W/mK}$) rod of length L and diameter $0.4D$ is used in place of copper rod, the heat transfer is \dot{q}_2 . The ratio $\frac{\dot{q}_1}{\dot{q}_2}$ is _____.
- Q.146** The time required for a lumped system (time constant, $\tau = 10\text{ s}$) to reach the average temperature, $T_{\text{avg}} = (T_i + T_\infty)/2$, where T_i is the initial temperature and T_∞ is the temperature of the environment, is _____ s. (Correct upto two decimal places)
- Q.147** A wall is made from an inhomogeneous material for which the thermal conductivity varies through the thickness according to $k = ax + b$ where, $a = 7 \times 10^4\text{ W/m}^2\text{K}$ and $b = 200\text{ W/mK}$. Assume that the heat flux is constant and is equal to $3.723 \times 10^6\text{ W/m}^2$, the temperature at $x = 10\text{ mm}$, is



- (a) 80°C (b) 94.4°C
(c) 20°C (d) 64°C

Multiple Select Questions (MSQ)

- Q.148** Which of the following statements is/are correct for turbulent flow through pipe?
- (a) Frictional head loss varies directly as the average velocity.
 - (b) Frictional head loss varies directly as the square of average velocity.
 - (c) Shear stress is due to fluctuation of the velocity in the direction of flow as well as transverse to it.
 - (d) The laminar sublayer is a region next to wall where the inertia force is predominate while the rest of the flow is turbulent.
- Q.149** Which of the following statements is/are correct in respect of Kaplan turbine?
- (a) It is a reaction turbine.
 - (b) It is mixed flow turbine
 - (c) Low frictional losses
 - (d) Part load efficiency is considerably high
- Q.150** In respect of free convection over a vertical flat plate the Nusselt number varies with Grashof number 'Gr' as
- (a) $Gr^{1/7}$ for turbulent flow
 - (b) $Gr^{1/3}$ for laminar flow
 - (c) $Gr^{1/4}$ for laminar flow
 - (d) $Gr^{1/3}$ for turbulent flow



Detailed Explanation

126. (c)

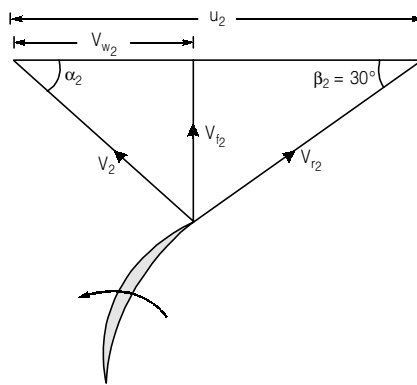
For an incompressible fluid, Navier-Stoke's equation, $\rho \frac{D\vec{V}}{Dt} = -\vec{\nabla}P + \rho\vec{g} + \mu\vec{\nabla}^2\vec{V}$

127. (a)

At the outlet, $u_2 = \frac{\pi D_2 N}{60} = \frac{\pi \times 0.30 \times 1200}{60} = 18.85 \text{ m/s}$

$V_{f2} = 2.0 \text{ m/s}$ and $\beta_2 = 30^\circ$

From the outlet velocity triangle,



$$\tan \beta_2 = \frac{V_{f2}}{u_2 - V_{w2}}$$

$$\tan 30^\circ = \frac{2.0}{18.85 - V_{w2}}$$

$$18.85 - V_{w2} = 3.464; \text{ and hence } V_{w2} = 15.386 \text{ m/s}$$

Manometric efficiency

$$\eta_m = \frac{gH}{u_2 V_{w2}}$$

Head developed,

$$H = \eta_m \frac{u_2 V_{w2}}{g} = \frac{0.85 \times 18.85 \times 15.386}{9.81} = 25.13 \text{ m}$$

128. (9.95) (9.8 to 10.0)

$$\text{Power per wheel} = \frac{3000}{2} = 1500 \text{ kW}$$

$$\text{Power} = \eta_o \gamma Q H$$

$$\Rightarrow 1500 = 0.90 \times 9.79 \times Q \times 300$$

$$\Rightarrow Q = 0.5674 \text{ m}^3/\text{s}$$

$$\text{Velocity of the jet, } V_1 = C_V \sqrt{2gH}$$

$$= 0.95 \sqrt{2 \times 9.81 \times 300} = 72.88 \text{ m/s}$$

$$\text{For the nozzle: } Q = \frac{\pi}{4} d^2 V_1$$

$$\Rightarrow 0.5674 = \frac{\pi}{4} \times d^2 \times 72.88$$

$$\Rightarrow d = 9.95 \text{ cm}$$

129. (1214.58)(1214.50 to 1214.65)

$$\text{Net available head, } H = 500 (1 - 0.05) = 475 \text{ m}$$

$$\text{Power per jet} = \frac{1500}{2} = 750 \text{ kW}$$

$$\text{Specific speed } (N_s) = \frac{N\sqrt{P}}{H^{5/4}}$$

$$\Rightarrow 15 = \frac{N\sqrt{750}}{(475)^{5/4}}$$

$$\Rightarrow N = 1214.58 \text{ rpm}$$

130. (d)

$$\sum F_x = -F = \dot{m}_{out} u_{out} - \dot{m}_{in} u_{in}$$

$$= \dot{m}(-V_j \cos \theta) - \dot{m} V_j = -\rho A_j V_j^2 (1 + \cos \theta)$$

$$F = \rho A_j V_j^2 (1 + \cos \theta)$$

$$\Rightarrow \frac{3}{2} \rho A_j V_j^2 = \rho A_j V_j^2 (1 + \cos \theta)$$

$$\cos \theta = \frac{1}{2} \Rightarrow \theta = 60^\circ$$

131. (252)

x -component of acceleration,

$$a_x = u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} + w \frac{\partial u}{\partial z}$$

$$a_x = x^2 y (2xy) + y^2 z (x^2) - (2xyz + yz^2)(0)$$

$$= 2x^3 y^2 + x^2 y^2 z$$

$$= 2(3)^3 (2)^2 + (3)^2 (2)^2 (1)$$

$$= 2 \times 27 \times 4 + 9 \times 4 \times 1$$

$$= 54 \times 4 + 36$$

$$= 216 + 36$$

$$= 252 \text{ units}$$

132. (-2133.33) (-2134.0 to -2132.0)

The velocity midway between the plates is the maximum velocity.

$$\text{Pressure gradient } \left(\frac{\partial p}{\partial x} \right),$$

$$\therefore U_{\max} = \frac{-1}{8\mu} \left(\frac{\partial p}{\partial x} \right) \times t^2$$

$$\Rightarrow 3 = \frac{-1}{8 \times 0.02} \left(\frac{\partial p}{\partial x} \right) \times (0.015)^2$$

$$\Rightarrow \left(\frac{\partial p}{\partial x} \right) = \frac{-3 \times 8 \times 0.02}{(0.015)^2} = -2133.33 \text{ N/m}^2/\text{m}$$

133. (d)

The length in the perimeter, $2\pi r$ and there are two surfaces of rubber sheet (inside and outside) by force balance,

$$\sigma \times 2\pi r \times 2 = mg$$

$$mg = \frac{1}{2} \times \frac{4}{3} \pi r^3 \rho g = \frac{1}{2} \times \frac{4}{3} \times \pi \times 0.25^3 \times 1000 \times 9.81 = 321.02 \text{ N}$$

$$\sigma = \frac{321.03}{2 \times 2\pi \times 0.25} \Rightarrow 102.187 \text{ N/m}$$

$$\sigma \approx 102.2 \text{ N/m}$$

134. (c)

As per given data:

$$u^* = \frac{u}{U} \text{ and } y^* = \frac{y}{\delta}$$

$$dy^* = \delta^{-1} dy$$

The given parabolic velocity distribution and the expression for the displacement thickness can then be expressed as

$$u^* = 2y^* - y^{*2}, \text{ and } \delta^* = \int_0^1 (1 - u^*) dy^*$$

Combining these equations gives,

$$\delta^* = \int_0^1 (1 - 2y^* + y^{*2}) dy^*$$

$$\delta^* = \delta \left[y^* - y^{*2} + \frac{1}{3} y^{*3} \right]_0^1$$

$$\delta^* = \frac{1}{3} \delta$$

$$\frac{\delta^*}{\delta} = \frac{1}{3}$$

135. (a)

Applying Bernoulli's equation between the two reservoirs, we get

$$12.5 = 0.5 \frac{V^2}{2g} + \frac{fLV^2}{2gD} + \frac{V^2}{2g}$$

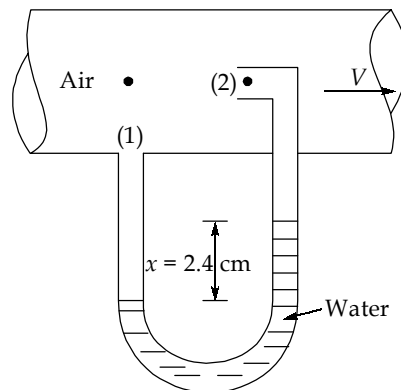
$$\Rightarrow 12.5 = \frac{V^2}{2g} \left[1.5 + \frac{fL}{D} \right]$$

$$\Rightarrow 12.5 = \frac{V^2}{2 \times 10} \left[1.5 + \frac{0.04 \times 1000}{0.5} \right]$$

$$\Rightarrow 12.5 = \frac{V^2}{20} \times 81.5$$

$$\Rightarrow V = 1.75 \text{ m/s}$$

136. (20.9)(20.8 to 21.0)



$$\rho_{\text{air}} = \frac{P}{RT} = \frac{98}{0.287(27 + 45)} = 1.0737 \text{ kg/m}^3$$

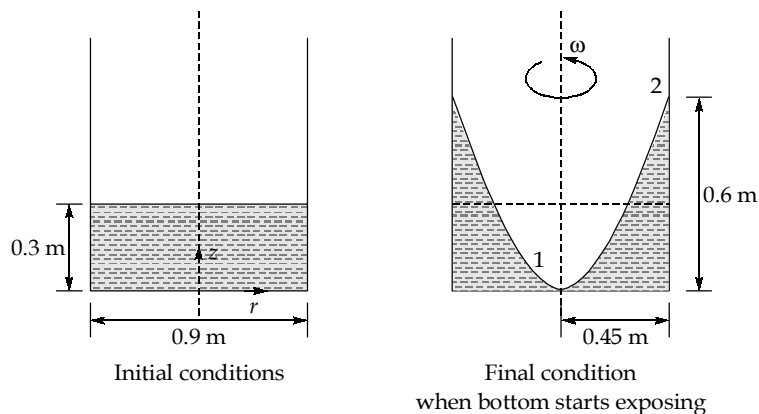
$$h = x \left(\frac{S_m}{s} - 1 \right) = 0.024 \left(\frac{1000}{1.0737} - 1 \right) = 22.326 \text{ m}$$

So,

$$V_1 = \sqrt{2gh} = \sqrt{2(9.81)(22.326)}$$

$$V_1 = 20.9 \text{ m/s}$$

137. (7.624) (7.520 to 7.820)



Apply forced vortex motion equation at points (1) and (2)

$$\frac{P_1}{\rho g} - \frac{(V_1)^2}{2g} + z_1 = \frac{P_2}{\rho g} - \frac{(V_2)^2}{2g} + z_2$$

At point 1, $P_1 = P_{\text{atm}} \Rightarrow P_{\text{gauge}} = 0$

$$V_1 = \omega R_1 = 0$$

$$z_1 = 0$$

At point, $P_2 = P_{\text{atm}} \Rightarrow P_{\text{gauge}} = 0$

$$z_2 = 0.6$$

Therefore, $0 - 0 + 0 = 0 - \frac{(\omega R_2)^2}{2g} + 0.6$

$$\Rightarrow \frac{\omega^2 (0.45)^2}{2 \times (9.81)} = 0.6$$

$$\Rightarrow \omega = 7.624 \text{ rad/s}$$

138. (c)

A dimension is a measure of a physical quantity (without numerical values), while a unit is a way to assign a number to that dimension.

139. (d)

$$\rho_{\text{water}} = 1000 \text{ kg/m}^3.$$

Apply the hydrostatic relation from the oil surface to the water surface, skipping the 8 cm part:

$$p_{\text{atm}} + (898)(9.81)(h + 0.12) - (1000)(9.81)(0.06 + 0.12) = p_{\text{atm}}$$

On solving, $h = 0.08 \text{ m}$

140. (d)

Free body diagram

From ΣF_y

$$T = F_{B1} - W_1$$

$$F_{B1} = \rho g (V)_{\text{submerged}} = (9.8 \times 1000)(50 \times 50 \times 7.5)(10^{-9})$$

$$F_{B1} = 0.18375 \text{ N}$$

$$W_1 = \gamma (\text{Specific gravity of block}) \times \text{Volume of block} = (9.8 \times 1000)(0.3)(50 \times 50 \times 10)(10^{-9}) = 0.0735 \text{ N}$$

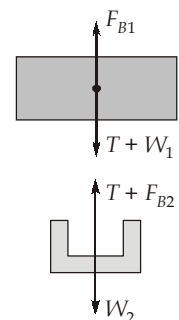
$$T = (0.18375 - 0.0735) = 0.11025 \text{ N}$$

Force equilibrium (vertical direction) applied to metal part:

$$F_{B2} = \gamma V_2 = (9800)(6600)(10^{-9}) = 0.06468 \text{ N}$$

$$W_2 = T + F_{B2} = (0.1102 \text{ N}) + (0.06468 \text{ N})$$

Mass of metal part, $m_2 = \frac{W_2}{g} = 0.01785 \text{ kg}$



141. (113.53)(113.50 to 113.59)

$$\overline{Nu} = C Re^m Pr^n$$

$$\overline{h}L \propto (VL)^m$$

$$\frac{h_1 L_1}{h_2 L_2} = \left(\frac{V_1 L_1}{V_2 L_2} \right)^m$$

$$L_1 = L_2 = L$$

$$\therefore \frac{60}{30} = \left(\frac{25}{15} \right)^m$$

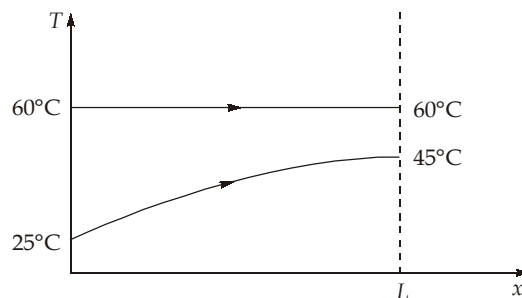
$$\therefore m = 1.3569$$

When $V = 40$ m/s

$$\frac{\overline{h}}{60} = \left(\frac{40}{25} \right)^{1.3569}$$

$$\Rightarrow h = 113.53 \text{ W/m}^2\text{K}$$

142. (c)



$$\Delta T_i = 60 - 25 = 35^\circ\text{C}$$

$$\Delta T_e = 60 - 45 = 15^\circ\text{C}$$

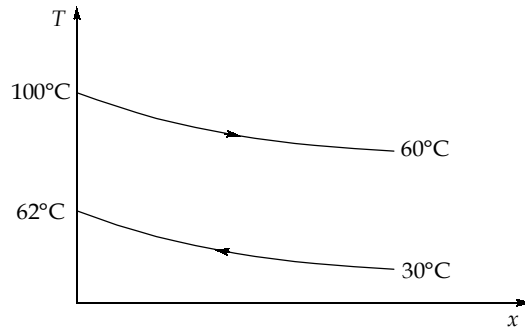
$$\text{LMTD} = \frac{\Delta T_i - \Delta T_e}{\ln\left(\frac{\Delta T_i}{\Delta T_e}\right)} = \frac{35 - 15}{\ln\left(\frac{35}{15}\right)} = 23.60^\circ\text{C}$$

$$q = UA(\text{LMTD}) = \dot{m}_s h_{fg}$$

$$2000 \times 30 \times 23.60 = \dot{m}_s \times 2358 \times 10^3$$

$$\dot{m}_s = 0.6 \text{ kg/s}$$

143. (70.23)(70.12 to 70.32)



$$q = \dot{m}_h c_{ph} (T_{h,i} - T_{h,o}) = 0.7 \times 2400 \times (100 - 60) = 67200 \text{ W}$$

$$\begin{aligned} 67200 &= \dot{m}_c c_{pc} (T_{c,o} - T_{c,i}) \\ &= 0.5 \times 4200 (T_{c,o} - 30) \end{aligned}$$

$$T_{c,o} = 62^\circ\text{C}$$

$$\text{LMTD} = \frac{\Delta T_1 - \Delta T_2}{\ln \frac{\Delta T_1}{\Delta T_2}} = \frac{38 - 30}{\ln \frac{38}{30}} = 33.84^\circ\text{C}$$

$$q = UA(\text{LMTD})$$

$$67200 = 300 \times 33.84 \times \pi(0.03)L$$

$$L = 70.228 \text{ m} \approx 70.23 \text{ m}$$

144. (466.8)(465 to 467)

$$\dot{q}_{12} = \frac{\sigma(T_1^4 - T_2^4)}{\frac{1-\epsilon_1}{\epsilon_1 A_1} + \frac{1}{F_{12}A_1} + \frac{1-\epsilon_1}{\epsilon_2 A_2}}$$

$$F_{12} = 1$$

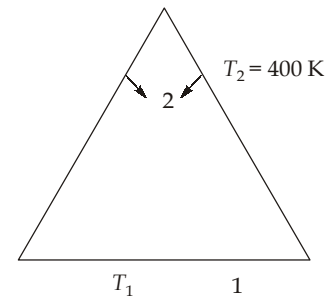
$$A_1 = 1.5 \times 1 = 1.5 \text{ m}^2$$

$$A_2 = 2 \times 1.5 \times 1 = 3 \text{ m}^2$$

$$1000 = \frac{5.67 \times 10^{-8} (T_1^4 - 400^4)}{\frac{1-0.9}{1.5 \times 0.9} + \frac{1}{1.5} + \frac{1-0.4}{3 \times 0.4}}$$

Solving,

$$T_1 = 466.8 \text{ K}$$



145. (5)(4.99 to 5.01)

For infinitely long fin,

$$\dot{q} = \sqrt{hPkA} (T_b - T_\infty)$$

For circular fin, $P = \pi D$

$$A = \frac{\pi D^2}{4}$$

So,

$$\dot{q} = \sqrt{h \times \pi D \times k \times \frac{\pi}{4} D^2} (T_b - T_\infty)$$

$$\dot{q} \propto \sqrt{k} D^{3/2}$$

$$\frac{\dot{q}_1}{\dot{q}_2} = \frac{\sqrt{k_1} D_1^{3/2}}{\sqrt{k_2} D_2^{3/2}} = \left(\frac{400}{250}\right)^{1/2} \left(\frac{D}{0.4D}\right)^{3/2} = 5$$

146. (6.93)(6.92 to 6.94)

$$\frac{T(t) - T_\infty}{T_i - T_\infty} = e^{-bt}$$

$$\Rightarrow \frac{\frac{T_i + T_\infty}{2} - T_\infty}{T_i - T_\infty} = e^{-bt}$$

$$\Rightarrow \frac{1}{2} = e^{-bt}$$

Where $b = \frac{1}{\tau}$

Time required, $t = \frac{\ln 2}{b}$

$$= \tau \ln 2 = 10 \times 0.693 = 6.93 \text{ s}$$

147. (c)

Wall thickness, $\delta = 10 \text{ mm} = 0.01 \text{ m}$

As given in question,

Thermal conductivity, $k = ax + b$

Heat flux, $q'' = -k \frac{dT}{dx}$

$$q'' = -(ax + b) \frac{dT}{dx}$$

$$\frac{q''}{ax + b} dx = -dT$$

On integrating,

$$q'' \int_0^\delta \frac{dx}{ax + b} = - \int_{T_1}^{T_2} dT$$

$$\Rightarrow \frac{q''}{a} [\ln|ax+b|]_0^\delta = -(T_2 - T_1)$$

$$\Rightarrow \frac{q''}{a} \ln \left| \frac{a\delta+b}{a \times 0+b} \right| = (T_1 - T_2)$$

$$\Rightarrow \frac{q''}{a} \ln \left| \frac{a\delta+b}{b} \right| = (T_1 - T_2)$$

$$\frac{3.723 \times 10^6}{7 \times 10^4} \ln \left| \frac{7 \times 10^4 \times 0.01 + 200}{200} \right| = (100 - T_2)$$

$$T_2 = 20.0046^\circ\text{C}$$

$$T_2 \simeq 20^\circ\text{C}$$

148. (b, c)

The laminar sublayer is a region, next to the wall where viscous force is predominate while the rest of the flow is turbulent.

149. (a, c, d)

150. (c, d)

In free convection,

$$\text{Nu} = C(\text{Gr} \cdot \text{Pr})^{1/4}, \text{ for laminar flow}$$

$$\text{Nu} = C(\text{Gr} \cdot \text{Pr})^{1/3}, \text{ for turbulent flow}$$

