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Important Questions for **GATE 2022**

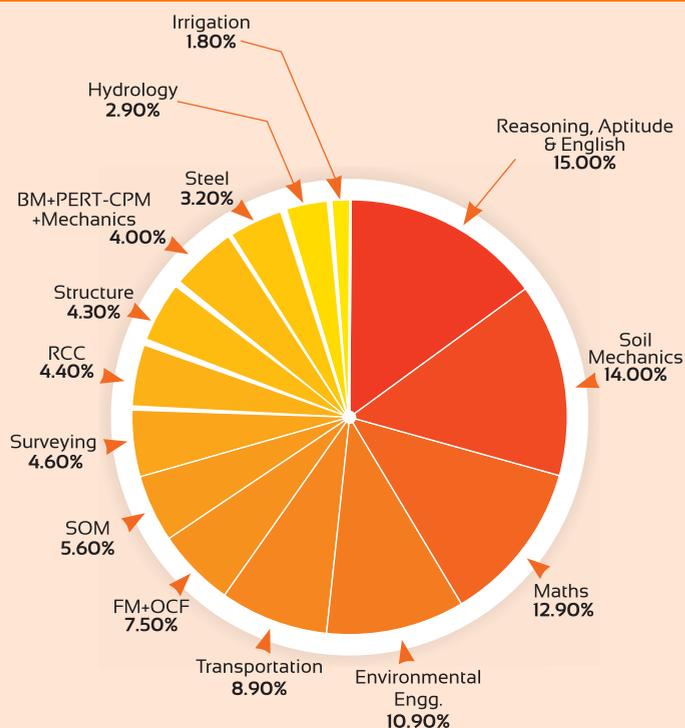
CIVIL ENGINEERING

Day 3 of 8

Q.51 - Q.75 (Out of 200 Questions)

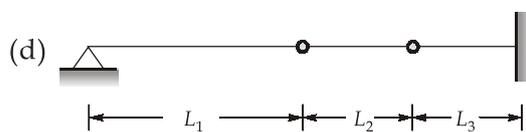
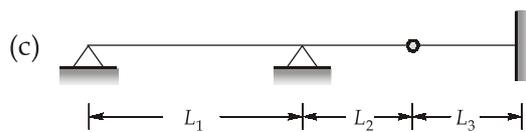
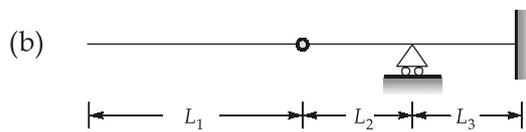
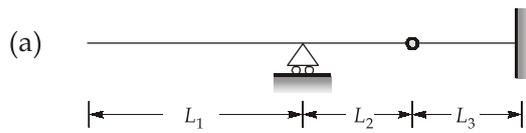
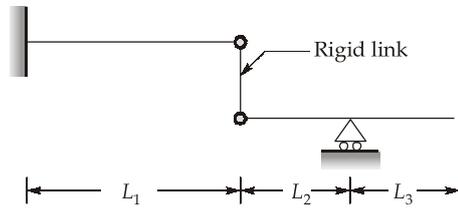
Solid Mechanics + RCC Structures and Prestressed Concrete

SUBJECT-WISE WEIGHTAGE ANALYSIS OF GATE SYLLABUS

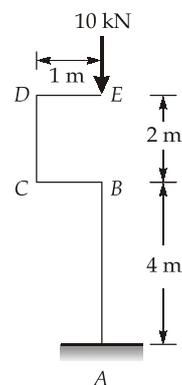


Subject	Average % (last 5 yrs)
Reasoning, Aptitude and English	15.00%
Soil Mechanics	14.00%
Engineering Mathematics	12.90%
Environmental Engineering	10.90%
Transportation Engineering	8.90%
Fluid Mechanics + OCF	7.50%
Strength of Materials	5.60%
Surveying Engineering	4.60%
Reinforced Cement Concrete	4.40%
Structural Analysis	4.30%
Building Materials+PERT-CPM+Mechanics	4.00%
Steel Structures	3.20%
Engineering Hydrology	2.90%
Irrigation Engineering	1.80%
Total	100%

Q.55 For the beam as shown in figure given below, which among the following is the conjugate beam?

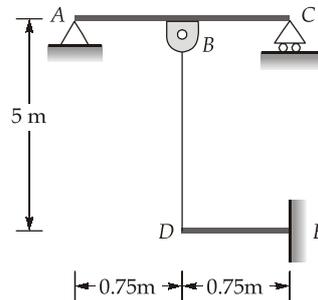


Q.56 What is the bending moment (in kN-m) at A for the bent column as shown in the figure given below?



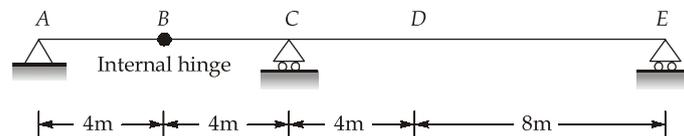
- (a) Zero
(c) 20

- (b) 10
(d) 40



- (a) 526.39 and tension (b) 526.39 and compression
(c) 775.41 and tension (d) 775.41 and compression

Q.61 A beam with internal hinge B is shown in figure below. A concentrated moving load of 5 kN and a uniform moving load of 500 N/m is subjected to beam together.



The maximum positive bending moment that can be developed at point ' D ' in the beam is _____ kNm.

[Consider self weight of beam = 300 N/m]

- Q.62** A beam is subjected to an axial compressive force of 100 kN along with the transverse loading. Maximum shear force in the section is 125 kN, and it has longitudinal tension reinforcement of 900 mm². Take M20 grade concrete and Fe415 grade steel. Corresponding to 0.6% of steel the design shear strength of M20 concrete is 0.512 N/mm². The design shear strength of given beam (in N/mm² correct upto 2-decimal places) is [Use LSM]
- Q.63** A beam section of size 400 mm × 600 mm and of span 8 mm is doubly reinforcement as limiting section. Area of reinforcement required in tension side to sustain under live load of 35 kNm will be _____ mm². [Take $f_{ck} = 20$ N/mm², $f_y = 415$ N/mm², $d_c = 50$ mm, effective cover = 50 mm]
- (a) 1745 mm² (b) 1196 mm²
(c) 3000 mm² (d) 3898 mm²
- Q.64** An isolated footing of size 4 m × 4 m supports square column of size 500 mm × 500 mm. The column is subjected to 3000 kN service load. Assume M 20 grade concrete for footing and M 25 grade concrete for the column. The bearing resistance of concrete at column footing interface is _____ kN.

- Q.69** A concrete beam is prestressed by a cable carrying an initial prestressing force of 500 kN. The cross-sectional area of the wires in the cable is 500 mm². The ratio of percentage loss of stress in the cable due to shrinkage of concrete in pre-tensioned and post-tensioned prestressed beam is _____. [Assume modulus of elasticity of steel (E_s) = 210 kN/mm² and age of concrete at transfer = 8 days]
- Q.70** If a simply supported concrete beam prestressed with a force of 2500 kN is designed by load balancing concept for an effective span of 10 m and to carry a uniformly distributed load of 40 kN/m (including self weight) then the central dip of the cable profile should be
- (a) 100 mm (b) 300 mm
(c) 200 mm (d) 400 mm
- Q.71** The deflection of prestressed concrete beam is excessive in the
- (a) Pre - cracking stage (b) Plastic stage
(c) Post - cracking stage (d) None of the above

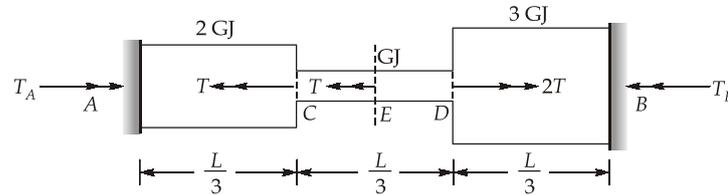
Multiple Select Questions (MSQ)

- Q.72** Which of the following statements are correct?
- (a) All load carrying members transmit load through basic modes of tension, compression, torsion and shear only.
(b) Beams carry transverse loads.
(c) Combined loading is a complicated loading.
(d) Nature of internal forces decides the aspect of combined loading.
- Q.73** Consider the following statements:
Mohr's Circle is used to determine the stress on an oblique section of a body subjected to
- (a) direct tensile stress on one plane accompanied by a shear stress.
(b) direct tensile stresses in two mutually perpendicular directions accompanied by a simple shear stress.
(c) direct tensile stress in two mutually perpendicular directions.
(d) a simple shear stress
- Q.74** Consider the following statements:
Percentage of steel for balanced design of a singly reinforced rectangular section by limit state method depends on
- (a) Characteristic strength of concrete.
(b) Yield strength of concrete.
(c) Modulus of elasticity of steel.
(d) Geometry of the section.
- Q.75** Shear strength of concrete in a reinforced concrete beam is a function of which of the following:
- (a) Compressive strength of concrete
(b) Percentage of shear reinforcement
(c) Percentage of longitudinal reinforcement in tension in the section
(d) Percentage total longitudinal reinforcement in the section



Detailed Explanations

51. (c)



From figure since both the ends is fixed

We know that,

$$\theta_{AB} = 0$$

$$\theta_{AC} + \theta_{CE} + \theta_{ED} + \theta_{DB} = 0$$

$$\frac{T_A \cdot L}{6GJ} + \frac{(T_A - T)L}{3GJ} + \frac{(T_A - 2T)L}{3GJ} + \frac{(T_A - 2T + 2T)L}{9GJ} = 0 \quad \left(\because \theta = \frac{TL}{GJ} \right)$$

$$\Rightarrow \frac{17}{18} T_A = \frac{T}{T_A} = \frac{18T}{17}$$

52. 55.35 (52 - 56)

$$\text{Torque in left half shaft, } T_1 = \frac{746 \times 25}{(200 \times 2\pi / 60)} = 890.47 \text{ N-m} \quad (\because \omega = 2\pi N / 60)$$

$$\text{Torque in right half shaft, } T_2 = \frac{746 \times 40}{(200 \times 2\pi / 60)} = 1424.75 \text{ N-m}$$

$$\text{Maximum shear stress, } \tau = \frac{Tr}{J}$$

$$\tau = \frac{1424.75 \times \left(\frac{0.0508}{2} \right)}{\frac{\pi}{32} (0.0508)^4} = 55.35 \text{ MPa}$$

53. (a)

As the cross section area of circular beam is increased upto 4 times, then it means that the diameter is increased by two times.

(i) Maximum bending moment does not depend upon the cross sectional property of the beam i.e. A - 2.

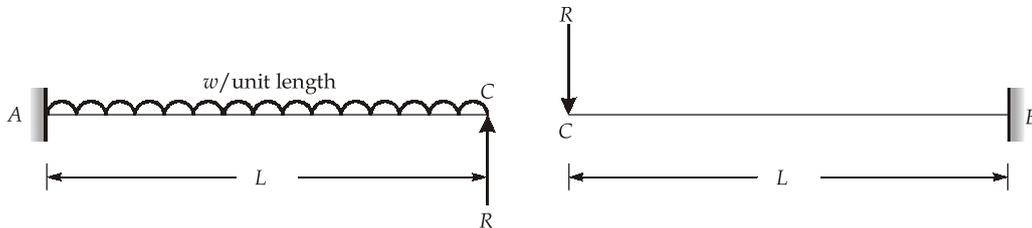
(ii) Deflection $\propto \frac{1}{I} \propto \frac{1}{A^2}$ i.e. B - 4

(iii) Bending stress $\propto \frac{1}{I/y} \propto \frac{y}{A^2} = \frac{1}{8} \left(\frac{D/2}{A^2} \right)$ i.e. C - 3

(iv) $Z \propto \frac{I}{y} \propto \frac{A^2}{y} = \frac{16}{2} \left(\frac{A^2}{D/2} \right) = 8 \left(\frac{A^2}{D/2} \right)$ i.e. D - 1

54. 187.5 (186 - 189)

Free body diagram of the given beam is shown below



Deflection of point C remains same for beam AC and CB.

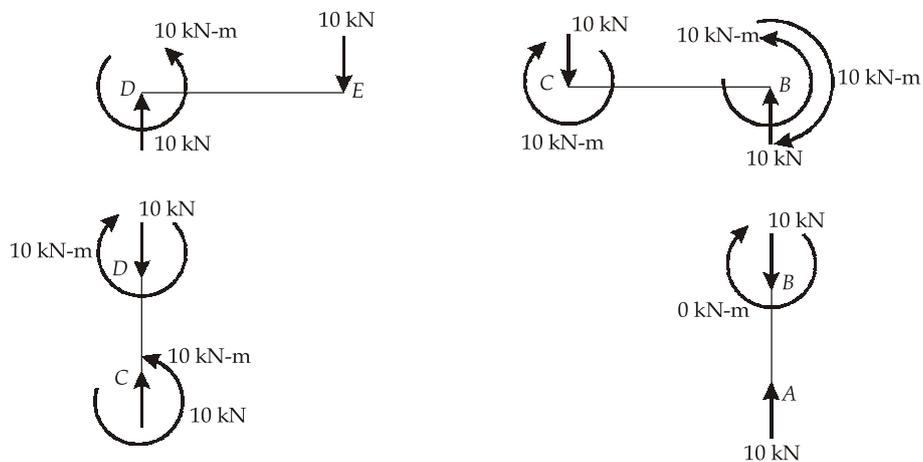
$$\Rightarrow \frac{wL^4}{8EI} - \frac{RL^3}{3EI} = \frac{RL^3}{3EI}$$

$$\Rightarrow \frac{2RL^3}{3EI} = \frac{wL^4}{8EI}$$

$$\Rightarrow R = \frac{3}{16}wL \times 1000 = 187.5wL \text{ N}$$

55. (a)

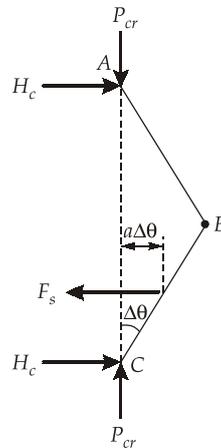
56. (a)



\therefore Bending moment at A = 0 kN-m

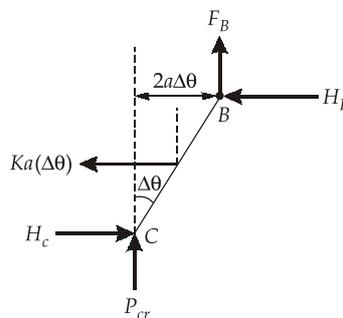
57. (b)

A free body diagram of the entire system of two rigid bars is shown below



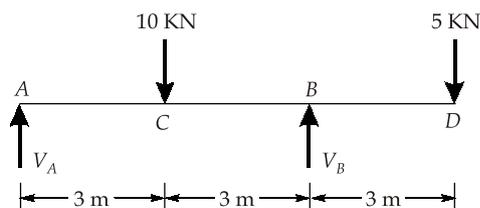
Take, $\sum M_A = 0$
 $\Rightarrow H_c \times 4a - F_s \times 3a = 0$
 $\Rightarrow H_c \times 4a - ka(\Delta\theta) \times 3a = 0$
 $\therefore H_c = \frac{3ka(\Delta\theta)}{4}$

Now, for the calculation of critical load, consider the free body diagram of lower bar BC, shown below



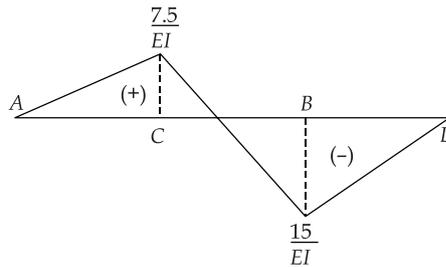
Take, $\sum M_B = 0$
 $\Rightarrow H_c \times 2a - P_{cr} \times 2a(\Delta\theta) - ka(\Delta\theta) \times a = 0$
 $\Rightarrow P_{cr} = \frac{ka}{4}$

58. (a)



$$\begin{aligned} \Sigma F_y &= 0 \\ \therefore V_A + V_B &= 15 && \dots (i) \\ \text{Taking, } \Sigma M_A &= 0 \\ \Rightarrow 10 \times 3 + 5 \times 9 &= V_B \times 6 \\ \therefore V_B &= 12.5 \text{ kN} \\ \text{and } V_A &= 2.5 \text{ kN} && \text{(by using equation (i))} \end{aligned}$$

$\frac{M}{EI}$ diagram of the above beam is shown below



From moment area theorem:

$$\begin{aligned} \Delta_C &= \theta_A \times L_{AC} - \delta_{C/A} \\ &= \frac{7.5}{EI} \times 3 - \left(\frac{1}{2} \times \frac{7.5}{EI} \times 3 \right) \times \frac{1}{3} \times 3 = \frac{11.25}{EI} \end{aligned}$$

59. 17.3 (17.1 - 17.4)

Strain energy stored will be given as,

$$U = \frac{1}{2E} [\sigma_1^2 + \sigma_2^2 - 2\mu\sigma_1\sigma_2] \times \text{Volume}$$

where, $\sigma_1 = \frac{50 \times 10^3}{30 \times 10} = 166.67 \text{ N/mm}^2$ (Tensile)

Also, $\sigma_2 = -100 \text{ N/mm}^2$ (i.e. compressive)

$$\Rightarrow U = \frac{1}{2 \times 2 \times 10^5} [(166.67)^2 + (-100)^2 - 2 \times 0.25 \times 166.67 \times (-100)] \times (500 \times 30 \times 10)$$

$$\therefore U = 17292 \text{ N-mm} = 17.29 \text{ J} \approx 17.3 \text{ J}$$

60. (c)

$$\begin{aligned} \text{Contraction of steel wire} &= L \propto \Delta T \\ &= 5 \times 10^3 \times 12 \times 10^{-6} \times 30 = 1.8 \text{ mm} \end{aligned}$$

Let, P be the force developed in wire due to contraction

$$\therefore \frac{Pl_1^3}{48EI} + \frac{Pl_2^3}{3EI} - \frac{Pl}{AE} = 1.8 \times 10^{-3}$$

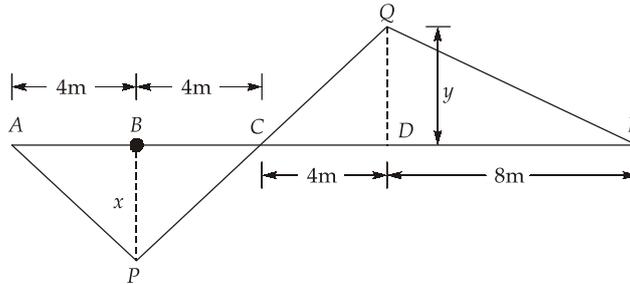
$$\frac{P}{EI} \left[\frac{l_1^3}{48} + \frac{l_2^3}{3} \right] - \frac{Pl}{AE} = 1.8 \times 10^{-3}$$

$$\Rightarrow \frac{P}{85 \times 10^3} \left[\frac{(1.5)^3}{48} + \frac{(0.75)^3}{3} \right] - \frac{P \times 5}{156 \times 2 \times 10^5} = 1.8 \times 10^{-3}$$

$$\therefore P = 775.41 \text{ N (tension)}$$

61. 22.96 (22 - 24)

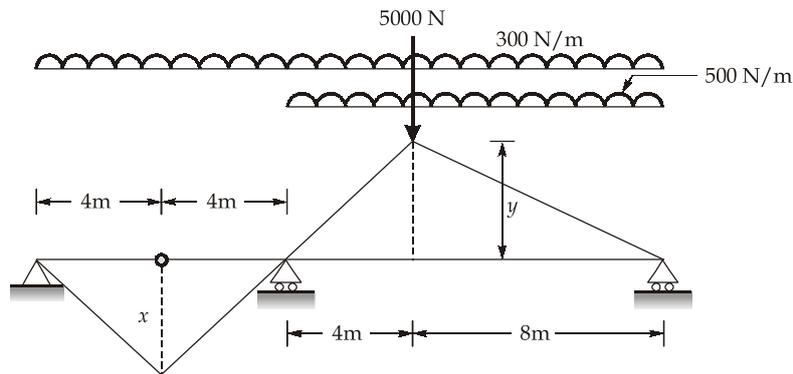
ILD for moment $M_D \rightarrow$



Ordinate 'y' \rightarrow

$$y = \frac{a(l-a)}{l} = \frac{4 \times 8}{12} = 2.67$$

In ΔBPC and ΔCQD , $x = y = 2.67$



$$M_{D_{\max}} = 5000 \times 2.67 + 500 \times \frac{1}{2} \times 12 \times 2.67 + 300 \times \frac{1}{2} \times 12 \times 2.67 - 300 \times \frac{1}{2} \times 8 \times 2.67$$

$$M_{D_{\max}} = 22.96 \text{ kNm}$$

62. 0.56 (0.54 - 0.58)

$$A_{st} = 900 \text{ mm}^2$$

$$p_t = 0.6\%$$

$$0.6 = \frac{A_{st}}{A_g} \times 100$$

$$A_g = 150000 \text{ mm}^2$$

Design shear strength of M20 concrete = 0.512 MPa.

As per IS 456:2000 Clause 40.2.2,

for members subjected to axial compression only, the design shear strength of concrete calculated on the basis of percentage of steel and grade of concrete is multiplied by the following factor

$$\delta = 1 + \frac{3P_u}{A_g \times f_{ck}} = 1 + \frac{3 \times 100 \times 1000}{300 \times 500 \times 20} = 1.1 < 1.5$$

So, design shear strength of beam = $1.1 \times 0.512 = 0.5632$ MPa.

63. (c)

$$\text{Dead load} = 0.4 \times 0.6 \times 1 \times 25 = 6 \text{ kN/m} \quad (x_u)_{\text{lim}} = 0.48 d \text{ (for 415)}$$

$$\text{Live load} = 35 \text{ kN/m}$$

$$\text{Total factored load} = 1.5 (6 + 35) = 61.5 \text{ kN/m}$$

$$\text{Bending moment (m)} = \frac{wl^2}{8} = \frac{61.5 \times 8^2}{8} = 492 \text{ kNm}$$

Now, moment resisting for a singly reinforced section (MR_1)

$$MR_1 = 0.36 f_{ck} B x_{u \text{ lim}} (d - 0.42 x_{u \text{ lim}})$$

$$MR_1 = 0.36 \times 20 \times 400 \times 0.48 \times 550 \times (550 - 0.42 \times 0.48 \times 550)$$

$$MR_1 = 333.87 \text{ kNm}$$

$$MR_2 = \text{Moment has to resist by compression steel} = 492 - 333.87$$

$$MR_2 = 158.13$$

$$A_{st} = \frac{MR_1}{0.87 f_y (d - 0.42 x_{u \text{ lim}})} + \frac{MR_2}{0.87 f_y (d - d_c)}$$

$$A_{st} = \frac{333.87 \times 10^6}{0.87 \times 415 \times [550 - 0.42 \times 0.48 \times 550]} + \frac{158.13 \times 10^6}{0.87 \times 415 \times (550 - 50)}$$

$$A_{st} = 2982 \text{ mm}^2 \simeq 3000 \text{ mm}^2$$

64. 2812.5 (2810 - 2820)

Limiting bearing stress at column footing interface

$$f_{br, \text{ max}} = 0.45 f_{ck} \sqrt{\frac{A_1}{A_2}}$$

(i) For column face

$$f_{ck} = 25 \text{ MPa}$$

$$A_1 = A_2 = (500)^2 \text{ mm}^2 = 250000 \text{ mm}^2$$

$$\begin{aligned} f_{br, \text{ max - col.}} &= 0.45 \times 25 \times \sqrt{\frac{(500)^2}{(500)^2}} \\ &= 11.25 \text{ MPa} \end{aligned}$$

(ii) For footing face

$$f_{ck} = 20 \text{ MPa}$$

$$A_1 = (4000)^2 \text{ mm}^2$$

$$A_2 = (500)^2 \text{ mm}^2$$

$$\sqrt{\frac{A_1}{A_2}} = \sqrt{\frac{(4000)^2}{(500)^2}} = \frac{4000}{500} = 8 \neq 2$$

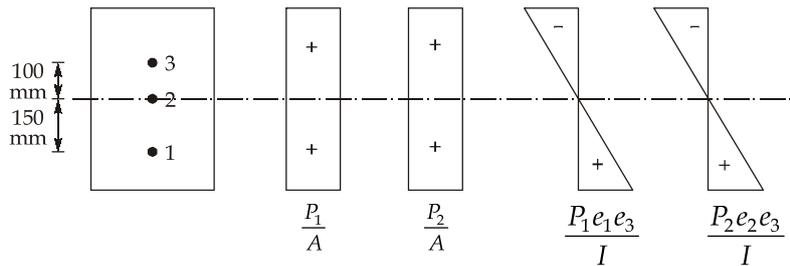
$$\therefore \sqrt{\frac{A_1}{A_2}} = 2$$

$$\Rightarrow f_{br, \text{max - footing}} = 0.45 \times 20 \times 2 = 18 \text{ MPa}$$

Limiting bearing stress is minimum of above two

$$\text{Limiting bearing resistance} = \frac{11.25 \times (500)^2}{1000} = 2812.5 \text{ kN}$$

65. 33.40 (32.00 - 37.00)



At ends: $e_1 = 150 \text{ mm}, e_2 = 0, e_3 = 100 \text{ mm}$

$$f_{c1} = \frac{P_1}{A} + \frac{P_2}{A} - \frac{P_1 e_1 e_3}{I} - \frac{P_2 e_2 e_3}{I}$$

$$f_{c1} = \frac{950 \times 10^3}{800 \times 500} + \frac{950 \times 10^3}{800 \times 500} - \frac{950 \times 10^3 \times 150 \times 100}{500 \times \frac{800^3}{12}} - \frac{950 \times 10^3 \times 0 \times 100}{500 \times \frac{800^3}{12}}$$

At mid span:

$$f_{c1} = 2.375 + 2.375 - 0.6679 - 0 = 4.0821 \text{ N/mm}^2$$

$$e_1 = e_2 = e_3 = 150 \text{ mm}$$

$$f_{c2} = \frac{P_1}{A} + \frac{P_2}{A} + \frac{P_1 e_1 e_3}{I} + \frac{P_2 e_2 e_3}{I}$$

$$f_{c2} = 2.375 + 2.375 + 2 \times \frac{950 \times 10^3 \times 150 \times 150}{500 \times \frac{800^3}{12}}$$

$$f_{c2} = 6.75 \text{ N/mm}^2$$

$$\text{Loss of stress} = m(f_c)_{avg}$$

$$= m \left[f_{c1} + \frac{2}{3}(f_{c2} - f_{c1}) \right]$$

$$= 5.7 \left[4.0821 + \frac{2}{3}(6.75 - 4.0821) \right]$$

$$= 33.40 \text{ N/mm}^2$$

66. 11.25 (10.75 - 11.50)

As per clause 23.3 of IS 456 : 2000

$$\left. \begin{array}{l} L \leq 25 B \\ \frac{100B^2}{d} \end{array} \right\} \text{minimum of two}$$

or

$$\Rightarrow L \leq 11.25 \text{ m or } 33.75 \text{ m}$$

$$\therefore L = 11.25 \text{ m}$$

67. (c)

$$\text{Effective depth, } d = 400 - 35 = 365 \text{ mm}$$

$$\text{Percentage tension steel, } p_t = \frac{100 A_{st}}{bd}$$

$$= \frac{100 \times 5 \times \frac{\pi}{4} \times 25^2}{300 \times 365}$$

$$= 2.24\% > p_{t\text{lim}} \left(= 41.61 \frac{f_{ck}}{f_y} \frac{x_{u\text{lim}}}{d} = 41.61 \times \frac{20}{415} (0.48) = 0.96\% \right)$$

\therefore Doubly reinforced section is required.

Design shear strength of concrete,

$$\tau_c = 0.79 + \frac{0.81 - 0.79}{2.25 - 2.00} (2.24 - 2.00)$$

$$\tau_c = 0.8092 \text{ N/mm}^2 \quad [\text{From table for } p_t = 2.24\%]$$

$$\text{Nominal shear stress, } \tau_v = \frac{V_u}{bd} = \frac{240 \times 10^3}{300 \times 365} = 2.19 \text{ N/mm}^2$$

$$\text{Area of shear stirrups, } A_{sv} = 2 \times \frac{\pi}{4} \times 12^2 = 226.19 \text{ mm}^2$$

\therefore Spacing of vertical shear stirrups,

$$S_v = \frac{0.87 f_y A_{sv} d}{(\tau_v - \tau_c) bd}$$

$$= \frac{0.87 \times 415 \times 226.19}{(2.19 - 0.8092) \times 300} \simeq 197 \text{ mm } (< 0.75d = 273.75 \text{ mm})$$

68. (d)

Average initial stress in concrete

$$f_c = \left(\frac{300 \times 10^3}{250 \times 250} \right) = 4.8 \text{ N/mm}^2$$

$$\text{Modular ratio, } m = \frac{E_s}{E_c} = 6.56$$

Loss due to elastic deformation

$$= \frac{E_s}{E_c} \times f_c = 6.56 \times 4.8$$

$$= 31.488 \text{ N/mm}^2 \simeq 31.5 \text{ N/mm}^2$$

Loss due to creep of concrete

$$\phi m f_c = 1.6 \times 6.56 \times 4.8 = 50.381 \text{ N/mm}^2 \simeq 50.38 \text{ N/mm}^2$$

Loss due to shrinkage of concrete

$$\begin{aligned} &= (200 \times 10^{-6}) \times E_s \\ &= 200 \times 10^{-6} \times 2.1 \times 10^5 \\ &= 42 \text{ N/mm}^2 \end{aligned}$$

Therefore, all options (i), (ii) and (iii) are correct.

69. 1.50 (1.40 - 1.60)

$$\text{Initial stress in wire} = \frac{500 \times 10^3}{500} = 1000 \text{ N/mm}^2$$

When the beam is pretensioned, the total residual shrinkage strain = 3×10^{-4} units

$$\therefore \text{Loss of stress} = (3 \times 10^{-4}) (210 \times 10^3) = 63 \text{ N/mm}^2$$

$$\therefore \text{Percentage loss of stress} = \left(\frac{63}{1000} \times 100 \right) = 6.3\%$$

When the beam is post tensioned, the total residual shrinkage strain

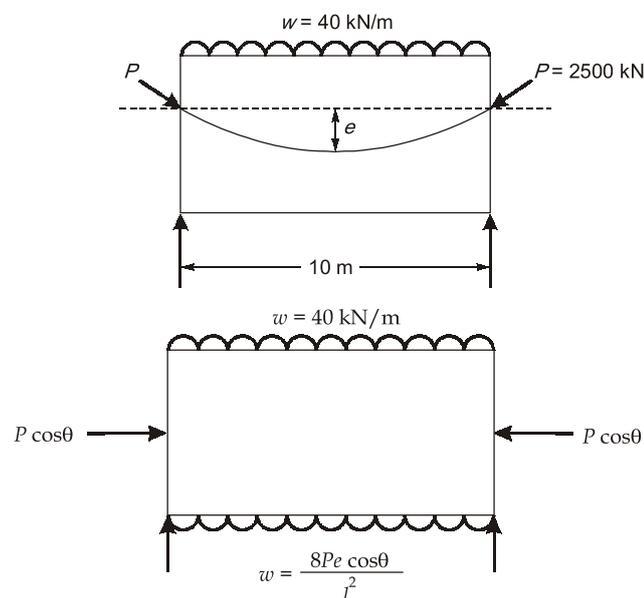
$$= \left[\frac{2 \times 10^{-4}}{\log_{10}(8+2)} \right] = 2 \times 10^{-4} \text{ units}$$

$$\therefore \text{Loss of stress} = (2 \times 10^{-4}) \times (210 \times 10^3) = 42 \text{ N/mm}^2$$

$$\therefore \text{Percentage loss of stress} = \left(\frac{42}{1000} \times 100 \right) = 4.2\%$$

$$\text{Required ratio} = \frac{6.3}{4.2} = 1.50$$

70. (c)



$$w = \frac{8Pe \cos \theta}{l^2}$$

$$\Rightarrow 40 = \frac{8 \times 2500 \times e \times 1}{10^2} \quad [\because \theta \text{ is very small thus } \cos \theta \simeq 1]$$

$$\Rightarrow \begin{aligned} e &= 0.2 \text{ m} \\ e &= 200 \text{ mm} \end{aligned}$$

71. (c)

72. (a, b)

Combined loading is not a complicated loading.

73. (a, b, c, d)

If the state of stress on two planes and angle between those planes is known, then with the help of Mohr's circle we can determine stresses on oblique section.

74. (a, c, d)

Percentage of steel is dependent on characteristic strength of concrete (f_{ck}) rather than its yield strength.

75. (a, c)

The design shear strength of concrete in RC beam depends upon grade of concrete i.e. compressive strength of concrete; percentage of longitudinal tension reinforcement; and axial compressive force.

