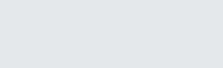


WORKDOOK 2025



Detailed Explanations of Try Yourself *Questions*

Electrical EngineeringSignals and Systems





Introduction



Detailed Explanation

of

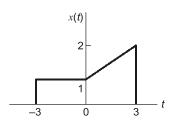
Try Yourself Questions

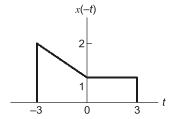
T1: Solution

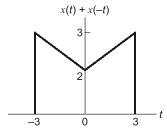
(a)

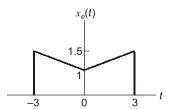
Even part of
$$x(t)$$
, $x_{\theta}(t) = \frac{1}{2} [x(t) + x(-t)]$

Signal $x_e(t)$ is obtained as follows:









T2: Solution

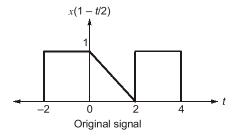
(c)

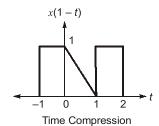
We can perform following sequence of transformation.

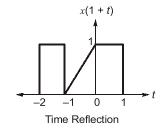
$$x\left(1-\frac{t}{2}\right) \xrightarrow{t-2t} x(1-t) \xrightarrow{t\to -t} x(t+1) \xrightarrow{t\to t-1} x(t)$$
 time compression $x(t+1) \xrightarrow{t\to t-1} x(t)$

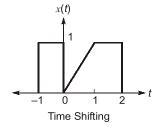


Graphically it is obtained as









T3: Solution

(a)

The expression of x(t) is $x(t) = \sum_{k=-\infty}^{\infty} \delta(t-4k) - \delta(t-4k-1)$.

So x(t) is a subtraction of two signals each periodic with period 4. So x(t) is periodic with period 4.

T4: Solution

The signal is,

$$x(t) = 3e^{-t}u(t)$$

Now, energy of signal will be

$$E_x = \int_{0}^{\infty} [3e^{-t}]^2 dt = 4.5$$

T5: Solution

(d)

$$y(t) = 4^{2} \cos^{2} \left(200t + \frac{\pi}{6} \right)$$

$$= 4^{2} \frac{\left(1 + \cos 2 \left(200t + \frac{\pi}{6} \right) \right)}{2}$$

$$= 8 + 8 \cos \left(400t + \frac{\pi}{3} \right)$$

Thus the DC component is 8.



T6: Solution

(b)

Cosine function is a periodic signal. As all periodic signals are power signals, therefore the given signal is power signal.

T7: Solution

(a)

$$\int_{-\infty}^{\infty} \delta(t) \cos\left(\frac{3t}{2}\right) dt = f(0) = \cos\left(\frac{3\times0}{2}\right) = \cos 0 = 1$$



Fourier Series



Detailed Explanation

Try Yourself Questions

T1: Solution

(a)

Given that Fourier series coefficient of x(t) is a_k

$$x(t) \xrightarrow{\text{F.S.}} a_k$$

Now, real part of x(t) is $\frac{x(t) + x^*(t)}{2}$

and if

$$x(t) \xrightarrow{\text{F.S.}} a_k$$

$$x^*(t) \xrightarrow{\text{F.S.}} a_{-k}^*$$

then

$$x^*(t) \xrightarrow{\mathsf{F.S.}} a^*_{-k}$$

So real part of
$$x(t)$$
,
$$\frac{x(t) + x^*(t)}{2} \xrightarrow{\text{F.S.}} \frac{a_k + a_{-k}^*}{2}$$

T2: Solution

(d)

T3: Solution

(b)

T4: Solution

$$\sum_{-\infty}^{\infty} |C_n|^2 \Rightarrow \sum_{-2}^{2} |C_n|^2$$

$$= \sum_{n=2}^{2} |C_n|^2 = (2)^2 + (8)^2 + (8)^2 + (2)^2 = 136$$

Publications

Fourier Transform



Detailed Explanation

Try Yourself Questions

T1: Solution

(b)

The Fourier transform is $X(\omega) = u(\omega) - u(\omega - 2)$, we know that

- If signal is real then $X(\omega)$ is conjugate symmetric.
- If signal is imaginary then $X(\omega)$ is conjugate anti-symmetric

The given $\textit{X}(\omega)$ is neither conjugate symmetric nor conjugate anti-symmetric.

So x(t) is complex signal.

T2: Solution

(c)

Fourier transform of x(t)

$$X(j\omega) = \int_{-\infty}^{\infty} x(t)e^{-j\omega t}dt = \int_{-\infty}^{\infty} x(t)\cos(\omega t)dt - j\int_{-\infty}^{\infty} x(t)\sin(\omega t)dt$$

If x(t) is odd, then x(t) sin ωt is an even function and x(t) cos ωt is an odd function.

So,
$$\int_{-\infty}^{\infty} x(t) \cos(\omega t) dt = 0$$

and,
$$X(j\omega) = \int_{-\infty}^{\infty} x(t) \sin(\omega t) dt$$

or,
$$X(j\omega) = -2j\int_{0}^{\infty} x(t)\sin(\omega t)dt$$

T3: Solution

(a)

Given $X(j\omega)$ is real and odd, so x(t) is imaginary and odd.



T4: Solution

(a)

Fourier transform is
$$G(\omega) = \frac{\omega^2 + 21}{\omega^2 + 9}$$

So,
$$G(\omega) = \frac{\omega^2}{\omega^2 + 9} + \frac{21}{\omega^2 + 9} = 1 + \frac{12}{\omega^2 + 9}$$

As we know that Fourier transform of $e^{-a|t|}$ is $\frac{2a}{a^2 + \omega^2}$

So
$$g(t) = \delta(t) + 2\exp(-3|t|)$$

T5: Solution

(d)

If,
$$x(t) \stackrel{F}{\longleftrightarrow} X(j\omega)$$

then, $\frac{dx(t)}{dt} \stackrel{F}{\longleftrightarrow} (j\omega)X(j\omega)$ (Time differentiation property)
and, $\frac{d^2x(t)}{dt^2} \stackrel{F}{\longleftrightarrow} -\omega^2X(j\omega)$
 $\frac{d^2[x(t-2)]}{dt^2} \stackrel{F}{\longleftrightarrow} -\omega^2e^{-j2\omega}X(j\omega)$ (Time-shifting property)

T6: Solution

(a)

We have,
$$y(t) = \int_{-\infty}^{\tau} x(\tau)d\tau$$

$$\int_{-\infty}^{\tau} x(\tau)d\tau \leftarrow \frac{F}{j\omega} + \pi X(0)\delta(\omega) \qquad \text{(Time integration property)}$$
So,
$$Y(j\omega) = \frac{X(j\omega)}{j\omega} + \pi X(0)\delta(\omega)$$

$$= \frac{1}{j\omega} \left(\frac{j\omega}{5 + \frac{j\omega}{10}}\right) + 0 = \frac{1}{\left(5 + \frac{j\omega}{10}\right)}$$
Now area under $y(t)$

Now, area under y(t), $\int_{-\infty}^{\infty} y(t)dt = Y(0)$

Thus, $Y(0) = \frac{1}{5+0} = \frac{1}{5}$



T7: Solution

(c)

Properties of distortionless system are:

- Magnitude should be constant w.r.t. frequency.
- Phase should depend linearly on frequency.

Only function given in option (c) follow the given conditions.

T8: Solution

(a)

The signal $x(t) = (2 + e^{-3t}) u(t)$ then final value i.e. $x(\infty)$ will be 2.



Laplace Transform



Detailed Explanation

of

Try Yourself Questions

T1: Solution

(b)

Convolution in time domain is multiplication in s-domain.

$$L[h(t)] = L[f(t)] \times L[g(t)] = \frac{1}{s+3}$$

T2: Solution

(c)

$$r(t) \xleftarrow{\text{L.T.}} \frac{1}{s^2}$$

$$r(t-a) \xleftarrow{\text{L.T.}} e^{-as} \times \frac{1}{s^2} = \frac{e^{-as}}{s^2}$$

T3: Solution

(c)

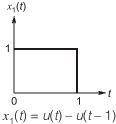
$$\lim_{t \to \infty} i(t) = \lim_{s \to 0} sI(s)$$
$$= \lim_{s \to 0} s \cdot \frac{2}{s(1+s)} = 2$$

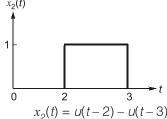
T4: Solution

(b)

We can express the given function in terms of unit step function as follows:







Thus,

$$x(t) = x_1(t) + x_2(t) + x_3(t) + \dots$$

= $u(t) - u(t-1) + u(t-2) - u(t-3) + \dots$

We know that

$$u(t) \longleftrightarrow \frac{1}{s}$$

$$u(t-t_0) \stackrel{L}{\longleftrightarrow} \frac{1}{s}e^{-st_0}$$
 (time-shifting)

The Laplace transform of x(t) is

$$X(s) = \frac{1}{s} - \frac{1}{s}e^{-s} + \frac{1}{s}e^{-2s} - \frac{1}{s}e^{-3s} + \frac{1}{s}e^{-4s} - \frac{1}{s}e^{-5s} + \dots$$

$$= \frac{1}{s} \left[1 + e^{-2s} + e^{-4s} + \dots \right] - \frac{1}{s} \left[e^{-s} + e^{-3s} + e^{-5s} + \dots \right]$$

$$= \frac{1}{s} \left[\frac{1}{1 - e^{-2s}} \right] - \frac{1}{s} \left[\frac{e^{-s}}{1 - e^{-2s}} \right]$$

$$= \frac{1}{s} \left[\frac{1 - e^{-s}}{1 - e^{-2s}} \right]$$

$$= \frac{1}{s} \left[\frac{1}{1 + e^{-s}} \right]$$

T5: Solution

(d)

From the time integration property of Laplace transform

$$x(t) \stackrel{L}{\longleftrightarrow} X(s)$$

$$\int_{0}^{t} x(\tau)d\tau \stackrel{L}{\longleftrightarrow} \frac{1}{s}X(s)$$

$$\int_{0}^{t} x(\tau)d\tau \stackrel{L}{\longleftrightarrow} \frac{(s+1)}{s(s^{2}+4s+5)}$$

Time integration Property

T6: Solution

(d)

$$H(s) = \frac{k(s^2 + \omega_0^2)}{s^2 + \left(\frac{\omega_0}{Q}\right)s + \omega_0^2}$$



So value of H(s) at $s \to \infty$ is k and value of H(s) at $s \to 0$ is k. So the filter is a band stop filter or notch filter.

T7: Solution

(c)

$$X(s) = L[x(t)] = \frac{s}{s^2 + 1}$$

$$H(s) = L[h(t)] = \frac{1}{s^2 + 1}$$

$$y(t) = x(t) * h(t)$$

$$Y(s) = L[x(t) * h(t)] = X(s)H(s) = \frac{s}{(s^2 + 1)^2}$$

$$Y(s) = \frac{-j/4}{(s - j)^2} + \frac{j/4}{(s + j)^2}$$

Using partial fractional,

We know that $te^{-at}u(t) \longleftrightarrow \frac{1}{(s+a)^2}$

so,
$$\frac{1}{(s-j)^2} \xleftarrow{L^{-1}} te^{jt}$$
$$\frac{1}{(s+j)^2} \xleftarrow{L^{-1}} te^{-jt}$$

$$y(t) = \frac{j}{4} \left[-te^{jt} + te^{-jt} \right] = \frac{j}{4} t \left[e^{-jt} - e^{jt} \right] = \frac{t}{2} \sin t, \qquad t \ge 0$$



Sampling Theorem and Discrete Time System



Detailed Explanation

of

Try Yourself Questions

T1: Solution

(c)

$$E = \sum_{n=-\infty}^{\infty} |x[n]|^2 = \sum_{n=-\infty}^{\infty} 1 = \infty$$

T2: Solution

(c)

$$y[n] = \sum_{n=-\infty}^{\infty} n^2 \delta[n+2]$$
$$= n^2 \Big|_{n=-2}$$
$$= (-2)^2 = 4$$

$$\sum_{n=-\infty}^{\infty} x[n]\delta[n-n_0] = x[n_0]$$

T3: Solution

(d)

(A)
$$y[n] = x[n^{2}]$$

$$x_{1}[n] \rightarrow y_{1}[n] = x_{1}[n^{2}]$$

$$x_{2}[n] \rightarrow y_{2}[n] = x_{2}[n^{2}]$$

$$ax_{1}[n] + bx_{2}[n] \rightarrow ax_{1}[n^{2}] + bx_{2}[n^{2}]$$

$$= ay_{1}[n] + by_{2}[n]$$
(B)
$$y[n] = x^{2}[n-1]$$

Hence the system is linear.

For a delayed input $x[n-n_0]$, output is

$$y[n, n_0] = x^2[n - n_0 - 1]$$

The delayed output

$$y[n-n_0] = x^2[n-n_0-1]$$



Since

$$y[n, n_0] = y[n - n_0]$$

Hence the system is time-invariant.

(C)

$$y[n] = x[n] + n$$

y[n] depends on present value of x[n], so the system is causal.

(D)

$$y[n] = x[3n]$$

$$y[-1] = x[-3]$$

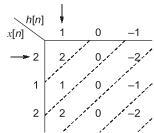
$$y[1] = x[3]$$

System has memory, therefore it is a dynamic system.

T4: Solution

(c)

Since x[n] is even symmetric about mid point (n = 1) and h[n] is odd symmetric about mid point (n = 1) so y[n] will be odd symmetric about its mid point n = 2.



$$y[n] = x[n] * h[n] = \{2, 1, 0, -1, -2\}$$

y[n] is odd symmetric about n = 2.

T5: Solution

(a)

Causality:

$$h[n] = 0, n < 0$$

The system is causal.

Stability:

$$\sum_{n=-\infty}^{\infty} |h[n]| = 2 \sum_{n=0}^{\infty} (0.4)^n - \sum_{n=0}^{\infty} (0.2)^n$$
$$= 2 \left[\frac{1}{1 - 0.4} \right] - \frac{1}{(1 - 0.2)} < \infty$$

The sytem is stable.

Z-Transform



Detailed Explanation

of

Try Yourself Questions

T1: Solution

(b)

Given that,

$$x(n) = \sum_{k=0}^{\infty} \delta(n-k)$$

$$x(n) = \delta(n) + \delta(n-1) + \delta(n-2) + \cdots$$

$$x(n) = u(n)$$

$$X(z) = Z.T.[u(n)]$$

$$X(z) = \frac{z}{z-1}$$

T2: Solution

(c)

z-transform of
$$x[n]$$
,

$$X(z) = \sum_{n = -\infty}^{\infty} x[n]z^{-n}$$

$$= \sum_{n = -\infty}^{\infty} \alpha^n z^{-n} u[n] + \sum_{n = -\infty}^{\infty} \alpha^{-n} z^{-n} u[n]$$

$$= \sum_{n = 0}^{\infty} (\alpha z^{-1}) + \sum_{n = 0}^{\infty} (\alpha z)^{-n} = \frac{1}{1 - \alpha z^{-1}} + \frac{1}{1 - (\alpha z)^{-1}}$$

Series I converges, if $\alpha z^{-1} < 1$ or $|z| > |\alpha|$

Series II converges, if $(\alpha z)^{-1} < 1$ or $\alpha z > 1$ or $|z| > \frac{1}{|\alpha|}$

So, ROC is interaction of both

$$ROC: |z| > max \left(|\alpha|, \frac{1}{|\alpha|} \right)$$



T3: Solution

(b)

$$X(z) = \frac{z+1}{z(z-1)}$$

$$= -\frac{1}{z} + \frac{2}{z-1} = -\frac{1}{z} + 2z^{-1} \left(\frac{z}{z-1}\right)$$

By partial fraction

Taking inverse z-transform

$$x[n] = -\delta[n-1] + 2u[n-1]$$

$$x[0] = -0 + 0 = 0$$

$$x[1] = -1 + 2 = 1$$

$$x[2] = -0 + 2 = 2$$

T4: Solution

(c)

By taking z-transform of x[n] and h[n]

$$H(z) = 1 + 2z^{-1} - z^{-3} + z^{-4}$$

$$X(z) = 1 + 3z^{-1} - z^{-2} - 2z^{-3}$$

From the convolution property of z-transform

$$Y(z) = H(z) X(z)$$

$$Y(z) = 1 + 5z^{-1} + 5z^{-2} - 5z^{-3} - 6z^{-4} + 4z^{-5} + z^{-6} - 2z^{-7}$$

Sequence is

$$y[n] = \{1, 5, 5, -5, -6, 4, 1, -2\}$$

$$y[4] = -6$$

T5: Solution

(d)

Given that x(n) is right sided and real, X(z) has two poles, two zeros at origin and one pole at $e^{j\pi/2}$, X(1) = 1. Since x(n) is real so poles of X(z) should be in conjugate pairs so other pole will be at $e^{-j\pi/2}$.

$$X(z) = \frac{k z^2}{(z - e^{-j\pi/2})(z - e^{+j\pi/2})} = \frac{k z^2}{z^2 + 1}$$

Since.

$$X(1) = 1$$
 so, $k = 2$

$$X(z) = \frac{2z^2}{z^2 + 1}$$
 and $|z| > 1$

T6: Solution

(a)

We know that,

$$\alpha^n u[n] \longleftrightarrow \frac{Z}{Z - \alpha}$$

$$\alpha^{n-10}u[n-10] \longleftrightarrow \frac{z}{z-\alpha}$$

(time shifting property)



T7: Solution

(b)

$$Y(z) - \frac{1}{3}z^{-1}Y(z) = X(z)$$

$$Y(z) \left[1 - \frac{1}{3}z^{-1}\right] = X(z)$$

$$\frac{Y(z)}{X(z)} = \frac{1}{1 - \frac{1}{3}z^{-1}}$$

$$X(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}$$

$$Y(z) = \frac{1}{\left(1 - \frac{1}{2}z^{-1}\right)\left(1 - \frac{1}{3}z^{-1}\right)} = \frac{3}{1 - \frac{1}{2}z^{-1}} - \frac{2}{1 - \frac{1}{3}z^{-1}}$$

$$y[n] = \left[3\left(\frac{1}{2}\right)^n - 2\left(\frac{1}{3}\right)^n\right]u[n]$$

T8: Solution

where.

٠.

(a)

We know that convolution of x[n] with unit step function u[n] is given by

$$x[n] * u[n] = \sum_{k=-\infty}^{\infty} x[k]$$

SO,

$$y[n] = x[n] * u[n]$$

Taking z-transform on both sides

$$Y(z) = X(z)\frac{z}{(z-1)} = X(z)\frac{1}{(1-z^{-1})}$$

Transfer function,

$$H(z) = \frac{Y(z)}{X(z)} = \frac{1}{(1-z^{-1})}$$

Now, consider the inverse system of H(z), let impulse response of the inverse system is given by $H_1(z)$, then we can write

$$H(z)H_{1}(z) = 1$$

$$H_{1}(z) = \frac{X(z)}{Y(z)} = 1 - z^{-1}$$

$$(1 - z^{-1})Y(z) = X(z)$$

$$Y(z) - z^{-1}Y(z) = X(z)$$

Taking inverse z-transform

$$v[n] - v[n-1] = x[n]$$

DTFT, DTFS & DFT



Detailed Explanation

of

Try Yourself Questions

T1: Solution

(c)

Since

$$x[n] \leftarrow DTFT \rightarrow X(e^{j\Omega})$$

Thus

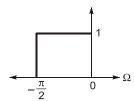
$$e^{j\Omega_0 n} x[n] \stackrel{DTFT}{\longleftrightarrow} X(e^{j(\Omega - \Omega_0)})$$

(Frequency shifting property)

 $\Omega_0 = -\pi/4$

$$e^{-j\frac{\pi}{4}n}x[n] \longleftrightarrow X(e^{j(\Omega+\pi/4)})$$

The graph of $X(e^{j\Omega})$ is shifting to left by $\frac{\pi}{4}$ units. So, DTFT of $e^{-j\frac{\pi n}{4}}x[n]$ is



T2: Solution

(a)

N-point DfT is given as

$$X_{DFT}[k] = \sum_{n=0}^{N-1} x[n]e^{-j\frac{2\pi nk}{N}}, k = 0, 1, ... N - 1$$
$$X_{DFT}[k] = \sum_{n=0}^{3} x[n]e^{-j\frac{\pi nk}{2}}$$

∵ *N* = 4



For
$$k=0$$
,
$$X_{DFT}[0] = \sum_{n=0}^{3} x[n]$$

$$= x[0] + x[1] + x[2] + x[3]$$

$$= \cos 0 + \cos \pi + \cos 2\pi + \cos 3\pi$$

$$= 1 - 1 + 1 - 1 = 0$$
For $k=1$,
$$X_{DFT}[1] = \sum_{n=0}^{3} x[n]e^{-j\frac{\pi n}{2}}$$

$$= x[0]e^{0} + x[1]e^{-j\frac{\pi}{2}} + x[2]e^{-j\pi} + x[3]e^{-j\frac{3\pi}{2}}$$

$$= \cos 0 + \cos \pi(-j) + \cos 2\pi(-1) + \cos 3\pi(j)$$

$$= 1 + (-1)(-j) + 1 (-1) + (-1)(j)$$

$$= 1 + j - 1 - j$$

$$= 0$$
Similarly we can obtain $X_{DFT}[2]$ and $X_{DFT}[3]$ for $k=2$ and $k=3$ respectively,
$$X_{DFT}[2] = 1 + 1 + 1 + 1 = 4$$

$$X_{DFT}[3] = 1 - j - 1 + j = 0$$

 $X_{DFT}[k] = \{0, 0, 4, 0\}$

T3: Solution

(c)

$$\begin{split} & \textit{X}(e^{j\Omega}) = \sum_{n=-\infty}^{\infty} x[n]e^{-j\Omega n} = \sum_{n=-2}^{2} e^{-j\Omega n} \\ & = e^{j2\Omega} + e^{j\Omega} + 1 + e^{-j\Omega} + e^{-j2\Omega} \\ & = e^{-j2\Omega} \left(1 + e^{j\Omega} + e^{j2\Omega} + e^{j3\Omega} + e^{j4\Omega} \right) \\ & = e^{-j2\Omega} \frac{\left(1 - e^{j5\Omega} \right)}{1 - e^{j\Omega}} \\ & = \frac{e^{-j5\pi/2} - e^{j5\Omega/2}}{e^{-j\pi/2} - e^{j\Omega/2}} = \frac{\sin 2.5\Omega}{\sin 0.5\Omega} \end{split} \tag{Summation of finite GP}$$

T4: Solution

(b)

$$X(e^{j\Omega}) = j4 \sin 4\Omega - 1$$
$$= 2(e^{j4\Omega} - e^{-j4\Omega}) - 1$$

Taking inverse Fourier transform, we have

$$x[n] = 2\delta[n+4] - 2\delta[n-4] - \delta[n]$$

Since, $\delta[n-n_0] \xleftarrow{\text{DTFT}} e^{-j\Omega n_0}$

