

NAME -

ROLL NO :—

TEST NO. 14

total
marks 263

Q. 1'a'

$$V_a = 300 \text{ m/s}, (\text{air speed})$$

(Ambient temp) $T_a = -10 + 273 = 263 \text{ K}$

$$h_a = \text{Ambient air enthalpy} = 265 \text{ kJ/kg}$$

$\therefore$ Stagnation enthalpy at inlet

$$h_i = h_a + \frac{V_a^2}{2}$$

$$\Rightarrow h_i = 265 + \frac{300^2}{2 \times 1000} = 310 \text{ kJ/kg}$$

Let $\dot{m}_a = \text{Mass flow of air}$

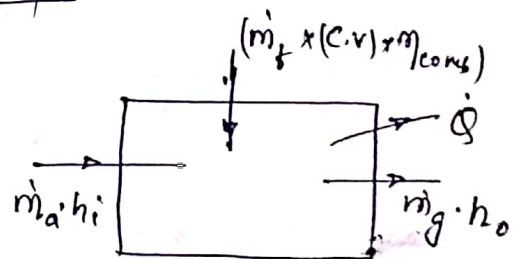
$\dot{m}_f = \text{Mass rate of fuel}$

$\therefore \dot{m}_g = \text{Mass of gas at nozzle} = (\dot{m}_a + \dot{m}_f)$

and Given

$$\frac{\dot{m}_a}{\dot{m}_f} = \frac{1}{0.022}$$

$h_o = \text{Stagnation enthalpy at nozzle outlet}$



$$\therefore \dot{m}_a h_i + \dot{m}_f \times (C.V) \times \eta_{comb} = (\dot{m}_a + \dot{m}_f) \times h_o + \dot{Q}$$

$$\Rightarrow \left(\frac{\dot{m}_a}{\dot{m}_f} \right) h_i + (C.V) \times \eta_{comb} = \left(\frac{\dot{m}_a}{\dot{m}_f} + 1 \right) \times h_o + \left(\frac{\dot{m}_a}{\dot{m}_f} \times 30 \right)$$

$$\Rightarrow \left(\frac{1}{0.022} \times 310 \right) + 44.5 \times 1000 \times 0.95 = \left(\frac{1}{0.022} + 1 \right) \times h_o + \frac{1}{0.022} \times 30$$

$$\Rightarrow h_o = \frac{55002.273}{(1 + \frac{1}{0.022})} = 1184 \text{ kJ/kg}$$

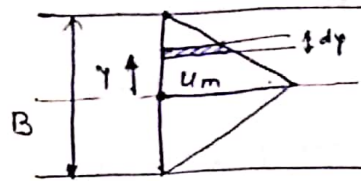
But $h_o = \text{Enthalpy at exit} + \frac{V_o^2}{2}$

$$\Rightarrow V_o = \sqrt{(1184 - 965) \times 1000 \times 2} = 661.82 \text{ m/s}$$

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$$Q = 1'6'$$

Consider a strip at a distance 'y' from centre of duct and of thickness dy.



$$dA = \text{Area of strip} = (dy \times 1)$$

u = velocity profile at any position

$$\Rightarrow u = \frac{u_m}{(B/2)} \times y = \frac{2 u_m}{B} \times y$$

Also Mass flow rate at Avg velocity = Mass flow rate at Actual velocity

$$\Rightarrow \rho \cdot (B \times 1) \times U_{avg} = \int_{-B/2}^{B/2} \rho \cdot (dy \times 1) \cdot u$$

$$\Rightarrow U_{avg} = \frac{1}{B} \times 2 \int_0^{B/2} \frac{2 u_m}{B} y dy$$

$$\Rightarrow U_{avg} = \frac{4 u_m}{B^2} \left[\frac{y^2}{2} \right]_0^{B/2} = \frac{2 u_m}{B^2} \left(\frac{B^2}{4} \right) = \frac{2 u_m}{4} = \frac{u_m}{2}$$

$\therefore \beta = \left(\text{Momentum Correction factor} \right) = \frac{(\text{Momentum/Sec}) \text{ at actual velocity}}{(\text{Momentum/Sec}) \text{ at Avg velocity}}$

$$\Rightarrow \beta = \frac{1}{A \times U_{avg}^2} \int_{-B/2}^{B/2} u^2 dA = \frac{1}{(B \times 1) \times \left(\frac{u_m}{2} \right)^2} \int_{-B/2}^{B/2} \left(\frac{2 u_m}{B} y \right)^2 dy$$

$$\Rightarrow \beta = \frac{4}{u_m^2 \times B} \times 2 \times \left(\frac{2 u_m}{B} \right)^2 \times \int_0^{B/2} y^2 dy = \frac{16 \times 2}{B^3} \left[\frac{y^3}{3} \right]_0^{B/2}$$

$$\Rightarrow \beta = \frac{16 \times 2}{3} \times \frac{1}{B^3} \left(\frac{B}{2} \right)^3 = \frac{16 \times 2}{3 B^3} \times \frac{B^3}{8} = \frac{4}{3} = 1.333$$

Q-1'c'

$$m_1 = m_2 + m_3$$

Mass Conservation

For ambient

$$T_a = 300K \quad \& \quad P_a = 1 \text{ bar}$$

Now

Available Energy

Availability at inlet Stream 1

$$\phi_1 = \dot{m}_1 [(h_1 - h_a) - T_a (s_1 - s_a)]$$

$$\Rightarrow \phi_1 = 2 \times \left[c_p (T_1 - T_a) - T_a \left\{ c_p \ln \left(\frac{T_1}{T_a} \right) - R \ln \left(\frac{P_1}{P_a} \right) \right\} \right]$$

$$\Rightarrow \phi_1 = 2 \times \left[1.005 \times (300 - 300) - 300 \left\{ 1.005 \times \ln \left(\frac{300}{300} \right) - 0.287 \times \ln \left(\frac{4}{1} \right) \right\} \right]$$

$$\Rightarrow \boxed{\phi_1 = 238.72 \text{ kW}}$$

* Availability at Stream 2

$$\phi_2 = \dot{m}_2 [(h_2 - h_a) - T_a (s_2 - s_a)]$$

$$\Rightarrow \phi_2 = 1 \times \left[1.005 \times (330 - 300) - 300 \left\{ 1.005 \times \ln \left(\frac{330}{300} \right) - 0.287 \times \ln \left(\frac{1}{1} \right) \right\} \right]$$

$$\Rightarrow \boxed{\phi_2 = 1.414 \text{ kW}}$$

* Availability at Stream 3

$$\phi_3 = \dot{m}_3 [(h_3 - h_a) - T_a (s_3 - s_a)]$$

$$\Rightarrow \phi_3 = 1 \times \left[1.005 \times (270 - 300) - 300 \left\{ 1.005 \times \ln \left(\frac{270}{300} \right) \right\} \right]$$

$$\Rightarrow \boxed{\phi_3 = 1.616 \text{ kW}}$$

η_{isen}

0.89

$$= 573.521 \text{ K}$$

$$P_2 = 1 \text{ bar}$$

$$T_2 = 330 \text{ K}$$

$$\dot{m}_2 = 1 \text{ kg/s}$$

$$\dot{m}_1 = 2 \text{ kg/s}$$

$$P_1 = 4 \text{ bar}$$

$$T_1 = 300 \text{ K}$$

$$\dot{m}_3 = 1 \text{ kg/s}$$

$$P_3 = 1 \text{ bar}$$

$$T_3 = 270 \text{ K}$$



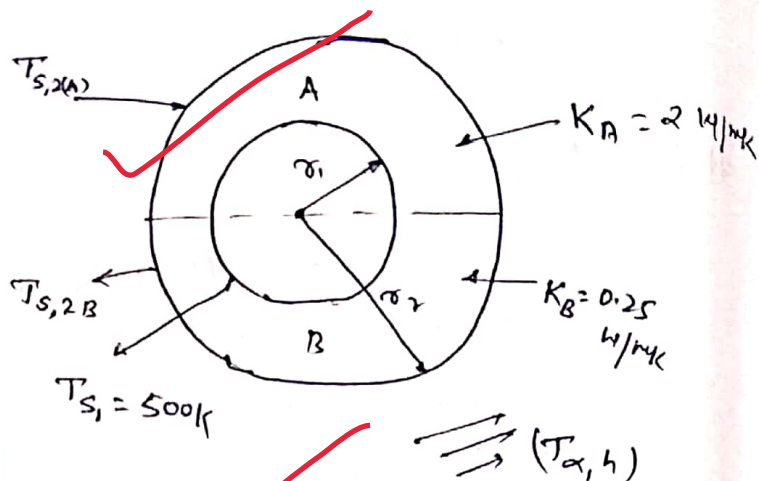
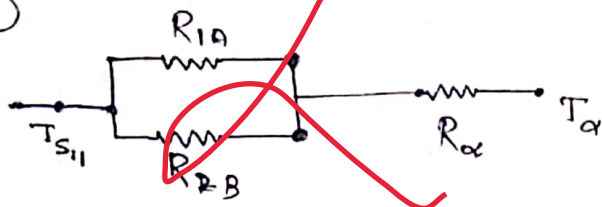
Q-1'd'

$$r_1 = 50 \text{ mm}$$

$$r_2 = 100 \text{ mm}$$

$$T_\alpha = 300 \text{ K}, h = 25 \text{ W/m}^2\text{K}$$

(i)



$$R_{1A} = \frac{\ln(r_2/r_1)}{2\pi K_A L}$$

$$R_{1A} = \frac{\ln(r_2/r_1)}{4\pi K_A L}$$

$$R_{2B} = \frac{\ln(r_2/r_1)}{4\pi K_B L}$$

and

$$R_\alpha = \frac{1}{h A_{\text{outer}}}$$

(ii)

$$\text{Total Loss, } \dot{Q} = \dot{Q}_A + \dot{Q}_B$$

$$\text{Total Loss, } \dot{Q} = \frac{(T_{S1} - T_\alpha)}{\left(\frac{R_{1A} * R_{2B}}{R_{1A} + R_{2B}} \right) + R_\alpha}$$

$$R_{1A} = \frac{\ln(r_2/r_1)}{4\pi K_A L} = \frac{\ln\left(\frac{0.1}{0.05}\right)}{4\pi \times 2 \times 1}$$

(assume unit length)

$$\Rightarrow R_{1A} = 0.02758 \frac{\text{K}}{\text{W}}$$

$$R_{2B} = \frac{\ln(r_2/r_1)}{4\pi k_B L} = \frac{\ln\left(\frac{0.1}{0.05}\right)}{4\pi \times 0.25 \times 1} = 0.2206 \frac{K}{W}$$

conv

$$R_{\alpha} = \frac{1}{h A_{outer}} = \frac{1}{25 \times 2\pi r_2 \times 1} = \frac{1}{50\pi \times 0.1}$$

$$R_{\alpha} = 0.06366 \text{ K/W}$$

$$\therefore Q = \frac{(500 - 300)}{\left(\frac{0.02758 \times 0.2206}{0.02758 + 0.2206} \right) + 0.06366}$$

$$\Rightarrow Q = 2268.215 \text{ W} \quad Q \Rightarrow \text{Heat loss per unit length}$$

Also

$$Q_A = \frac{(T_{S,2A} - T_{\alpha})}{\frac{1}{h \times 2\pi r_2 \times 1}} = \frac{(T_{S1} - T_{S,2A})}{\frac{\ln(r_2/r_1)}{4\pi k_A \times 1}}$$

$$\Rightarrow (T_{S,2A} - 300) \times \pi \times 0.1 \times 25 = \frac{(500 - T_{S,2A}) \times 4\pi \times 0.2}{\ln\left(\frac{0.1}{0.05}\right)}$$

$$\Rightarrow 0.2166 \times (T_{S,2A}) - 0.2166 \times 300 = 500 - T_{S,2A}$$

$$\Rightarrow (T_{S,2A}) = 464.39 \text{ K}$$

Similarly

$$(T_{S,2B} - T_{\alpha}) \times h \pi r_2 = \frac{4\pi k_B \times (T_{S1} - T_{S,2B})}{\ln(r_2/r_1)}$$

$$\Rightarrow (T_{S,2B} - 300) \times 25 \times \pi \times 0.1 \times \ln\left(\frac{0.1}{0.05}\right) = (500 - T_{S,2B}) \times 4\pi \times 0.25$$

$$\Rightarrow 1.733 \times T_{S,2B} - 1.733 \times 300 = 500 - T_{S,2B}$$

$$\Rightarrow T_{S,2B} = 373.18 \text{ K}$$

Q-11e

No. of Cylinder, $K = 4$

4-stroke

Diameter of Orifice, $d = 8 \text{ cm}$

$C_d = 0.65$

Given

$D = \text{Bore dia} = 10 \text{ cm}$

$L = \text{Stroke} = 15 \text{ cm}, N = 2500 \text{ rpm}$

$$\therefore \dot{V}_s = \text{Swept vol.} = \frac{\pi}{4} \times D^2 \times L \times K \times \frac{N}{60 \times 2}$$

$$\Rightarrow \dot{V}_s = \frac{\pi}{4} \times (0.1)^2 \times 0.15 \times 4 \times \frac{2500}{120}$$

$$\Rightarrow \dot{V}_s = 9.817 \times 10^{-2} \text{ m}^3/\text{sec}$$

$$\dot{m}_f = \text{fuel consumption} = 10 \text{ kg/hr} = \left(\frac{10}{3600} \right) \text{ kg/s}$$

$$(C.V)_{\text{fuel}} = 42000 \text{ kJ/kg}$$

$$\therefore \text{Heat Added, } Q = \dot{m}_f \times (C.V) = \frac{10}{3600} \times 42000$$

$$\Rightarrow \dot{Q} = 116.67 \text{ kW}$$

Also (P_{air}) at free air condition

$$P_{\text{air}} = \frac{P}{RT} = \frac{100}{0.287 \times 290} = 1.201 \text{ kg/m}^3$$

$\therefore$ pressure drop across the orifice, $\Delta P = \rho_{\text{water}} \times 4 \text{ cm}$

$$\Rightarrow \Delta P = \rho_{\text{water}} \times g \times h = 1000 \times 9.81 \times \frac{4}{100} = 392.4 \text{ Pa}$$

$\therefore$ Air Column height, corresponding to this pressure drop

$$\Rightarrow h_{\text{air}} = \frac{\Delta P}{\rho_{\text{air}} \times g} = \frac{392.4}{9.81 \times 1.201} = \frac{5.771}{33.306} \text{ m}$$

$\therefore$ Theoretical air velocity, $V_{\text{air}} = \sqrt{2gh_{\text{air}}}$

$$\Rightarrow V_{\text{air}} = \sqrt{2 \times 9.81 \times \frac{5.771}{33.306}} = \frac{10.64}{25.56} \text{ m/s}$$

∴ Actual Mass Flow Rate, $\dot{m}_{air} = C_d \cdot \rho_{air} A_o V_{air}$

$$\Rightarrow \dot{m}_{air} = 0.65 \times 1.201 \times \frac{\pi}{4} \times (0.08)^2 \times 10.64 = 25.58$$

$$\Rightarrow \boxed{\dot{m}_{air} = \frac{0.4175}{0.1003} \text{ Kg/s}}$$

∴ Actual Volume Flow rate of air, $\dot{V}_a = \frac{\dot{m}_{air}}{\rho_{air}}$

$$\Rightarrow \boxed{\dot{V}_a = \frac{0.4175^{0.1003}}{1.201} = \frac{0.03476}{0.08351} \text{ m}^3/\text{sec}}$$

①

Brake thermal η

$$\Rightarrow \eta_{th} = \frac{B.P.}{Q} \times 100 = \frac{36}{116.67} \times 100$$

$$\Rightarrow \boxed{\eta_{th} = 30.86\%}$$

②

Brake mean effective pressure

$$P_{bmep} = \frac{B.P.}{\dot{V}_s} = \frac{36}{9.817 \times 10^{-2}} = 366.71 \text{ kPa}$$

$$= 3.6671 \text{ bar}$$

③

$$\boxed{P_{bmep} = 3.6671 \text{ bar}}$$

④

volumetric $\eta = \frac{\dot{V}_a}{\dot{V}_s} \times 100 = \frac{0.08351}{9.817 \times 10^{-2}} \times 100$

$$\Rightarrow \boxed{\eta_{vol} = 35.408\%}$$

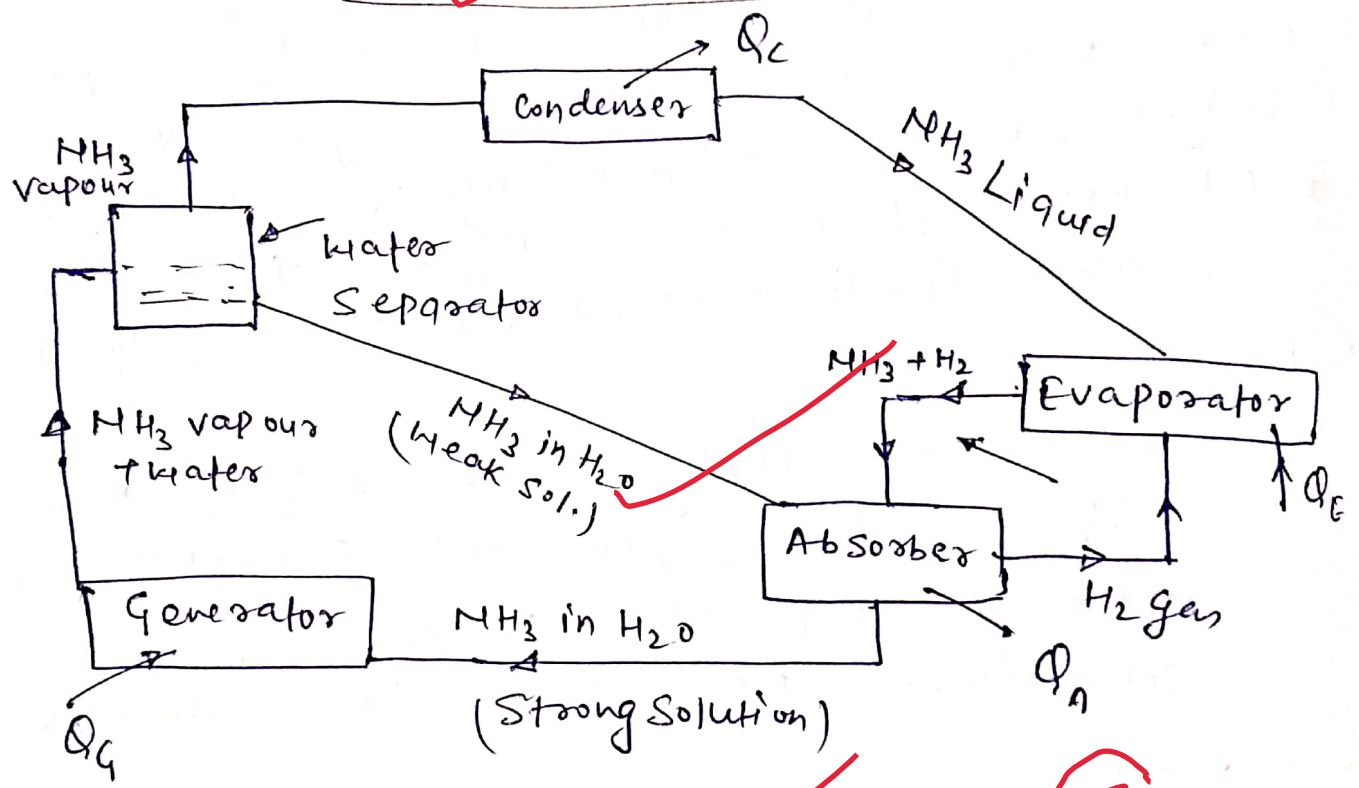
$$\Rightarrow \boxed{\eta_{vol} = 85.067\%}$$

②

Q-4'a

①

Schematic diagram of Electrolux Refrigerator



Electrolux Refrigerator

07

Q-4'a' (11)

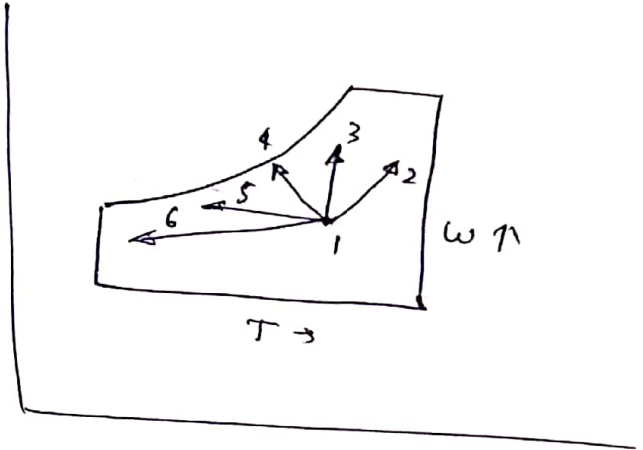
* various processes, which can be done in air washer due to variation of mean surface temp. of water:

(i)

Process 1-2

→ Heating and dehumidification
($T_s > T_i$)

→ Mean surface of temp of water is greater than dry-bulb temp of air. Heat is supplied to water externally



(ii)

Process 1-3 (humidification)

→ If water from pan is heated to the dry-bulb temp of air and then sprayed, the air would only be humidified.
→ This is practically not possible

(iii)

Process 1-4

→ The recirculated water reaches the equilibrium temp which is equal to the thermodynamic wet-bulb temp.

(iv)

Process (1-5)

→ Sensible cooling

→ If water is cooled up to the dew point temp of air, the process 1-5 would be sensible cooling process

(v)

Process (1-6) (Cooling & dehumidification)

→ Water is cooled to the temp below the dew point of air

10

Q-4b

Given

$$\text{Stroke vol.} = 0.0015 \text{ m}^3$$

$$\Rightarrow (V_1 - V_2) = 0.0015 \text{ m}^3$$

$r = 6 \Rightarrow$ Compression Ratio

$$P_2 = 8 \text{ bar}, T_2 = (350 + 273) \text{ K}$$

$$T_2 = 623 \text{ K}$$

$$P_3 = 25 \text{ bar}$$

$$\text{and } (V_3 - V_2) = \frac{1}{30} \times (V_1 - V_2) = \frac{1}{30} \times 0.0015 = 5 \times 10^{-5} \text{ m}^3$$

$\therefore$ work done during process 2-3

$$W_{2-3} = \text{Area under 2-3}$$

$$= P_2 \times (V_3 - V_2) + \frac{1}{2} \times (P_3 - P_2) \times (V_3 - V_2)$$

$$\Rightarrow W_{2-3} = 800 \times (5 \times 10^{-5}) + \frac{1}{2} \times (25 - 8) \times 100 \times 5 \times 10^{-5}$$

$$\Rightarrow W_{2-3} = 0.0825 \text{ kJ} = 82.5 \text{ J}$$

Also

$$(V_1 - V_2) = 0.0015$$

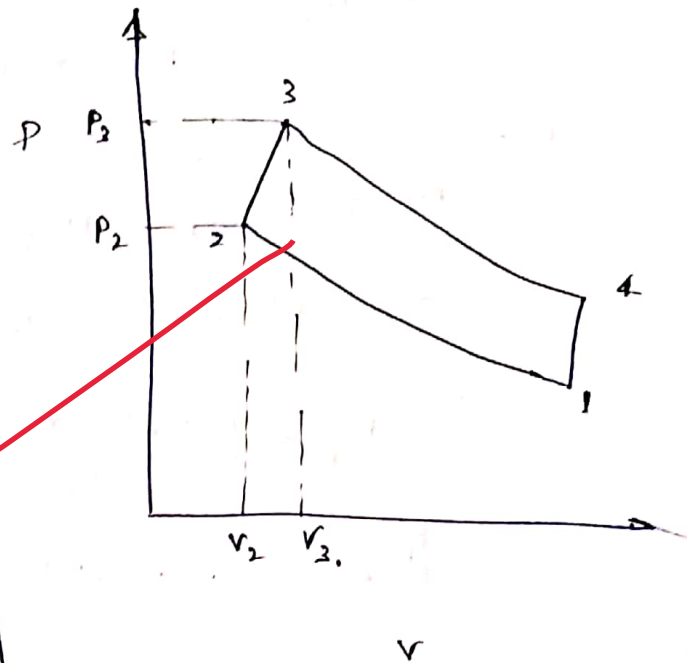
$$\Rightarrow \left(\frac{V_1}{V_2} \right) - \left(\frac{V_2}{V_2} \right) = \frac{0.0015}{V_2}$$

$$\Rightarrow r - 1 = \frac{0.0015}{V_2}$$

$$\Rightarrow V_2 = \left(\frac{0.0015}{6 - 1} \right) = 3 \times 10^{-4} \text{ m}^3$$

$$\text{and } V_3 = 5 \times 10^{-5} + 3 \times 10^{-4} = 3.5 \times 10^{-4} \text{ m}^3$$

$$\text{also } m_2 = \frac{P_2 V_2}{R T_2} \quad (\text{Assuming ideal Gas})$$



$$\Rightarrow m_2 = \frac{800 \times 1000 \times 3 \times 10^{-4}}{287 \times 623} = 1.3423 \times 10^{-3} \text{ kg}$$

Also

$$m_2 = m_{\text{mixt}} = m_a + m_f$$

$$\Rightarrow (1.3423 \times 10^{-3}) = 16 \times m_f + m_f \quad \left[\text{Given } \frac{m_a}{m_f} = \frac{16}{1} \right]$$

$$\Rightarrow m_f = \left(\frac{1.3423 \times 10^{-3}}{17} \right) \text{ kg} \Rightarrow \text{Mass of Gasoline}$$

$$\Rightarrow m_f = 7.896 \times 10^{-5} \text{ kg}$$

Now

$$T_3 = \frac{P_3 V_3}{m_2 R} = \frac{25 \times 10^5 \times 3.5 \times 10^{-4}}{1.3423 \times 10^{-3} \times 287} = 2271.31 \text{ K}$$

And (Change in Internal Energy in process 2-3), $\Delta U = m_2 C_v (T_3 - T_2)$

$$\Rightarrow (\Delta U)_{2-3} = (1.3423 \times 10^{-3}) \times (C_p - R) \times (2271.31 - 623)$$

$$\Rightarrow (\Delta U)_{2-3} = 2.2125 \times (1000 - 287)$$

$$\Rightarrow (\Delta U)_{2-3} = 1577.51 \text{ J}$$

$\therefore$ Actual Heat transfer in 2-3

$$Q_{2-3} = (\Delta U)_{2-3} + W_{2-3} = 1577.51 + 88.5$$

$$\Rightarrow Q_{2-3} = 1660.01 \text{ J}$$

But Actual heat ~~is~~ Given by fuel

$$= m_f \times (C.V) = (7.896 \times 10^{-5}) \times (42000 \times 1000) \text{ J}$$

$$= 3316.32 \text{ J}$$

$$\therefore \left(\text{Heat Lost per kg of charge} \right) = \left(\frac{3316.32 - 1660.01}{1.3423 \times 10^{-3}} \right) \times 10^{-3} = 1233.93 \text{ kJ/kg}$$

Q. 4(c)

Given

a Cone with

Dia, $D = 24 \text{ cm}$

Height, $h = 20 \text{ cm}$

Centre of Gravity of Inverted
(C.G.)

Cone = $\left(\frac{3h}{4}\right)$ (from vertex)

$$\Rightarrow (C.G.) = \frac{3 \times 20}{4} = 15 \text{ cm}$$

* 'B' is the Centre of buoyance
and L = Length of cone
submerged.

$\therefore$ Buoyance 'B' is at $\left(\frac{3L}{4}\right)$ from vertex

$\therefore$ Distance between C.G. & B

$$= BG = \left(15 - \frac{3L}{4}\right) \quad \text{--- (1)}$$

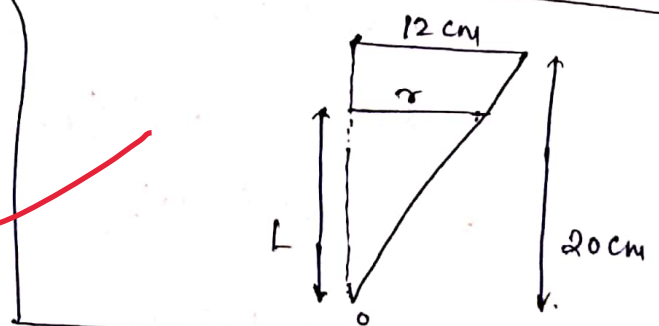
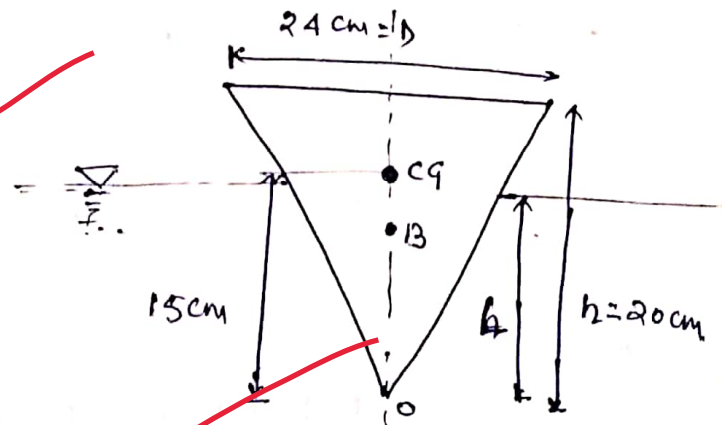
Now At free surface,

r = Radius of Cone

$\therefore$ from similar triangle

$$\frac{12}{r} = \frac{20}{L}$$

$$\Rightarrow \boxed{r = \frac{12L}{20} = \frac{3L}{5} = 0.6L}$$



Now for stability.

$$\left[\left(\frac{I_{\min}}{V} \right) - BG \geq 0 \right]$$

where $I_{\min}^{\text{Min}}$ At GOI of the free Surface

$$= \frac{\pi}{64} \times (2r)^4 \quad (i)$$

and V - Submerged Volume of Cone.

$$= \frac{1}{3} \pi r^2 L \quad (ii)$$

Now By Theory of flotation of body

(Weight of cone) = Weight of the water displaced by the submerged vol.

$$\Rightarrow \rho_c \times g \times (Vol.)_{\text{cone}} = \rho_w \times g \times (V)_{\text{submerged}}$$

$$\Rightarrow 800 \times \frac{1}{3} \times \pi \times \left(\frac{D}{2}\right)^2 \times h = 1000 \times \frac{1}{3} \pi \times (2r)^2 \times L$$

$$\Rightarrow 800 \times \left(\frac{24}{2}\right)^2 \times 20 = 1000 \times (0.6L)^2 \times L$$

$$\Rightarrow 0.36 \times L^3 = 0.8 \times (12)^2 \times 20$$

$$\Rightarrow L = \left(\frac{0.8 \times (12)^2 \times 20}{0.36} \right)^{1/3} = 18.567 \text{ cm}$$

$$\therefore BG = 15 - \frac{3 \times 18.567}{4} = 1.07475 \text{ cm}$$

$$\text{and } \left(\frac{I_{\min}}{V} \right) = \frac{\left(\frac{\pi}{64} \right) \times (2r)^4}{\frac{1}{3} \times \pi \times r^2 \times L} = \frac{16 \times (0.6L)^4}{64 \times \frac{1}{3} \times (0.6L)^2 \times L}$$

$$\Rightarrow \left(\frac{I_{\min}}{V} \right) = \frac{16 \times (0.6)^4 \times (18.567)^4 \times 3}{64 \times 0.36 \times (18.567)^3} = 5.01309 \text{ cm}$$

$$\therefore \left[\left(\frac{I_{\min}}{V} \right) - BG \right] = 5.01309 - 1.07475 = 3.93834 > 0$$

So, Cone is in stable equilibrium.

Q-5'a

* Solar Still

* ~~Const~~

* Purpose

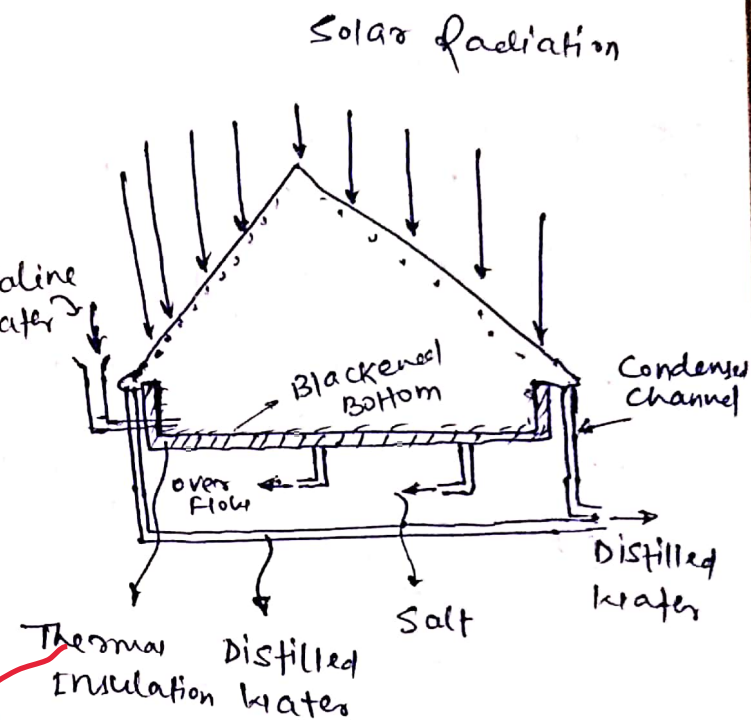
↳ Solar still is used to convert or obtained distilled water from saline water, for the various applications, like Agriculture, Household use etc.

* Construction

- It consists of a blackened bottom surface on which saline water is heated
- A roof-like transparent structure, to allow solar radiation. It is slopy.
- Condensed channels are present to use which flows the distilled water obtained to desired location

* Working

↳ Solar radiation is passes through



Simple Solar Still

the transparent roof and it is absorbed by the black bottom, which raises the saline water temp, and it evaporates.

→ Evaporated water is condensed on ~~roof~~ inside of roof surface which is ~~to~~ less temp.

→ This condensed distilled water is collected through condensate channels.

→ In generally saline water level maintains at 10 5 to 10 cm.

[Q-5'b']

* Classification of Reaction turbine

- ~~There~~ (i) Francis turbine
- (ii) Kaplan turbine
- (iii) propeller turbine

① Francis turbine

→ ~~Kaplan~~ Francis turbine is a reaction turbine

ie pressure change occurs in both ~~the~~ stator & rotor.

→ It may be Radially inward flow or Radially outward flow turbine

→ Generally, Radially inward flow is preferred in which direction of motion of water is along radial, in which water is entered radial at outer radius and exit at inner radius.

→ part load efficiency of Francis ~~Kaplan~~ turbine is poor

→ Its specific speed is in between 60 to 300

→ Its size is Large for a given Load as compared to Kaplan and No. of blades are also more in number.

(ii) Kaplan turbine

→ Kaplan turbine is an axial flow reaction turbine, in which direction of motion water is along the axis of rotation of blades i.e. axially.

→ Due to axial motion, losses are less in Kaplan turbine and hence its Efficiency is more.

→ Part Load efficiency is good.

→ Blades of Kaplan turbine are adjustable, which can be adjusted about its pivot to satisfy the required flow and hence it can be adjusted for fluctuating load, and hence Part Load efficiency is good.

→ No. of Rotors are less as compared to Francis's. So, frictional losses are also less.

→ Its specific speed is in between 600 to 1000.

→ Size of the Kaplan turbine is less for the same power output as compared to Francis's turbine.

(iii) propeller turbine

→ propeller turbine is also an axial flow turbine, like Kaplan.

→ But it cannot adjust its blades, so part load efficiency is poor for this turbine.

→ Specific speed is in between 300 to 600.

$$Q = 5' C'$$

Given

$$V_1 = 900 \text{ m/s (velocity leaving Nozzle)}$$

Nozzle angle, $\alpha = 20^\circ$, u , blade velocity = 300 m/s

$$K = \text{blade friction coefficient} = 0.7 = \frac{V_{r2}}{V_{r1}}$$

$$\dot{m} = 1 \text{ kg/s}$$

Given Symmetrical blading

$$\text{i.e. } \theta = \phi$$

$$V_{w1} = V_1 \cos \alpha = 900 \times \cos 20^\circ$$

$$\Rightarrow V_{w1} = 845.72 \text{ m/s}$$

and $V_{f1} = V_1 \sin \alpha = 900 \times \sin 20^\circ$

$$\Rightarrow V_{f1} = 307.82 \text{ m/s}$$

Also $V_{r1}^2 = (V_{f1})^2 + (V_{w1} - u)^2$

$$\Rightarrow V_{r1} = \sqrt{(307.82)^2 + (845.72 - 300)^2}$$

$$\Rightarrow V_{r1} = 626.55 \text{ m/s}$$

and $V_{r2} = K V_{r1} = 0.7 \times 626.55 = 438.585 \text{ m/s}$

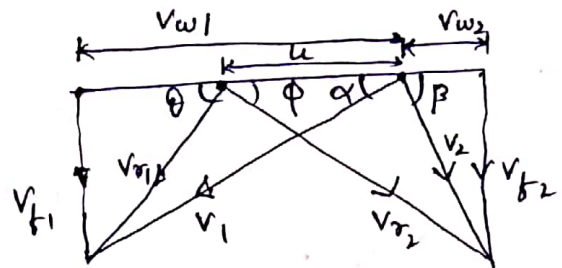
①

Blade inlet angle (θ)

$$\tan \theta = \left(\frac{V_{f1}}{V_{w1} - u} \right)$$

$$\Rightarrow \theta = \tan^{-1} \left(\frac{307.82}{845.72 - 300} \right)$$

$$\Rightarrow \theta = 29.43^\circ = \phi$$



Velocity triangle

②

Symmetrical blading

$$\therefore \theta = \phi$$

$$\therefore \cos \phi = \frac{u + V_{w2}}{V_{r2}}$$

$$\Rightarrow V_{w2} = V_{r2} \cos \phi - u = 438.585 \times \cos(29.43) - 300$$

$$\Rightarrow V_{w2} = 81.99 \text{ m/s}$$

$\therefore$ Driving force on wheel

$$= \dot{m}(V_{w1} + V_{w2}) = 1 \times (845.72 + 81.99)$$

$$\Rightarrow F_D = 927.71 \text{ N}$$

③

Axial Thrust

$$\tan \phi = \frac{V_{f2}}{u + V_{w2}}$$

$$\Rightarrow V_{f2} = (300 + 81.99) \times \tan(29.43)$$

$$\Rightarrow V_{f2} = 215.5 \text{ m/s}$$

$\therefore$ Axial Thrust

$$F_a = \dot{m}(V_{f1} - V_{f2}) = 1 \times (307.82 - 215.5)$$

$$\Rightarrow F_a = 92.32 \text{ N}$$

④

Diagram power

$$P = F_D \times u = \frac{927.71 \times 300}{1000} \text{ kW}$$

$$\Rightarrow P = 278.313 \text{ kW}$$

⑤ Diagram efficiency

$$\eta = \frac{P_D}{\left(\frac{1}{2} \dot{m} V_1^2\right)} = \left\{ \frac{278.313 \times 2 \times 1000}{1 \times (900)^2} \right\}$$

$$\Rightarrow \boxed{\eta = 0.6872 = 68.72 \%}$$

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$$Q = 5' d'$$

$$\text{Mass flow rate, } \dot{m} = 4 \text{ kg/s}$$

$$T_1 = 300 \text{ K}$$

$$\text{No. of stages, } N = 10$$

$$\eta_{isen} = 0.89$$

$$V_f = \text{Axial Velocity} = 125 \text{ m/s}$$

$$u = 200 \text{ m/s}$$

$$R = \text{Degree of Reaction} = 50\%$$

$$\text{ie } \boxed{\theta = \beta} \text{ and } \boxed{\alpha = \phi}$$

$$R = 0.5$$

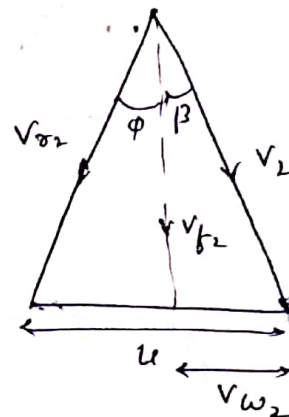
$$\Rightarrow \frac{V_f}{2u} (\tan \theta + \tan \phi) = 0.5$$

$$\Rightarrow \tan \theta + \tan \phi = \frac{0.5 \times 2 \times 200}{125}$$

$$\Rightarrow \boxed{(\tan \theta + \tan \phi) = 1.6} \quad (1)$$



Inlet velocity triangle



Outlet velocity triangle

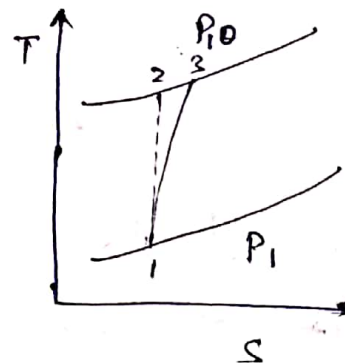
and Also from velocity triangle

$$u = V_f (\tan \theta + \tan \alpha)$$

$$\left(\frac{P_{10}}{P_1} \right) = (\sigma_p) = 8$$

$$\Rightarrow \left(\frac{T_2}{T_1} \right) = (\sigma_p)^{\frac{\gamma-1}{\gamma}}$$

$$\Rightarrow T_2 = (8)^{0.4/1.4} \times 300 = 543.434 \text{ K}$$



$$T_3 = T_1 + \frac{T_2 - T_1}{\eta_{isen}} = 300 + \frac{543.434 - 300}{0.89} = 573.521 \text{ K}$$

Assuming equal Temp change in each stage

$$(\Delta T)_{\text{stage}} = \frac{T_3 - T_1}{N} = \frac{573.521 - 300}{10} = 27.352 \text{ K}$$

$$(\Delta T)_{\text{stage}} = 27.352 \text{ K}$$

Also

$$c_p (\Delta T)_{\text{stage}} = (V_{w2} - V_{w1}) \times u$$

$$\Rightarrow (V_{w2} - V_{w1}) = \frac{1.005 \times 27.352 \times 1000}{200}$$

$$\Rightarrow (V_{w2} - V_{w1}) = 137.444 \text{ m/s}$$

$$\Rightarrow (V_f \tan \beta - V_f \tan \alpha) = 137.444$$

$$\Rightarrow (\tan \theta - \tan \phi) = \frac{137.444}{125} = 1.1 \quad \text{--- (1)}$$

($\because \theta = \beta \text{ and } \phi = \alpha$)

∴ from (1) & (11)

$$2 + \tan \theta = 1.6 + 1.1 = 2.7$$

$$\Rightarrow \theta = \tan^{-1} \left(\frac{2.7}{2} \right) = 53.47^\circ$$

$$\text{and } \tan \phi = \tan \theta - 1.1 = \tan(53.47) - 1.1$$

$$\Rightarrow \phi = \tan^{-1} [\tan(53.47) - 1.1]$$

$$\Rightarrow \phi = 14.03^\circ$$

$$\therefore \theta = \beta = 53.47^\circ \text{ and } \alpha = \phi = 14.03^\circ$$

And power given to air

$$P = \dot{m} c_p (\Delta T)_{\text{total}}$$

$$\Rightarrow P = 4 \times 1.005 \times (573.521 - 200)$$

$$\Rightarrow P = 1099.55 \text{ kW}$$

Q-5'e'

* Variation of wind speed with height:

→ At surface wind speed is zero and it increases with height

→ Wind Shear

↳ The change of wind speed with height is called wind shear.

→ Gradient height

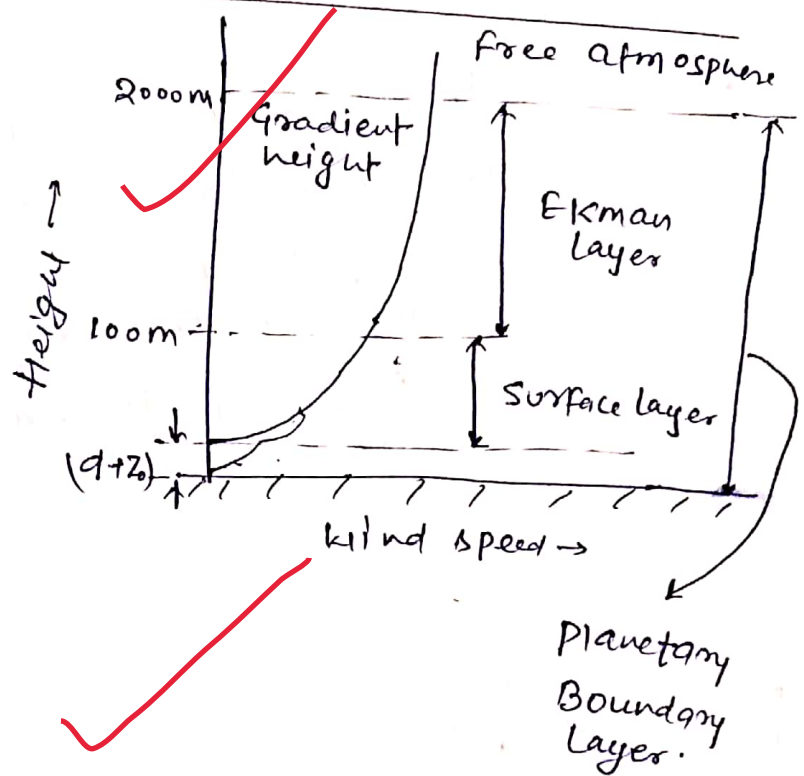
↳ Due to resistance between the layers of air motion, lower layer opposes the upper layer and mean air velocity changes with the height. At the sufficient height, when this shear effect is negligible, that height is called Gradient height. It is generally 2000 m.

→ Free atmosphere

↳ Above the Gradient height, shear effect are negligible and ~~air~~ wind speed is not much affected by ground conditions. This is called Free atmosphere.

→ Planetary boundary layer

↳ The layer of air from ground to the gradient height is called Planetary boundary layer.



→ Two parts of Planetary boundary layer

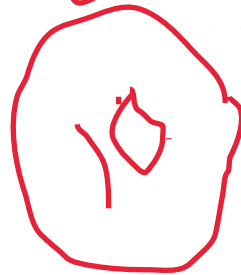
↳ ① Surface layer → upto 100 m

↳ ② Ekman layer → from 100 m to gradient height

→ A simple empirical Power Law model can be used to estimate wind speed, u_z at a height z relative to that available at standard ref. height H

$$u_z = u_H \left(\frac{z}{H} \right)^a$$

a → Depends on Surface roughness



Q-6 (a)

① Priming

2 Priming is the process in which the impeller of a centrifugal pump will get fully submerged in liquid without any air trap inside.

→ This is required before the start of pump

* Need of priming

2 Head developed by the pump is independent of density.

→ So; if pump is run with air, head developed is same but it is the form of head of air.

→ Since, air has low density, if we convert the developed head in terms of water head, it will be very small and chances are there, that water may not suck. So priming is necessary.

②

* Methods of priming

- 2 ① Manually
- ② With vacuum pump
- ③ With Jet pump
- ④ With separator

① In manually, water is poured in the pump through funnel. When priming is being done, an air escapes through air vent valve.

(i) With vacuum pump

- In this method, a small size reciprocating pump is used priming the main centrifugal pump.
- The suction line of reciprocating pump is connected to the delivery line of main centrifugal pump.

(ii) With Jet Pump

- In this method, water available at high head is allowed to flow through a nozzle.
- The nozzle is so designed that at the jet outside the nozzle the pressure is less than atm pressure so it is possible to suck water from the sump.

(iv) With separator

- An air separator is provided on the delivery side of pump and bent suction pipe portion is provided at the inlet of pump.
- Bent suction pipe always contains some liquid.
- The liquid heavier than air, so it falls back into separator and air moves in upward air.
- Therefore the liquid & air are separated in separator.

* Self priming

- Self priming of centrifugal pump is necessary in that case when, pump

Q-11

has to be placed above the level of liquid,
ex - when emptying an underground storage tank

→ A self-priming centrifugal pump has two phases of operation

- ① priming mode
- ② pumping mode

→ In priming mode, the pump essentially acts as a liquid-ring pump. The rotating impeller generates a vacuum at the impeller's eye, which draws air into the pump from the suction line. At the same time, it also creates a cylindrical ring of liquid on the inside of the pump casing. This effectively forms a gas tight-seal, stopping air returning from the discharge line to the suction line. Air bubbles are trapped in the liquid within the impeller's vanes and transported to the discharge port.

12

Q-6'b'

for Gas turbine

$r_p = \text{PR Ratio} = 9$

$$T_1 = 298 \text{ K}$$

$$T_4 = (1127^\circ\text{C} + 273) \text{ K}$$

$$\Rightarrow T_4 = 1400 \text{ K} \quad T_7 = 450 \text{ K}$$

$$\eta_{\text{comp}} = \eta_{\text{turb}} = 0.88$$

$$T_3 = T_1 + \frac{T_2 - T_1}{\eta_{\text{comp}}}$$

$$\Rightarrow T_3 = 298 + \frac{T_2 - 298}{0.88}$$

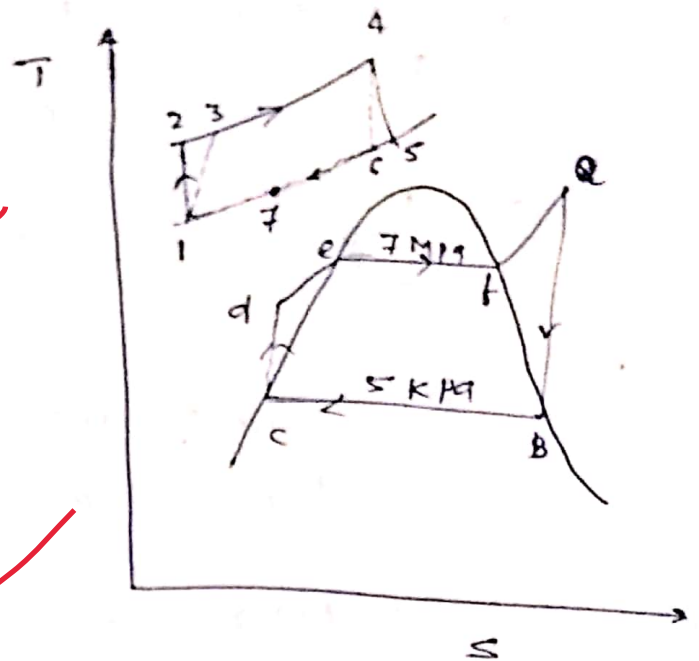
$$\therefore T_3 = 298 + \frac{(558.286 - 298)}{0.88}$$

$$\Rightarrow T_3 = 593.78 \text{ K}$$

$$T_2 = T_1 \times (r_p)^{\frac{\gamma-1}{\gamma}}$$

$$\Rightarrow T_2 = (298) \times (9)^{0.4/1.4}$$

$$\Rightarrow T_2 = 558.286 \text{ K}$$



Given

At 7 MPa, $t_{\text{seal}} = 285.83^\circ\text{C} = t_f = t_c$

and $t_a = 500^\circ\text{C}$.

Now

$$T_6 = T_4 \times \left(\frac{1}{r_p} \right)^{\frac{\gamma-1}{\gamma}} = 1400 \times \left(\frac{1}{9} \right)^{0.4/1.4}$$

$$\Rightarrow T_6 = 747.29 \text{ K}$$

and

$$T_5 = T_4 - (T_4 - T_6) \times \eta_{\text{turb}} = 1400 - 0.88 \times (1400 - 747.29)$$

$$\Rightarrow T_5 = 825.615 \text{ K}$$

$\therefore \text{at } P = 7 \text{ MPa } \Delta t = 500^\circ\text{C}$

$$h_a = \frac{3074.3}{3410.6} \text{ kJ/kg}$$

and $h_g = \frac{1267.5}{2773.4} \text{ kJ/kg}$

$\therefore$ (i) Let m_{com} = mass of combustion gases
 m_g = mass of steam

$\therefore$ By Energy Conservation

$$\dot{m}_s \times (h_a - h_f) = \dot{m}_a \cdot (C_{pa}) \cdot (T_6 - T_7)$$

$$\Rightarrow \left(\frac{\dot{m}_s}{\dot{m}_{\text{com}}} \right) = \frac{1.005 \times (747.29 - 450)}{1267.5 - 3410.6}$$

$$\Rightarrow \left(\frac{\dot{m}_s}{\dot{m}_{\text{com}}} \right) = 0.469$$

(ii) $(W_{\text{net}})_{\text{gas turbine}} = (W_T) - (W_{\text{comp}})$

$$\Rightarrow (W_{\text{net}})_{GT} = (C_{pa}) \cdot (T_2 - T_5) - (C_{pa}) \cdot (T_3 - T_1)$$

$$\Rightarrow (W_{\text{net}})_{GT} = 1.005 \times [1400 - 825.615 - 593.78 + 298]$$

$$\Rightarrow (W_{\text{net}})_{GT} = 279.998 \text{ kJ/kg of comb. gases}$$

Also $s_a = s_b = 6.8 \text{ kJ/kgK}$ [at 7 MPa, 500°C]

$$\Rightarrow s_c + s_{g@5\text{kPa}} \times x_b = 6.8$$

$$s_c = (s_g)_{@5\text{kPa}} = 0.4762 \text{ kJ/kgK}$$

Ans $s_{fg} = 7.9176 \text{ KJ/kg K}$

$$\therefore x_b = \frac{6.8 - 0.4762}{7.9176} \approx 0.8$$

$\therefore h_b = h_c + x_b \times (h_{fg}) @ 5 \text{ kPa}$

$$\Rightarrow h_b = 137.75 + 0.8 \times 2423 = 2076.15 \text{ KJ/kg}$$

Also $h_d = h_c + v \Delta P = 137.75 + 0.001005 \times (7000 - 5)$

$$\Rightarrow h_d = 144.78 \text{ KJ/kg}$$

$\therefore \eta_I = \text{Efficiency of Gas turbine}$

$$\Rightarrow \eta_I = \frac{(W_{net})_{GT}}{\text{Heat Add.}} = \frac{279.998}{C_p \times [T_4 - T_3]} \times 100$$

$$\Rightarrow \eta_I = \frac{279.998}{1.005 \times (1400 - 593.78)} \times 100$$

$$\Rightarrow \eta_I = 34.56\%$$

Ans $\eta_{II} = \text{Efficiency of steam turbine.}$

$$(W_{net})_{\text{steam turbine}} = (W_T) - (W_P) = (h_a - h_b) - (h_d - h_c)$$

$$\Rightarrow (W_{net})_{\text{steam}} = (3410.6 - 2773.4) - (144.78 - 137.75)$$

$$\Rightarrow (W_{net})_{\text{steam}} = 627.17 \text{ KJ/kg}$$

$$\therefore \eta_{II} = \frac{(W_{net})_{\text{steam}}}{Q_{\text{boiler}}} = \frac{627.17}{991.12} \times 100 = \frac{627.17}{(2773.4 - 144.78)} \times 100 = 23.86\%$$

$$\therefore \eta_p = (\text{overall}) = \eta_I + \eta_{II} - \eta_I \times \eta_{II} = 0.3456 + 0.2386 - 0.3456 \times 0.2386 = 0.4233 = 42.33\%$$

10.5'd'

η_D = efficiency of steam turbine

$$(W_{net})_{\text{Steam}} = (W_T) - (W_C) = (h_a - h_b) - (h_d - h_c)$$

$$\Rightarrow (W_{net})_{\text{Steam}} = (3410.6 - \overset{2076.15}{2773.4}) - (144.78 - 137.75)$$

$$\Rightarrow (W_{net})_{\text{Steam}} = \frac{627.17}{1327.42} \text{ KJ/Kg}$$

and $Q_{\text{boiler}} = (h_f - h_d) = (2773.4 - 144.78) = 2628.62 \text{ KJ}$

$$\therefore (\eta_D) = \frac{(W_{net})_{\text{Steam}}}{Q_{\text{boiler}}} = \frac{1327.42}{2628.62} \times 100 = 50.5\%$$

$$\therefore \eta_{\text{overall}} = (\eta_E) + (\eta_D) - \eta_D \times \eta_E$$

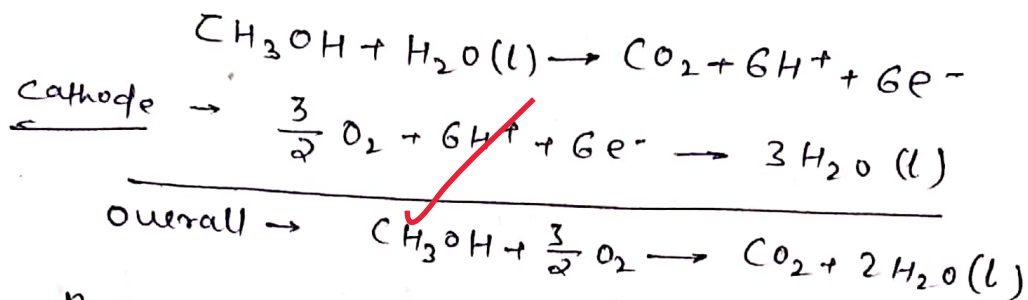
$$\Rightarrow \eta_o = \frac{34.56}{100} + \frac{50.5}{100} - \frac{34.56 \times 50.5}{10000}$$

$$\Rightarrow \eta_o = 0.676 = 67.6\%$$

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Q-6'c1

Anode Reaction



$\therefore n = \text{No. of electrons transferred} = 6$

ΔG ; Gibbs free energy change $= -39.59 \text{ KCal/mol}$

$$= -39.59 \times 4.186 \times 1000 \frac{\text{KJ}}{\text{kg mole}}$$

$$\Rightarrow \Delta G = -165723.74 \frac{\text{KJ}}{\text{kg mole}}$$

Cend

ΔH , Enthalpy change $= -56.8 \text{ KCal/mol}$

$$\Rightarrow \Delta H = -56.8 \times 1000 \times 4.18 \frac{\text{KJ}}{\text{kg mole}}$$

$$\Rightarrow \Delta H = -237764.8 \frac{\text{KJ}}{\text{kg mole}}$$

① Fuel Voltage at no load

$$(V_{\text{noLoad}}) = \frac{-\Delta G}{n \cdot F}$$

$F = \text{Faraday's const} = 96500 \text{ Coulomb/gram mole}$

$$\therefore (V_{\text{noLoad}}) = \frac{-(-165723.74)}{6 \times 96500} = 0.286 \text{ volt}$$

②

Max η

By First Law
of Thermodynamics

$$(\Delta Q - \Delta W) = \Delta H + \Delta KE + \Delta PE$$

* Assuming

$$\Delta KE = 0, \Delta PE = 0$$

$$\therefore \boxed{\Delta Q - \Delta W = \Delta H} \quad \text{--- (i)}$$

Now for max $W_{\max}$, process has to be Reversible

$$\therefore \boxed{\Delta Q = T(\Delta S)} \quad \text{--- (ii) for Reversible process}$$

$\therefore$ from (i) & (ii)

$$(T\Delta S) - \Delta W_{\max} = \Delta H$$

$$\Rightarrow \boxed{(\Delta W)_{\max} = (T\Delta S - \Delta H)} \quad \text{--- (iii)}$$

Also

Gibbs free energy

$$G = H - TS$$

$$\Rightarrow \Delta G = \Delta H - (T\Delta S + S\Delta T)$$

Assuming No temp change, i.e. $\Delta T = 0$

$$\therefore \Delta G = \Delta H - T\Delta S$$

$$\Rightarrow \boxed{(-\Delta G) = (T\Delta S - \Delta H)} \quad \text{--- (iv)}$$

From eq. (iii) & (iv)

$$\boxed{\Delta W_{\max} = -\Delta G}$$

$$\therefore \eta_{\max} = \left(\frac{\Delta W_{\max}}{-\Delta H} \right) = \frac{-\Delta G}{-(\Delta H)} = \left(\frac{\Delta G}{\Delta H} \right)$$

$$\Rightarrow \boxed{\eta_{\max} = \frac{165723.71}{237764.8} \times 100 = 69.7\%}$$

(iii) Now

$$W_{\max} = -\Delta G = .39.59 \times 4.186 = 165.724 \text{ KJ/mole.}$$

(1e)

165.724 kJ of electrical energy is produced by 1 mole of CH_3OH & $\frac{3}{2} = 1.5$ mole of O_2

1e
1 mole of $\text{CH}_3\text{OH} = (12 + 3 \times 1 + 16 + 1) = 32 \text{ g}$
1 mole of $\text{O}_2 = 32 \text{ g}$

1e
32 g of $\text{CH}_3\text{OH} \rightarrow 165.724 \text{ kJ}$
and $1.5 \times 32 \text{ g} = 48 \text{ g}$ of $\text{O}_2 \rightarrow 165.724 \text{ kJ}$

1e for 165.724 $\frac{\text{kJ}}{\text{s}}$ (kW) required $\rightarrow 32 \text{ g/sec}$ of CH_3OH

∴ 100 kW power required $\rightarrow \left(\frac{32}{165.724} \times 100 \right) \frac{\text{g}}{\text{sec}}$ of CH_3OH

∴ Flow Rate of Methanol = $\left(\frac{32 \times 100}{165.724} \times \frac{3600}{1000} \right) \frac{\text{kg}}{\text{hr}} = 69.513 \frac{\text{kg}}{\text{hr}}$

and Flow Rate of $\text{O}_2 = \left(\frac{48 \times 100}{165.724} \times \frac{3600}{1000} \right) \frac{\text{kg}}{\text{hr}} = 104.27 \frac{\text{kg}}{\text{hr}}$

(iv)

Now

Heat Removal

$$\Delta Q = \Delta H + \Delta W = (\Delta H - \Delta G) = -56.8 + 39.59$$
$$\Rightarrow \Delta Q = -17.21 \frac{\text{kJ}}{\text{mole}} \cdot \text{Kcal/mole} = -72.041 \frac{\text{kJ}}{\text{mole}}$$

-ve sign indicated heat removal

For 1 mole of $\text{CH}_3\text{OH} = 32 \text{ g}$.

ie 32 g/sec ie 1 mole of $\text{CH}_3\text{OH} \rightarrow 72.041 \frac{\text{kJ}}{\text{sec}}$

$$\therefore \left(\frac{69.513 \times 1000}{3600} \right) \frac{\text{g}}{\text{s}} \rightarrow \frac{72.041}{32} \times \left(\frac{69.513 \times 1000}{3600} \right)$$

∴ Heat Removed = 43.47 kW

Q-8'a'

Given

Dark Saturation Current, $I_0 = 1.7 \times 10^{-8} \text{ A/m}^2$
Short circuit Current density, $I_{sc} = 250 \text{ A/m}^2$

$$\text{Temp, } T = 27 + 273 = 300 \text{ K}$$

$$k = 1.381 \times 10^{-23} \text{ J/K}$$

$$e = 1.602 \times 10^{-19} \text{ J/V}$$

① Open circuit voltage (V_{oc})

$$I = I_{sc} - I_0 \left[\exp\left(\frac{eV}{kT}\right) - 1 \right]$$

When, $V = V_{oc}$,
then $I = 0$

$$0 = I_{sc} - I_0 \left[\exp\left(\frac{eV_{oc}}{kT}\right) - 1 \right]$$

$$\Rightarrow \exp\left(\frac{eV_{oc}}{kT}\right) - 1 = \frac{I_{sc}}{I_0}$$

$$\Rightarrow \left(\frac{eV_{oc}}{kT}\right) = \ln\left(1 + \frac{I_{sc}}{I_0}\right) = \ln\left(1 + \frac{250}{1.7 \times 10^{-8}}\right)$$

$$\Rightarrow V_{oc} = \left(\frac{kT}{e}\right) \times 23.411 = \frac{(1.381 \times 10^{-23}) \times 300 \times 23.411}{1.602 \times 10^{-19}}$$

$$\Rightarrow \boxed{V_{oc} = 0.605 \text{ Volt}}$$

②

$$\text{Power, } P = V \times I = V \times \left[I_{sc} - I_0 \left\{ \exp\left(\frac{eV}{kT}\right) - 1 \right\} \right]$$

$$\Rightarrow \boxed{P = V I_{sc} - V I_0 \exp\left(\frac{eV}{kT}\right) + V I_0}$$

For max power

$$\frac{dP}{dV} = 0$$

$$\Rightarrow \frac{d}{dV} \left[V I_{sc} - V I_0 \exp\left(\frac{eV}{kT}\right) + V I_0 \right] = 0$$

$$\Rightarrow I_{sc} + I_0 - I_0 \left\{ \cancel{V \times V \times \exp\left(\frac{eV}{kT}\right)} + V \left(\frac{e}{kT}\right) \cdot \exp\left(\frac{eV}{kT}\right) + \exp\left(\frac{eV}{kT}\right) \right\} = 0$$

$$\Rightarrow I_{sc} + I_0 - I_0 \left[\exp\left(\frac{eV}{kT}\right) \left\{ 1 + \frac{eV}{kT} \right\} \right] = 0$$

$$\Rightarrow \left(1 + \frac{eV}{kT} \right) \exp\left(\frac{eV}{kT}\right) = \frac{I_{sc} + I_0}{I_0} = \left(1 + \frac{I_{sc}}{I_0} \right)$$

$$\Rightarrow \exp\left(\frac{eV_{max}}{kT}\right) = \frac{\left(1 + \frac{250}{1.7 \times 10^{-8}} \right)}{1 + \frac{1.602 \times 10^{-19} \times V_{max}}{1.381 \times 10^{-23} \times 300}}$$

$$\Rightarrow \exp\left(\frac{1.602 \times V_{max} \times 10^{-19}}{1.381 \times 10^{-23} \times 300}\right) = \left(\frac{1.4706 \times 10^{10}}{1 + 38.668 \times V_{max}} \right)$$

$$\Rightarrow (38.668) \times V_{max} = \ln(1.4706 \times 10^{10}) - \ln(1 + 38.668 \times V_{max})$$

$$\Rightarrow V_{max} = \frac{23.4115}{38.668}$$

$$\Rightarrow (38.668) \times V_{max} + \ln(1 + 38.668 \times V_{max}) - 23.4115 = 0$$

on solving

$$V_{max} = 0.5264 \text{ volt} \Rightarrow \text{Voltage at Maxm Power}$$

(iii) current density at Maxm power, I_{max}

$$I_{max} = I_{sc} - I_0 \left[\exp\left(\frac{eV_{max}}{kT}\right) - 1 \right]$$

$$\Rightarrow I_{max} = 250 - 1.7 \times 10^{-8} \left[\exp \left(\frac{1.602 \times 10^{-19} \times 0.5269}{1.381 \times 10^{-23} \times 300} \right) - 1 \right]$$

$$\Rightarrow \boxed{I_{max} = 238.24 \text{ A/m}^2}$$

$$\textcircled{iv} : P_{max} = V_{max} \times I_{max} = 0.5264 \times 238.24$$

$$\Rightarrow \boxed{P_{max} = 125.409 \text{ W/m}^2}$$

$$\textcircled{v} \quad \eta_{max} = \frac{P_{max}}{\text{Solar intensity}} \times 100 = \frac{125.409}{820} \times 100 = 15.294\%$$

$$\therefore \boxed{\eta_{max} = 15.294\%}$$

Also

$$\text{output} = 20 \text{ W}$$

$$\therefore \text{Min}^m \text{ area Required, } A = \frac{20}{P_{max}} = \frac{20}{125.409} \text{ m}^2$$

$$\Rightarrow \boxed{A = 0.159 \text{ m}^2}$$

$$\rightarrow \text{Fill factor} = \frac{V_m \times I_m}{V_{oc} \times I_{sc}} = \frac{125.409}{0.605 \times 750}$$

$$\boxed{F.F. = 0.276}$$

20

1Q-8'b1

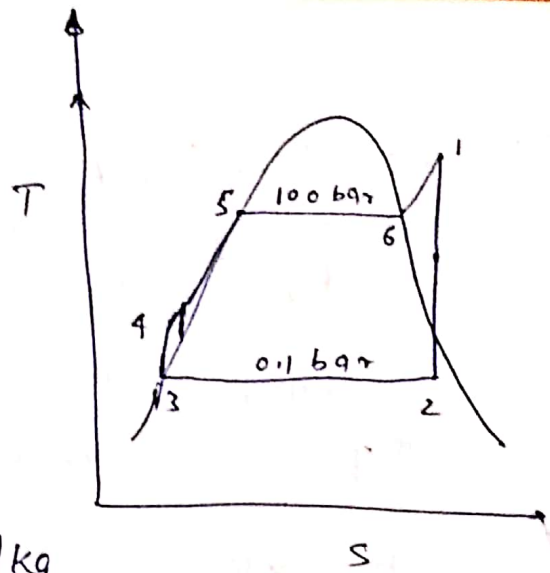
Given,

Entry to turbine is at

1 (100 bar, 500°C)

$$\therefore h_1 = 3375.1 \text{ kJ/kg}$$

$$s_1 = 6.5995 \text{ kJ/kgK} = s_2$$



Also

At 0.1 bar

$$s_3 = s_f @ 0.1 \text{ bar} = 0.6492 \text{ kJ/kgK}$$

$$s_{fg} @ 0.1 \text{ bar} = 7.4995 \text{ kJ/kgK}$$

$$\therefore s_2 = s_3 + x_2 \cdot s_{fg}$$

$$\Rightarrow x_2 = \frac{6.5995 - 0.6492}{7.4995} = 0.793$$

and

$$h_3 = h_f @ 0.1 \text{ bar} = 191.81 \text{ kJ/kg}$$

$$h_{fg} @ 0.1 \text{ bar} = 2392.1 \text{ kJ/kg}$$

$$\therefore h_2 = h_3 + x_2 \cdot h_{fg} = 191.81 + 0.793 \times 2392.1$$

$$\Rightarrow h_2 = 2088.7453 \text{ kJ/kg}$$

①

Given

$$P = 120 \text{ MW}$$

$$\Rightarrow \dot{m}_s [W_T - W_P] = 120 \times 1000$$

Neglecting pump work.

$$\dot{m}_s W_T = 120 \times 1000$$

$$\Rightarrow \dot{m}_s = \frac{120 \times 1000}{(h_1 - h_2)} = \frac{120 \times 1000}{3375.1 - 2088.7453} = 93.29 \text{ kg/s}$$

(Steam Rate)

② Fuel burning Rate

$$h_f = 675.5 \text{ KJ/kg}$$

$$\eta_{\text{boiler}} = 0.9$$

$$\dot{m}_f = \text{fuel rate}, (C.V.)_{\text{fuel}} = 25.7 \text{ MJ/kg}$$

$$\therefore (\dot{m}_f) \times (C.V.)_{\text{fuel}} \times \eta_{\text{boiler}} = \dot{m}_s \times (h_1 - h_4)$$

$$\Rightarrow (\dot{m}_f) = \frac{(93.29) \times (3375.1 - 675.5)}{(25.7 \times 1000) \times 0.9}$$

$$\Rightarrow \boxed{\dot{m}_f = 10.89 \text{ kg/s}} = 39204 \frac{\text{kg}}{\text{hr}} = 39.204 \frac{\text{ton}}{\text{hr}}$$

③ Evaporation Factor

$$E.F. = \frac{(h_1 - h_5)}{(h_{fg})_{@100^\circ\text{C}}} = \frac{(3375.1 - 1407.8)}{2256.9}$$

$$\Rightarrow \boxed{E.F. = 0.872}$$

④ Pressure head available for natural circulation

$$\boxed{\Delta P = gH(\rho_f - \rho_m)}$$

H = Height of Furnace wall = 40m

ρ_f = Density of Liquid = $\frac{1}{v_f}$

and ρ_m = Mean Density of Liquid vapour mixt in Riser

$$\boxed{\rho_m = \left(\frac{\rho_{\text{top}} + \rho_f}{2} \right)}$$

Now At 100 bar

$$v_f = 0.001452 \text{ m}^3/\text{kg}$$

and ~~$v_{fg} = v_g = 0.018028 \text{ m}^3/\text{kg}$~~

$$\therefore v_{top} = v_f + x_{top} \cdot v_{fg} = 0.001452 + 0.08 \times (0.018028 - 0.001452)$$

$$\Rightarrow v_{top} = \frac{2.89424 \times 10^{-3}}{2.77808} \text{ m}^3/\text{kg}$$

$$\therefore \rho_f = \frac{1}{v_f} = \frac{1}{0.001452} = 688.705 \text{ kg/m}^3$$

and $\rho_{top} = \frac{1}{v_{top}} = \frac{1}{\frac{2.89424 \times 10^{-3}}{2.77808}} = \frac{345.514}{359.96} \text{ kg/m}^3$

$$\therefore \rho_m = \left(\frac{\rho_{top} + \rho_f}{2} \right) = \left(\frac{\frac{345.514}{359.96} + 688.705}{2} \right) = \frac{524.33}{517.11} \text{ kg/m}^3$$

pressure head, $\Delta p = 9.81 \times 40 \times (688.705 - 517.11)$

$$\Rightarrow \Delta p = \frac{67333.88 \text{ Pa} = 67.334 \text{ kPa}}{64500.75 \text{ Pa} = 64.5 \text{ kPa}}$$

⑤ circulation Ratio (CR)

$$CR = \frac{1}{x_{top}} = \frac{1}{0.08} = 12.5$$

$$CR = 12.5$$

⑥

Riser outer diameter, $D_o = 60 \text{ mm}$

Wall thickness, $t = 3 \text{ mm}$

$$\therefore \text{Inner diameter, } D_i = D_o - 2t = 60 - 6 = 54 \text{ mm}$$

$$\therefore \left(\text{Max flow of steam formation in riser} \right) = \left(\frac{\pi}{4} D_i^2 \times \rho_{top} \times v_i \times x_{top} \right)$$

$$\therefore \text{Mass of steam in one riser} = \frac{\pi}{4} \times \left(\frac{54}{1000} \right)^2 \times (345.575) \times (0.08) \times 2$$

$$\Rightarrow m_{\text{one riser}} = \frac{0.1266}{0.132} \text{ kg/s}$$

$$\therefore \text{No. of Riser} = \frac{\dot{m}_s}{\dot{m}_{\text{one riser}}} = \frac{93.29}{0.1266} = 706.74$$

$$n = 707$$

⑦

Heat Absorption Rate per unit projected area of Riser

$$\text{Projected area, } A_p = D_o \times H = 0.06 \times 40 = 2.4 \text{ m}^2$$

$$\therefore \text{Heat Absorption} = \frac{m_{\text{one riser}} \times (h_{fg})_{@100\text{bar}}}{A_p}$$

$$\Rightarrow (\text{Heat absorption}) = \frac{0.132 \times (1319.7)}{2.4}$$

$$\Rightarrow \text{Heat absorption} = 72.58 \text{ kW/m}^2$$

③

Evaporation factor

$$E.F. = \frac{\dot{m}_s}{\dot{m}_f} = \frac{93.29}{10.89} = 8.57$$

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$$T = 81^\circ\text{C}$$

Total isentropic enthalpy drop

$$\Rightarrow \Delta h = 1467.4 \text{ kJ/kg}$$

$$u = 300 \text{ m/s}$$

$$\eta_{\text{nozzle}} = 0.95 \text{ (except Curtis)}$$

$$\eta_{\text{nozzle}} = 0.9 \text{ (Curtis)}$$

$$\alpha_i = 15^\circ \Rightarrow \text{Nozzle angle for impulse stages}$$

$$\alpha_r = 25^\circ \Rightarrow \text{Nozzle angle for reaction stages}$$

①

All Simple impulse stages

For impulse stage, optimum speed ratio

$$\rho = \frac{u}{v_1} = \frac{\cos \alpha_i}{2}$$

$$\Rightarrow v_1 = \left(\frac{2u}{\cos \alpha_i} \right) = \frac{2 \times 300}{\cos 15^\circ} = 621.166 \text{ m/s}$$

$$L \frac{1}{n} = 1$$

for one stage

$$v_1^2 = 2(\Delta h)_{\text{stage}} \times \eta_{\text{nozzle}}$$

$$\Rightarrow v_1^2 = 2 \times$$

$$\Rightarrow (\Delta h)_{\text{stage}} = \frac{v_1^2}{2 \times \eta_{\text{nozzle}}} = \frac{(621.166)^2}{2 \times 0.95} \times 10^{-3}$$

$$\Rightarrow (\Delta h)_{\text{stage}} = 203077.47 \text{ kJ/kg}$$

$$\therefore n = \text{No. of stage} = \frac{(\Delta h)_{\text{total}}}{(\Delta h)_{\text{stage}}} = \frac{1467.4}{203.077} = 7.23$$

$$\therefore n = 8$$

② All 50% reaction stages

for 50% reaction stage,

optimum speed ratio, $\phi = \frac{u}{V_1} = \cos \alpha_r$

$$\Rightarrow V_1 = \frac{u}{\cos \alpha_r} = \frac{300}{\cos 25^\circ} = 331.013 \text{ m/s}$$

$\therefore$ In 50% reaction stage, enthalpy drop of equal amount occurs in both stator and rotor.

$$\therefore V_1^2 = 2 \left\{ \frac{(\Delta h)_{\text{stage}}}{2} \right\} \cdot (\eta_{\text{nozzle}})$$

$$\Rightarrow (\Delta h)_{\text{stage}} = \left(\frac{V_1^2}{\eta_{\text{nozzle}}} \right) \times 10^{-3} \text{ KJ/kg}$$

$$\Rightarrow (\Delta h)_{\text{stage}} = \left(\frac{331.013^2}{0.95} \right) \times 10^{-3} = 115.336 \text{ KJ/kg}$$

$$\therefore \text{No. of stages, } n = \frac{(\Delta h)_{\text{total}}}{(\Delta h)_{\text{stage}}} = \frac{1467.4}{115.336} = 12.72$$

$$\therefore \boxed{n = 13}$$

③ A - 2-row currier stage followed by a simple impulse stage

for 2-row currier stage, $\phi = \frac{u}{V_1} = \frac{\cos \alpha_i}{4}$

$$\Rightarrow V_1 = \frac{4u}{\cos \alpha_i} = \frac{4 \times 300}{\cos 15^\circ} = 1242.33 \text{ m/s}$$

$$\therefore V_1^2 = 2 \times (\Delta h)_{\text{2-row currier}} \times \eta_{\text{nozzle}}$$

$$\Rightarrow (\Delta h)_{\text{2-row currier}} = \frac{(1242.33)^2}{2 \times 0.9} \times 10^{-3} \text{ KJ/kg}$$

$$\Rightarrow (\Delta h)_{\text{2-row currier}} = 857.435 \text{ KJ/kg}$$

$$\therefore \left(\text{Enthalpy drop in Remaining following Simple impulse stage} \right) = \text{Enthalpy drop in simple impulse stage, if all stages are simple stage}$$

$$\therefore \left(\text{Enthalpy drop in following impulse stage} \right) = (\Delta h)_{\text{isent or total}} - (\Delta h)_{2\text{-row Curtis}}$$

$$= 1467.4 - 857.435$$

$$\Rightarrow (\Delta h)_{\text{impulse stage}} = 609.965 \text{ kJ/kg}$$

$$\therefore \text{No. of stages of impulse} = \left(\frac{609.965}{203.077} \right) = 3$$

i.e. Here,

$$n = \underbrace{1}_{\substack{\downarrow \\ \text{2-row Curtis}}} + \underbrace{3}_{\substack{\downarrow \\ \text{Simple impulse stage}}}$$

④ A - 2 row Curtis stage followed by 50% Reaction stage

$$(\Delta h)_{2\text{-row Curtis stage}} = 857.435 \text{ kJ/kg}$$

$$\therefore \left(\text{Enthalpy drop in Remaining following 50% Reaction stage} \right), (\Delta h)_{50\%} = (\Delta h)_{\text{isent}} - (\Delta h)_{2\text{-row Curtis}}$$

$$= 1467.4 - 857.435$$

$$= 609.965 \text{ kJ/kg}$$

$$\therefore \text{No. of stages of 50% Reaction} = \frac{609.965}{115.336} = 5.29$$

$$\approx 6$$

$$\therefore n = \underbrace{1}_{\substack{\downarrow \\ \text{2-row Curtis}}} + \underbrace{6}_{\substack{\downarrow \\ \text{50\% Reaction}}}$$