

India's Best Institute for IES, GATE & PSUs

# **ESE 2019 : Mains Test Series**

ENGINEERING SERVICES EXAMINATION

### **Civil Engineering**

Test-5: Flow of Fluids, Hydraulic Machines and Hydro Power Design of Concrete and Masonry Structures-1

Name :	YATI	N MAL	ength of Mate HOTRA	erials-2	
Roll No:	CEI	9 MB	DLAS	22	
Test Cent	res				Student's Signature
Delhi Lucknow Hyderabad	Bhopal ☐ Pune ☐	Noida 🗌 Kolkata 🗌	Jaipur  Bhubaneswar	Indore  Patna	Willey.

#### **Instructions for Candidates**

- Do furnish the appropriate details in the answer sheet (viz. Name & Roll No).
- Answer must be written in English only. 2.
- Use only black/blue pen. 3.
- The space limit for every part of the question is specified in this Question Cum Answer Booklet. Candidate should write the answer in the space provided.
- Any page or portion of the page left blank in the Question Cum Answer Booklet must be clearly struck off.
- Last two pages of this booklet are provided for rough work. Strike off these two pages after completion of the examination.

Question No.	Marks Obtained
Section	on-A
Q.1	50
Q.2	
Q.3	60
Q.4	
Secti	on-B
Q.5	51-27
Q.6	
Q.7	46
Q.8	58
Total Marks Obtained	265-2

Cross Checked by

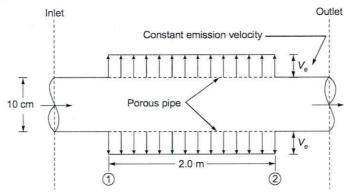
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#### Section A: Flow of Fluids, Hydraulic Machines and Hydro Power

- A circular pipe 10 cm in diameter has a 2 m length which is porous. In this porous section the velocity of exit is known to be constant as shown in figure. If the velocities at inlet and outlet of the porous section are 2.0 m/s and 1.2 m/s respectively. Estimate
  - (i) the discharge emitted out through the walls of the porous pipe and
  - (ii) the average velocity of this emitted discharge.



[12 marks]

Acc. to the law of conservation of mass:

incoming Discharge 2 outgoing discharge.

If x too 0.12 x 2 = Aporous + If x 0.12 x 1.2

Aporous = 6.283 lit /sec.

(ii) Area of the emitting section. RDL = RXO.1X2.
= 0.28 m²

Discharge of emitting section = 2 6,283 X10<sup>-3</sup> m³/s.

Awg. velocity. Area

- 6.283×10

0.2×17.

V. = 1cm/sec.

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- (i) Explain forced vortex flow occurring in a centrifugal pump.
- (ii) Water is flowing through a smooth pipe of 100 mm diameter at rate of 0.036 m<sup>3</sup>/s. Determine
  - (a) Darcy's friction factor
  - (b) Normal thickness of viscous sub layer

Take kinematic viscosity =  $10^{-6}$  m<sup>2</sup>/s and f (Darcy's friction factor) =  $0.0032 + \frac{0.221}{R_e^{0.237}}$ 

[6 + 6 marks]

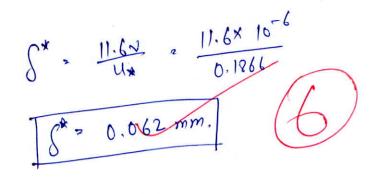
Given Diameter : 
$$0.1m$$
.  
 $0.036m^2/s$ .  
 $0.0032 + 0.221$   
 $0.0032 + 0.237$ 

(a) Ray nold's number =  $\frac{V.D}{2}$ .  $\frac{0.036}{2 \times 0.1^2} \times 0.1 \times \frac{1}{10^{-6}}$   $R_0 = 453366.236$ .

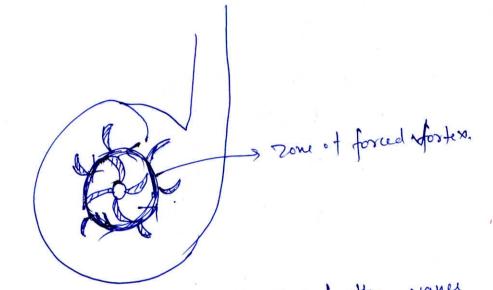
Friction factor  $f^2 = 0.0032 + \frac{0.221}{(458366.236)^{0.237}}$ 

(b) twickness of laminor sub layer - 11.6 2 Ux.

$$U_{*} = \sqrt{\frac{f}{8}} = \frac{0.036}{\frac{9}{4} \times 0.1^{2}} \sqrt{\frac{8}{8}} = 0.1866 \text{ m/s}$$



di



Due to sil sopid movement of the vanes
the water trapped blu the guide vanes
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Show that at the critical state of flow, the specific energy in a rectangular channel is equal to 1.5 times the depth of flow. Also find at critical flow condition whether the depth of flow will be greater or less than  $\frac{2}{3}$  times specific energy for a trapezoidal channel.

[12 marks]

For Critical flow in a channel:

$$\frac{0^{2}T}{A^{2}g} = 1$$

$$A = B. yc.$$

$$A = B. yc.$$

$$\frac{1}{A^{2}g} = \frac{1}{A^{2}g} = \frac{1}$$

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rectangular channel is also a trajeroidal channel with 90° slope. In in that care, Ec = 2 ye

Q.1(d)An empty tank with all sides closed is 12.5 m long, 0.7 m broad and 0.6 m high. The surface of sheet metal weighs 363 N/m<sup>2</sup> and the tank is allowed to float in fresh water with 0.6 m side vertical. Determine the state of equilibrium.

[12 marks]

Ams

Wsheet metal. 363N/m2 Surface area of en cuboid.  $= 12.5\times0.6\times2 + 0.7\times0.6\times2$ +12.5×0.7×2

= 33.34 m²

Weight of cuboid: 33.34 x 363 = 12.102 km. For state of equilibrium by floating, same weight of water is to be displaced.

Depth of James sion =  $12.5 \times 0.7 \times \pi = \frac{12.102 \times 10^3}{1000 \times 9.81}$ 

x. = 0.141m.

Heyce, at equilibrium, cuboid floats with 0.141m immersion in water.

Centre of Gravity is at 1/2

= 0.3m from the bottom.

Course of Buoyanay 2 2. 0.0705m.

Cantre of Buoyany la blow Centre of gravity.

AL

 $GM = \frac{12.5 \times 0.7^{2}}{\sqrt{12}} - (0.3 - 0.0705)$ 

at = 0.06 = 0. tul.

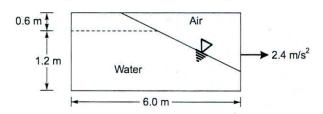
& Hence foot is in stable equilibrium.

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#### **EASY** Question Cum Answer Booklet

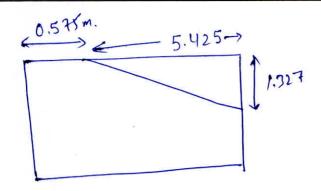
Q.1 (e) A closed tank 6 m long, 2 m wide and 1.8 m deep initially contains water to a depth of 1.2 m. The top has an opening in the front part to have air space at atmospheric pressure. If the tank has given a horizontal acceleration at a constant value of 2.4 m/s<sup>2</sup> along its length, calculate the total pressure force on the top of the tank.



[12 marks]



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As No. component of acceleration du to gravity results in premue on top.

Prusure on top of tank: Box gxanx 0.575m. z 1380 Pa.

-0.575-

Total Premue force 2 0.5×1380 × 0.575 × 2.

793.5 N

Q.2 (a)

A cylinder 0.25 m in radius and 2 m in length rotates coaxially inside a fixed cylinder of the same length and 0.30 m radius. Olive oil of viscosity  $4.9 \times 10^{-2} \, \text{Ns/m}^2$  fills the annular space between the cylinders. A torque 4.9 N-m is applied to the inner cylinder. After constant velocity is attained, calculate the velocity gradient at the cylinder walls, the resulting rpm, and the power dissipated by fluid resistance ignoring end effect.

[20 marks]

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Do not write in this margin Q.2(b) A pump impeller is 37.5 cm in diameter and discharges water with velocity components of 2 m/s and 12 m/s in the radial and tangential directions respectively. The impeller is surrounded by a concentric cylindrical chamber with parallel sides, the outer diameter being 45 cm. If the flow in this chamber is a free-spiral vortex, find the components of velocity of water on leaving and the pressure rise in the shroud if there is no loss.

[20 marks]

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Q.2 (c)

(i) Many researchers believe that the problem of air-entertainment in free surface vortex formation at intakes is influenced by forces of viscosity and surface tension. Show that for dynamic similarity between model and prototype, the following relationship must be satisfied:

$$\left(\frac{\mu V}{\sigma}\right)_m = \left(\frac{\mu V}{\sigma}\right)_p$$

Also prove that by use of the same liquid results in the "equal-velocity" concept of model testing.

- (ii) Water from a reservoir flowing through a rigid 150 mm diameter pipe, with a velocity 2.4 m/s is completely stopped by closure of a valve situated 1100 m from the reservoir, determine the maximum rise in pressure, when valve closure takes place
  - (1) In one second and
  - (2) In five seconds

Without damping of pressure wave. Consider the velocity of sound in water as 1432 m/s.

[10 + 10 marks]

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Do not write in this ma An inward flow reaction turbine has inlet and outlet diameters of 1.2 m and 0.6 m respectively. The breadth at the inlet is 0.25 m and at the outlet it is 0.35 m. At a speed of rotation of 250 rpm, the relative velocity at entrance is 3.5 m/s and is radial. Calculate the (i) absolute velocity at entrance and the inclination to the tangent of the runner, (ii) discharge and (iii) the velocity of flow at the outlet.

[20 marks]

$$D_{1} = 1.2m.$$

$$D_{2} = 0.6m.$$

$$B_{1} = 0.25m.$$

$$B_{2} = 0.35m.$$

$$N = 350 \text{ pm.}$$

$$V_{1} = 3.5 \text{ m/s.}$$

$$V_{1} = 4.5 \text{ m/s.}$$

(ii) Discharge = B RD, B, XVf, = N × 1.2 × 0.25 × 3.5 Q = 3.298 m<sup>2</sup>/s

No. 1.2 × 0.25 × 3.5. N× 0.6× 0.35× V/2

N/1.2 × 0.25 × 3.5. N× 0.6× 0.35× V/2

Show that for a submerged hydraulic jump just downstream of a sluice gate, in a horizontal rectangular channel,

$$\frac{y_s}{y_1} = \sqrt{2F_1^2 \left(\frac{y_1}{y_2} - 1\right) + \left(\frac{y_2}{y_1}\right)^2}$$

where  $y_1$  is the depth of opening of the sluice gate,  $y_2$  is the depth of flow downstream of the submerged hydraulic jump,  $y_s$  is the water depth on the downstream side of the sluice gate and  $F_1$  is the Froude number of flow through the sluice opening.

[20 marks]

Assuming horizontal, frictionless channel.

Acc. to the momentum egn:

2 -> V2 P2 -> Pressure thousand at section

V2 → relocity of sectio (2)

P, + (-P2) = M2+(-M,) Yw. y. (4s.B) - Yw yz. (42B) = fa(V22-Y12) = fA2V22-fA,V12

 $= \rho Q^2 \left( \frac{1}{3.92} \frac{1}{89.} \right).$  $= \int_{R}^{2} \left( \frac{1}{y_{1}} - \frac{1}{y_{1}} \right)$ 

write ir

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$$\frac{y_{2}}{2} \left[ y_{3}^{2} - y_{1}^{2} \right] = \int_{\mathbb{R}^{2}} \left[ \frac{1}{y_{3}} - \frac{1}{y_{1}} \right] \\
\frac{y_{2}}{2} \left[ y_{3}^{2} - y_{1}^{2} \right] = \int_{\mathbb{R}^{2}} \left[ \frac{1}{y_{3}} - \frac{1}{y_{1}} \right] \\
\frac{1}{2} \left[ y_{3}^{2} - y_{1}^{2} \right] = \int_{\mathbb{R}^{2}} \frac{2^{2}}{y_{1}^{2}} \left[ \frac{1}{y_{3}} - \frac{1}{y_{1}^{2}} \right] \\
\frac{1}{2} \left[ y_{3}^{2} - y_{1}^{2} \right] = \int_{\mathbb{R}^{2}} \frac{2^{2}}{y_{1}^{2}} \left[ \frac{1}{y_{1}^{2}} - \frac{1}{y_{1}^{2}} \right] \\
\frac{1}{2} \left[ \frac{y_{3}^{2}}{y_{1}^{2}} - \frac{y_{1}^{2}}{y_{1}^{2}} \right] = \int_{\mathbb{R}^{2}} \frac{2^{2}}{y_{1}^{2}} \left[ \frac{y_{1}}{y_{1}^{2}} - \frac{1}{y_{1}^{2}} \right] \\
\frac{1}{2} \left[ \frac{y_{3}^{2}}{y_{1}^{2}} - \frac{y_{1}^{2}}{y_{1}^{2}} \right] = \int_{\mathbb{R}^{2}} \frac{2^{2}}{y_{1}^{2}} \left[ \frac{y_{1}^{2}}{y_{1}^{2}} - \frac{1}{y_{1}^{2}} \right] \\
\frac{1}{2} \left[ \frac{y_{3}^{2}}{y_{1}^{2}} - \frac{y_{1}^{2}}{y_{1}^{2}} \right] = \int_{\mathbb{R}^{2}} \frac{2^{2}}{y_{1}^{2}} \left[ \frac{y_{1}^{2}}{y_{1}^{2}} - \frac{1}{y_{1}^{2}} \right] \\
\frac{1}{2} \left[ \frac{y_{3}^{2}}{y_{1}^{2}} - \frac{y_{1}^{2}}{y_{1}^{2}} \right] = \int_{\mathbb{R}^{2}} \frac{2^{2}}{y_{1}^{2}} \left[ \frac{y_{1}^{2}}{y_{1}^{2}} - \frac{1}{y_{1}^{2}} \right] \\
\frac{1}{2} \left[ \frac{y_{3}^{2}}{y_{1}^{2}} - \frac{y_{1}^{2}}{y_{1}^{2}} \right] = \int_{\mathbb{R}^{2}} \frac{2^{2}}{y_{1}^{2}} \left[ \frac{y_{1}^{2}}{y_{1}^{2}} - \frac{1}{y_{1}^{2}} \right] \\
\frac{1}{2} \left[ \frac{y_{3}^{2}}{y_{1}^{2}} - \frac{y_{1}^{2}}{y_{1}^{2}} \right] = \int_{\mathbb{R}^{2}} \frac{2^{2}}{y_{1}^{2}} \left[ \frac{y_{1}^{2}}{y_{1}^{2}} - \frac{y_{1}^{2}}{y_{1}^{2}} \right] = \int_{\mathbb{R}^{2}} \frac{2^{2}}{y_{1}^{2}} \left[ \frac{y_{1}^{2}}{y_{1}^{2}} - \frac{y_{1}^{2}}{y_{1}^{2}} \right] = \int_{\mathbb{R}^{2}} \frac{y_{1}^{2}}{y_{1}^{2}} \left[ \frac{y_{1}^{2}}{y_{1}^{2}} - \frac{y_{1}^{2}}{y_{1}$$

:)

- (i) What is meant by local and convective acceleration? For a one dimensional flow described by *V* (*x*, *t*), derive the expression for convective acceleration in terms of velocity and its gradient.
- (ii) A rectangular channel 5.2 m wide has a discharge of 10 m³/sec at a velocity of 1.25 m/s. At a certain section the bed width is reduced to 3.0 m through a smooth transition. A smooth flat hump is to be built in this contracted section to cause critical flow for flow measurement purposes. Estimate the height of the hump necessary for this purpose. (Assume no loss of energy at the transition.)

[10 + 10 marks]

Local acceleration -> Rate of change of velocity wector (dv) with respect to time in a flow.

Convectione acceleration -> Rate of change of velocity vector with respect to space.

(200)

In a flow.

Velocity of flow.

Velocity varies with space of time.

Velocity varies with space of the time.

Velocity varies with space of time.

9n x - direction. acceleration: 2

$$a_{x} = v \cdot \frac{\partial v}{\partial s} = v \cdot \frac{\partial v}{\partial s}$$
 $\frac{\partial u}{\partial s} = \frac{\partial u}{\partial u} + \frac{\partial u}{\partial s} + \frac{\partial u}{\partial s}$ 
 $\frac{\partial v}{\partial s} = \frac{\partial u}{\partial s} + \frac{\partial u}{\partial s} + \frac{\partial u}{\partial s}$ 

Similarly as the flow is one direction.

Tano u. du as vous o.

where u -> velocity

Ju -> gradient.

Discharge Intensity at original metion: 10 m3/s/m. o throat or = 10 m2/s/m.

Energy at ups of the section = y + \frac{1}{29}.

 $y = \frac{10}{1.25 \times 5.2} = 1.538m$ .

E = 1.6181 m.

Let the height of hump toe. DZ:

Critical flow of dis section.

Critical =  $\frac{3}{2}$  yc' =  $\frac{3}{2} \left[ \frac{(10/3)^2}{9.81} \right]^{1/3}$ 

= 1.5635 m

Energy Conservation:

1.6181 = 1.5635 + DZ.

Δ2 2 0.0545 m.

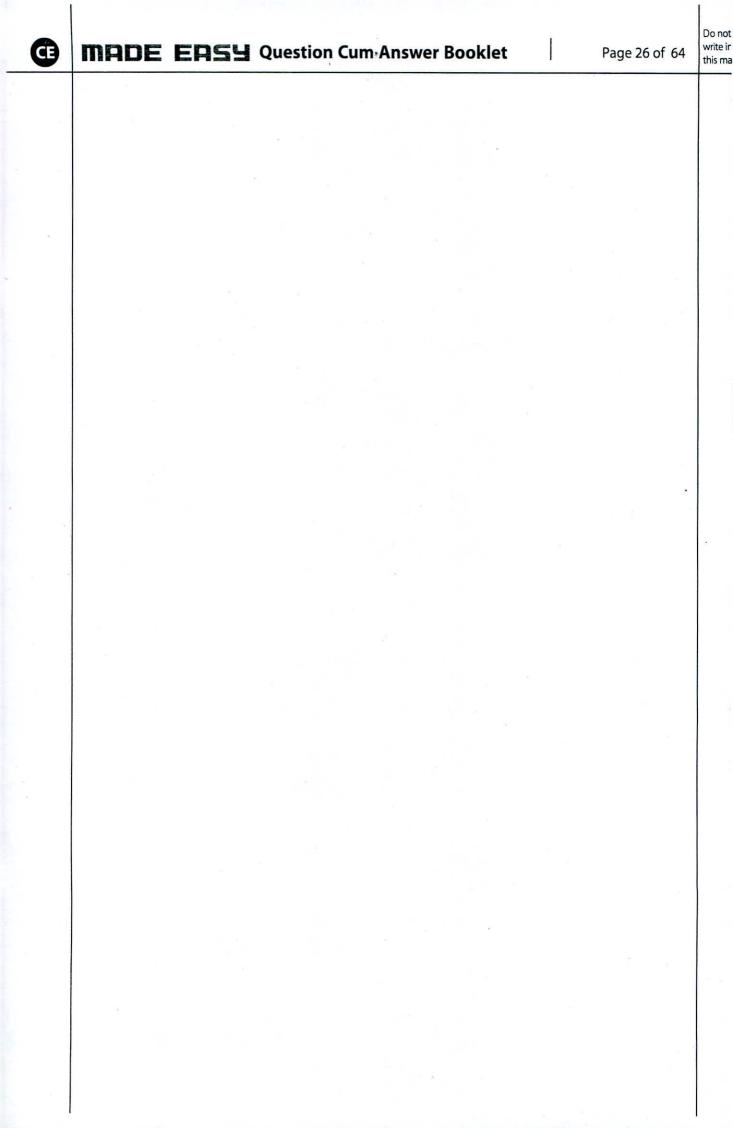
Hump required 0.0 545m.

- Q.4 (a)
- (i) For the velocity profile,  $\frac{u}{U_{\infty}} = \frac{3}{2} \left( \frac{y}{\delta} \right) \frac{1}{2} \left( \frac{y}{\delta} \right)^3$  on a flat plate, find out the average velocity and kinetic energy correction factor.
- (ii) Calculate the friction drag on a flat plate 15 cm wide and 45 cm long placed longitudinally in a stream of oil of relative density 0.925 and kinematic viscosity 0.9 stoke, flowing with a free stream velocity of 6.0 m/s. Also, find the thickness of the boundary layer and shear stress at the trailing edge.

[10 + 10 marks]

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A stream is spanned by a bridge which is a single masonry arch in the form of a parabolic arch, the crown being 2.5 metre above the springings which are 9 meters apart. The overall width of the bridge is 6 metres. During a flood the stream rises to a level 2 metres measured in the direction of the stream above the springings. Calculate the force tending to lift the bridge from its foundations if the arch remains water tight.

[20 marks]



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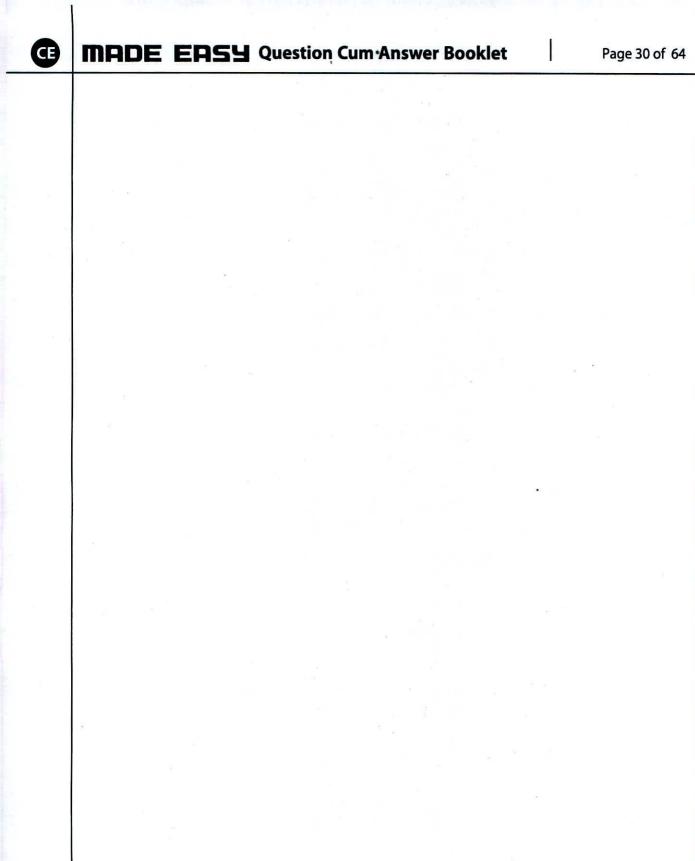
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- (i) Define bulk modulus of elasticity of a fluid. What is the SI unit of bulk modulus of elasticity? Discuss the factors affecting bulk modulus of elasticity of a fluid. Why liquids are generally considered incompressible?
- (ii) Show that the theoretical discharge in an open channel flow may be expressed as:

$$Q = A_2 \sqrt{\frac{2g(\Delta y - h_f)}{1 - \left(\frac{A_2}{A_1}\right)^2}}$$

where  $A_1$  and  $A_2$  are the cross-sectional areas of flow at sections (1) and (2) respectively,  $\Delta y$  is the drop in the water surface between the two sections and  $h_f$  is the energy head loss between the two sections.

[10 + 10 marks]



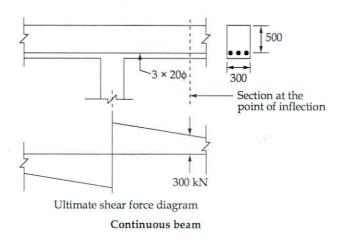
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#### Section B: Design of Concrete and Masonry Structures-1 + Strength of Materials-2

Q.5 (a) Check for bond stress at the point of inflection of a continuous beam as shown in figure, if it is subjected to an ultimate shear force of 300 kN at the point of inflection. Consider concrete of grade M20 and steel of grade Fe415. [Take design bond stress for M20 concrete = 1.2 N/mm<sup>2</sup>]



[12 marks]

Aus

Neutral axis = Xu, 0.87 fy. Ast 0.36 x fex. P = 0.87 X415 X 3 X 17 X 202 0.36 × 30× 300

Nu = 157.54mm.

Nu limiting = 0.48 d = 0.48 × 500.

So, Under Reinf Section.

MOR : 0.36 fex. B. Mu (d-0.42Mu) = 0.36 ×20 × 300× 157.54 (500 - 0.42 × 157.54)

Mui. > 147.627 KNm.

Mui = 147.627 × 10<sup>3</sup> = 1492.09 mm. < La reg.

Not sater.
Anchorage required = 448.14 = 450mm.

Cheek, Ld L My + Lo.
(8) -2 = 6

State the assumptions made while analyzing the reinforced concrete beam using Limit Q.5 (b) State of Flexure as per IS 456:2000 Code.

[12 marks]

Au

Assumption:

ii) Plane section before bending remains plane after bending

-s 9t serves as tou of advantage during analysts.

-> linear strain.

Ha Hinimum stress in the steel (1) 0.87 fy. + 0.002.

Da Strain at the most compressed concrete (111) fiber 1 0.0095.

Ctreus-Ctrain cume of the concrete in Compression with linear, parabolic or (W) any shape which conforms to the fest results.

(V). Concrete below the 10 NA @ (Concrete in Tension doesn't take any tension. Whole of the tension is taken by steel.

Three exactly similar mild steel tube specimens have the external and internal diameters 37.5 mm and 31.25 mm respectively. One of these specimens was tested in pure tension and limit of proportionality was recorded to be 70 kN. The second specimen was tested in torsion whereas the third was tested in torsion with superimposed bending moment of 350 Nm. If the failure criterion is the maximum shear stress, determine the torque at which the two specimens would have failed?

[12 marks]

For first case. 
$$\rightarrow$$
 Principle strees.  $\frac{P}{A}$ .

$$\frac{1}{P_1} = \frac{70 \times 10^3}{P_2(37.5^2 - 31.25^2)} \Rightarrow 207.42. \text{ HPa}.$$

Max. shear strees.  $\frac{307.42}{2}$ ,  $\frac{102.77}{2}$  MPa.

max shear strength:  $\frac{103.71}{R}$  MPa.

where  $\frac{167}{R}$   $\frac{167}{R}$   $\frac{1}{2}$   $\frac{1}{$ 

(1)

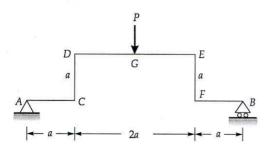
Let failue Torque be T' Bending Forque Moment = 350Nm. Equivalent shear Torsion: VM2+T2 Teg 2 \sqrt{350^2 + T^2} 16 Teg × 10 6 2 103.71 At failur. Teg 2 555.98 T' = 431.99. T'= 431.99 = 432 Nm.

)

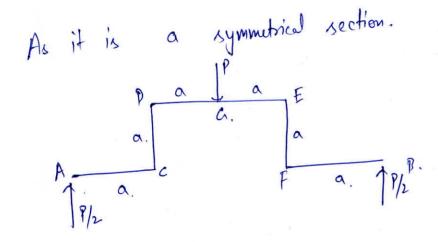
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Find the central deflection of the framed beam using strain energy method as shown in figure. [EI is constant]



[12 marks]



$$V_{AC} = \int \frac{H_{x}^{2} du}{g \cdot a \cdot \epsilon I} = \int \frac{\left(\frac{P}{2}x\right)^{2} du}{g \cdot \epsilon I} = \int \frac{P^{2}}{g \cdot \epsilon I} = \frac{P^{2}}{g \cdot \epsilon I} = \frac{P^{2}a^{3}}{g \cdot \epsilon I}$$

$$= \frac{P^{2}}{g \cdot \epsilon I} \times \frac{a^{3}}{3} = \frac{P^{2}a^{3}}{g \cdot \epsilon I}$$

$$U_{cD} = \int \frac{H_{x^{2}} du}{g \epsilon I} = \int \frac{\left(\frac{Pa}{ga}\right)^{2} du}{g \epsilon I} = \frac{P^{2}a^{3}}{g \epsilon I}$$

Upa, 
$$\int \frac{Hu^2 du}{9\varepsilon I} = \int \left(\frac{Pa + Pn}{9\varepsilon I}\right)^2 du = \frac{7}{94} \frac{p^2 a^2}{9\varepsilon I}$$

$$\Rightarrow \int \frac{P^2 a^2}{4} = \frac{1}{92} \frac{p^2 a^2}{92} = \frac{1}{94} \frac{p^2 a^2}{92}$$

Utotal? 
$$\left(2 \times \frac{1}{24} + 2 \times \frac{1}{8} + 9 \times \frac{7}{94}\right) \times \frac{P^2 a^2}{EE}$$
Utotal?  $\frac{11}{12} \frac{P^2 a^2}{EE}$ 

deflection?  $\frac{\partial U}{\partial P} = \frac{11}{12} \frac{9Pa^2}{EE}$ 
 $\left(\frac{1}{8}\right) = \frac{11}{6} \frac{Ra^2}{EE}$ 

A machine component is made of a material whose ultimate strength in tension, compression and shear are  $40 \text{ N/mm}^2$ ,  $110 \text{ N/mm}^2$  and  $55 \text{ N/mm}^2$  respectively. At the critical point in the component, the state of stress is represented by

$$\sigma_x = 25 \text{ N/mm}^2 \text{ and } \sigma_y = -75 \text{ N/mm}^2$$

Find the maximum value of the shear stress  $\tau_{xy}$  which will cause failure of the component? [12 marks]

Check with 
$$\sqrt{p_1} = \sqrt{0} \text{ MPa}$$
.

 $\sqrt{p_1} = \sqrt{\sqrt{2}} + \sqrt{\sqrt{2}} + \sqrt{\sqrt{2}} + \sqrt{2} + \sqrt$ 

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Max shear stree that can be applied - 19291 MPa.

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Design a rectangular beam section of 300 mm width and 500 mm effective depth which is subjected to an ultimate bending moment of 50 kNm, ultimate shear force of 50 kN and ultimate torsional moment of 40 kNm. Consider concrete of grade M20 and steel of grade Fe415. [Assume effective cover = 35 mm]

<i>p</i> <sub>t</sub> (%)	≤0.15	0.25	0.5	0.75	1
$\tau_c (N/mm^2)$	0.28	0.36	0.48	0.56	0.62

[20 marks]

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- Q.6 (b)
- (i) A ring beam of water tank has a diameter of 12.5 m. It is subjected to outward radial force of 25 kN/m. Design the section of ring beam using M25 and Fe415. Assume m = 11 and allowable stress in tension as 1.2 N/mm<sup>2</sup>.
  - (ii) Calculate the development length in tension and compression for a single mild steel bar of diameter  $\phi$  in concrete of grade M20. Assume  $\tau_{bd}$  = 1.2 N/mm<sup>2</sup>.

[14 + 6 marks]

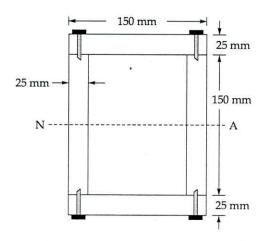
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The box beam as shown in figure below is made up of four 150 mm  $\times$  25 mm wooden planks connected by screws. Each screw can safely transmit a shear force of 1250 N. Estimate the minimum necessary spacing of screws along the length of the beam if the maximum shear force transmitted by the cross-section is 5000 N. Also determine the shear stress distribution across the section.

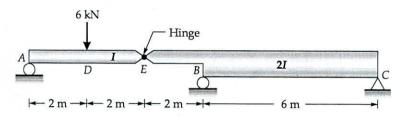


[20 marks]

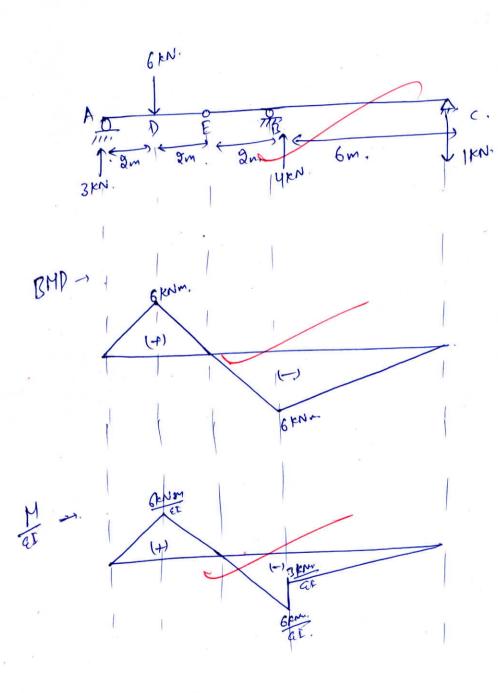
Page 48 of 64

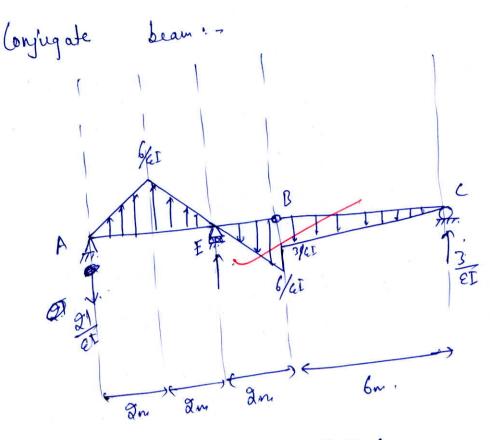
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A hinged beam system is loaded as shown below. Determine the slope at point E and D. Also determine the deflection at D. Use Conjugate beam method.



[20 marks]





$$R_{c} = \frac{0.5 \times 6 \times \frac{3}{4L} \times \frac{6}{3}}{6} = \frac{3}{4L}$$

$$\frac{8}{8} = -0.5 \times 4 \times 6 \times \frac{1}{8} + 0.5 \times 6 \times \frac{1}{8} \times \frac{1}{8} \times \frac{1}{1}$$

$$+ 0.5 \times 6 \times 3 \times (6 + \frac{6}{3})$$

$$R_{A} = -0.5 \times 6 \times \frac{4}{\epsilon I} \times 4 + 0.5 \times 6 \times 2 \times \frac{2}{3} \times \frac{20}{\epsilon I} \times \frac{20}{5} \times \frac{2$$

Slote at E = 20 Coloranie)

 $-\frac{21}{eI} + 0.5 \times 4 \times 6 = \frac{-9}{eI}$ 

LHS of E = 2 anticlockwin.

RHS of E. - 2 + 20 2 11 clockwin

Slope at D= -31 + 0.5x2x6.

Op. = 15 anticlockwise.

flower at D. Deflection at D: ->

- 21 x2 + 0.5 x 2 x 6 x 9 03

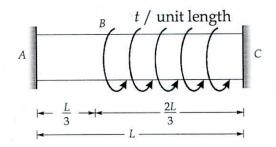
SD. = -38 €I

Deflection: 38 clownwards.

Do writ

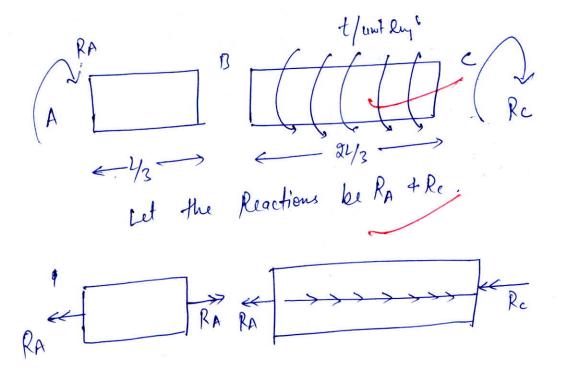
this

Q.7 (b) A solid circular cross-section shaft is clamped at both ends and loaded by a twisting moment *t* per unit length as shown in figure below. Determine the reactive twisting moment at each end of the bar.



[20 marks]





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Total angle of twist between, A 4 C = 0.

Angle of twist is zero.

for span BC:

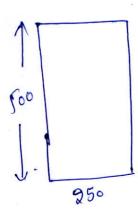
20

$$\frac{R_{A}\cdot \frac{4}{2}}{aJ} + \int_{0}^{\frac{91}{3}} \frac{R_{A}-t_{M}}{aJ} dn. = 0.$$

$$\frac{R_{A}\cdot \frac{1}{2}}{aJ} + \frac{1}{aJ}\left[R_{A}\left(\frac{at}{3}\right) - t\left[\frac{R_{J}^{2}}{2}\right]\right] = 0.$$

Design a reinforced concrete rectangular section of size 250 × 500 mm for a factored moment of 225 kN. The grades of concrete and HYSD steel are M20 and Fe415, respectively. [Take effective cover = 50 mm,  $f_{sc}$  = 353 MPa]

[20 marks]



Factored BM: 925 kNm. M20, Fe415.

eff cour. 50mm. fse 2 353 MPa. d2 450 mm.

Limiting
Homent of Resistance 2 0.188 fee bd.

~ 0.138 x 20 x 2500 x 80 4502

Mu, 2 139.725 KNm.

Unbalanced BM 2 85.275 KNm. - Muz

Section will be designed as Doubly Reinforced section.

No liniting 2 0.48 x dz 0.48 x 41(2 199.2 mm.

Territor Reing " for Mujer. (Act,).

Ast, = 139.725×10 (450-0.42 × 199.2)

- 1056.39 mm²

wri

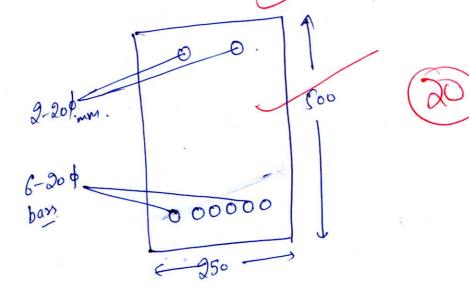
Astz for Unbalanced. Muz.

Compression side Reinf".

Provide. 6-20 ¢ mm bor.

Ast . 1646.85 mm2. Provide 2 - 200 mm bon.

Asc : 619.73 mm



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write in

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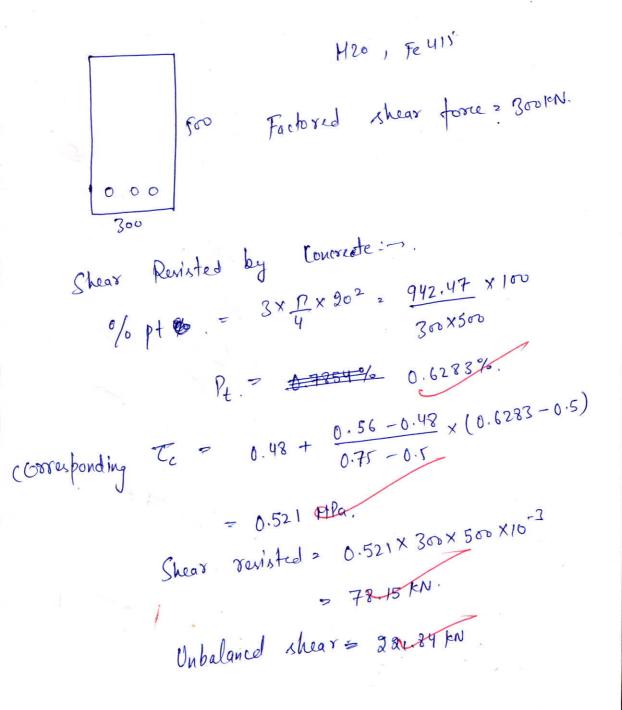
#### **EPSY** Question Cum Answer Booklet

A rectangular beam section of 300 mm width and 500 mm effective depth is reinforced with 5 bars of 20 mm φ, out of which 2 bars have been bent at 45°. Determine the shear resistance of the bent up bars and additional shear reinforcement required if it is subjected to an ultimate shear force of 300 kN. Consider concrete of grade M20 and steel of grade Fe415.

<i>p</i> <sub>t</sub> (%)	≤0.15	0.25	0.5	0.75	1
$\tau_c \left( N/mm^2 \right)$	0.28	0.36	0.48	0.56	0.62

(ii) Determine the ultimate load capacity of a circular column of 400 mm diameter reinforced with 6 × 25 mm \$\phi\$ bars adequately tied with (i) lateral ties and (ii) spirals. Consider concrete of grade M25 and steel of grade Fe415.

[10 + 10 marks]



Shear capacity of bent up bans. Aso. x 0.87 ty x Sinx. = 2 x 12 x 202 x 0.87 x 415 x Sin45°

Baxs Capacity = 160.4+N.

Addition shear reinf required for shear ->

max. ( Vue., Yue - V) = (221.84) 221.84-160.4)

Design Capacit. 110.92 KN.

Providing 10 mm & stirrups. 9-legged.

Sv 2 0.87 × 415 × 2× 102 × 1000 × 1000

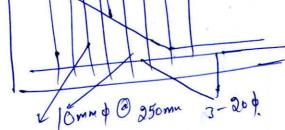
Su 2 255.65 mm. Provide 10mm & stimb at 250 mm spacing

0.87×415×2×2×10 (375)

min space 2

11×10×100

2.20° = 427.6 > 300 = 250m. 010





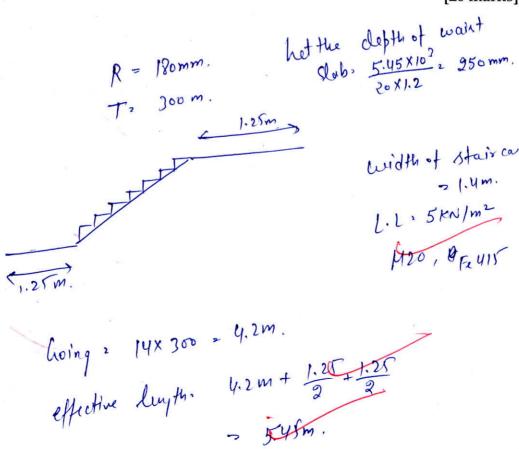
(Load carrying capacity 7 by 5%)

Pu: 1.05 (2046.11).

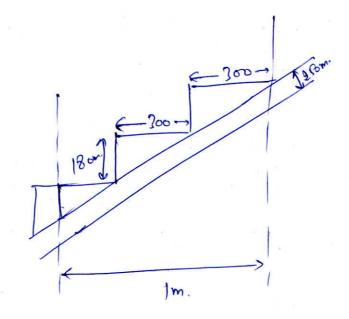
Pu: 2 2148.41 KN.

A staircase consists of 14 steps, each of 300 mm tread and 180 mm rise, plus two landings of each 1.25 m length. The width of staircase is 1.4 m. Design the staircase for a live load of  $5 \text{ kN/m}^2$ . Use M20 grade concrete and Fe415 reinforcement.

[20 marks]



Loads. For Im. length horizontal & Im width.



DL ->. Slab load = 1.1662 × 1× 25 × 0.25

= 20 150 km/m. 7.29 kN/m.

Steps = 1000 × 0.5×0.18×0.2 ×25

= 2.25 tex m.

LL -> D 5KN/m2 X /m, 5KN/m.

Total ? 14.54 KN/m.

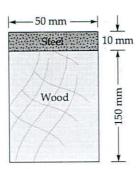
Factored Load = 14.54 x 1.52 21.81 KN/m

Factored Bending Moments When 2 21.81x5.47

- 80.9469 KNM

taking eff. cover - 50 mm. All sign MOR? 110.4KNM. So, Act, 0.5×20 [1- 1- 1- 4.6 × 80.9 × 1000 × 2002] × 1000 × 2002 1294.85mm2 Provide 16 mm bars @ 150 mm c/c. Distribution -> 0.12% of 1000 x 200 Provide Zmm & @ 200 mm c/c. 18mm 6 - 200 mm 1/c 16 mm bar @ 150 mm c/c.

- Q.8 (c)
- (i) A wooden beam 50 mm wide and 150 mm deep is reinforced by gluing a steel plate 10 mm thick and 50 mm wide on the top of section. The beam is simply supported over its ends which are 5 m away from each other. The beam carries a point load of 500 kN at mid of beam. Calculate maximum shear stress at the junction of wood and steel plate. Take m = 20.



(ii) Find the dimensions of a hollow steel shaft of internal diameter 0.6 times the external diameter, to transmit 150 kW at 250 rpm, if the shearing stress is not to exceed 70 N/mm<sup>2</sup>. If a bending moment of 3000 Nm is now applied to the shaft, find the speed at which it must be driven to transmit the same power for the same value of maximum shearing stress.

[10 + 10 marks]

Anu

Bending Homent = PL, 500×5, 625 kNm.

max. Shear force. 250 kN

Transformed rection:

50×20

100

To 150

To 50×150×75 + 1000×10×10 ff

50×150×150×150×10

20.7mm.

$$I_{NA} = \frac{\int_{0}^{6} \times \frac{100}{150^{2}} \int_{0}^{2} \int_{0}^{2} \times \int_{$$

INA. > 41574408 mmy

Shear strue at junction. VAT

250×10<sup>2</sup>× 50×20×10× (155 - 120.7)

That. - 41.25 MPa.

Tmax? 70 MPa.

Tosque => 20 NT = 150 X103

16 x 5.73 x 10 70

D. 72.24 mm 14 d. 46.94 mm

Py



& For same Equivalent Torque. Teg = 5.73 kNm. V 30'32+ 5000 T2 = 5-732 T= 4.88 KNM  $N_{2985}$   $N_{3985}$   $N_{38}$ Power is same. AL



India's Best Institute for IES, GATE & PSUs

# **ESE 2019 : Mains Test Series**

UPSC ENGINEERING SERVICES EXAMINATION

#### **Civil Engineering**

Test-5: Flow of Fluids, Hydraulic Machines and Hydro Power Design of Concrete and Masonry Structures-1 Strength of Materials-2

Name :	УО	WE ZH	KUMAR		
Roll No :	CEI	9 M B	DLB	746	
Test Centre	es				Student's Signature
Delhi Lucknow Hyderabad	Bhopal  Pune	Noida   Kolkata	Jaipur  Bhubaneswar	Indore  Patna	Jeg

#### **Instructions for Candidates**

- Do furnish the appropriate details in the answer sheet (viz. Name & Roll No).
- Answer must be written in English only.
- Use only black/blue pen. 3.
- The space limit for every part of the question is specified in this Question Cum Answer Booklet. Candidate should write the answer in the space provided.
- Any page or portion of the page left blank in the Question Cum Answer Booklet must be clearly struck off.
- 6. Last two pages of this booklet are provided for rough work. Strike off these two pages after completion of the examination.

FOR OFF	ICE USE		
Question No.	Marks Obtained		
Section	on-A		
Q.1	37-2		
Q.2			
Q.3	58		
Q.4			
Section	on-B		
Q.5	5-6		
Q.6			
Q.7	60-1=		
Q.8	5-3		
Total Marks Obtained	264-		

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Signature of Evaluator

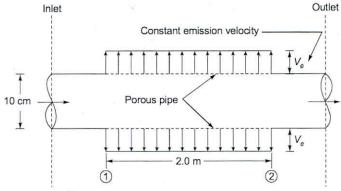
· Nevermen.



#### Section A: Flow of Fluids, Hydraulic Machines and Hydro Power

A circular pipe 10 cm in diameter has a 2 m length which is porous. In this porous section the velocity of exit is known to be constant as shown in figure. If the velocities at inlet and outlet of the porous section are 2.0 m/s and 1.2 m/s respectively. Estimate

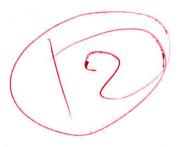
- the discharge emitted out through the walls of the porous pipe and
- (ii) the average velocity of this emitted discharge.



[12 marks]

 $V = \frac{6.283 \times 10^{-3}}{11 \times 0.10 \times 2}$  V = 0.01 m/fee V = 1 cm/fee

v = 1 conffee)
any velocity



Do not write in this margin

- (i) Explain forced vortex flow occurring in a centrifugal pump.
  - (ii) Water is flowing through a smooth pipe of 100 mm diameter at rate of 0.036 m<sup>3</sup>/s. Determine
    - (a) Darcy's friction factor

)

(b) Normal thickness of viscous sub layer

Take kinematic viscosity =  $10^{-6}$  m<sup>2</sup>/s and f (Darcy's friction factor) =  $0.0032 + \frac{0.221}{R_0^{0.237}}$ 

[6 + 6 marks]

in Centrifuged Pump rotation Provided to Pump due to which w is generated in water also and energy es Previoled to Flew.

where VE

= 100m = 45.8590 ×109 418599



durey's friction factor

 $F = 0.032 + \frac{0.221}{Re^{0.237}}$ 

0.032 + 0.221 (4r8599) 0.237

0.01326

Normal Thicknes of Viscous Sub lares

For Turbula Flow



Show that at the critical state of flow, the specific energy in a rectangular channel is equal to 1.5 times the depth of flow. Also find at critical flow condition whether the depth of flow will be greater or less than  $\frac{2}{3}$  times specific energy for a trapezoidal channel.

rect. chard having width 3 marks]

3 p. energy of change

Exist y + v2

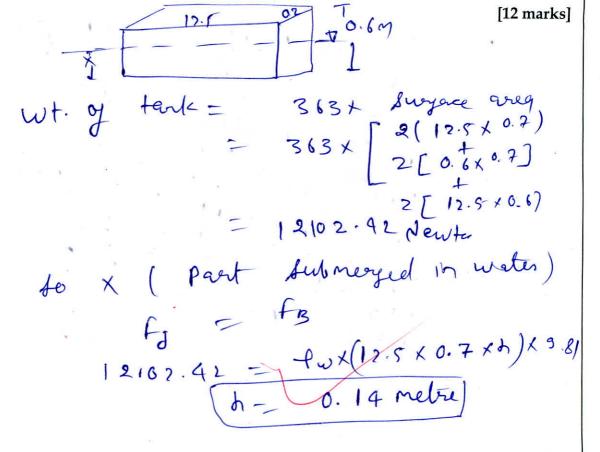
3  $d + \frac{y^2}{2g} = d + \frac{gd}{2g}$ 

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this mar

Q.1 (d) An empty tank with all sides closed is 12.5 m long, 0.7 m broad and 0.6 m high. The surface of sheet metal weighs 363 N/m<sup>2</sup> and the tank is allowed to float in fresh water with 0.6 m side vertical. Determine the state of equilibrium.

Ma



naw

Steebility condito

BW MM = I Vol. 8rb.

here BV7 =  $0.6 - \frac{0.14}{2} = 0.229 \text{ m}$ 

(9) stability about mej or 9 mis

In= 0.7 x (12.5) 3

 $60.7 \times (12.5)^{3}/12 - 0.229$ 

- 98.77 ) 0

8 teble

In = 12.1 × 0.73

 $M = (12.5 \times 0.7^3)/2 - 0.229$ 

12.5 × 0.7 × 0.1 g

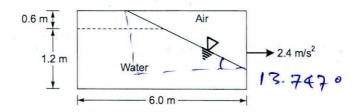
= (0.0626 M> 0/

so stable about both

9 min



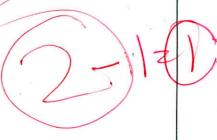
Q.1 (e) A closed tank 6 m long, 2 m wide and 1.8 m deep initially contains water to a depth of 1.2 m. The top has an opening in the front part to have air space at atmospheric pressure. If the tank has given a horizontal acceleration at a constant value of 2.4 m/s² along its length, calculate the total pressure force on the top of the tank.



[12 marks]

teno = 
$$\frac{9n}{92+9}$$
  $9n=0$   
teno =  $\frac{2.4}{9.81}$  = 0.249  
8 = teno 0.249

6 = 13.740



Do not write in this margin MADE EASY Question Cum Answer Booklet Page 9 of 64

Œ

Q.2 (a)

A cylinder 0.25 m in radius and 2 m in length rotates coaxially inside a fixed cylinder of the same length and 0.30 m radius. Olive oil of viscosity  $4.9 \times 10^{-2} \,\mathrm{Ns/m^2}$  fills the annular space between the cylinders. A torque 4.9 N-m is applied to the inner cylinder. After constant velocity is attained, calculate the velocity gradient at the cylinder walls, the resulting rpm, and the power dissipated by fluid resistance ignoring end effect.

[20 marks]

Page 11 of 64

Do not write in this margin Q.2 (b) A pump impeller is 37.5 cm in diameter and discharges water with velocity components of 2 m/s and 12 m/s in the radial and tangential directions respectively. The impeller is surrounded by a concentric cylindrical chamber with parallel sides, the outer diameter being 45 cm. If the flow in this chamber is a free-spiral vortex, find the components of velocity of water on leaving and the pressure rise in the shroud if there is no loss.

[20 marks]

Page 13 of 64

Do not write in this margin Q.2 (c) (i) Many researchers believe that the problem of air-entertainment in free surface vortex formation at intakes is influenced by forces of viscosity and surface tension. Show that for dynamic similarity between model and prototype, the following relationship must be satisfied:

$$\left(\frac{\mu V}{\sigma}\right)_m = \left(\frac{\mu V}{\sigma}\right)_p$$

Also prove that by use of the same liquid results in the "equal-velocity" concept of model testing.

- (ii) Water from a reservoir flowing through a rigid 150 mm diameter pipe, with a velocity 2.4 m/s is completely stopped by closure of a valve situated 1100 m from the reservoir, determine the maximum rise in pressure, when valve closure takes place
  - (1) In one second and
  - (2) In five seconds

Without damping of pressure wave. Consider the velocity of sound in water as 1432 m/s.

[10 + 10 marks]

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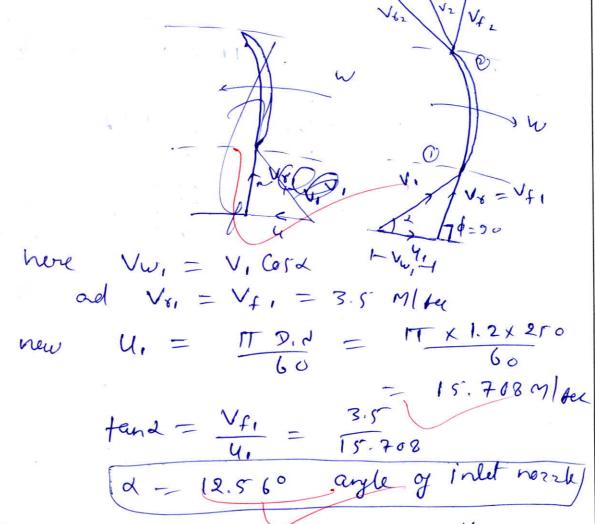
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An inward flow reaction turbine has inlet and outlet diameters of 1.2 m and 0.6 m respectively. The breadth at the inlet is 0.25 m and at the outlet it is 0.35 m. At a speed of rotation of 250 rpm, the relative velocity at entrance is 3.5 m/s and is radial. Calculate the (i) absolute velocity at entrance and the inclination to the tangent of the runner, (ii) discharge and (iii) the velocity of flow at the outlet.

$$D_1 = 1.2$$
 $B_2 = 0.6M$  [20 marks]

 $B_3 = 0.3\Gamma$ 
 $N = 250$ 
 $N_0 = whihl velocity at$ 
 $N_1 = 3.5\Gamma$ 
 $N_1 = 3.5\Gamma$ 
 $N_1 = 90^\circ$ 



 $V_{i} \quad \text{cos} \quad d = V_{i} \quad V_{i} = \frac{V_{i}}{\text{cor} \lambda}$   $V_{i} = 16.09 \text{ m/sec}$ 

So absolute relacity at inlet = 16.097/de indination to tayet = 12.5%

(11)

M D, B, Vf1

- 11 × 1.2 × 6.28 × 3.5

- [3. 299] M3/fee

(iii)

velocity of Flow at outled

Q - IT D, B, Vf, = IT D2B2V1

3.299 - IT X 0.6x 0.35 XV

to flow relacity at

outlet = 5 m/fee



Show that for a submerged hydraulic jump just downstream of a sluice gate, in a horizontal rectangular channel,

$$\frac{y_s}{y_1} = \sqrt{2F_1^2 \left(\frac{y_1}{y_2} - 1\right) + \left(\frac{y_2}{y_1}\right)^2}$$

where  $y_1$  is the depth of opening of the sluice gate,  $y_2$  is the depth of flow downstream of the submerged hydraulic jump,  $y_s$  is the water depth on the downstream side of the sluice gate and  $F_1$  is the Froude number of flow through the sluice opening.

[20 marks]

Fox Subreyed Submoyed Jump will take place when dis water level is higher than Jump of depth to in that Case en fluid mens 9 b cd applying P1 - P2 = M2 - M1 Pop P2 - Hyd force lones are reglected +19 yr x (Byr) - +9 y2 (By2) = + @ (V2-V1)

$$\frac{3}{2} \left[ y_s^2 - y_z^2 \right] = \frac{9^2 y_1^3 \left[ \frac{1}{y_2} - \frac{1}{y_1} \right]}{y_1^3}$$

$$\frac{(x + x^2 + y^2)}{(y + y^2)^2} = \frac{y^2 - y^2}{(y + y^2$$

$$\left(\frac{y_r}{y_r}\right)^2 = \left(\frac{y_r}{y_r}\right)^2 + \left(\frac{y_2}{y_r}\right)^2$$

$$\frac{y_s}{y_1} = \sqrt{\frac{2f_1^2/y_1-1}{y_2}} + \sqrt{\frac{y_2}{y_1}}$$



c)

- (i) What is meant by local and convective acceleration? For a one dimensional flow described by V(x, t), derive the expression for convective acceleration in terms of velocity and its gradient.
- (ii) A rectangular channel 5.2 m wide has a discharge of 10 m³/sec at a velocity of 1.25 m/s. At a certain section the bed width is reduced to 3.0 m through a smooth transition. A smooth flat hump is to be built in this contracted section to cause critical flow for flow measurement purposes. Estimate the height of the hump necessary for this purpose. (Assume no loss of energy at the transition.)

[10 + 10 marks]

when rate of chape of villeity

if enpressed as a function of

dist (the of) is could too

convective acceleration and when

it is represented in terms

of function of time it is

called local accele

The of the

Cenv. ace local accelerates

Do not

write ir

this ma

demen

$$V = V_n$$

$$Q_n = \frac{dV_n}{dt} + \frac{JV}{dh} + \frac{dh}{dt}$$

[iii]

$$B = 5.2M$$
  $Q = 10M3/fe$   
 $V = 1.2rM/s$   $Y_1 = \frac{10}{5.2 \times 1.2r}$ 

 $F_{8} = \frac{V}{\sqrt{99}} = 0.32$ Sub critical Flow

arguny notens of energy at

Transition  $E_1 = y_1 + \frac{V^2}{29}$ 

$$E_1 = y_1 + \frac{V^2}{2y}$$

Do not

write in this margin



- Q.4 (a)
- (i) For the velocity profile,  $\frac{u}{U_{\infty}} = \frac{3}{2} \left( \frac{y}{\delta} \right) \frac{1}{2} \left( \frac{y}{\delta} \right)^3$  on a flat plate, find out the average velocity and kinetic energy correction factor.
- (ii) Calculate the friction drag on a flat plate 15 cm wide and 45 cm long placed longitudinally in a stream of oil of relative density 0.925 and kinematic viscosity 0.9 stoke, flowing with a free stream velocity of 6.0 m/s. Also, find the thickness of the boundary layer and shear stress at the trailing edge.

[10 + 10 marks]



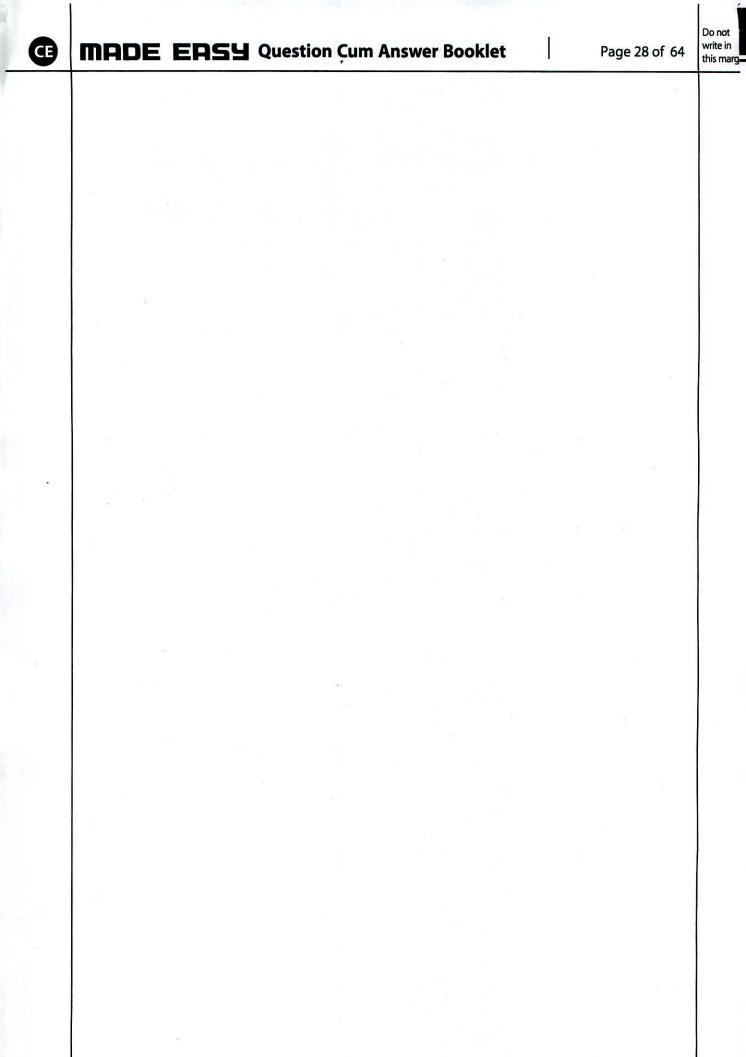
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b)

A stream is spanned by a bridge which is a single masonry arch in the form of a parabolic arch, the crown being 2.5 metre above the springings which are 9 meters apart. The overall width of the bridge is 6 metres. During a flood the stream rises to a level 2 metres measured in the direction of the stream above the springings. Calculate the force tending to lift the bridge from its foundations if the arch remains water tight.

[20 marks]



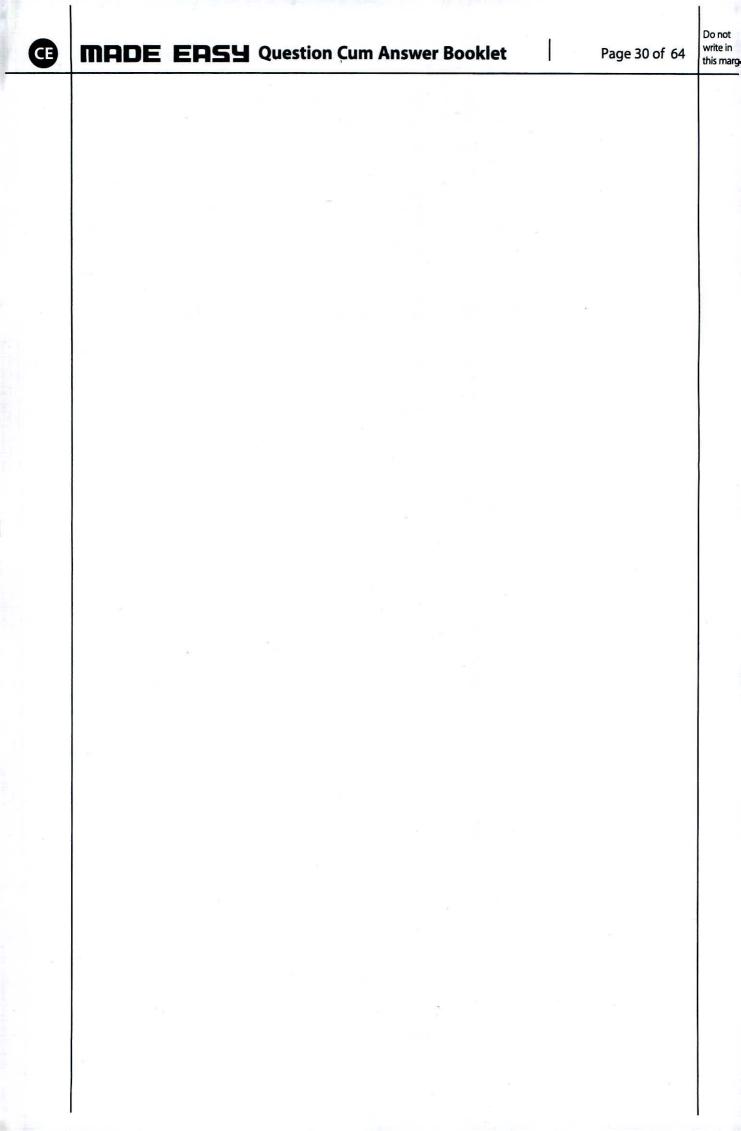
(c)

- (i) Define bulk modulus of elasticity of a fluid. What is the SI unit of bulk modulus of elasticity? Discuss the factors affecting bulk modulus of elasticity of a fluid. Why liquids are generally considered incompressible?
  - (ii) Show that the theoretical discharge in an open channel flow may be expressed as:

$$Q = A_2 \sqrt{\frac{2g(\Delta y - h_f)}{1 - \left(\frac{A_2}{A_1}\right)^2}}$$

where  $A_1$  and  $A_2$  are the cross-sectional areas of flow at sections (1) and (2) respectively,  $\Delta y$  is the drop in the water surface between the two sections and  $h_f$  is the energy head loss between the two sections.

[10 + 10 marks]

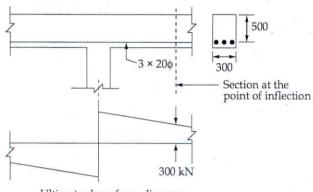




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### Section B: Design of Concrete and Masonry Structures-1 + Strength of Materials-2

Check for bond stress at the point of inflection of a continuous beam as shown in figure, Q.5 (a) if it is subjected to an ultimate shear force of 300 kN at the point of inflection. Consider concrete of grade M20 and steel of grade Fe415. [Take design bond stress for M20 concrete  $= 1.2 \text{ N/mm}^2$ 



Ultimate shear force diagram

Continuous beam

[12 marks]

 $M_1 \rightarrow Usp. to Art = 3 \times 20$  = 942 nm

 $0.36 \text{ fck} dy b = 0.87 \times 417 \times 942$  dy = 187.47mm  $M8 = 0.36 \text{ fue} dy b \left[ d - 0.42hy \right]$ 

My = 142.55 KdM

ld = 0.87 fg

hu

0.07 x 415 X 20 ( d 4 x 1.2 x 1.6 ld - 940.23mm 142 55 × 106 = 491.83 (dor 12 d) mans 500, 240 491.83 +500 991.83 In

**(1)** 

Q.5 (b) State the assumptions made while analyzing the reinforced concrete beam using Limit State of Flexure as per IS 456:2000 Code.

[12 marks]

F

0.87 fg

les -

Bending [ linear strain Variation]

3. Stress block digram for Concrete in Compression Can be taken as per results matched. With actual candition as Per Is 476 it is taken Parabolic than straight my I 3 thy

-> charact evistic streyth are used

-) for mild steel and total stress
if telen as Constant year

Yield ( Prog stren fy

- section is designed

Collapse at Flumere and sheen

and checked for deplection

Cracking.

Three exactly similar mild steel tube specimens have the external and internal diameters 37.5 mm and 31.25 mm respectively. One of these specimens was tested in pure tension and limit of proportionality was recorded to be 70 kN. The second specimen was tested in torsion whereas the third was tested in torsion with superimposed bending moment of 350 Nm. If the failure criterion is the maximum shear stress, determine the torque at which the two specimens would have failed?

[12 marks]

In objection tension tens,

$$\sigma_{y} \times A_{r} = 70 \text{ KB}$$
 $\sigma_{y} \times A_{r} = 70 \text{ KB}$ 
 $\sigma_{y} \times A_{r} =$ 

in sample Theree

Tren - 57

Tm. = 2

o, due to bending =

与一型

 $\sigma = \frac{M}{L} \times 3 = \frac{3r0 \times 10^3 \times 37.5}{[54](37.5)(37.5)}$ 

5 = 130.57 MP9

Try due to Forci - Try

Tru = (5) + (m) = 5

= J (65.287)2+ Try

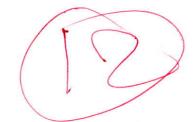
V(65.287) 2+ Tm2 = 103.71

Tmy - 80. 58

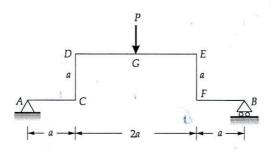
Ti = Tmy x II [ Pot-Dit ]

Ti - 80.58 x TT [37.54 - 31.254]

T2 - 431.98 NM



Find the central deflection of the framed beam using strain energy method as shown in figure. [EI is constant]



[12 marks]

dy of frame using 
$$S = P_1 = P_2 = P_2$$

$$P_1 = P_2 = P_2$$

$$P_2 = P_2$$

same as left lide

$$V = 2 \int \frac{\int M_{c}^{2} dh}{2EI} + \int \frac{M_{c}^{2} dh}{2EI} + \int \frac{M_{c}^{2} dh}{2EI} + \int \frac{M_{c}^{2} dh}{2EI}$$

$$V = 2 \int \frac{\int M_{c}^{2} dh}{2EI} + \int \frac{M_{c}^{2} dh}{2EI} + \int \frac{M_{c}^{2} dh}{2EI} + \int \frac{M_{c}^{2} dh}{2EI}$$

$$V = 2 \int \frac{\int M_{c}^{2} dh}{2EI} + \int \frac{Q}{2} \frac{Q}{2EI} + \int \frac{Q}{2} \frac{Q}{2} \frac{Q}{2EI} + \int \frac{Q}{2} \frac{Q}{2} + \int \frac{Q}{2} \frac{Q}{2} \frac{Q}{2} + \int \frac{Q}{2} \frac{Q}{2} + \int \frac$$

$$\frac{1}{10} - \frac{1}{EI} \int_{-\frac{1}{4}}^{\frac{1}{4}} \int_{0}^{ph^{2}} dh + \frac{2}{4} \int_{0}^{pq^{2}} dh + 2 \int_{0}^{p(h+9)^{2}} dh + 2 \int_{0}^{p(h+9)^{2}} dh$$

$$D = \frac{1}{EI} \left( \frac{1}{2} \times \frac{pq^3}{3} + \frac{1}{2} \times \frac{pq^3}{3} + \frac{p}{2} \left( \frac{2q^3 + q^3}{3} \right) \right)$$

$$0 - \frac{P}{EL} \left[ \frac{9^3}{6} + \frac{9^3 + 9^3 + 9^3}{6} \right]$$

### MADE EASY Question Cum Answer Booklet

A machine component is made of a material whose ultimate strength in tension, compression and shear are 40 N/mm<sup>2</sup>, 110 N/mm<sup>2</sup> and 55 N/mm<sup>2</sup> respectively. At the critical point in the component, the state of stress is represented by

$$\sigma_x = 25 \text{ N/mm}^2 \text{ and } \sigma_y = -75 \text{ N/mm}^2$$

Find the maximum value of the shear stress  $\tau_{xy}$  which will cause failure of the component?

[12 marks]

tabig tive as tension
$$a - ive as Comp.$$

$$\sigma_1 = 2r + \sqrt{2r + 2r} + \sqrt{2r + 2r} + \sqrt{2r}$$

$$= -2r + \sqrt{50^2 + \sqrt{2r}}$$

$$= -100$$

$$= -2r - \sqrt{50^2 + \sqrt{2r}} = -100$$

JS02+Tmg = 55

Tmy = 22.91 mpg)

So resterial will fails at Try = 22.9, MP9 in shear.

# **MADE EASY** Question Cum Answer Booklet

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Design a rectangular beam section of  $300 \, \text{mm}$  width and  $500 \, \text{mm}$  effective depth which is subjected to an ultimate bending moment of  $50 \, \text{kNm}$ , ultimate shear force of  $50 \, \text{kN}$  and ultimate torsional moment of  $40 \, \text{kNm}$ . Consider concrete of grade M20 and steel of grade Fe415. [Assume effective cover =  $35 \, \text{mm}$ ]

$p_t(\%)$	≤0.15	0.25	0.5	0.75	1
$\tau_c \left( N/mm^2 \right)$	0.28	0.36	0.48	0.56	0.62

[20 marks]

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Do no write this n MADE EASY Question Cum Answer Booklet

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Do not write in this margin Q.6 (b)

- (i) A ring beam of water tank has a diameter of 12.5 m. It is subjected to outward radial force of 25 kN/m. Design the section of ring beam using M25 and Fe415. Assume m = 11 and allowable stress in tension as 1.2 N/mm<sup>2</sup>.
  - (ii) Calculate the development length in tension and compression for a single mild steel bar of diameter  $\phi$  in concrete of grade M20. Assume  $\tau_{bd}$  = 1.2 N/mm<sup>2</sup>.

[14 + 6 marks]

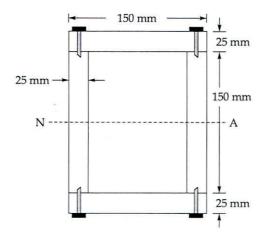
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### **MADE EASY** Question Cum Answer Booklet

The box beam as shown in figure below is made up of four 150 mm  $\times$  25 mm wooden planks connected by screws. Each screw can safely transmit a shear force of 1250 N. Estimate the minimum necessary spacing of screws along the length of the beam if the maximum shear force transmitted by the cross-section is 5000 N. Also determine the shear stress distribution across the section.



[20 marks]

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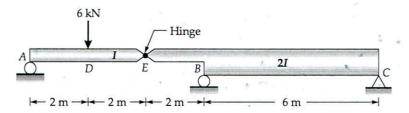
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## MADE EASY Question Cum Answer Booklet

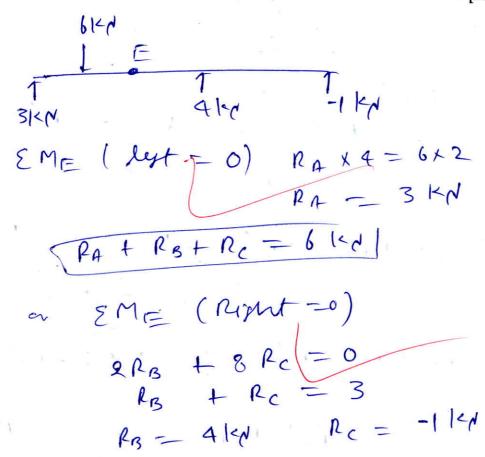
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A hinged beam system is loaded as shown below. Determine the slope at point *E* and *D*. Also determine the deflection at *D*. Use Conjugate beam method.

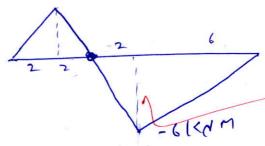


[20 marks]

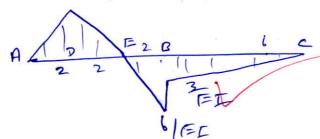


BMZ

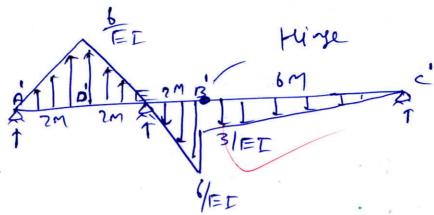
PKGW



M diam EI bles



Conjugate Bear



$$EMB'$$
 Right = 0  
 $\frac{1}{2} \times \frac{3}{EL} \times 6 \times \left[\frac{k}{3}\right] = R_c' \times k$ 
 $R_c' = \frac{3}{EL}$ 

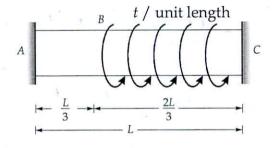
and 
$$E^{M}$$
 left = 0  $-0$ 

$$\frac{1}{12} - \frac{22}{12} + \frac{4}{12} = \frac{-18}{12}$$





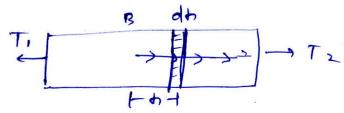
Q.7 (b) A solid circular cross-section shaft is clamped at both ends and loaded by a twisting moment *t* per unit length as shown in figure below. Determine the reactive twisting moment at each end of the bar.



[20 marks]

and OAC = 0

0 AB + OBC = 0



Torque acting at distance to frame

 $- T_1 - \int_0^{\infty} t dh da$ 

to  $\theta_{AB} + \theta_{BC} = 0$ 

 $\frac{T_{i}(L|3)}{\ln T_{p}} + \int_{0}^{2L/3} (T_{i} - th) dh = 0$ 

 $T_{1}\frac{L}{3} + 2T_{1}L - t \frac{h^{2}}{2} = 0$ 

T, L - 1/2 [ 412]

T, L = 2 + 12

T, - 2+L

T, + T2 - 2+L

 $T_2 - 2tL - 2tL = \frac{(6-2)tL}{9}$ 

Ti = 24L/9

$$T_2 = 4 + L$$

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Do writ this

### DE EPSY Question Cum Answer Booklet

Design a reinforced concrete rectangular section of size 250 × 500 mm for a factored moment of 225 kN. The grades of concrete and HYSD steel are M20 and Fe415, respectively. [Take effective cover = 50 mm,  $f_{sc} = 353 \text{ MPa}$ ]

[20 marks]

250

ey Gver = d-500-50 Meo Fear

finding trum = 0.48 d [Feari Bal. moment

216 MM cap of Section

Carryin

My - 0.138 Fac bd2

My - 0.13 Bx 20x 200 x 4102

= 1 135. 725 KNM

My - 225 KN se section will be designed by doubly Alt Fection MR = MR, +MR? 22r = 139.73 KNM 85.27 KNM

new duigning section at du = dulim= 216mm Csp. to no steel at Art, 19) MA - 139. 73 KNm

CE

$$A_{5+1} = \frac{8.36 \text{ fgc fig b}}{0.87 \text{ fg}} = \frac{0.36 \times 20 \times 216 \times 250}{0.82 \times 415}$$

$$= \frac{1077 \text{ mm}^2}{1077 \text{ mm}^2}$$

254 600

of 20 d

### **NADE EASY** Question Cum Answer Booklet

(i) A rectangular beam section of 300 mm width and 500 mm effective depth is reinforced with 5 bars of 20 mm φ, out of which 2 bars have been bent at 45°. Determine the shear resistance of the bent up bars and additional shear reinforcement required if it is subjected to an ultimate shear force of 300 kN. Consider concrete of grade M20 and steel of grade Fe415.

$p_t(\%)$	≤0.15	0.25	0.5	0.75	1
$\tau_c \left( N/mm^2 \right)$	0.28	0.36	0.48	0.56	0.62

(ii) Determine the ultimate load capacity of a circular column of 400 mm diameter reinforced with 6 × 25 mm φ bars adequately tied with (i) lateral ties and (ii) spirals. Consider concrete of grade M25 and steel of grade Fe415.

[10 + 10 marks]300 500 Vy = 300 KM M 20 Fe 41r (i)at support after beiling up 9425 x100 = 0.6284. Tc CSP to PY1 = 0.628 tc- 0.48 + [0.56-0.48][0.678-05] tc + 0.52 N/mm2 &bd = 78. 16 KM Vc = T&bd - 0.87 fg Art Sind taling d = 45 = 0.87 × 415 × 942.5 × 1 240.62 KN but manimum Capacity of bent up bary - + (Tv-Tc) &d

do best been Cap = 1 [300 - 78.16] - 110.92 Kd

to bent up bas falce 8f = 110.92kg

additional shere force = 271.84 - 110.92 110-92 KN

Providing 8 & 2 legged bars

5v - 0.87 fg Arv d \_ 163.53 mm

Man spacing + Arv > 0.4

SV < 307.32 MM

to Providing 84 2 leged bors (2)

(ii) (9) when tied with lateral ties Pu = 0.4 fac Bd + (0.67 fg - 0.4 fgc) × Arc

Py - 0.4 x 25 x 11 x 400 2 + [0.67 x 415 -0.9x 25

x 6×11×252

Py = 1256.637 + 789.47 KM = 2046.11/KM]

Page - Wit load Carrying

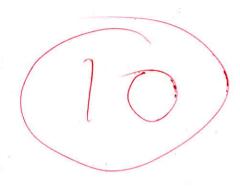
Cap = 2046.11 KN

when spirals are there capis (B) in creased by 5%.

Py = 1-05[0.4 fex Ac + 0.675-1.4 fqx) \* Arc 7

Py - 1.05 x 2096-11

= 2198.41 (cm)



A staircase consists of 14 steps, each of 300 mm tread and 180 mm rise, plus two landings of each 1.25 m length. The width of staircase is 1.4 m. Design the staircase for a live load of 5 kN/m<sup>2</sup>. Use M20 grade concrete and Fe415 reinforcement.

[20 marks] T = 300mn Rice = (8cmm)

Flight digt = 0.3 x 14 = 4.2 m

4 1-1.25 TC

assuming steincase is supposted on landing where landing is meno lithically costed into wells

to ley = 4:2+ 1:25 +1:25

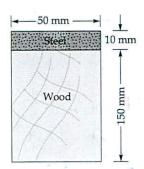
= 5.45 m (KIM)

☐ Question Cum Answer Booklet Page 60 of 64 loading on stein Core width 5 KMM due to stab arring stab thickens = 150 MM Dl = JR3+TL x 25 x1 x 0.15 Year = 25/5/1/2 = \J300241802 \ 2rx1x0, rr = 9.37 KMM De due to steins ( per m)  $=\frac{1000}{300}\times\left(\frac{1}{2}\times0.3\times0.18\right)\times22$ density of 2 KN/M Flooring DL = 105 Kilm steer Core resonary (in cluding Rise Tread) So Total load = 12.87 Irly factored load = [19.5] Idlm Wlen BM dum -(c)

Shear stress = \frac{\omega \tau \text{ } \frac{21.85 \text{ } 10^3 \text{ } 80^7 \text{ } \frac{2 \text{ } 1000 \text{ } 180 \text{ } \frac{2 \text{ } \text{ } 1000 \text{ } 180 \text{ } \text{ } \text{ } \text{ } \frac{2 \text{ } \text{ } 1000 \text{ } 180 \text{ } \text



- Q.8 (c)
- (i) A wooden beam 50 mm wide and 150 mm deep is reinforced by gluing a steel plate 10 mm thick and 50 mm wide on the top of section. The beam is simply supported over its ends which are 5 m away from each other. The beam carries a point load of  $500 \, \text{kN}$  at mid of beam. Calculate maximum shear stress at the junction of wood and steel plate. Take m = 20.



(ii) Find the dimensions of a hollow steel shaft of internal diameter 0.6 times the external diameter, to transmit 150 kW at 250 rpm, if the shearing stress is not to exceed 70 N/mm<sup>2</sup>. If a bending moment of 3000 Nm is now applied to the shaft, find the speed at which it must be driven to transmit the same power for the same value of maximum shearing stress.

at Junetion

$$= \frac{SAY}{Ib} = \frac{SAY}{I} = \frac$$

$$\frac{\Gamma_{CA} - \frac{50 \times 150^{3} + (50 \times 150) \times [120.71-71]^{2}}{12}}{1200 \times 10^{3} + (1000 \times 10) \times 34.29^{2}}$$

(my = 70)

78.24MM

outer d = 78.2, cm.
Interned dia = 0.6 do

96.95 mm

Pert I

N N