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Leading Institute for ESE, GATE & PSUs

ESE 2026 : Mains Test Series

UPSC ENGINEERING SERVICES EXAMINATION

Electrical Engineering

Test-3 : Power Systems + Digital Electronics-1 + Microprocessor-1 + Electrical Circuits-2 + Systems and Signal Processing-2

Name : ....

Roll No :

Test Centres			Student's Signature
Delhi ☑	Bhopal ☐	Jaipur ☐	
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Instructions for Candidates

1. Do furnish the appropriate details in the answer sheet (viz. Name & Roll No).
2. There are Eight questions divided in TWO sections.
3. Candidate has to attempt FIVE questions in all in English only.
4. Question no. 1 and 5 are compulsory and out of the remaining THREE are to be attempted choosing at least ONE question from each section.
5. Use only black/blue pen.
6. The space limit for every part of the question is specified in this Question Cum Answer Booklet. Candidate should write the answer in the space provided.
7. Any page or portion of the page left blank in the Question Cum Answer Booklet must be clearly struck off.
8. There are few rough work sheets at the end of this booklet. Strike off these pages after completion of the examination.

FOR OFFICE USE

Question No.	Marks Obtained
Section-A	
Q.1	34
Q.2	50
Q.3	28
Q.4	
Section-B	
Q.5	17
Q.6	
Q.7	49
Q.8	
Total Marks Obtained	178

Signature of Evaluator: Saurabh kumar

Cross Checked by: ....

IMPORTANT INSTRUCTIONS

CANDIDATES SHOULD READ THE UNDERMENTIONED INSTRUCTIONS CAREFULLY. VIOLATION OF ANY OF THE INSTRUCTIONS MAY LEAD TO PENALTY.

DONT'S

1. Do not write your name or registration number anywhere inside this Question-cum-Answer Booklet (QCAB).
2. Do not write anything other than the actual answers to the questions anywhere inside your QCAB.
3. Do not tear off any leaves from your QCAB, if you find any page missing do not fail to notify the supervisor/invigilator.
4. Do not leave behind your QCAB on your table unattended, it should be handed over to the invigilator after conclusion of the exam.

DO'S

1. Read the Instructions on the cover page and strictly follow them.
2. Write your registration number and other particulars, in the space provided on the cover of QCAB.
3. Write legibly and neatly.
4. For rough notes or calculation, the last two blank pages of this booklet should be used. The rough notes should be crossed through afterwards.
5. If you wish to cancel any work, draw your pen through it or write "Cancelled" across it, otherwise it may be evaluated.
6. Handover your QCAB personally to the invigilator before leaving the examination hall.

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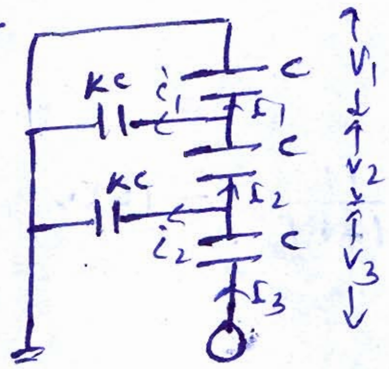
Section A : Power Systems

Q.1 (a) The three bus-bar conductors in an outdoor substation are supported by units of post type insulators. Each unit consists of a stack of 3-pin type insulators fixed one on the top of the other. The voltage across the lower insulator is 13.1 kV and that across the next is 11 kV. Find the bus-bar voltage of the station.

[12 marks]

Answer



given

$V_3 = 13.1\text{ kV}$

$V_2 = 11\text{ kV}$

from above

$$I_3 = I_2 + i_2$$

$$V_3 \omega C = V_2 \omega C + (V_1 + V_2) K\omega C$$

$$V_3 = V_2(1+K) + KV_1 \quad \text{--- (1)}$$

Now

$$I_2 = I_1 + i_1$$

$$V_2 \omega C = V_1 \omega C + V_1 K\omega C$$

$$V_2 = V_1(1+K) \quad \text{--- (2)}$$

from (1) and (2)

$$V_3 = V_1\left[(1+K)^2 + K\right]$$

$$V_3 = V_1\left[K^2 + 3K + 1\right] \quad \text{--- (3)}$$

Also from (1) and (2)

$$V_3 = V_2(1+K) + K\frac{V_2}{1+K}$$

By putting values of V_2 and V_3

$$13.1 = 11(1+K) + 11\frac{K}{1+K}$$

$$13.1(1+k) = 11\left[(1+k)^2 + K\right]$$

$$11K^2 + 33K + 11 = 13.1 + 13.1K$$

$$11K^2 + 19.9k - 2.1 = 0$$

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By solving

$K = 0.1 \quad , -1.90$

So $\boxed{K = 0.1}$

So from ③ and ②

$V_3 = V_1 \{ K^2 + 3K + 1 \}$

and

$V_1 = \dfrac{V_2}{1+K} = \dfrac{11}{1+0.1} = 10\,kV$

$\cancel{V_3} = \dfrac{\cancel{V_2}}{1+K} \cancel{[K^2+3K+1]}$

So

$V = V_1 + V_2 + V_3$

$V = 10 + 11 + 13.1$

$\boxed{V = 34.1\,kV}$ Bus station voltage

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$\sqrt{3} \times 34.1$

$= 59\,kV.$

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Q.1 (b) A certain 3-phase equilateral transmission line has a total corona loss of 53 kW at 106 kV and a loss of 98 kW at 110.9 kV. What is the disruptive critical voltage? What is the corona loss at 113 kV?

[12 marks]

Answer

As we know

$P_L \propto (V_{ph} - V_d)^2$ —(1)

here V_d = disruptive critical voltage

So

$\frac{P_{L_2}}{P_{L_1}} = \left(\frac{V_{ph_2} - V_d}{V_{ph_1} - V_d}\right)^2$ —(2)

$P_{L_2} = 98$ KW
$V_{ph_2} = 110.9$ KV
$P_{L_1} = 53$ KW
$V_{ph_1} = 106$ KV

$\frac{98}{53} = \frac{(110.9 - V_d)^2}{(106 - V_d)^2}$

$1.3598(106 - V_d) = \cancel{1.3598}(110.9 - V_d)$

$\cancel{0.3598 V_d} = \cancel{44.80}$

$\cancel{V_d = 124.51}$

$0.3598 V_d = 33.2388$

$\boxed{V_d = 92.38 \text{ KV}}$

Now $\cancel{P_{L_4}}$ let at $V_{ph_3} = 113$ KV, Loss is P_{L_3}

So

$\frac{P_{L_3}}{P_{h_1}} = \left(\frac{V_{ph_3} - V_d}{V_{ph_1} - V_d}\right)^2$

$P_{L_3} = \left(\frac{113 - 92.38}{106 - 92.38}\right)^2 \times 53$

$\boxed{P_{L_3} = 121.47 \text{ KW}}$

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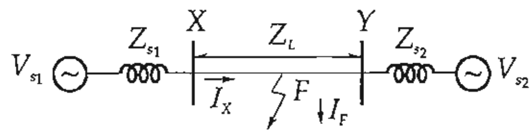
Improve presentation

Q.1 (c) Given that: $V_{s1} = V_{s2} = 1 + j0$ p.u, +ve sequence impedance are:
$Z_{s1} = Z_{s2} = 0.001 + j0.01$ p.u and $Z_L = 0.006 + j0.06$ p.u, 3-ϕ. Base MVA = 100, voltage base = 400 kV($L - L$). Nominal system frequency = 50 Hz.



The reference voltage for phase 'a' is defined as $V(t) = V_m \cos(\omega t)$. A symmetrical 3-$\phi$ fault occurs at centre of the line, i.e. at point 'F' at time 't_0' the +ve sequence impedance from source S_1 to point 'F' equals $(0.004 + j0.04)$ p.u. The wave form corresponding to phase 'a' fault current from bus X reveals that decaying d.c. offset current is -ve and in magnitude at its maximum initial value. Assume that the negative sequence are equal to +ve sequence impedances and the zero sequence impedance (Z) are 3 times +ve sequence (Z). Find the instant (t_0) of the fault.

[12 marks]

Answer

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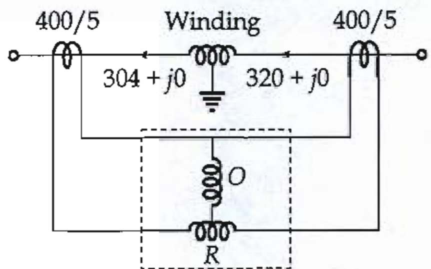
Q.1 (d) The figure given below shows percentage differential relay applied to the protection of an alternator winding. The relay has 0.1 ampere minimum pick-up and 10% slope of characteristic $(I_1 - I_2)$ vs $(I_1 + I_2)/2$. A high-resistance ground fault occurred near the grounded neutral end of generator winding, while the generator is carrying load. As a consequence, the currents in ampere flowing at each end of the winding are shown in the figure. Assume CT ratio of 400/5. Will the relay operate to trip the breaker?



[12 marks]

Answer

given $I_0 = 0.1$ A , $K = 10\%$

Let $I_1 = 304 + j0$, $I_2 = 320 + j0$

So Secondary currents

$i_1 = 304 \times \frac{5}{400}$, $i_2 = 320 \times \frac{5}{400}$

$i_1 = 3.8$ A , $i_2 = 4$ Amp.

Let Restraining coil current i_R

then $i_R = i_2 - i_1$

So $i_R = 4 - 3.8 = 0.2$ Amp.

Now checking for breaker trip or Not, then

$i_R \geq I_0 + K\left(\frac{I_1 + I_2}{2}\right)$

$0.2 \geq 0.1 + 0.1 \times \left(\frac{3.8 + 4}{2}\right)$

$0.2 \geq 0.49$

As above condition is Not ~~fulfilli~~ fulfilled for breaker operation.

$\boxed{\text{So Breaker will Not trip.}}$

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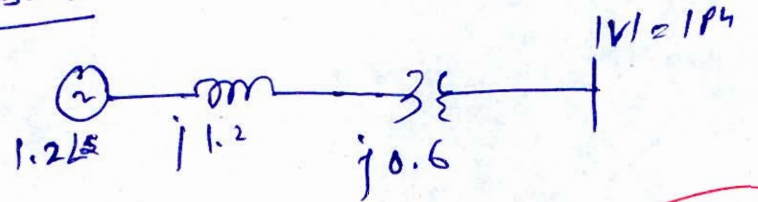
Q.1 (e) A synchronous generator of reactance 1.20 p.u. is connected to an infinite bus bar ($|V| = 1.0$ p.u.) through transformers and a line of total reactance of 0.60 p.u. The generator no-load voltage is 1.20 p.u. and its inertia constant is $H = 4$ MW s/MVA. The resistance and machine damping may be assumed negligible. The system frequency is 50 Hz. Calculate the frequency of natural oscillations if the generator is loaded to 80% of its maximum power limit.

[12 marks]

Answer



$H = 4$ MW-s/MVA
$f = 50$ Hz

given generator is loaded to 80% of Pmax

$0.8\, P_{max} = P_{max} \sin\delta$

$\delta = \sin^{-1}(0.8) = 53.13^\circ$

$P = \frac{EV}{X_T} \sin\delta$

$P = \frac{1.2 \times 1}{1.8} \sin\delta$

So

$\frac{\partial P}{\partial \delta} = \frac{1.2}{1.8} \cos\delta = K$

frequency of oscillation

$f_n = \frac{1}{2\pi}\sqrt{\frac{K}{M}} = \frac{1}{2\pi}\sqrt{\frac{\frac{1.2}{1.8}\cos\delta_0 \Big|_{\delta = 53.13}}{\frac{GH}{\pi f}}}$

$f_n = \frac{1}{2\pi}\sqrt{\frac{0.4}{4} \times}$

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Incomplete Solution

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Q.2 (a) (i) A three-phase, 100 MVA, 25 kV generator has solidly grounded neutral. The positive, negative and the zero sequence reactances of the generator are 0.2 pu, 0.2 pu and 0.05 pu, respectively, at the machine base quantities. If a bolted single phase to ground fault occurs at the terminal of the unloaded, generator. Find the fault current in amperes immediately after the fault.

[10 marks]

Answer

given $X_1 = 0.2$, $X_2 = 0.2$, $X_0 = 0.05$

for Line to ground fault

$$I_{a_1} = \frac{E_1}{X_1 + X_2 + X_0}$$

$E_1 = 1\,pu$ (pre fault voltage)

$$I_{a_1} = \frac{1}{j(0.2 + 0.2 + 0.05)}$$

$I_{a_1} = -j2.22\,pu$ or $|I_{a_1}| = 2.22\,pu$

So fault current

$I_f = 3 I_{a_1} = 3 \times 2.22$

$I_f = 6.67\,pu$

Now Base current $= \dfrac{100 \times 10^6}{\sqrt{3} \times 25 \times 10^3}$

$I_B = 2309.40$ Amp.

So fault current $= 6.67 \times I_B$

$I_f (kA) = 6.67 \times 2309.40$

$$\boxed{I_f = 15.403\ kA}$$

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Good Approach

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Q.2 (a) **(ii)** A generator delivers power of 1.0 p.u. to an infinite bus through a purely reactive network. The maximum power that could be delivered by the generator is 2.0 p.u. A three-phase fault occurs at the terminals of the generator which reduces the generator output to zero. The fault is cleared after t_c second. The original network is then restored. The maximum swing of the rotor angle is found to be δ_{max} = 110 electrical degree. Calculate the rotor angle in electrical degrees at $t = t_c$.

[10 marks]

Answer

given $P_s = 1$ pu.

$P_{max_1} = P_{max_3} = 2$ pu.

As we know

$P_s = P_{max} \sin\delta_0$

$1 = 2 \sin\delta_0$

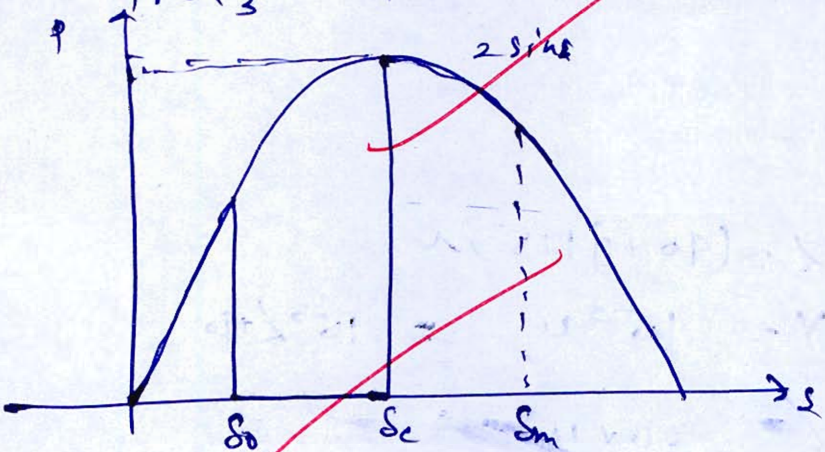
$\boxed{\delta_0 = 30^\circ}$

given $\boxed{\delta_{max} = 110^\circ}$

Let P_{max_1} = Before fault maximum power

P_{max_2} = During fault maximum power

P_{max_3} = After fault maximum power



As we know

$$\delta_c = \cos^{-1}\left[\frac{P_s(\delta_{max}-\delta_0) + P_{max_3}\cos\delta_{max} - P_{max_2}\cos\delta_0}{P_{max_3} - P_{max_2}}\right]$$

As $P_{max_2} = 0$

So

$$\delta_c = \cos^{-1}\left[\frac{1\times(110-30)\times\frac{\pi}{180} + 2\cos 110}{2}\right]$$

$\boxed{\delta_c = 69.16^\circ}$ at $t = t_c$

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(Critical clearing Angle)

Good Approach

Q.2 (b) A 50 Hz, 3 phase transmission line 300 km long has total series impedance of (40 + j125) ohm and a total shunt admittance of 10^{-3} mho. The receiving end load is 50 MW at 220 kV with 0.8 lagging power factor. Calculate the sending end voltage, current, power and power factor using:

(i) Short line approximation.

(ii) Nominal π method.

(iii) Exact transmission line equation of long line.

(iv) Approximation of long line.

[20 marks]

Answer

$$Z = (40 + j125)\,\Omega$$

$$Y = 10^{-3}\ \mho = 10^{-3}\angle +90$$

Now

$$I_R = \frac{50\times10^6}{\sqrt{3}\times 220\times10^3\times0.8}$$

$$I_R = 164\angle -36.86$$

(i) Short line Approximation

— shunt admittance will be Neglected

then

$$V_S = V_{Rph} + I_R \times Z$$

$$V_S = \frac{220\times10^3}{\sqrt{3}} + (164\angle -36.86)(40+j125)$$

$$V_{Sph} = 145.099\ kV \angle 4.928^\circ$$

$$\boxed{V_{SLine} = 251.319\ kV}$$

$$\cos\phi = \cos(4.928 + 36.86)$$

$$\boxed{\cos\phi = 0.745\ \text{Lag.}}\ ,\quad \boxed{I_S = I_R = 164\angle -36.86}$$ Amp.

$$P_{in} = \sqrt{3}\times V_S I_S \cos\phi$$

$$P_{in} = \sqrt{3}\times 251.319\times164\times0.745$$

$$\boxed{P_{in} = 53.228\ MW}$$

(ii) Nominal π-method

$$\begin{pmatrix} V_s \\ I_s \end{pmatrix} = \begin{bmatrix} 1+\frac{YZ}{2} & Z \\ Y\left(1+\frac{YZ}{4}\right) & 1+\frac{YZ}{2} \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

$$A = 1+\frac{YZ}{2} = D = 1+\frac{(40+j125)(j10^{-3})}{2} = 0.937\angle 1.22^\circ$$

$$B = Z = 40+j125 = 131.24\angle 72.25^\circ$$

$$C = Y\left(1+\frac{YZ}{4}\right) = j10^{-3}\left[1+\frac{(40+j125)(j10^{-3})}{4}\right] = 9.68\times10^{-4}\angle 90^\circ$$

So

$$V_s = AV_R + BI_R = 0.937\times\frac{220\times10^3}{\sqrt{3}}\angle 1.22 + 131.24\angle 72.25\times 164\angle -36.86$$

$$V_{s_{ph}} = 137.35\angle 6.289^\circ$$

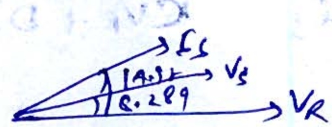
$$\boxed{V_{s\,Line} = 237.89\text{ kV}}$$, ~~$\phi = 6.289 + 36.86$~~

~~$\phi = 43.15^\circ$~~

$$\boxed{\cancel{\cos\phi = \cos 43.15^\circ = 0.7295} \text{ Lag.}}$$

$$I_s = CV_R + DI_R = j9.68\times10^{-4}\times\frac{220\times10^3}{\sqrt{3}} + 0.937\angle 1.22\times 164\angle -36.86$$

$$\boxed{I_s = 129.27\angle -14.97^\circ}\text{ Amp.}$$



$$\cos\phi = \cos(14.97 + 6.289)$$

$$\boxed{\cos\phi = 0.9885 \text{ lead}}$$

$$P_{in} = \sqrt{3}\times 237.89\times 129.27\times 0.9885$$

$$\boxed{P_{in} = 52.65\text{ kW}}$$

(iii) Long line

$$\begin{pmatrix} V_s \\ I_s \end{pmatrix} = \begin{bmatrix} \cosh \gamma l & Z_c \sinh \gamma l \\ \frac{1}{Z_c}\sinh \gamma l & \cosh \gamma l \end{bmatrix}$$

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$A = \cosh \gamma l$

$\gamma l = \sqrt{ZY} = \sqrt{(40 + j125)(j10^{-3})} = 0.3622 \angle 81.125$

$\gamma l = \alpha l + j\beta l = 0.0558 + j0.3578$

$e^{\gamma l} = e^{\alpha l} \angle \beta l^{rad} = e^{0.0558} \angle 0.3578^{rad} = 1.0573 \angle 20.50^\circ$

$e^{-\gamma l} = e^{-\alpha l} \angle -\beta l = e^{-0.0558} \angle -0.3578^{rad} = 0.9457 \angle -20.50$

$\cosh \gamma l = \dfrac{e^{\gamma l} + e^{-\gamma l}}{2} = 0.938 \angle 1.2^\circ$

$\sinh \gamma l = \dfrac{e^{\gamma l} - e^{-\gamma l}}{2} = 0.3546 \angle 81.52^\circ$

$Z_c = \sqrt{\dfrac{Z}{Y}} = \sqrt{\dfrac{131.24 \angle 72.25}{10^{-3} \angle 90}} = 362.27 \angle -8.875^\circ$

So

$V_S = AV_R + BI_R = 0.938 \angle 1.2 \times \dfrac{220 \times 10^3}{\sqrt{3}} + 362.27 \times 0.3546 \angle 81.52 \times 164 \angle -36.86$

~~$V_S =$ 20.824~~ $V_S = 135.32 \angle 7.29^\circ$

$\boxed{V_{S\,Line} = 234.38 \text{ kV}}$

$I_S = CV_R + DI_R = \dfrac{1}{Z_c} \sinh \gamma l \cdot \dfrac{220 \times 10^3}{\sqrt{3}} + 0.938 \angle 1.2 \times 164 \angle -36.86$

$I_S = \dfrac{1}{362.27} \times 0.3546 \angle 81.52 \times \dfrac{220 \times 10^3}{\sqrt{3}} + 0.938 \angle 1.2 \times 164 \times \angle -36.86$

$\boxed{I_S = 147.136 \angle 13.07}$ Amp.

$pf = \cos\phi = \cos(13.07 - 7.29) = 0.9949$ Lead

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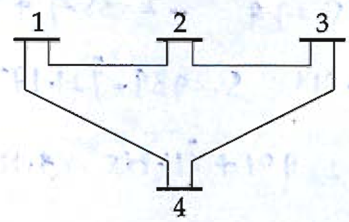
$P_{in} = \sqrt{3} \times 234.38 \times 147.136 \times 0.9949$

$\boxed{P_{in} = 59.426 \text{ MW}}$

Q.2 (c) The figure below shows a four-bus system.



The shunt admittances at the buses are negligible. The line impedances are as under:

Line (bus to bus)	:	1 - 2	2 - 3	3 - 4	4 - 1
R(p.u.)	:	0.025	0.02	0.05	0.04
X(p.u.)	:	0.10	0.08	0.20	0.16

(i) Formulate Y_{bus}.

(ii) Which elements of the Y_{bus} obtained in (i) are affected when a new line from bus 1 to bus 3 is added?

[20 marks]

Answer from above data

$Z_{12} = 0.025 + j0.1 \Rightarrow y_{12} = 2.3529 - j9.412$

$Z_{23} = 0.02 + j0.08 \Rightarrow y_{23} = 2.941 - j11.765$

$Z_{34} = 0.05 + j0.2 \Rightarrow y_{34} = 1.1765 - j4.7058$

$Z_{41} = 0.04 + j0.16 \Rightarrow y_{41} = 1.471 - j5.882$

So $Y_{11} = y_{12} + y_{41} = 3.8234 - j15.294$

$Y_{12} = -y_{12} = -2.3529 + j9.412 = Y_{21}$

$Y_{13} = 0 = Y_{31}$

$Y_{14} = -y_{14} = Y_{41} = -1.471 + j5.882$

$Y_{22} = y_{12} + y_{23} = 5.2939 - j21.177$

$Y_{23} = -y_{23} = -2.941 + j11.765 = Y_{32}$

$Y_{24} = 0 = Y_{42}$

$Y_{33} = y_{23} + y_{34} = 4.1175 - j16.4708$

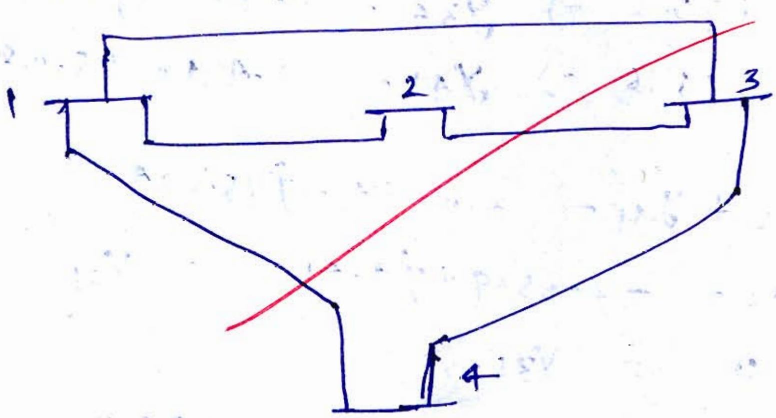
$Y_{34} = -y_{34} = Y_{43} = -1.1765 + j4.7058$

$Y_{44} = y_{41} + y_{34} = 2.6475 - j10.5878$

$$[Y]_{Bus} = \begin{bmatrix} 3.8234-j15.294 & -2.3529+j9.412 & 0 & -1.47+j5.88 \\ -2.3529+j9.412 & 5.2939-j21.177 & -2.941+j11.765 & 0 \\ 0 & -2.941+j11.765 & 4.1175+j16.4708 & -1.1765+j4.7058 \\ -1.47+j5.88 & 0 & -1.765+j4.7508 & 2.6475-j10.5878 \end{bmatrix}$$

$$[Y_{Bus}] = \begin{bmatrix} Y_{11} & Y_{12} & Y_{13} & Y_{14} \\ Y_{21} & Y_{22} & Y_{23} & Y_{24} \\ Y_{31} & Y_{32} & Y_{33} & Y_{34} \\ Y_{41} & Y_{42} & Y_{43} & Y_{44} \end{bmatrix}$$

(ii) Now a New line is added between Bus ① and Bus ③



from above After adding line between bus ① and Bus ③ elements will be affected are given below

Y_{11}, Y_{13}, Y_{31}, Y_{33}

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Good Approach

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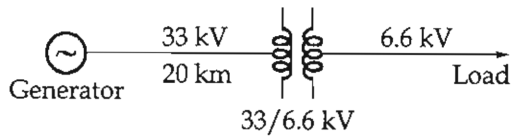
Q.3 (a) (i) A 3-phase load of 2000 kVA, 0.8 power factor is supplied at 6.6 kV, 50 Hz means of a 33 kV transmission line 20 km long and 33/6.6 kV step-down transformer. The resistance and reactance of each conductor are 0.4 Ω and 0.5 Ω per km respectively. The resistance and reactance of transformer primary are 7.5 Ω and 13.2 Ω, while those of secondary are 0.35 Ω and 0.65 Ω respectively. Find the voltage necessary at sending end of transmission line when 6.6 kV is maintained at the receiving end. Determine also the sending end power factor and transmission efficiency.



[15 marks]

Answer given Load 2000 kVA, at 0.8 pf lag.

So $I_L = \dfrac{2000 \times 10^3}{\sqrt{3} \times 6.6 \times 10^3} = 175 \angle{-36.86}$

given for Line $(0.4 + j0.5)$ / km =

$Z_{line} = 8 + j10$

for transformer $Z_1 = 7.5 + j13.2$

$Z_2 = 0.35 + j0.65$

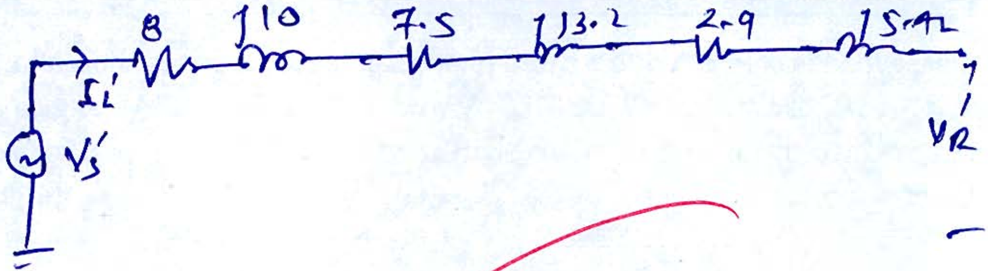
By transferring Z_2 into primary side

$Z_2' = (0.35 + j0.65) \times \left(\dfrac{33/\sqrt{3}}{6.6}\right)^2$

$Z_2' = 2.91 + j5.42$

$I_L' = 175 \angle{-36.86} \times \dfrac{6.6}{33} \times \sqrt{3}$

$I_L' = 60.62 \angle{-36.86}$



$V_S = \frac{33\times10^3}{\sqrt{3}}\angle 0 + I_L' \times (Z_T)$

$V_S = \frac{33\times10^3}{\sqrt{3}}\angle 0 + 60.62\angle -36.86\,[18.4 + j28.62]$

$V_{S_{ph}} = 20.99\angle 1.96'$

$\boxed{V_{S_{Line}} = 36.36\ \text{KV}}$

power factor $= \cos(1.96 + 36.86)$

$= 0.7797$ lag.

Losses $= I_L^2 \times R_T = (60.62)^2[8 + 7.5 + 2.9]$

Losses $= 67616.03$ watt $= 67.616$ KW

$P_{in} = \sqrt{3} \times V_S \times I_L \times \cos\theta = \sqrt{3} \times 36.36 \times 60.62 \times 0.7797$

$P_{in} = 2976.65$ KW

% efficiency $= \frac{P_{in} - \text{Losses}}{P_{in}}$

7

$= \frac{2909 \times \cancel{0.8}}{2976.65} \times 100$

$= 97.72$ %

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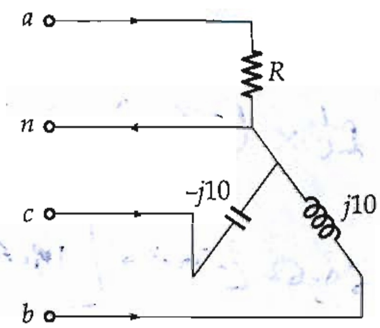
Q.3 (a) (ii) A three-phase load is connected to a three-phase balanced supply as shown in the figure. If $V_{an} = 100\angle 0°$ V, $V_{bn} = 100\angle -120°$ V and $V_{cn} = 100\angle -240°$ V (angles are considered positive in the anti-clockwise direction), find the value of R for zero current in the neutral wire.



[5 marks]

Answer

As $I_n = 0$

So $\Rightarrow I_a + I_b + I_c = 0$

$$\frac{V_{an}}{R} + \frac{V_{bn}}{j10} + \frac{V_{cn}}{-j10} = 0$$

$$\frac{100\angle 0}{R} + \frac{100\angle -120}{10\angle 90} + \frac{100\angle -240}{10\angle -90} = 0$$

$$\frac{100\angle 0}{R} = 17.32$$

$$\boxed{R = 5.77\,\Omega}$$

Good Approach

5

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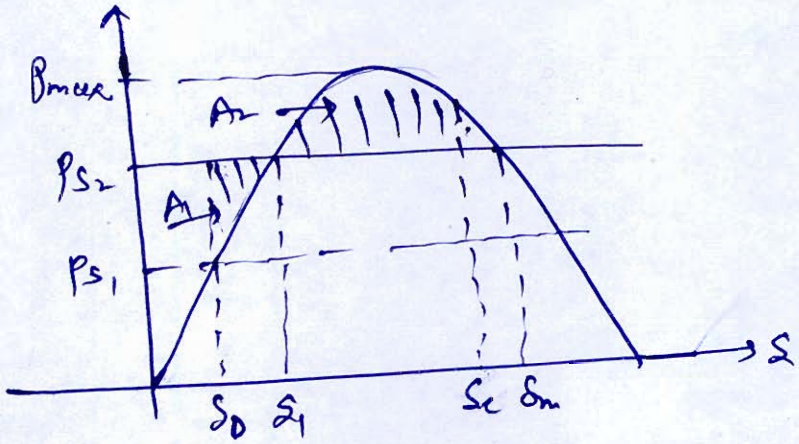
Q.3 (b) (i) Derive an expression for the critical clearing angle for a power system consisting of a single machine supplying to an infinite bus, for a sudden load increment.

[10 marks]

Answer

for sudden load increment



from Equal Area Criteria

As P_{s_1} is shaft load at starting and P_{s_2} is load after sudden increment.

So

$$\int_{\delta_0}^{\delta_1} A_1\, d\delta = \int_{\delta_1}^{\delta_c} A_2\, d\delta$$

$$\int_{\delta_0}^{\delta_1} (P_{s_2} - P_{max}\sin\delta)\, d\delta = \int_{\delta_1}^{\delta_c} (P_{max}\sin\delta - P_{s_2})\, d\delta.$$

$$P_{s_2}(\delta_1 - \delta_0) + P_{max}[\cos\delta_1 - \cos\delta_0] = P_{max}[-\cos\delta_c + \cos\delta_1] - P_{s_2}[\delta_c - \delta_1]$$

$$\boxed{P_{max}\cos\delta_c + P_{s_2}\delta_c = P_{s_2}[\delta_0] + P_{max}\cos\delta_0}$$

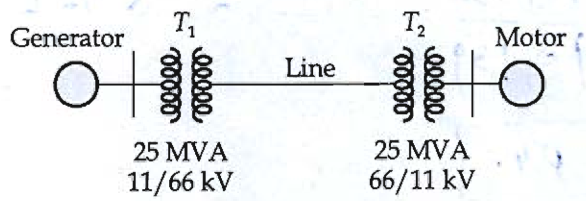
from above equation we can calculate δ_c by using trancedental equation solving method.

3

Incomplete solution

Do not write in this margin

Q.3 (b) (ii) A synchronous generator and a synchronous motor each rated 25 MVA, 11 kV having 15% subtransient reactance are connected through transformers and a line as shown in the figure below. The transformers are rated 25 MVA, 11/66 kV and 25 MVA, 66/11 kV with leakage reactance of 10% each. The line has a leakage reactance of 10% on a base of 25 MVA, 66 kV. The motor is drawing 15 MW at 0.8 power factor leading and a terminal voltage of 10.6 kV when a symmetrical 3-phase fault occurs at the motor terminals. Find the subtransient current in the generator, motor and fault.



[10 marks]

Answer Base: 25 MVA, 11 kV

Motor Load ⇒ 15 MW at 0.8 pf, 10.6 kV

$P_L = \frac{15}{25} = 0.6$ pu

So and $V_M = \frac{10.6}{11} = 0.9636$ pu.

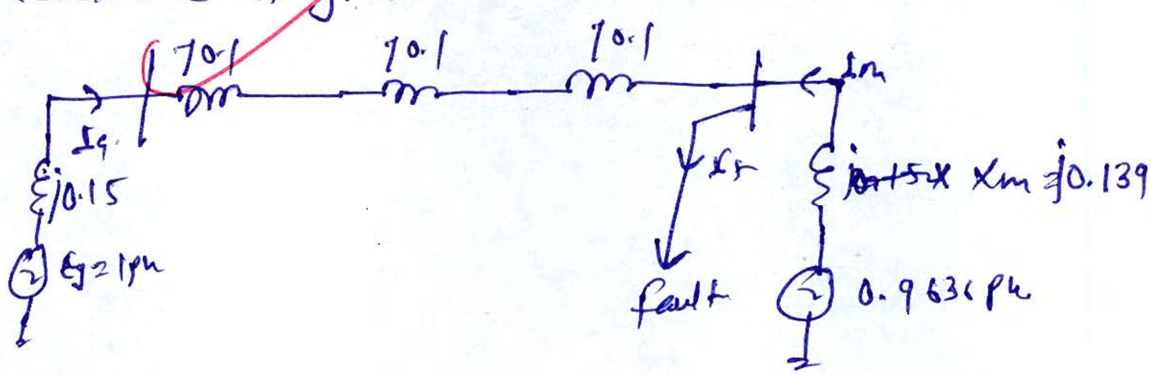
As $P = VI\cos\phi$

$0.6 = 0.9636 \times I \times 0.8$

$I = 0.7783 \angle 36.86$

So $Z_{Load} = \frac{V}{I} = \frac{0.9636\angle 0}{0.7783\angle 36.86} = 0.9905 - j0.7428$

Reactance diagram



$X_m = 0.15 \times \left(\frac{10.6}{11}\right)^2 = 0.139$ pu

$$I_g = \frac{1}{j0.15 + j0.1 + j0.1 + j0.1} = 2.22\angle{-90^\circ}$$

$$\boxed{I_g = 2.22 \text{ pu}}$$

$$I_m = \frac{0.9636}{j0.139} = 6.93\angle{-90^\circ}$$

$$\boxed{I_m = 6.93 \text{ pu.}}$$

$$I_f = \bar{I}_m + \bar{I}_g$$

$$\boxed{I_f = 9.15 \text{ pu}}$$

So

$$I_g = 2.22 \times \frac{25 \times 10^6}{\sqrt{3} \times 11 \times 10^3}$$

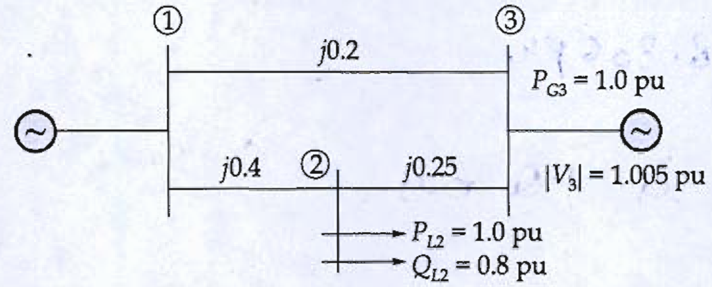
$$\boxed{I_g = 2.912 \text{ KA}}$$

$$I_m = 6.93 \times \frac{25 \times 10^6}{\sqrt{3} \times 10.6 \times 10^3}$$

$$\boxed{I_m = 9.436 \text{ KA}}$$

6

Q.3 (c) For the power system network shown in figure, compute the bus voltages using the Gauss-Seidel iteration method. Line reactances and loads are shown in figure. Bus-1 is the slack bus ($V_1 = 1.04\angle 0°$) and bus-2 and bus-3 are the load and voltage-control buses respectively. Assume tolerance equal to 1×10^{-5}.



Compute V_1, V_2 and V_3 upto one iteration.

[20 marks]

Answer

given $Z_{13} = j0.2 \Rightarrow Y_{13} = -j5$

$Z_{12} = j0.4 \Rightarrow Y_{12} = -j2.5$

$Z_{23} = j0.25 \Rightarrow Y_{23} = -j4$

$$Y_{Bus} = \begin{bmatrix} -j7.5 & j2.5 & j5 \\ j2.5 & -j6.5 & j4 \\ j5 & j4 & -j9 \end{bmatrix}$$

given $V_1 = 1.04\angle 0°$, $V_3 = 1.005$

Let $V_2 = 1$ pu, $\delta_2 = \delta_3 = 0$

Also given $P_{G3} = P_{i3} = 1$ pu

As Bus-3 is PV Bus. So we have to calculate Q at Bus ③

$$Q_3 = -\sum_{k=1}^{3} |Y_{3k}||V_3||V_k| \sin(\theta_{3k} + \delta_k - \delta_3)$$

$$Q_3 = -\Big[|Y_{31}||V_3||V_1| \sin(\theta_{31} + \delta_1 - \delta_3) + |Y_{32}||V_3||V_2| \sin(\theta_{32} + \delta_2 - \delta_3) + |Y_{33}||V_3||V_3| \sin(\theta_{33} + \delta_3 - \delta_3) \Big]$$

$$Q_3 = -\left[5\times 1.005\times 1.04\ \sin(90) + 4\times 1.005\times 1\ \sin(90) + 9\times 1.005\times 1.005\times \sin 90\right]$$

$$Q_3 = -18.336\ pu$$

As Bus-② is PQ Bus.
So

$$P_2 = P_{g2} - P_{L2} = 0 - 1 = -1\ pu$$

$$Q_2 = Q_{g2} - Q_{L} = 0 - 0.8 = -0.8\ pu$$

So Now Using Gauss Seidal method

$$V_2' = \frac{1}{Y_{22}}\left[\frac{P_2 - jQ_2}{V_2^{0*}} - \left[Y_{21} V_1^0 + Y_{23} V_3^0\right]\right]$$

$$V_2' = \frac{1}{-j16.5}\left[\frac{-1+j0.8}{(1\angle 0)^*} - \left[j12.5\times 1.04 + j4\times 1.005\right]\right]$$

$$\boxed{V_2' = 0.9085\angle -9.749}$$

$$\boxed{V_2' = 0.9085\ pu}\ ,\ \boxed{V_1 = 1.04}$$

Go Through the made easy Solution

15

Q.4 (a) (i) The insulation resistance of a single-core cable is 495 MΩ per km. If the core diameter is 2.5 cm and resistivity of insulation is 4.5×10^{14} Ω-cm. Find the insulation thickness.

[10 marks]

Q.4 (a) (ii) A 3-phase, 2-pole, 50 Hz, synchronous generator has a rating of 250 MVA, 0.8 pf lagging. The kinetic energy of the machine at synchronous speed is 1000 MJ. The machine is running steadily at synchronous speed and delivering 60 MW power at a power angle of 10 electrical degrees. If the load is suddenly removed, assuming the acceleration is constant for 10 cycles, find the value of the power angle after 5 cycles in electrical degrees.

[10 marks]

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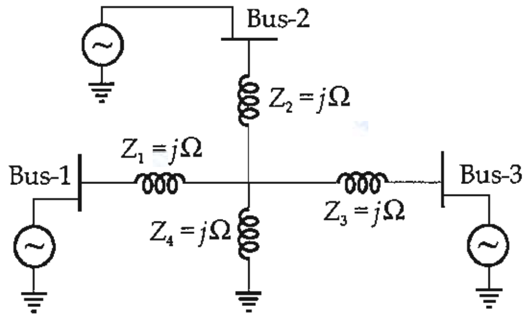
Q.4 (b) (i) What is the effect of fault impedance on the performance of distance protection? Suggest a method for overcoming this effect.

[14 marks]

Q.4 (b) (ii) A 3 Bus network is shown below. Consider generators as an ideal voltage sources. If rows 1, 2 and 3 of the Y_{Bus} matrix correspond to Bus 1, 2 and 3 respectively, find Y_{Bus} of the network shown.



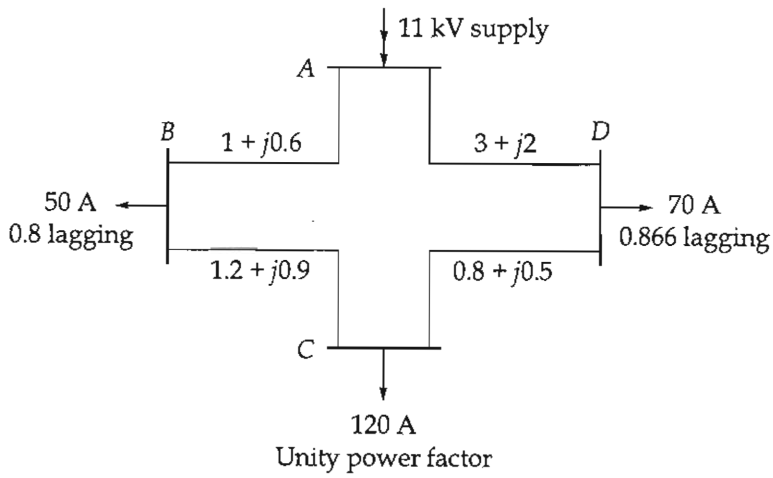
[6 marks]

Q.4 (c) A 3-phase ring main *ABCD* fed at *A* at 11 kV supplies balanced loads of 50 A at 0.8 p.f. lagging at *B*. 120 A at unity power factor at *C* and 70 A at 0.866 lagging at *D*, the load currents being referred to the supply voltage at *A*. The impedances of the various sections are:

Section $AB = (1 + j0.6)\Omega$; Section $BC = (1.2 + j0.9)\Omega$

Section $CD = (0.8 + j0.5)\Omega$; Section $BC = (1.2 + j0.9)\Omega$

Calculate the currents in various sections and station bus-bar voltages at *B*, *C* and *D*.



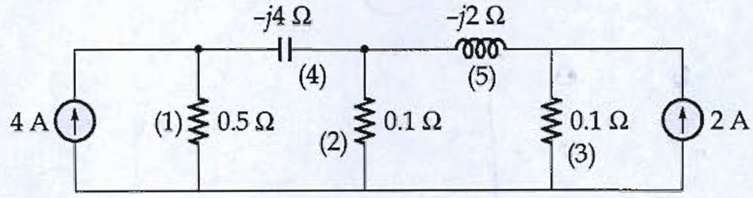
[20 marks]

Section B : Digital Electronics-1 + Microprocessor-1 + Electrical Circuits-2 + Systems and Signal Processing -2

Q.5 (a) For the circuit diagram shown below, draw its graph and

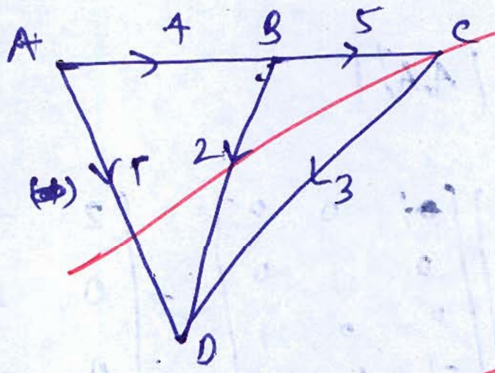
(i) Obtain incidence matrix and cut-set matrix.

(ii) How many trees are possible for this circuit?



[12 marks]

Answer graph of above Network.



[Note! current source will be act as open circuit]

Let Nodes are A, B, C, D

(i) Incidence Matrix

$$
\begin{array}{c} \\ A \\ B \\ C \\ D \end{array}
\begin{array}{c}
\begin{array}{ccccc} 1 & 2 & 3 & 4 & 5 \end{array} \\
\begin{bmatrix} -1 & 0 & 0 & -1 & 0 \\ 0 & -1 & 0 & 1 & -1 \\ 0 & 0 & -1 & 0 & 1 \\ 1 & 1 & 1 & 0 & 0 \end{bmatrix}
\end{array}
$$

Note: for outward $= -1$

for incoming $= +1$

(ii) Reduced Incidence matrix

$$A_r = \begin{bmatrix} -1 & 0 & 0 & -1 & 0 \\ 0 & -1 & 0 & 1 & -1 \\ 0 & 0 & -1 & 0 & 1 \end{bmatrix}$$

$$A_r^T = \begin{bmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \\ -1 & 1 & 0 \\ 0 & -1 & 1 \end{bmatrix}$$

Number of trees $= |A_r A_r^T|$

$$= \begin{bmatrix} -1 & 0 & 0 & -1 & 0 \\ 0 & -1 & 0 & 0 & -1 \\ 0 & 0 & -1 & 0 & 1 \end{bmatrix}_{3\times5} \begin{bmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \\ -1 & 1 & 0 \\ 0 & -1 & 1 \end{bmatrix}_{5\times3} = \begin{bmatrix} 2 & -1 & 0 \\ 0 & 2 & -1 \\ 0 & -1 & 2 \end{bmatrix}$$

$$|A_r A_r^T| = 2[4-1] + 1[0] + 0$$

$$= 6$$

So possible No. of trees $= 6$

3

GO Through the made easy solution

Q.5 (b) Find the z-transform $X(z)$ and sketch the pole-zero plot with the ROC for each of the following sequences :

(i) $x[n] = \left(\frac{1}{2}\right)^n u[n] + \left(\frac{1}{3}\right)^n u[n]$.

(ii) $x[n] = \left(\frac{1}{3}\right)^n u[n] + \left(\frac{1}{2}\right)^n u[-n-1]$.

(iii) $x[n] = \left(\frac{1}{2}\right)^n u[n] + \left(\frac{1}{3}\right)^n u[-n-1]$.

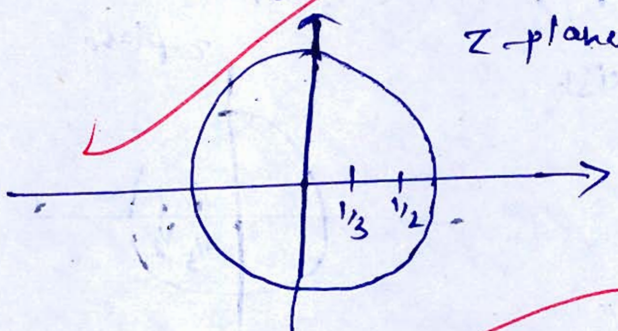
[12 marks]

Answer (i)

$$x(n) = \left(\frac{1}{2}\right)^n u(n) + \left(\frac{1}{3}\right)^n u(n)$$

By taking z-transform

$$X(z) = \frac{1}{1-\frac{1}{2}z^{-1}} + \frac{1}{1-\frac{1}{3}z^{-1}} \quad ; \text{ROC} : |z| > 1/2$$



$z = re^{j\omega}$

Note: $a^n u(n) \overset{Z.T.}{\rightleftharpoons} \frac{1}{1-az^{-1}}$; ROC $|z| > a$

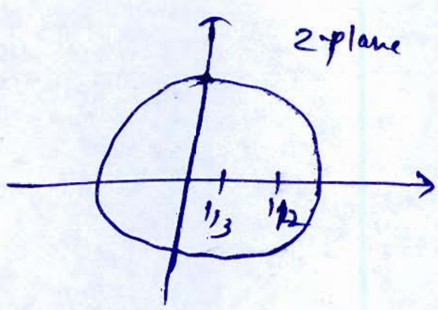
(ii) $x(n) = \left(\frac{1}{3}\right)^n u(n) + \left(\frac{1}{2}\right)^n u(-n-1)$

$$x(n) = \left(\frac{1}{3}\right)^n u(n) - \left[-\left(\frac{1}{2}\right)^n u(-n-1)\right]$$

By taking Z-transform

$$X(z) = \frac{1}{1-\frac{1}{3}z^{-1}} - \frac{1}{1-\frac{1}{2}z^{-1}}$$

ROC: $\frac{1}{3} < |z| < 1/2$



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(iii) $x(n) = \left(\frac{1}{2}\right)^n u(n) + \left(\frac{1}{3}\right)^n u(-n-1)$

$x(n) = \left(\frac{1}{2}\right)^n u(n) - \left[-\left(\frac{1}{3}\right)^n u(-n-1)\right]$

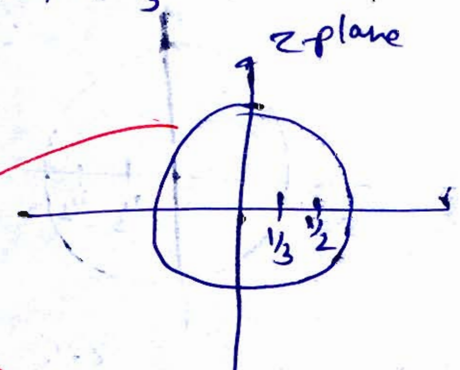
Note: $-(a)^n u(-n-1) \xrightleftharpoons{Z.T.} \frac{1}{1-az^{-1}}$; ROC : $|z| < |a|$

So By taking z-transform from above signal

$$X(z) = \frac{1}{1-\frac{1}{2}z^{-1}} - \frac{1}{1-\frac{1}{3}z^{-1}}$$

ROC: $|z| > 1/2 \cap |z| < 1/3$

ROC : Does not exist



8

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Q.5 (c) $y(n+2)-\frac{3}{4}y(n+1)+\frac{1}{8}y(n) = x(n+2)+x(n+1).$

Solve the above difference equation using z-transform if it is given that $y(-1)=0$, $y(-2)=-1$ and input is $x(n)=u(n)$ and calculate zero input response and zero state response separately.

[12 marks]

Answer

Zero state Response.

$$y(n+2) - \frac{3}{4}y(n+1) + \frac{1}{8}y(n) = x(n+2) + x(n+1)$$

By taking z-transform

$$z^2 Y(z) - \frac{3}{4}z Y(z) + \frac{1}{8}Y(z) = z^2 X(z) + z X(z)$$

$$\frac{Y(z)}{X(z)} = \frac{z^2+z}{z^2 - 3/4 z + 1/8}$$

given $x(n) = u(n)$

$$X(z) = \frac{1}{1-z^{-1}} = \frac{z}{z-1}$$

from Above

$$Y(z) = \frac{z(z^2+z)}{(z-1)(z^2 - \frac{3}{4}z + 1/8)}$$

$$\frac{Y(z)}{z} = \frac{z^2+z}{(z-1)(z-1/2)(z-1/4)} = \frac{A}{z-1/4} + \frac{B}{z-1/2} + \frac{C}{z-1}$$

$$Y(z) = \frac{5/3}{1-\frac{1}{4}z^{-1}} - \frac{6}{1-\frac{1}{2}z^{-1}} + \frac{8/3}{1-z^{-1}}$$

By taking Inverse z-transform

$$\boxed{y(n) = \left[\frac{5}{3}\left(\frac{1}{4}\right)^n - 6\cdot\left(\frac{1}{2}\right)^n + 8/3\right]u(n)} \quad ZSR$$

Do not write in this margin

Zero Input Response

$$y(n+2) - \frac{3}{4}y(n+1) + \frac{1}{8}y(n) = 0$$

By taking z-transform

$$z^2Y(z) - z^2y(-1) - zy(-2) - \frac{3}{4}\left[zY(z) - zy(-1)\right] + \frac{1}{8}Y(z) = 0$$

$$z^2Y(z) - 0 - z(-1) - \frac{3}{4}\left[zY(z)\right] + \frac{1}{8}Y(z) = 0$$

$$Y(z)\left[z^2 - \frac{3}{4}z + \frac{1}{8}\right] = -z$$

$$\frac{Y(z)}{z} = \frac{-1}{(z-1/2)(z-1/4)} = \frac{A}{z-1/4} + \frac{B}{z-1/2}$$

$$Y(z) = \frac{4}{1-\frac{1}{4}z^{-1}} + \frac{-4}{1-\frac{1}{2}z^{-1}}$$

By taking Inverse z-transform

$$\boxed{y(n) = 4\left[\left(\frac{1}{4}\right)^n u(n) - \left(\frac{1}{2}\right)^n u(n)\right]}$$

ZIR

4

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Q.5 (d) Specify the truth table of an octal to binary priority encoder. Provide an output V to indicate that atleast one of the inputs is present. The input with highest subscript number has the highest priority. What will be the values of four outputs if inputs D_2 and D_6 are 1 at the same time?

[12 marks]

Answer 8 to 2 priority encoder

Truth table

Y_7	Y_6	Y_5	Y_4	Y_3	Y_2	Y_1	Y_0	A	B	V
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	1	0	0	0
0	0	0	0	0	0	1	0	0	0	[illegible]
0	0	0	0	0	1	0	0	0	1	0
0	0	0	0	1	0	0	0	0	[illegible]	[illegible]
0	0	0	1	0	0	0	0	1	0	0
0	0	1	0	0	0	0	0	1	0	[illegible]
0	1	0	0	0	0	0	0	1	1	0
1	0	0	0	0	0	0	0	1	1	1

2

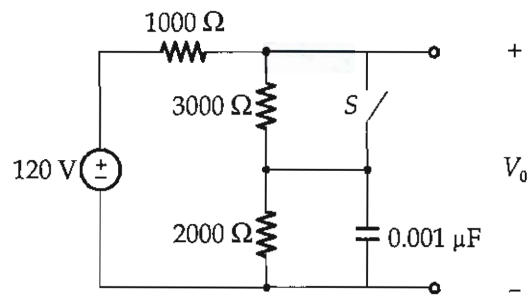
Incomplete solution

Do not write in this margi

Q.5 (e) Set of three 8-bit data readings are stored in memory starting at XX50 H. Sort the readings in ascending order using assembly level program on an 8085 microprocessor.

[12 marks]

Q.6 (a) In the network of figure below, the switch S has been closed for a long time. The switch is suddenly opened at $t = 0$ and reclosed at $t = 20$ μs. Find the expression for the voltage V_0 for $t \leq 20$ μs and $t > 20$ μs.



[20 marks]

Q.6 (b) The instruction code 0100 1111 (4FH) is stored in memory location 2005H. Illustrate the data flow and list the sequence of events when the instruction code is fetched by the 8085 microprocessor.

[20 marks]

Q.6 (c) (i) Implement the following Boolean function with a 4 × 1 multiplexer and external gates :

$$F(A, B, C, D) = \Sigma(1, 3, 4, 11, 12, 13, 14, 15)$$

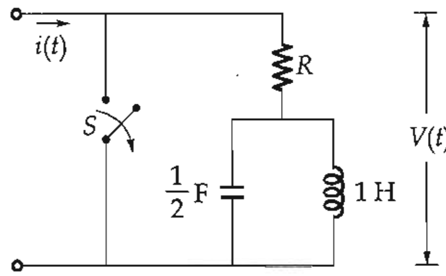
Connect inputs A and B to the selection lines. The input requirements for the four data lines will be a function of variables C and D. These values are obtained by expressing F as a function of C and D for each of the four cases when AB equals 00, 01, 10 and 11. This function may have to be implemented with external gates.

[12 marks]

.6 (c) **(ii)** Write an assembly language program to obtain 2's complement of a 16-bit number.

[8 marks]

Q.7 (a) The circuit shown below has zero initial energy. At $t = 0$, the switch 'S' is opened. Find the value of resistor R for the given excitation such that the response is $V(t) = 0.5\sin\sqrt{2}t\,u(t)$.



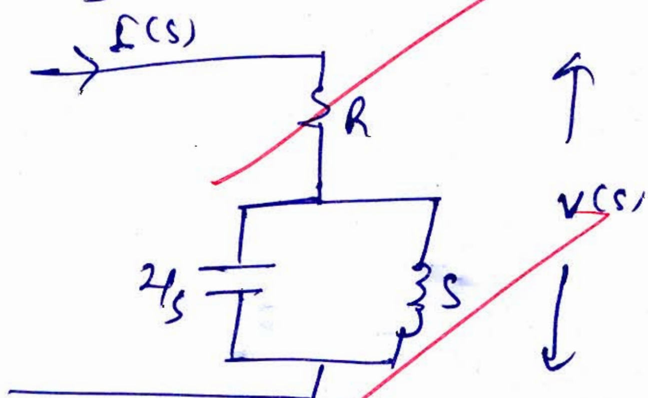
The excitation is $i(t) = te^{-\sqrt{2}t}\,u(t)$.

[20 marks]

Answer $\quad i(t) = t e^{-\sqrt{2}t} u(t)$

At $t = 0^-$ $\Rightarrow i(t) = 0$

By using Laplace transform At $t > 0$



$$V(s) = I(s)\left\{R + \frac{s \times 2/s}{s + 2/s}\right\} = I(s)\left[R + \frac{2s}{s^2+2}\right]$$

$$V(s) = I(s)\cdot\left[\frac{s^2R + 2R + 2s}{s^2+2}\right] \quad \text{—— (1)}$$

Now

$$v(t) = 0.5 \sin\sqrt{2}t\, u(t)$$

So By Laplace transform

$$V(s) = \frac{0.5 \times \sqrt{2}}{s^2 + 2} \quad \text{—— (2)}$$

And $i(t) = t e^{-\sqrt{2}t} u(t)$

as $e^{-\sqrt{2}t} u(t) \longrightarrow \frac{1}{s+\sqrt{2}} = X(s)$

and $t e^{-\sqrt{2}t} u(t) \longrightarrow -\frac{d}{ds} X(s) = -\frac{[-1]}{(s+\sqrt{2})^2}$

$I(s) = \frac{1}{s^2 + 2\sqrt{2}s + 2}$ —— (3)

from (1) (2) and (3)

$$\frac{0.5\sqrt{2}}{s^2+2} = \frac{1}{(s+\sqrt{2})^2}\left[\frac{s^2 R + 2R + 2s}{s^2+2}\right]$$

$$(s^2 + 2\sqrt{2}s + 2)\frac{1}{\sqrt{2}} = Rs^2 + 2R + 2s$$

$$\frac{1}{\sqrt{2}}s^2 + 2s + 2/\sqrt{2} = s^2 R + 2R + 2s$$

By comparing

$$\boxed{R = 1/\sqrt{2} = 0.707\ \Omega}$$

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Good Approach

Q.7 (b) (i) For the second order FIR lattice filter with reflection coefficients $K_1 = \frac{1}{2}$, $K_2 = \frac{1}{4}$, find the FIR system.

(ii) Obtain a lattice filter implementation of the FIR filter $H(z) = 8 + 4z^{-1} + 2z^{-2} + z^{-3}$.

[10 + 10 marks]

Answer (i) given $K_1 = \frac{1}{2}$, $K_2 = \frac{1}{4}$

Let $A_0(z) = B_0(z) = 1$

then $A_1(z) = A_0(z) + K_1 B_0(z) \cdot z^{-1}$

$A_1(z) = 1 + \frac{1}{2}z^{-1}$

So $B_1(z) =$ Rerverse of $A_1(z)$

$B_1(z) = \frac{1}{2} + z^{-1}$

Now

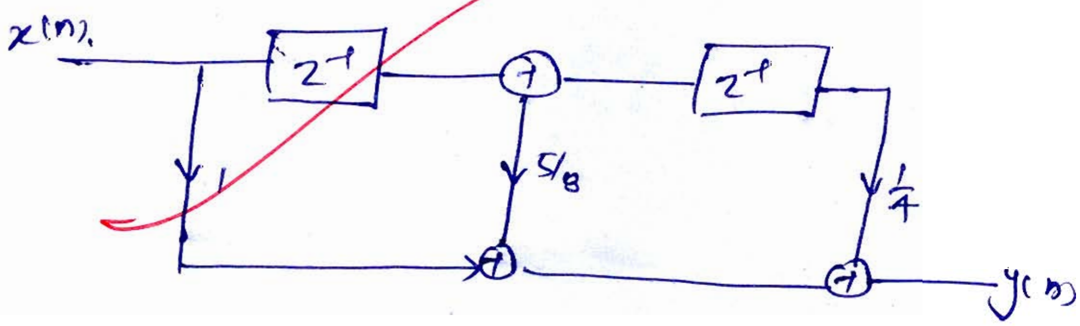
$A_2(z) = A_1(z) + K_2 z^{-1} B_1(z)$

$A_2(z) = \left(1 + \frac{1}{2}z^{-1}\right) + \frac{1}{4}z^{-1}\left[\frac{1}{2} + z^{-1}\right]$

$A_2(z) = 1 + \frac{1}{2}z^{-1} + \frac{1}{8}z^{-1} + \frac{1}{4}z^{-2}$

$\boxed{A_2(z) = 1 + \frac{5}{8}z^{-1} + \frac{1}{4}z^{-2}} = H(z)$

Direct form of above filter



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(ii) given

$$H(z) = 8 + 4z^{-1} + 2z^{-2} + z^{-3}$$

By taking coefficient of z^0 as 1. then

$$H(z) = 1 + \frac{1}{2}z^{-1} + \frac{1}{4}z^{-2} + \frac{1}{8}z^{-3}$$

So from above $\boxed{K_3 = 1/8}$

Now

$$A_3(z) = 1 + \frac{1}{2}z^{-1} + \frac{1}{4}z^{-2} + \frac{1}{8}z^{-3}$$

then

$$B_3(z) = \frac{1}{8} + \frac{1}{4}z^{-1} + \frac{1}{2}z^{-2} + z^{-3}$$

So

$$A_2(z) = \frac{A_3(z) - K_3 B_3(z)}{1 - K_3^2}$$

$$A_2(z) = \frac{\left(1 + \frac{1}{2}z^{-1} + \frac{1}{4}z^{-2} + \frac{1}{8}z^{-3}\right) - \frac{1}{8}\left[\frac{1}{8} + \frac{1}{4}z^{-1} + \frac{1}{2}z^{-2} + z^{-3}\right]}{1 - (1/8)^2}$$

$$A_2(z) = 1 + \frac{10}{21}z^{-1} + \frac{4}{21}z^{-2}$$

So $\boxed{K_2 = \frac{4}{21}}$

Now

$$B_2(z) = \frac{4}{21} + \frac{10}{21}z^{-1} + z^{-2}$$

then

$$A_1(z) = \frac{A_2(z) - K_2 B_2(z)}{1 - K_2^2}$$

$$A_1(z) = \frac{\left(1 + \frac{10}{21}z^{-1} + \frac{4}{21}z^{-2}\right) - \frac{4}{21}\left(\frac{4}{21} + \frac{10}{21}z^{-1} + z^{-2}\right)}{1 - \left(\frac{4}{21}\right)^2}$$

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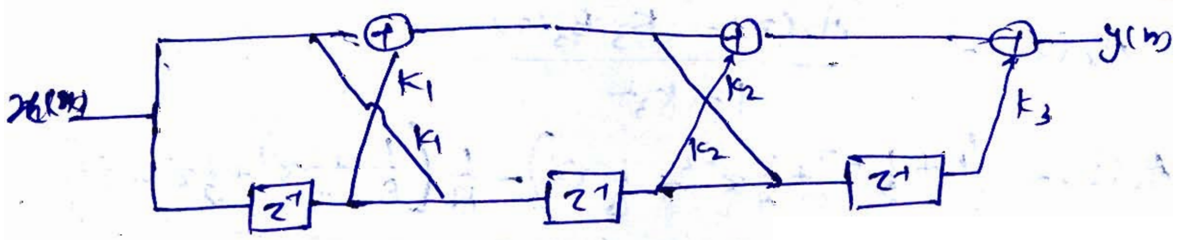
$A_1(z) = 1 + \frac{2}{5} z^{-1}$

So $\boxed{K_1 = 2/5}$

So $\boxed{K_1 = 2/5, \quad K_2 = \frac{4}{21}, \quad K_3 = 1/8}$

Lattice filter Implementation will be



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Incomplete solution

Q.7 (c) Design a synchronous 3-bit gray code up-counter using J-K flip-flop.

[20 marks]

Answer

Gray code up counter sequence will be like

0 — 1 — 3 — 2 — 6 — 7 — 5 — 4

000 — 001 — 011 — 010 — 110 — 111 — 101 — 100

So Using J-K flip flop

	Present state			Next state			Output					
	Q_2	Q_1	Q_0	Q_2	Q_1	Q_0	J_2	K_2	J_1	K_1	J_0	K_0
0	0	0	0	0	0	1	0	X	0	X	1	X
1	0	0	1	0	1	1	0	X	1	X	X	0
3	0	1	1	0	1	0	0	X	X	0	X	1
2	0	1	0	1	1	0	1	X	X	0	0	X
6	1	1	0	1	1	1	X	0	X	0	1	X
7	1	1	1	1	0	1	X	0	X	1	X	0
5	1	0	1	1	0	0	X	0	0	X	X	1
4	1	0	0	0	0	0	X	1	0	X	0	X

Note: Excitation table of J-K flip flop

Q_{n+1}	Q_n	J	K
0	0	0	X
0	1	1	X
1	0	X	1
1	1	X	0

So

$J_2 = \Sigma m(2) + d(6, 7, 5, 4)$, $K_2 = \Sigma m(4) + d(0, 1, 2, 3)$

$Q_2 \backslash Q_1Q_0$	00	01	11	10
0				1
1	X	X	X	X

$J_2 = Q_1\bar{Q_0}$

$Q_2 \backslash Q_1Q_0$	00	01	11	10
0	X	X	X	X
1	1			

$K_2 = \bar{Q_1}\bar{Q_0}$

$J_1 = \Sigma m(1) + d(3,2,6,7)$

$Q_2 \backslash Q_1Q_0$	00	01	11	10
0		1	X	X
1			X	X

$J_1 = \bar{Q}_2 Q_0$

$K_1 = \Sigma m(7) + d(0,1,4,5)$

$Q_2 \backslash Q_1Q_0$	00	01	11	10
0	X	X		
1	X	X	1	

$K_1 = Q_2 Q_0$

$J_0 = \Sigma m(0,6) + d(1,3,5,7)$

$Q_2 \backslash Q_1Q_0$	00	01	11	10
0	1	X	X	
1		X	X	1

$J_0 = \bar{Q}_2 \bar{Q}_1 + Q_2 Q_1$

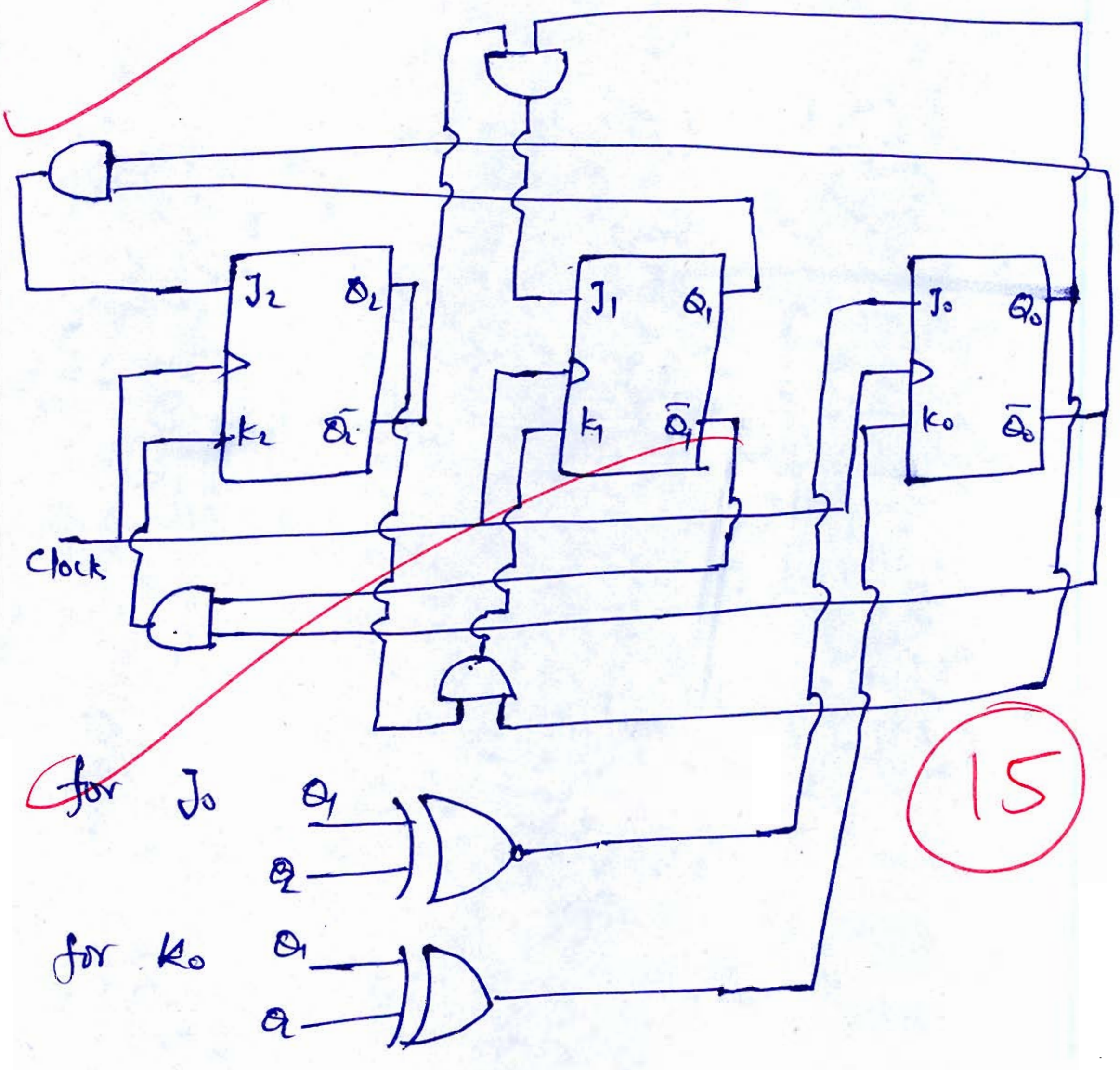
$J_0 = Q_2 \odot Q_1$

$K_0 = \Sigma m(3,5) + d(0,2,6,4)$

$Q_2 \backslash Q_1Q_0$	00	01	11	10
0	X		1	X
1	X	1		X

$K_0 = Q_2 \bar{Q}_1 + \bar{Q}_2 Q_1$

$K_0 = Q_2 \oplus Q_1$



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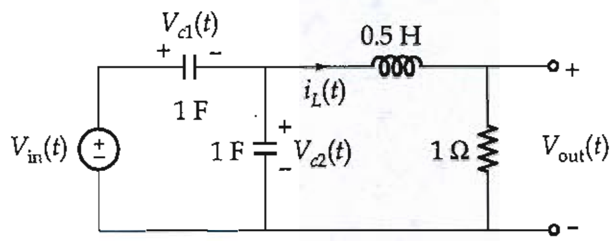
Q.8 (a) Design a sequential circuit with two J-K flip-flops A and B and two inputs E and F. If $E = 0$, the circuit remains in the same state regardless of the value of F. When $E = 1$ and $F = 1$, the circuit goes through the state transitions from 00 to 01, to 10, to 11, back to 00, and repeat. When $E = 1$ and $F = 0$, the circuit goes through its state transitions from 00 to 11, to 10, to 01, to 00, and repeats.

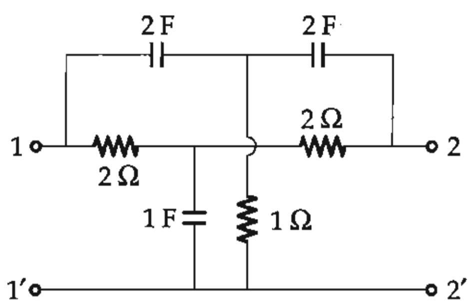
[20 marks]

Q.8 (b) (i) Consider the circuit below in which $V_{in}(t) = 5u(t)$ V, $V_{c1}(0^-) = 3$ V, $V_{c2}(0^-) = 0$ V and $i_L(0^-) = 2$ A. Find $V_{out}(t)$ and also obtain V_{out} at $t = 1$ sec.



[10 marks]

(b) (ii) Determine the Y-parameters of given network.



[10 marks]

3 (c) A sequential circuit has two J-K flip-flops A and B, two inputs x and y, and one output z. The flip-flop input equations and circuit output equation are:

$J_A = \bar{A}Bx$; $K_A = A + Bx\bar{y}$; $J_B = B\bar{x} + y$; $K_B = \bar{B}\bar{y}$; $Z = Axy + B\bar{x}\,\bar{y}$

(i) Draw the logic diagram of the circuit.

(ii) Tabulate the state table.

(iii) Derive the state equations for A and B.

[20 marks]

0000

Space for Rough Work

Space for Rough Work

Space for Rough Work

	00	01	11	10
0	0	1	3	2
1	4	5	7	6

0 1 3 2 6, 7, 5, 4

$A(1-\frac{1}{2}) + B(1-\frac{1}{4}) = -1$

$-\frac{1}{4}A = -1$ | $B\cdot\frac{1}{4} = -1$

$\boxed{A = 4}$ | $B = -4$

$A(2-\frac{1}{2}) + B(2-\frac{1}{4}) = -1$ $\quad \frac{1}{4}B = -\frac{1}{2}$ $\quad \boxed{B = -2}$

$A\,\frac{1}{4}$ | $B\,\frac{1}{4} = -1$

$\boxed{A = -4}$ | $B = 4$

$A(1-\frac{1}{2}) + B(1-\frac{1}{4}) = -2$

$-\frac{1}{4}A = -1/4$ $\quad \boxed{A = 1}$

$y(n+2) = z^2 y(z) - z^2 y(-1) - z y(-2)$

$y(n+1) = z^{-1} y(z) + y(0)$

$y(n-1) = z^{-1} y(z) + z^{-1} y(0) + y(-1)$

$y(n-2) = z^{-2} y(z) + \ldots$

$Q_i = \sum Y_{ik} V_k V_i \sin(\delta_{ik} + \delta_k - \delta_i)$

$Q_3 = \sum_{k=1}^{3} Y_{3k} V_k V_3 \sin(\delta_{3k} + \delta_k - \delta_3)$

$A(z-\frac{1}{2})(z-1) + B(z^2-\frac{1}{4})(z-1) + C(z-\frac{1}{2})(z-\frac{1}{4}) = z^2 + \ldots$

$+\frac{1}{4} \times \frac{3}{4} A = \frac{1}{16} + \frac{4}{16} = \frac{5}{16}$

$\boxed{A = 5/3}$ | $-\frac{1}{4} \times \frac{1}{2} = \frac{1}{4} + \frac{2}{4}\ 3/4$

$\boxed{B = -6}$

$1 \times \frac{3}{4} = 2$

$\boxed{C = 8/3}$