



MADE EASY
Leading Institute for ESE, GATE & PSUs

ESE 2026 : Mains Test Series

UPSC ENGINEERING SERVICES EXAMINATION

Civil Engineering

Test-1 : Section A : Geo-technical & Foundation Engineering [All Topics]
Section B : Environmental Engineering [All Topics]

Name :

Roll No : []

Test Centres	Student's Signature
Delhi <input checked="" type="checkbox"/> Bhopal <input type="checkbox"/> Jaipur <input type="checkbox"/> Pune <input type="checkbox"/> Hyderabad <input type="checkbox"/>	

Instructions for Candidates

1. Do furnish the appropriate details in the answer sheet (viz. Name & Roll No).
2. There are Eight questions divided in TWO sections.
3. Candidate has to attempt FIVE questions in all in English only.
4. Question no. 1 and 5 are compulsory and out of the remaining THREE are to be attempted choosing at least ONE question from each section.
5. Use only black/blue pen.
6. The space limit for every part of the question is specified in this Question Cum Answer Booklet. Candidate should write the answer in the space provided.
7. Any page or portion of the page left blank in the Question Cum Answer Booklet must be clearly struck off.
8. There are few rough work sheets at the end of this booklet. Strike off these pages after completion of the examination.

FOR OFFICE USE

Question No.	Marks Obtained
Section-A	
Q.1	45
Q.2	—
Q.3	—
Q.4	46
Section-B	
Q.5	48
Q.6	50
Q.7	54
Q.8	—
Total Marks Obtained	243

Signature of Evaluator

Cross Checked by

.....

IMPORTANT INSTRUCTIONS

CANDIDATES SHOULD READ THE UNDERMENTIONED INSTRUCTIONS CAREFULLY. VIOLATION OF ANY OF THE INSTRUCTIONS MAY LEAD TO PENALTY.

DONT'S

1. Do not write your name or registration number anywhere inside this Question-cum-Answer Booklet (QCAB).
2. Do not write anything other than the actual answers to the questions anywhere inside your QCAB.
3. Do not tear off any leaves from your QCAB, if you find any page missing do not fail to notify the supervisor/invigilator.
4. Do not leave behind your QCAB on your table unattended, it should be handed over to the invigilator after conclusion of the exam.

DO'S

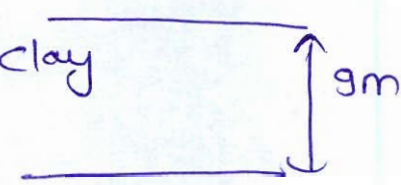
1. Read the Instructions on the cover page and strictly follow them.
2. Write your registration number and other particulars, in the space provided on the cover of QCAB.
3. Write legibly and neatly.
4. For rough notes or calculation, the last two blank pages of this booklet should be used. The rough notes should be crossed through afterwards.
5. If you wish to cancel any work, draw your pen through it or write "Cancelled" across it, otherwise it may be evaluated.
6. Handover your QCAB personally to the invigilator before leaving the examination hall.

Section A : Geo-technical & Foundation Engineering

- a) A homogeneous clay layer, 9 m thick, is expected to have an ultimate settlement of 308 mm. After a time span of 2 years, the average settlement was measured to 108 mm. How much longer will it take for the average settlement to attain 220 mm?

[12 marks]

Given, ultimate settlement
of clay layer = 308 mm clay



After $t = 2$ years \rightarrow avg settlement = 108 mm

$t = ? \rightarrow$ avg. settlement = 220 mm

(A) degree of consolidation for 220 mm settlement

$$U = \frac{\Delta h}{\Delta H} \times 100 = \frac{220 \text{ mm}}{308 \text{ mm}} \times 100 = 71.429\% > 60\%$$

$$\begin{aligned} \therefore T_v (\text{time factor}) &= 1.781 - 0.933 \log(100 - U\%) \\ &= 1.781 - 0.933 \log(100 - 71.429) \\ &= 0.4226 \end{aligned}$$

$$\therefore T_v = C_v \frac{t}{d^2} \quad t = \text{time}$$

$C_v = \text{degree of consolidation}$

$$0.4226 = \frac{C_v}{d^2} \times \text{years} \rightarrow \text{---}$$

(12)

Also \rightarrow ~~$T_v =$~~ $U = \frac{108}{308} \times 100 = 35.065\% < 60\%$

$$T_v = \frac{\pi}{4} U^2 = \frac{\pi}{4} [0.35065]^2$$

$$\frac{\pi}{4} [0.35065]^2 = \left[\frac{C_v}{d^2} \right] \times 2 \text{ years} \rightarrow \text{---}$$

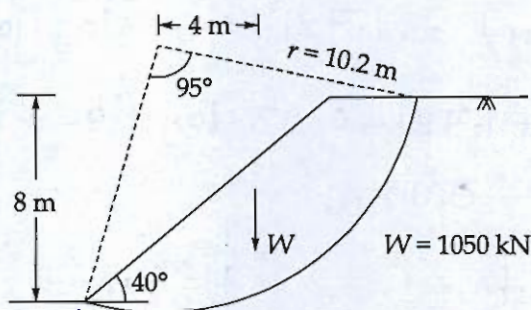
from (i) & (ii)

$$t \neq \frac{\frac{\pi}{4} (0.35065)^2}{0.4226} = \frac{\left(\frac{C_v}{d^2} \right) \times 2 \text{ years}}{\left(\frac{C_v}{d^2} \right) \times t}$$

$$\boxed{t = 8.75 \text{ years}} \quad (\text{Ans})$$

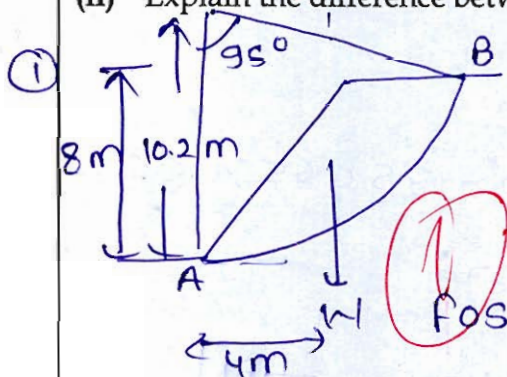
Time required to attain settlement of 220mm is = $8.75 - 2$
 = 6.75 years (Ans)

Q.1(b) (i) A 40° slope is excavated to a depth of 8 m in a deep layer of saturated clay ($c = 50 \text{ kN/m}^2$ and $\phi = 0^\circ$, $\gamma = 19 \text{ kN/m}^3$). Determine the factor of safety for the trial failure surface shown in Figure.



(ii) Explain the difference between soil liquefaction and quick sand condition.

[6 + 6 = 12 marks]



Given, $W = 1050 \text{ kN}$
 $c = 50 \text{ kN/m}^2$
 $\phi = 0^\circ$, $\gamma = 19 \text{ kN/m}^3$
 $R = 10.2 \text{ m}$

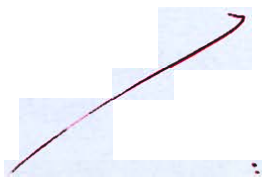
$FOS = \frac{M_{\text{resisting}}}{M_{\text{overturning}}}$

~~$\frac{CLR}{W \cdot R}$~~

$FOS = \frac{W \cdot l \cdot \sin \theta}{c [L_{AB} \cdot l \cdot m] \times R}$

, $L_{AB} = R \theta$

$FOS = \frac{1050 \text{ kN} \times 4 \text{ m}}{50 \frac{\text{kN}}{\text{m}^2} \left(\frac{10.2 \text{ m} \times 95^\circ \times 17}{180} \right) \times 10.2} = \underline{\underline{0.487}}$
 (Ans)



- (c) A soil sample has a maximum dry density of 1.65 g/cc at an optimum moisture content (OMC) of 14.5%. The specific gravity of the soil solids is 2.70. Determine the degree of saturation and the percentage air voids at OMC. Also estimate the theoretical maximum dry density.

Given, maximum dry density, $\gamma_d = 1.65 \text{ g/cc}$ [12 marks]

Optimum moisture content, $w = 14.5\%$

$$G_s = 2.7$$

$$S = ?$$

$$\eta = ?$$

$$\gamma_{dth} = ?$$

$$a) \therefore \gamma_d = \frac{(1 - \eta_a) G_s \gamma_w}{1 + w G_s} \quad \eta_a = \% \text{ air voids}$$

$$1.65 \text{ g/cc} = \frac{(1 - \eta_a) 2.7 \times 1 \text{ g/cc}}{1 + 0.145 \times 2.7}$$

$$\eta_a = 0.1496 = 14.96\% \text{ (Ans)}$$

also $\gamma_d = \frac{G_s \gamma_w}{1 + e}$

$$1.6 = \frac{2.7 \times 1}{1 + e}$$

$$\Rightarrow e = 0.6875$$

from $se = w G_s$

$$S = \frac{w G_s}{e} = \frac{0.145 \times 2.7}{0.6875} = 0.5694 = 56.94\%$$

$$\boxed{S = 56.94\%} \text{ (Ans)}$$

$\Rightarrow \gamma_{dth}$ theoretical at zero air content & 100% saturated soil

$$\gamma_{dth} = \frac{G_s \gamma_w}{1 + w G_s} = \frac{2.7 \times 1}{1 + 0.145 \times 2.7} = 1.94 \text{ g/cc}$$

$$\boxed{\gamma_{dth} = 1.94 \text{ g/cc}} \text{ (Ans)}$$

Q.1 (d) Two square footings with a contact pressure of 300 kPa under each are placed 6 m apart (center-to-center) on the ground surface.

Footing A: 2.5 m × 2.5 m

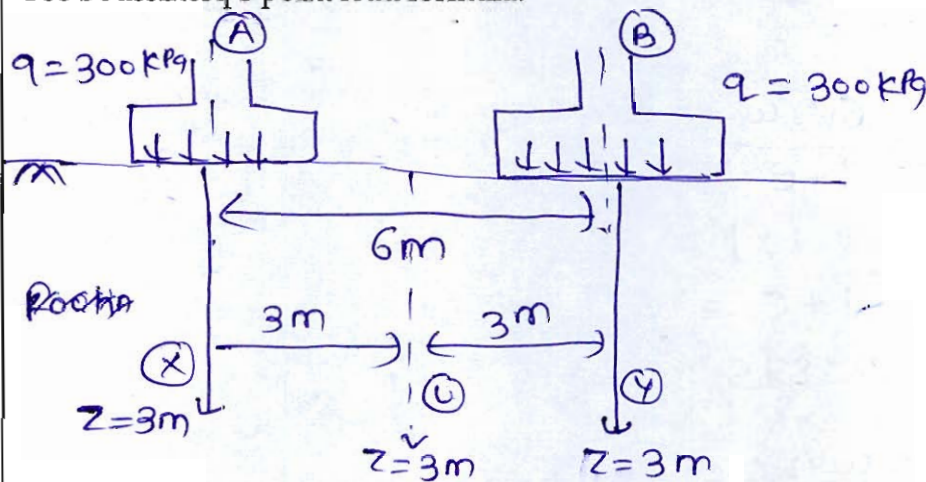
Footing B: 3.0 m × 3.0 m

Determine the increase in vertical stress at a depth of 3 m below the ground surface at the following locations:

- Vertically below the center of Footing A
- Vertically below the center of Footing B
- Vertically below the midpoint between the two footings.

Use Boussinesq's point load formula.

[12 marks]



Footing A \rightarrow 2.5 m \times 2.5 m

Footing B = 3 m \times 3 m

\rightarrow Boussinesq's point load formula

$$\sigma_z = \frac{3}{2\pi} \frac{Q}{z^2} \left[\frac{1}{1 + \left(\frac{r}{z}\right)^2} \right]^{3/2}$$

$$\sigma_{2B} = \frac{3}{2\pi} \left[\frac{300 \times 3 \times 3}{32} \right] \left[\frac{1}{1 + \left(\frac{3}{3}\right)^2} \right]^{5/2}$$

$$= 25.321 \text{ kN/m}^2$$

$$\sigma_2 = 17.584 + 25.321 = \underline{42.905 \text{ kN/m}^2}$$

(Ans)

12

- Q.1(e) An undisturbed soil in a borrow area has a water content of 16%, a void ratio of 0.55, and a specific gravity of solids of 2.7. This soil is used to construct an embankment with a finished volume of 60,000 m³. The soil is excavated and transported via trucks with a 5 m³ capacity. When loaded to capacity, these trucks contain a net weight of soil equal to 70 kN. During construction, water is added to bring the water content to 19%. The soil is then compacted to a dry unit weight of 18.0 kN/m³. Using unit weight of water = 10 kN/m³.

Calculate:

1. The degree of saturation, bulk unit weight, and dry unit weight of the undisturbed borrow material.
2. The number of truck loads required for construction.
3. The amount of water (in litres) to be added per truck load.

Undisturbed soil in borrow area

[6 + 3 + 3 = 12 marks]

→ water content, $w = 16\%$

$e = 0.55$

$G = 2.7$

→ Embankment → $V_{\text{soil}} = 60,000 \text{ m}^3$

Case (A)

$S = ?$ saturation

$\therefore s_e = wG$

$$S = \frac{wG}{e} = \frac{0.16 \times 2.7}{0.55} = 0.7854$$

$S = 78.54\%$ (Ans)

Bulk unit wt

$$\gamma_b = \left[\frac{G + s_e}{1 + e} \right] \gamma_w = \left[\frac{2.7 + 0.7854 \times 0.55}{1 + 0.55} \right] \times 9.81$$

$\gamma_b = 19.822 \text{ kN/m}^3$ (Ans) 20.206 kN/m^3 (Ans)

~~γ_d~~ dry unit weight

$$\gamma_d = \frac{\gamma_b}{1 + w} = \frac{19.822}{1 + 0.16} = 17.088 \text{ kN/m}^3$$

~~17.42 kN/m^3 (Ans)~~

8

b) Assuming, during ~~trans~~ excavation and ~~transportation~~ volume of solids remain same & hence weight of solids also remain same. $(W_s)_{emb} = (W_s)_{B.A.}$

→ Embankment → $\gamma_d = 18 \text{ kN/m}^3$

~~$V_{soil} = 60,000 \text{ m}^3$~~

Mass of dry soil, $W_d = W_s = \gamma_d \times V_{soil}$
 $= 18 \times 60,000$

$W_s = \frac{256,000 \text{ kN}}{1080,000}$ — (1)

In Borrow area

$\gamma_d = 17.42 \text{ kN/m}^3 = \frac{W_s}{V_{B.S.}} \Rightarrow$

$W_s = 17.42 \times V_{B.S.}$

$\therefore (W_s)_{BA} = (W_s)_{em} \Rightarrow 17.42 V_{B.S.} = 256,000$

~~$V_{B.S.} = 14695.7$~~

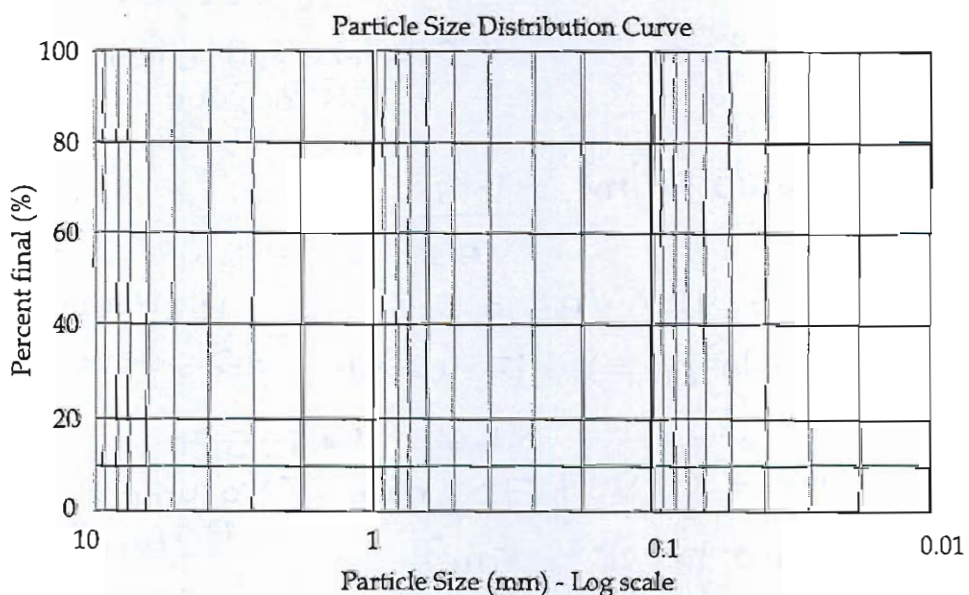
$V_{B.S.} = 61997.704 \text{ m}^3$ (Volume of Borrow soil)

Capacity of one truck = 5 m^3

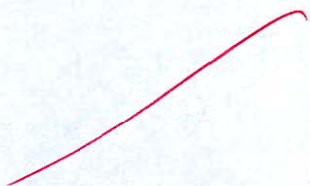
No. of trucks = $\frac{V_{B.S.}}{\text{Capacity}} = \frac{61997.704 \text{ m}^3}{5 \text{ m}^3}$

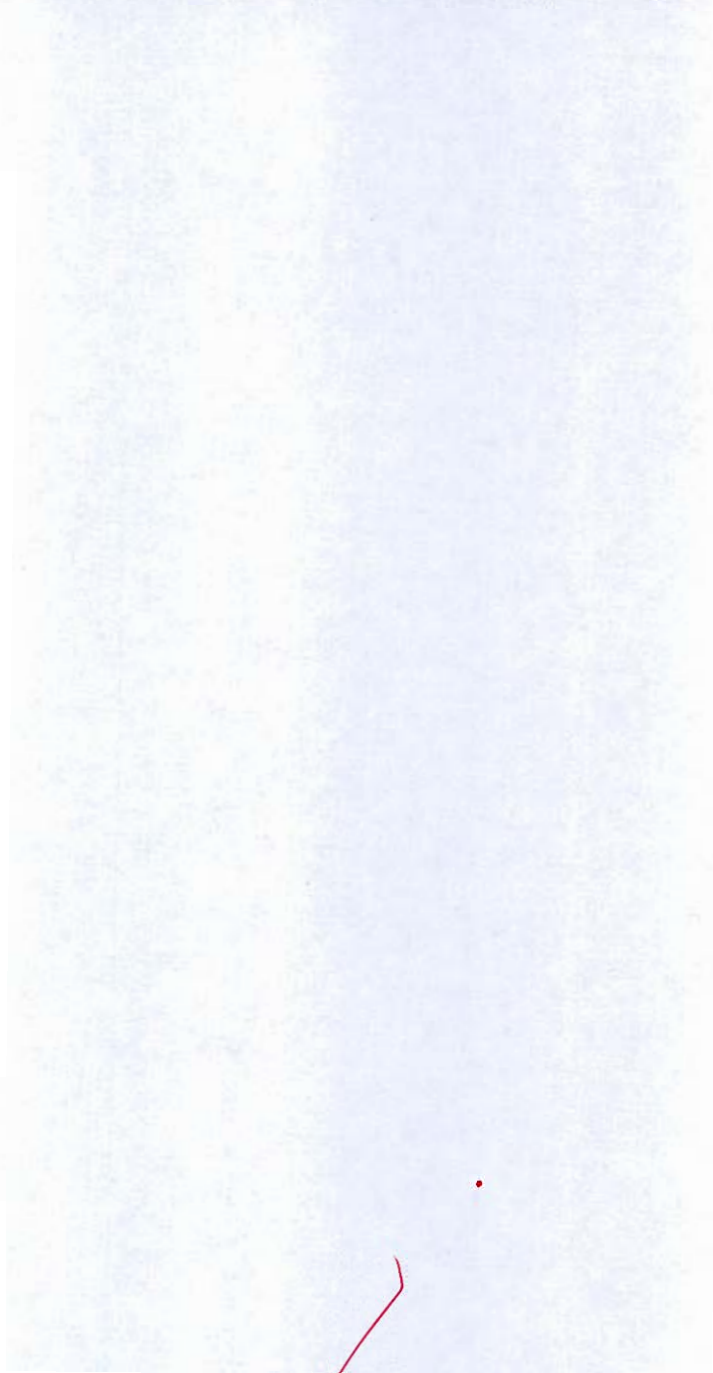
$= 12339.54 \Rightarrow 12340$ trucks (Ans)

- Q.2(a) A 500 g dry soil sample was subjected to a sieve analysis. The masses of soil retained on each sieve are as follows: 12 g on 4.75 mm sieve, 160 g on 2.00 mm sieve, 115 g on 1.00 mm sieve, 95 g on 425 μm sieve, 45 g on 212 μm sieve, 25 g on 150 μm sieve, 40 g on 75 μm sieve, and 8 g in the pan. Plot the Particle Size distribution curve on semi log graph given below. Determine the soil fractions and the gradation of the soil classify the soil also.



[20 marks]





- b) Consolidated undrained triaxial tests were performed on two identical specimens of saturated clay with pore pressure measurements. The observations are as follows: Determine the shear strength parameters in terms of both total and effective stresses.

Specimen	Cell pressure (σ_3)	Deviator stress ($\Delta\sigma_d$)	Pore Pressure (u)
1	100 kPa	160 kPa	40 kPa
2	300 kPa	320 kPa	120 kPa

[20 marks]

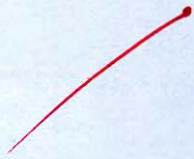




- (c) (i) A footing is constructed 2.0 m below the ground surface. The base is 3.0 m × 3.0 m and carries a total load of 2100 kN. The substrata consist of:
- Sand & Gravel Layer: From ground to 5.0 m depth ($\gamma = 21.0 \text{ kN/m}^3$).
- Water Table: Located at 5.0 m below the ground surface.
- Clay Layer: A 3.0 m thick normally consolidated clay layer exists below the sand ($e_0 = 1.1$, $C_c = 0.6$, $G_s = 2.72$).
- Compute the probable ultimate consolidation settlement of footing.
- (ii) Explain the criteria for design of protective filters in earthen dams.

[10 + 10 = 20 marks]



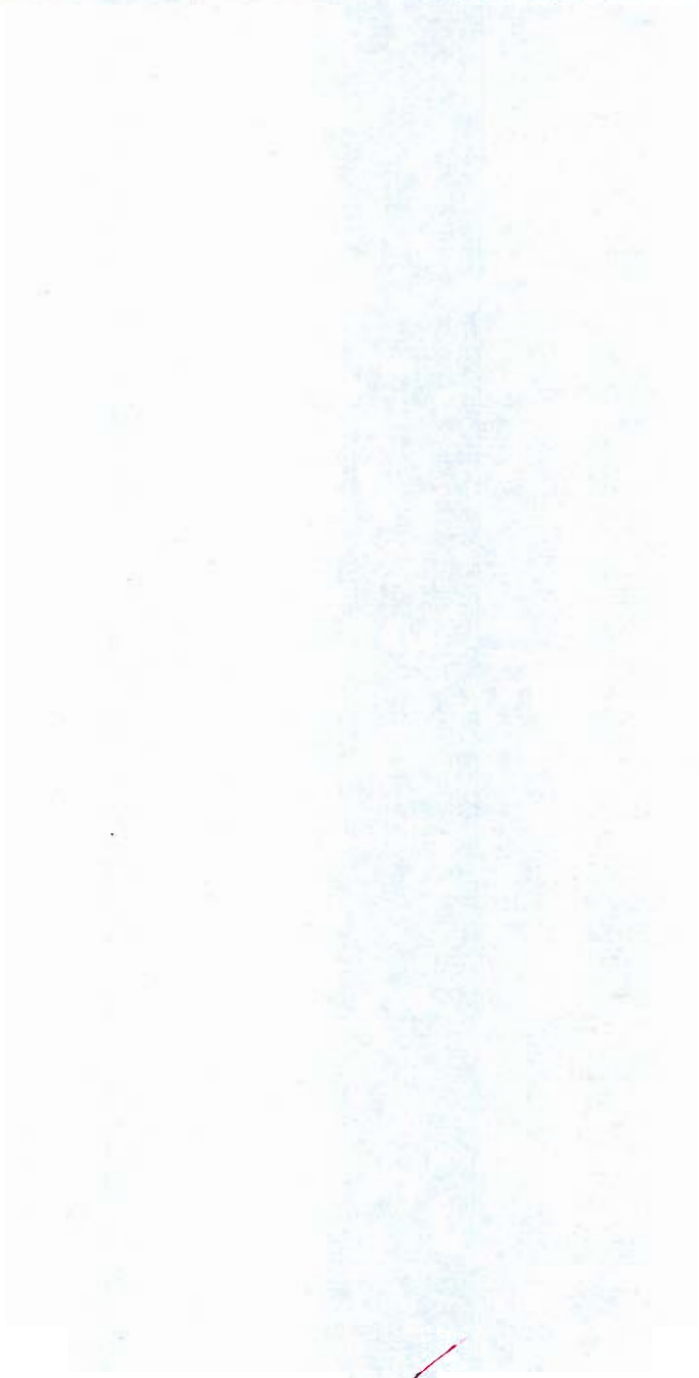


- Q.3 (a) (i) At a proposed construction site, the soil profile consists of a 5 m thick layer of sand ($G = 2.66$, $e = 0.70$, $D_{10} = 0.2$ mm) underlain by a 4 m thick layer of clay ($G = 2.72$, $w = 30\%$). Below the clay layer lies a dense, impermeable hardpan. The water table is located at a depth of 3 m below the ground surface. A uniform surcharge load of 20 kN/m^2 is applied over the entire ground surface. Assuming the capillary rise constant $C = 0.5 \text{ cm}^2$ and that the clay layer is fully saturated, determine and plot the distribution of pore water pressure, total stress and effective stress.
- (ii) Write short note over bulking of sand.

[15 + 5 = 20 marks]

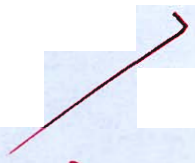




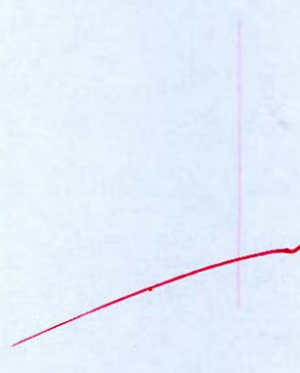




- Q.3 (b) (i) A pumping-out test was carried out in the field to determine the average coefficient of permeability of a 22 m thick sand layer. The ground water table was located at a depth of 3.5 m below the ground level. A steady state was reached when the discharge from the well was 25.0 lit/sec. At this stage, the drawdown in the test well was 3.10 m, while the drawdowns in two observation wells situated at 10 m and 25 m from the test well were found to be 2.15 m and 1.60 m respectively. Determine:
- (a) Coefficient of permeability of the sand layer in m/day.
 - (b) Radius of influence of the test well.
 - (c) Effective size of the sand using Allen Hazen's formula (take $C = 110$). ✓
- [4 + 4 + 2 = 10 marks]
- (ii) Discuss the type of foundations to be provided in Expansive soils. [10 marks]







Q.3 (c)

A square group of 16 piles (arranged in a 4×4 formation), each 12 m long and 400 mm in diameter, supports a raft footing founded 1.5 m below the ground surface. The pile group is spaced at 1.2 m center-to-center. The foundation soil consists of a 19.5 m thick layer of normally consolidated clay underlain by dense sand, with the water table residing at the ground level.

The gross load carried by the pile group is 350 t. The properties of the clay are:

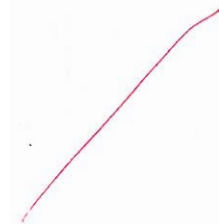
Water content (w): 32%

Specific Gravity (G): 2.67

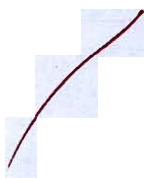
Liquid Limit (LL): 50%

Estimate the probable consolidation settlement of the pile group. Assume the load is distributed at an angle of 60° with the horizontal from an equivalent raft located at $2/3$ of the pile length. For accuracy, divide the compressible clay layer into three sublayers of 3 m, 3 m, and 4 m thickness.

[20 marks]

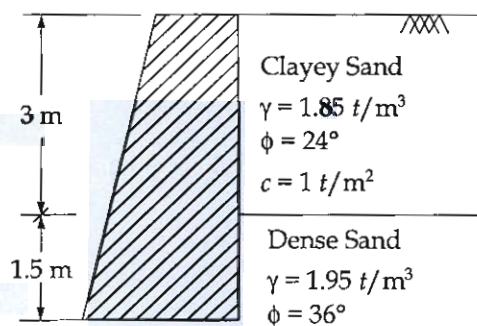






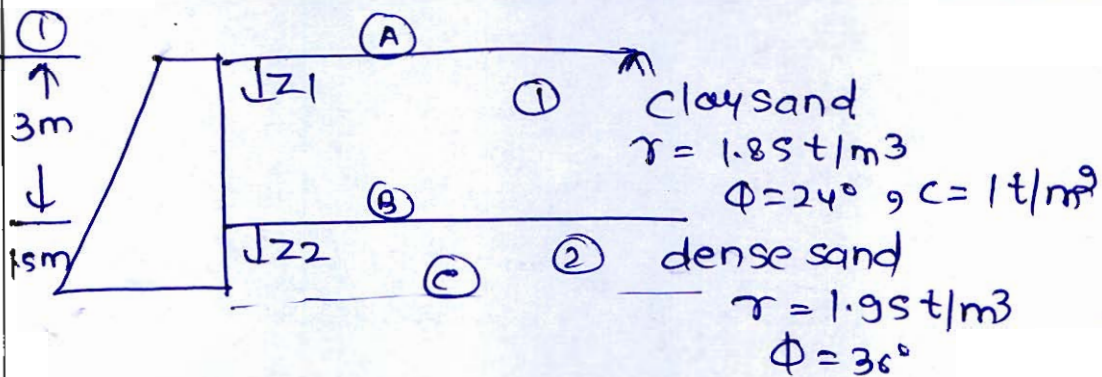
- 4 (a) (i) Compute the total active thrust and its point of application for the retaining wall shown in Figure. The wall has a smooth back face.

Assume: Tension crack are developed



- (ii) In a shrinkage limit test, a container of volume 9.6 cc was filled with soil slurry. The weight of the saturated soil was 17.46 g. The slurry was then gradually dried, first in atmosphere and then in an oven at a constant temperature of 110°C . The weight and volume of the dried soil were 11.58 g and 5.22 cc, respectively. Determine the shrinkage limit of the soil and the shrinkage ratio.

[12 + 8 = 20 marks]



As the wall has a smooth back, using Rankine earth Pressure theory

→ Computing active earth pressure coefficient

$$\text{Layer ①} \rightarrow K_{a1} = \frac{1 - \sin \phi}{1 + \sin \phi} = \frac{1 - \sin 24^\circ}{1 + \sin 24^\circ}$$

$$= \underline{0.4217}$$

$$K_{a2} = \frac{1 - \sin 36^\circ}{1 + \sin 36^\circ} = \underline{0.3905}$$

⇒ Vertical pressure computation

$$\text{At [A]} \quad \bar{\sigma}_v = 0 \times 1.85 = 0$$

$$\text{At [B]} \quad \bar{\sigma}_v = 3 \times 1.85 = 5.55 \text{ t/m}^2$$

$$\text{at [C]} \quad \bar{\sigma}_v = 5.55 + 1.5 \times 1.95 = 8.475 \text{ t/m}^2$$

⇒ Active earth pressure computation

$$\text{at [A]} \quad P_a = [K_{a1} \bar{\sigma}_v - 2c] K_{a1}$$

$$= 0.4217 \times 0 - 2 \times 1 \sqrt{0.4217} =$$

$$= \underline{-1.2988 \text{ t/m}^2}$$

at [B] Just above

$$P_a = 0.4217 \times 5.55 - 2 \times 1 \sqrt{0.4217}$$

$$= 1.0417 \text{ t/m}^2$$

at [B] Just below

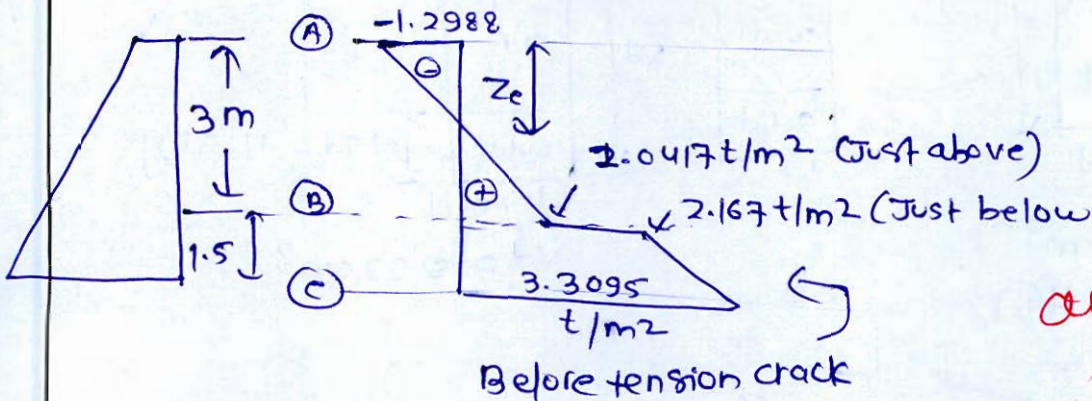
$$P_a = K_{a2} \bar{\sigma}_v - 2 \times c_2 \sqrt{K_{a2}}$$

$$= 0.3905 \times 5.55 - 2 \times 0 \sqrt{0.3905}$$

$$= \underline{2.167 \text{ t/m}^2}$$

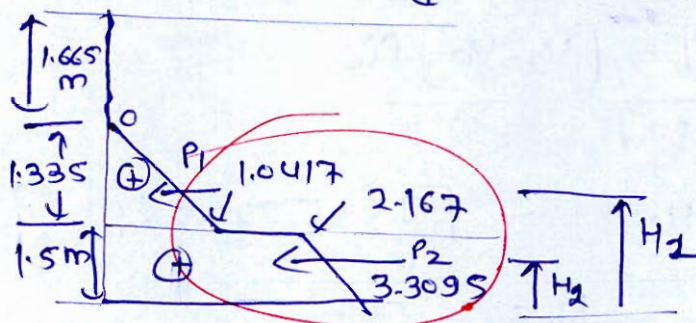
6

at C $P_a = 0.3905 \times 8.475$
 $= 3.3095 \text{ t/m}^2$



avoid silly mistakes and Calculator Error

After tension crack



depth of tension crack

$$z_c = \frac{2C_1}{\gamma \sqrt{K_a}}$$

$$= \frac{2 \times 1}{1.85 \sqrt{0.4217}}$$

$$= 1.665 \text{ m}$$

Active thrust

$$P_{total} = P_1 + P_2$$

$$P_1 = \frac{1}{2} [0 + 1.0417] \times 1.335 \times 1 \quad \left| \quad H_1 = 1.5 + \frac{1}{3} \times 1.335 \right.$$

$$= 0.695 \text{ t/m length} \quad \left. \quad \quad \quad = 1.945 \text{ m} \right.$$

$$P_2 = \frac{1}{2} [2.167 + 3.3095] \times 1.5 \times 1 \quad \left| \quad H_2 = \left[\frac{2 \times 2.167 + 3.3095}{2.167 + 3.3095} \right] \times \frac{1.5}{3} \right.$$

$$= 4.1074 \text{ t/m length of wall} \quad \left. \quad \quad \quad H_2 = 0.698 \text{ m} \right.$$

$$P_{total} = 0.695 + 4.1074$$

$$= 4.8024 \text{ t/m length of wall (Ans)}$$

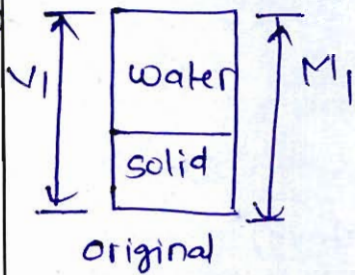
Point of application

$$Z = \frac{P_1 H_1 + P_2 H_2}{P_{total}}$$

$$= \frac{0.695 \times 1.945 + 4.1074 \times 0.698}{4.8024}$$

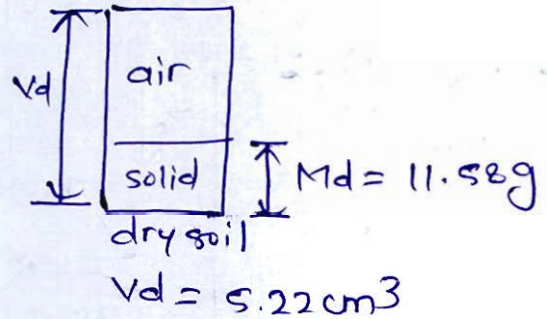
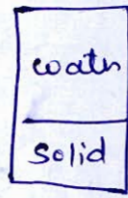
$$Z = 0.878 \text{ m from base of wall (Ans)}$$

①



$$V_1 = 9.6 \text{ cm}^3$$

$$M_1 = 17.46 \text{ g}$$



$$V_d = 5.22 \text{ cm}^3$$

① Shrinkage limit (w_s)

$$w_s = \frac{[M_1 - M_d] - [V_1 - V_d] \rho_w}{M_d}$$

$$= \frac{[17.46 - 11.58] - [9.6 - 5.22] \times 1}{11.58}$$

$$= 0.1295$$

$$w_s = 12.95\% \text{ Ans) } \textcircled{b}$$

Shrinkage Ratio, R

$$R = \frac{V_1 - V_d}{V_d (w_1 - w_d)}$$

$$w_1 = \frac{M_1 - M_d}{M_d} = \frac{17.46 - 11.58}{11.58} = 0.5078$$

$$R = \frac{[9.6 - 5.22]}{5.22 \times [0.5078 - 0.1295]}$$

$$R = 2.218 \text{ Ans}$$

- (b) (i) A raft foundation is supported by a group of 12 concrete piles, each with a diameter of 400 mm and a length of 12 m, arranged in a rectangular formation of 3 rows and 4 columns. The piles are spaced at 1.0 m center-to-center in both directions and are embedded in a deep layer of clay having an undrained cohesion of 4.5 t/m^2 and a unit weight of 1.8 t/m^3 . Assuming an adhesion factor of 0.9 and using a Factor of Safety of 2, determine the allowable net capacity of the pile group.
- (ii) What factors should be considered while determining the appropriate depth of footing for a civil structure?

Given, no. of piles = 12 concrete

[12 + 8 = 20 marks]

dia of pile, $d = 0.4 \text{ m}$

length of pile, $L = 12 \text{ m}$

spacing, $S = 1 \text{ m}$

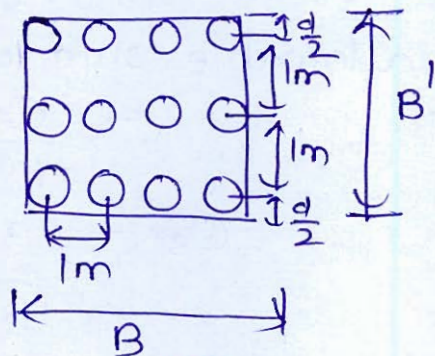
$c_u = 4.5 \text{ t/m}^2$

$\gamma = 1.8 \text{ t/m}^3$

$\alpha = 0.9$

FOS = 2

Allowable = ?



12

$$B' = 2s + d = 2 \times 1 + 0.4 = 2.4 \text{ m}$$

$$B = 3s + d = 3 \times 1 + 0.4 = 3.4 \text{ m}$$

④ Ultimate capacity of group of piles

$$= \min \left\{ \begin{array}{l} \text{Group action} \\ \text{Individual pile action} \end{array} \right\} = \phi_{ug}$$

$$\text{Individual pile action} = N \phi_{up}$$

① Individual pile action

$$N \phi_{up} = N [\phi_{eb} + \phi_{sf}]$$

$$= N [9c A_b + \alpha \bar{c} A_s]$$

$$= N \left[9c \cdot \frac{\pi d^2}{4} + \alpha \bar{c} \cdot \pi d L \right]$$

$$= 12 \left[9 \times 4.5 \times \frac{\pi \times 0.4^2}{4} + 0.9 \times 4.5 \times \pi \times 0.4 \times 12 \right]$$

$$N \phi_{up} = 793.94 \text{ t/m}^2$$

② Group action of piles

$$\phi_{ug} = 9c [B \times B'] + \bar{c} [2(B+B') \times L]$$

$$= 9 \times 4.5 \times [2.4 \times 3.4] + 4.5 \times 2 [2.4 + 3.4] \times 12$$

$$= \underline{956.88 \text{ t/m}^2}$$

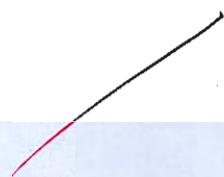
$$\Rightarrow \phi_u = \min \{ 793.94, 956.88 \}$$

$$\phi_u = 793.94 \text{ t/m}^2$$

allowable safe load capacity

$$= \frac{\phi_u}{\text{FOS}} = \frac{793.94}{2}$$

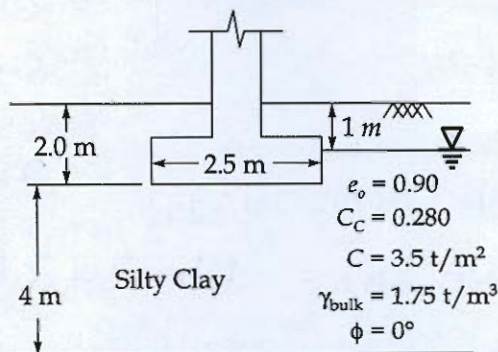
$$\phi_s = \underline{396.97 \text{ t/m}^2} \text{ (Ans)}$$



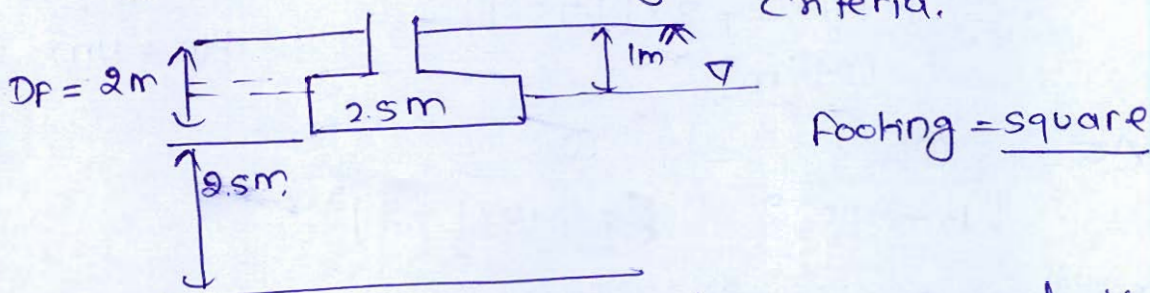


✓

- 4(c) A square footing of dimensions $2.5 \text{ m} \times 2.5 \text{ m}$ is proposed to be constructed at a depth of 2.0 m below ground level in a deep, uniform deposit of soft silty clay. The foundation soil has an undrained cohesion of 3.5 t/m^2 , a bulk unit weight of 1.75 t/m^3 , and an angle of internal friction equal to 0° . Laboratory consolidation tests on the clay indicate a compression index $C_c = 0.280$ and an initial void ratio $e_0 = 0.90$. The groundwater table is located at a depth of 1.0 m below the ground surface. Determine the allowable net bearing capacity of the footing such that a factor of safety of 3 is ensured against shear failure and the total consolidation settlement is limited to a maximum of 5.0 cm . For the analysis of shear failure, use Skempton's method. Take $\gamma_w = 10 \text{ kN/m}^3$.



Case (A) $q_{ns} = ? \rightarrow$ checking shear failure criteria. [20 marks]



As per Skempton's method, for square footing

$$\frac{D_f}{B} = \frac{2}{2.5} = 0.8 < 2.5$$

$$q_{nu} = C N_c \quad \text{where}$$

$$q_{nu} = 3.5 \times 6.96 = 24.36 \text{ t/m}^2$$

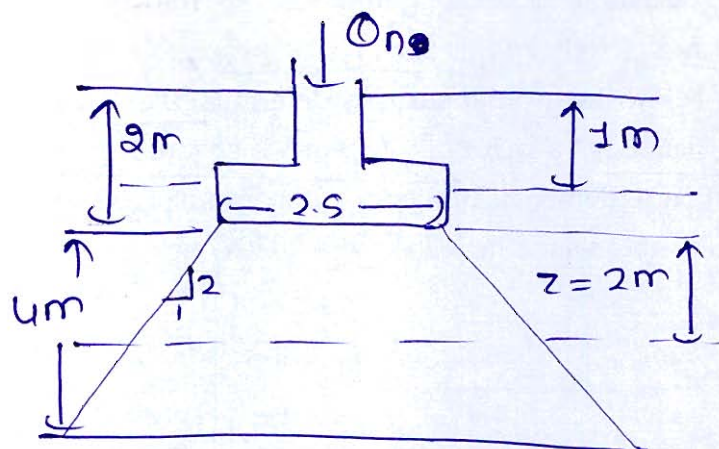
$$FOS = 3$$

$$N_c = 6 \left[1 + 0.2 \frac{D_f}{B} \right] = 6 [1 + 0.2 \times 0.8] = 6.96$$

$$q_{ns} = \frac{q_{nu}}{FOS} = \frac{24.36}{3} = 8.12 \text{ t/m}^2$$

① Settlement Criteria

Total consolidation settlement is limited
= 50mm = 5cm



$$\gamma_b = 1.75 \text{ t/m}^3$$

γ_{sub}

$$e = 0.9$$

$$C_c = 0.280$$

$$\phi = 0^\circ$$

$$\gamma_w = 10 \text{ kN/m}^3$$

$$= 1 \text{ t/m}^3$$

assuming

$$\gamma_w = 1 \text{ t/m}^3$$

$$H_0 = 4 \text{ m}$$

Assuming load dispersion $2V:1H$

② Initial effective stress at mid of clay layer

$$\bar{\sigma}_0 = \gamma_b \times 1 \text{ m} + 3 \times \gamma_{\text{sub}}$$

$$= 1.75 \times 1 + 3 \times [1.75 - 1]$$

$$= 4 \text{ t/m}^2$$

$$\Delta \bar{\sigma} = \frac{0}{(B + 2nz)^2} = \frac{0}{(2.5 + 2 \times \frac{1}{2} \times 2)^2}$$

$$= \frac{0}{20.25} \text{ t/m}^2$$

$$\therefore S = \Delta H = \frac{H_0}{1+e_0} C_c \log \left[\frac{\bar{\sigma}_0 + \Delta \bar{\sigma}}{\bar{\sigma}_0} \right]$$

$$50 \text{ mm} \times 10^{-3} \frac{\text{m}}{\text{mm}} = \frac{4 \text{ m}}{1+0.9} \times 0.28 \log \left[1 + \frac{\Delta \bar{\sigma}}{4} \right]$$

$$\Delta \bar{\sigma} = 0.8627 \text{ t/m}^2 = \frac{0}{20.25}$$

$$0 = 17.47 \text{ tonn}$$

$$q_{\text{allowable}} = \frac{0}{2.5^2} = \frac{17.47}{2.5^2} = \underline{\underline{2.795 \text{ t/m}^2}}$$

$$AF = 2/5 \text{ (or)}$$

$$FOS = \frac{2.795}{2.795} = 2.795$$

allowable net bearing capacity of footing

$$= \min [2.795 \text{ t/m}^2, 8.12 \text{ t/m}^2]$$

$$= 2.795 \text{ t/m}^2$$

20

Section B: Environmental Engineering [All Topics]

- Q.5 (a) (i) A water supply scheme is under preparation for a city. Data shows the population of the city has grown from 40,000 to 1,60,000 and then to 4,00,000 in the last two successive periods of each of 20 years. Using the logistic curve method, determine
- The saturation population of the city.
 - The expected population of the city after next 50 years.
- (ii) Explain the following terms in relation to the aquifers a) Specific Capacity; b) Specific yield.

[8 + 4 = 12 marks]

①

Time	Population
$t=0$	40,000 $\leftarrow P_0$
$t=20$	160,000 $\leftarrow P_1$
$t=40$	400,000 $\leftarrow P_2$

$\Delta t = 20 \text{ years}$

Using logistic curve method,

a) Saturation population of city

$$P_s = \frac{2 P_0 P_1 P_2 - P_1^2 [P_0 + P_2]}{P_0 P_2 - P_1^2}$$

$$P_s = \underline{640,000 \text{ (Ans)}}$$

b) Population after 50 years from present
 $t = 40 + 50 = 90 \text{ years from } \underline{t=0}$

$$P_t = \frac{P_s}{1 + m e^{-nt}}$$

$$\text{where } m = \frac{P_s - P_0}{P_0}$$

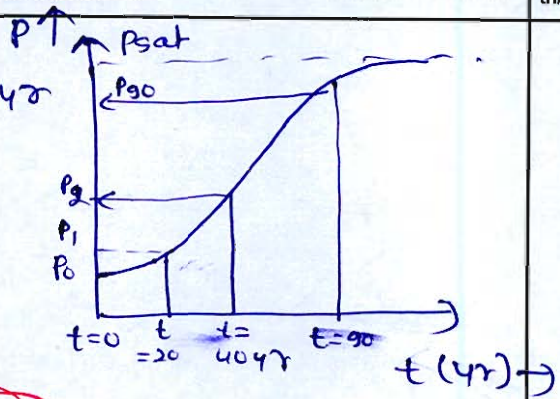
$$n = \frac{1}{\Delta t} \ln \left[\frac{P_0}{P_1} \left[\frac{P_s - P_1}{P_s - P_0} \right] \right]$$

$$m = \frac{640,000 - 40,000}{40,000} = 15, \quad n = -0.0804742$$

$$P_{90} = \frac{640,000}{1 + 15e^{-0.0804742 \times 9042}}$$

$$= 633202.597$$

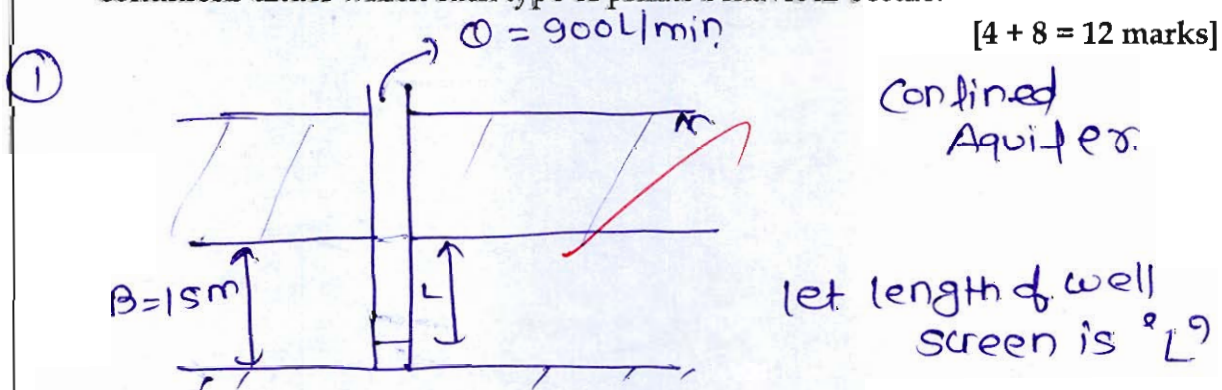
$$\approx \underline{\underline{633203}}$$



8

11

- Q.5 (b) (i) A fully penetrating well is constructed in a confined sandy aquifer that is bounded above and below by impervious clay strata. The well has a maximum discharge capacity of 900 L/min. The thickness of the aquifer is 15 m. Determine the required length of the well screen, assuming that the available strainer has 13% open area and the borehole diameter is 15 cm. The maximum permissible velocity through the strainer is 2 cm/sec.
- (ii) Draw the neat sketches of the different types of plume behaviour observed for emissions from a chimney. Also illustrate the corresponding atmospheric lapse rate conditions under which each type of plume behaviour occurs.



Area of holes = $0.13 \times A_{\text{total}}$
 borehole diameter = $15 \text{ cm} = d$
 Velocity (max) = 2 cm/s through strainer.

$$\therefore Q = \text{Area of holes} \times \text{Velocity through strainer}$$

$$900 \frac{\text{L}}{\text{min}} \times 10^{-3} \frac{\text{m}^3}{\text{L}} \times \frac{1 \text{ min}}{60 \text{ sec}} = 0.13 \times [\pi d L] \times 2 \times 10^{-2} \frac{\text{m}}{\text{s}}$$

$$\frac{960 \times 10^3 \cdot \text{m}^3}{60 \text{ s}} = 0.13 \times \pi \times 0.15 \times L \times 2 \times 10^2 \text{ m/s}$$

$$L = 12.243 \text{ m (Ans)}$$

4

11

(c) To determine the pollution level in the river, the BOD_5 test was performed. The river water sample was diluted 10% with distilled water. The dissolved oxygen of river water sample was measured as 2.5 mg/l and that of diluted water as 6 mg/l before incubation. After incubation of 5 days at 20°C , the DO of the sample was recorded as 1.2 mg/l. Calculate the 5 day standard BOD of the river water and also calculate 3-day BOD at 27°C . Given deoxygenation constant at $20^\circ\text{C} = 0.23$ per day.

[12 marks]

Given

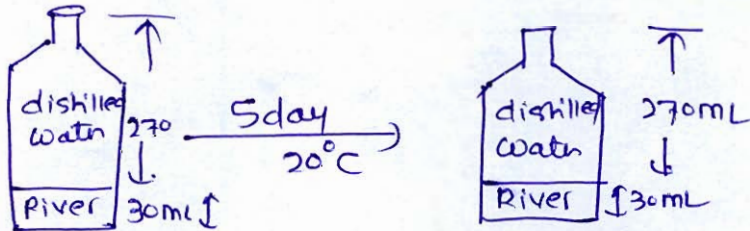
→ ~~Dilution Ratio~~

dilution factor of River sample = 10%

Dissolved oxygen in River, $DO_R = 2.5 \text{ mg/L}$

Dissolved oxygen of distilled water, $DO_w = 6 \text{ mg/L}$

$k_d = 0.23 \text{ day}^{-1}$ (assume base)



$(DO_i)_{mix} = 5.65 \text{ mg/L}$

$(DO_f)_{mix} = 1.2 \text{ mg/L}$

$(DO_f)_{mix} = 1.2 \text{ mg/L}$

⇒ Step ① $(DO_i)_{mix} = \frac{(DO_w) \times V_w + (DO_R) \times V_R}{V_w + V_R}$

$= \frac{6 \text{ mg/L} \times 270 \text{ mL} + 2.5 \times 30 \text{ mL}}{300 \text{ mL}}$

$= 5.65 \text{ mg/L}$

$BOD_5(20^\circ\text{C}) = [(DO_i)_{mix} - (DO_f)_{mix}] \times \frac{300 \text{ mL}}{30 \text{ mL}}$

$= \left[\frac{5.65 \text{ mg}}{\text{L}} - \frac{1.2 \text{ mg}}{\text{L}} \right] \times \frac{300}{30}$

$= 44.5 \text{ mg/L}$ (ANS)

∴ BOD ultimate

$BOD_u = \frac{BOD_{5t}}{1 - e^{-k_d t}} = \frac{BOD_5}{1 - e^{-k_d \times 5}} = \frac{44.5 \text{ mg/L}}{1 - e^{-0.23 \times 5}}$

$BOD_u = 66.12 \text{ mg/L}$

$$K_{27^{\circ}\text{C}} = K_{20^{\circ}\text{C}} [1.047]^{27-20}$$

$$= 0.23 [1.047]^7$$

$$= 0.317 \text{ day}^{-1}$$

$$T > 20^{\circ}\text{C}$$

$$K_D(T) = K_D(20) [1.047]^{T-20}$$

$$\text{BOD}_3(27^{\circ}\text{C}) = \text{BOD}_0 \left[1 - e^{-K_D(27) \times 3} \right]$$

$$= 66.12 \text{ mg/L} \left[1 - e^{-0.317 \times 3} \right]$$

$$= 40.574 \text{ mg/L (Ans)}$$

12

Q.5(d) Two primary settling basins, each of 25 m diameter and having a side water depth of 2.0 m, are provided with single effluent weirs located along the periphery of the tanks. For a total wastewater flow of 25,000 m³ per day, calculate:

1. The surface area and volume of the settling basins,
2. The surface overflow rate (in m³/m² day),
3. The detention time (in hours), and
4. The weir loading (in m³/m day).

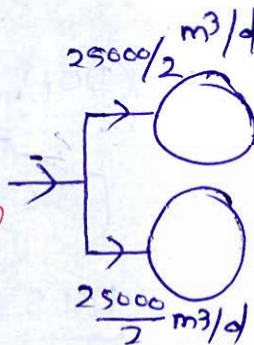
→ Diameter of each basin, $D = 25 \text{ m}$

sidewater depth, $H = 2 \text{ m}$

$$\text{Total} = 25,000 \text{ m}^3/\text{d}$$

discharge entering per basin

$$\text{in each basin, } Q = \frac{25000}{2} = 12,500 \text{ m}^3/\text{d}$$



[12 marks]

a) Surface area & Volume of settling basin

$$\text{Surface area} = \frac{\pi}{4} D^2 = \frac{\pi}{4} \times 25^2$$

$$= 490.874 \text{ m}^2 \text{ (Ans)}$$

$$\begin{aligned} \text{Volume, } V &= D^2 [0.785H + 0.011D] \\ &= 25^2 [0.785 \times 2 + 0.011 \times 25] \end{aligned}$$

$$V = 1153.125 \text{ m}^3 \text{ (Ans)}$$

(ii) Surface overflow rate

$$\text{SOR} = \frac{\text{discharge}}{\text{Surface area}}$$

$$= \frac{12500 \text{ m}^3/\text{d}}{490.874 \text{ m}^2}$$

$$\text{SOR (Vo)} = 25.465 \text{ m}^3/\text{m}^2/\text{d} \text{ (Ans)}$$

(iii) Detention time

$$D_t = \frac{\text{Volume}}{\text{discharge}}$$

$$= \frac{1153.125 \text{ m}^3 \times 24 \text{ hr}}{12500 \frac{\text{m}^3}{\text{d}}}$$

$$D_t = 2.214 \text{ hr} \text{ (Ans)}$$

(12)

(iv) Weir loading rate

$$= \frac{\text{discharge}}{\text{Perimeter}}$$

$$= \frac{12500 \text{ m}^3/\text{d}}{\pi \times 25 \text{ m}}$$

$$= 159.155 \text{ m}^3/\text{m}/\text{d} \text{ (Ans)}$$

- Q.5(e) A factory is consuming 2 ML of fuel every month. Determine the safe height of chimney from which the flue gases emitted contains following pollutants per ML per year,
- Particulate Matter = 2.5 tonnes
 SO_2 = 15 tonnes
 Oxides of Nitrogen = 4 tonnes
 HC, CO and other = 2 tonnes

[12 marks]

$$\Rightarrow \text{Fuel consumption per month} = 2 \text{ ML}$$

$$\text{Annual fuel consumption} = 12 \times 2 \frac{\text{ML}}{\text{month}}$$

$$= 24 \text{ ML/year}$$

\therefore From 1 ML of fuel per year

$$\text{PM} = 2.5 \text{ tonnes}$$

$$\text{SO}_2 = 15 \text{ tonnes}$$

\rightarrow From 24 ML of fuel per year

$$\text{PM} = \frac{2.5 \text{ tonnes}}{\text{ML}} \times 24 = 60 \text{ tonnes/year}$$

$$= \frac{60 \text{ tonnes}}{365 \times 24 \text{ hr}} = 6.849 \times 10^{-3} \text{ tonne/hr}$$

$$\rightarrow \text{SO}_2 = \frac{15 \text{ tonne}}{\text{ML}} \times 24 \text{ ML} = 360 \text{ tonne/year}$$

$$= \frac{360 \times 1000 \text{ kg}}{365 \times 24 \text{ hr}} = 41.096 \text{ kg/hr}$$

Safe height of chimney (max of below criteria)

(i) Absolute min height = 30m

(ii) Based on PM

$$H = 74 [Q]^{0.27}$$

\rightarrow tonne/hr

$$= 74 [6.849 \times 10^3]^{0.27}$$
$$= 19.268 \text{ m}$$

(iii) Based on SO_2

$$H = 14 [Q]^{0.3}$$

\rightarrow kg/hr

$$= 14 [41.096]^{0.3}$$
$$= 42.68 \text{ m}$$

12

Safe height of chimney = max $\left[\begin{array}{l} 30\text{m}, 19.268\text{m}, \\ 42.68\text{m} \end{array} \right]$

$$= \underline{42.68\text{m}} \text{ (Ans)}$$

Q.6(a)

Given the following data, obtain the required size of an anaerobic digestion tank.

Domestic sewage treated in plant = 4.5 MLD

Suspended solids in incoming flow = 220 mg/L

Solids removal efficiency of primary clarifier = 65%

Moisture content of influent sludge = 95%

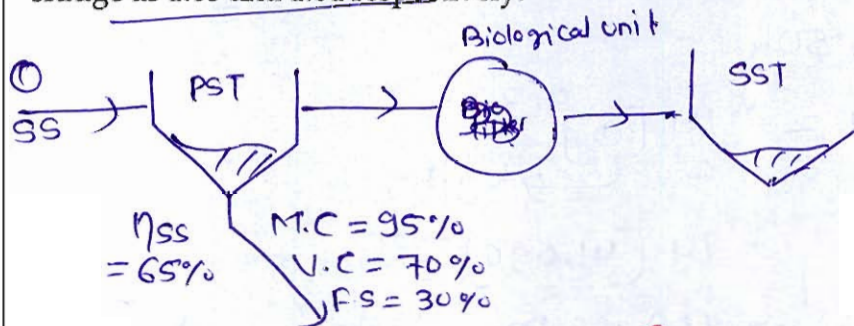
Volatile solid content in influent sludge = 70%

After digestion, volatile solids in the digested sludge are reduced by 35 % of that in influent sludge.

Digested sludge moisture content = 92%

Consider, the detention time as 20 days and specific gravity of primary sludge & digested sludge as 1.03 and 1.04 respectively.

[20 marks]

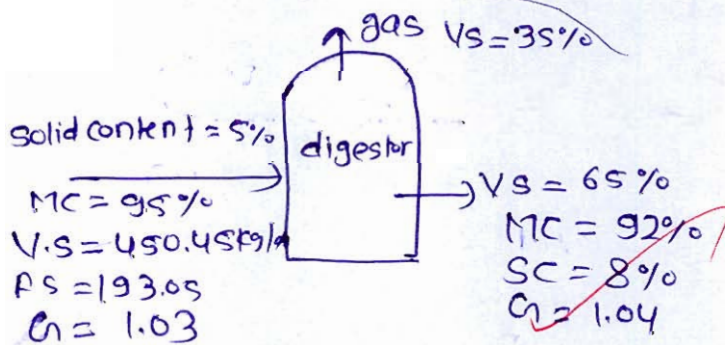


wastewater discharge, $Q = 4.5 \text{ MLD}$

Suspended solid in incoming = 220 mg/L

$$\text{SS removed in PST} = 0.65 \times 220 = 143 \text{ mg/L}$$

$$\text{Solids removed per day from PST} = 143 \times 10^{-6} \frac{\text{kg}}{\text{L}} \times 4.5 \times 10^6 \frac{\text{L}}{\text{d}} = 643.5 \text{ kg/d}$$



Volatile solids in influent sludge = 0.7×643.5

$$= 450.45 \text{ kg/d}$$

Fixed Solid = $643.5 - 450.45$

$$= 193.05 \text{ kg/d}$$

∴ Solid content of influent sludge = 5%

$$\begin{aligned} \text{Weight of influent sludge} &= 643.5 \text{ kg/d} \times \frac{100}{5} \\ &= 12870 \text{ kg/d} \end{aligned}$$

Volume of influent sludge

$$V_1 = \frac{12870 \text{ kg/d}}{1.03 \times 1000 \text{ kg/m}^3} \quad \left[V = \frac{M}{\rho \times \text{spw}} \right]$$

$$= 12.495 \text{ m}^3/\text{d}$$

→ After digestion

$$\begin{aligned} \text{Volatile solids} &= 0.65 \times 450.45 \\ (\text{35\% destroyed in digester}) &= 292.793 \text{ kg/d} \end{aligned}$$

$$\begin{aligned} \text{Fixed solids} &= 193.05 \text{ kg/d} \\ (\text{as original}) & \end{aligned}$$

$$\begin{aligned} \text{Solids present in digested} &= 292.793 + 193.05 \\ \text{sludge} &= 485.843 \text{ kg/d} \end{aligned}$$

$$\therefore \text{Solid content of digested sludge} = 8\%$$

$$\begin{aligned} \text{Total weight of digested sludge} &= 485.843 \text{ kg/d} \\ &\times \frac{100}{8} \\ &= 6073.04 \text{ kg/d} \end{aligned}$$

Volume of digested sludge

$$V_2 = \frac{M_{DS}}{\rho_{DS} \times \rho_w} = \frac{6073.04 \text{ kg/d}}{1.04 \times 1000 \text{ kg/d}}$$

$$V_2 = 5.84 \text{ m}^3/\text{d}$$

→ Detention time = 20 days = Dt

Size of Anaerobic digestion tank

$$V = \left[V_1 - \frac{2}{3} [V_1 - V_2] \right] Dt \quad (\text{FAIR ETAL formula})$$

$$= \left[12.495 - \frac{2}{3} [12.495 - 5.84] \right] \times 20$$

$$V = 161.167 \text{ m}^3 \quad (\text{ANS})$$

- Q.6 (b) (i) A low lying area is to be identified for the municipal solid waste disposal using landfill method for a design life of 35 years. Estimate the volume of landfill site required for a city of having population as four persons per household generating the 2.5 kg of solid waste per capita per day. Survey shows the compacted density of MSW may be assumed as 900 kg/m³ for design. Assuming the ratio of solid waste to cover as 4:1, what volume of cover soil is needed on yearly basis. Total number of households in the city are 5000.
- (ii) Explain the different methods used for land filling in dry areas. Also explain the ways to control the gas and leachate movement in landfills.

① ⇒ Design life of landfill = 35 years [12 + 8 = 20 marks]

Persons in household = $\frac{4}{1}$

Per capita waste generation = 2.5 kg/day

Compacted density of waste = 900 kg/m³

$\frac{\text{Solid waste}}{\text{Cover}} = \frac{4}{1}$

Total no. of households = 5000

Ⓐ Total population of city = 5000 × 4
= 20,000 person

Total waste generated
Per day, $M_w = 20,000 \text{ person} \times 2.5 \text{ kg}$
Person × d

$$M_w = 50,000 \text{ kg/d}$$

$$\begin{aligned} \text{Volume of waste generated} &= \frac{M_w}{\rho_{\text{waste}}} \\ \text{per day} &= \frac{50,000 \text{ kg/d}}{900 \text{ kg/m}^3} \\ &> 55.56 \text{ m}^3/\text{d} \end{aligned}$$

$$\begin{aligned} \rightarrow \text{Total volume of waste} \\ \text{generated per year} &= 55.56 \frac{\text{m}^3}{\text{d}} \times 365 \frac{\text{d}}{\text{yr}} \\ &= 20279.4 \text{ m}^3/\text{yr} \end{aligned}$$

$$\begin{aligned} \rightarrow \text{Volume of cover soil} \\ \text{required per year} &= \frac{1}{4} \times 20279.4 \\ &= 5069.85 \text{ m}^3/\text{yr} \text{ (Ans)} \end{aligned}$$

$$\begin{aligned} \rightarrow \text{Total volume of landfill site required} \\ \text{for design life of 35 years} \\ &= 20279.4 \frac{\text{m}^3}{\text{year}} \times 35 \text{ year} \end{aligned}$$

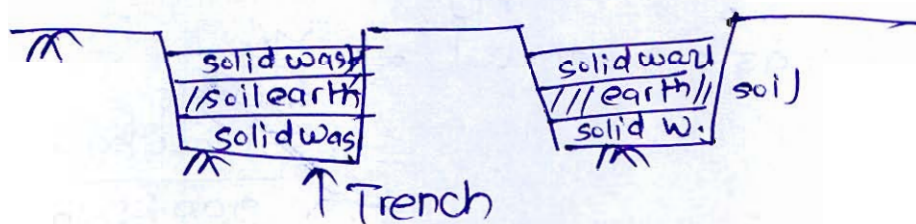
$$\begin{aligned} \text{Volume of} \\ \text{landfill} &= \underline{\underline{709779 \text{ m}^3}} \text{ (Ans)} \end{aligned}$$

11) The methods of land filling in dry areas are

- (i) Trench method
- (ii) Area Method
- (iii) Depression Method

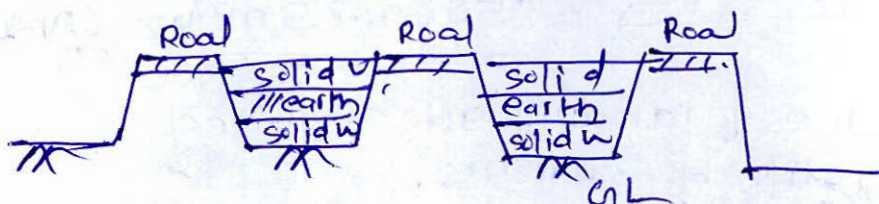
→ (i) Trench method

This method is suitable when adequate earth cover soil is available and water table is at greater depths. Trenches are excavated in area and solid wastes are disposed in layers by layer and separated by soil earth.



Area Method

→ This method is adopted when terrain is not suitable for trench excavation and water table is high. The whole area is divided into no. of subareas called cells by embankment and Road.



12 + 6

Depression Method

This is adopted when natural or artificial depressions are available for landfill. It can be in form of canyons, quarries, borrow pit etc. The techniques used for waste disposal depend on geometry of area, characteristic of waste, hydrology & geology of waste.

- (c) Determine the dimensions of a high-rate trickling filter using the following data: the sewage flow is 3.5 MLD, the recirculation ratio is 1.5, and the BOD of raw sewage is 220 mg/l. The primary settling tank removes 25% of the BOD, and the desired final effluent BOD concentration is 30 mg/l. Take depth of filter as 1.5 m.

Further, determine by what percentage the diameter of the filter would need to be modified if the filter were designed instead as a standard-rate trickling filter to meet the same treatment requirements.

$$\Rightarrow \text{Sewage flow} = 3.5 \text{ MLD} \quad [15 + 5 = 20 \text{ marks}]$$

$$= 3.5 \times 10^6 \frac{\text{L}}{\text{d}} = 3500 \frac{\text{m}^3}{\text{d}}$$

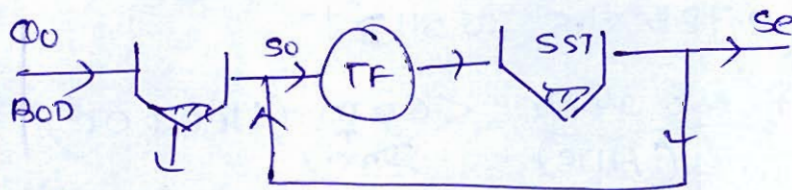
$$\text{Recirculation Ratio, } R = 1.5$$

$$\text{BOD of raw sewage} = 220 \text{ mg/L}$$

$$\text{BOD removed in PST (Primary settling Tank)} = 25\%$$

$$\text{BOD in effluent} = 30 \text{ mg/L}$$

$$\text{Depth of filter, } H = 1.5 \text{ m}$$



$$\eta_{\text{BOD}} = 25\%$$

$$\rightarrow \text{BOD applied to HRTF} = 0.75 \times 220 \text{ mg/L}$$

$$S_0 = 165 \text{ mg/L}$$

$$\text{BOD of effluent} = 30 \text{ mg/L} = S_e$$

$$\text{efficiency of TF} \Rightarrow \eta = \frac{S_0 - S_e}{S_0} \times 100$$

$$= \frac{165 - 30}{165} \times 100 = 81.82\%$$

From NRC formula

$$\eta = \frac{100}{(1 + 0.44 \sqrt{\frac{\text{OLR}}{F}})}$$

where OLR = organic loading rate ($\text{kg/m}^3/\text{d}$)

F = Recirculation factor,

$$F = \frac{1 + R}{(1 + (1 - f)R)^2}, \quad f = \text{treatability factor}$$

$$= 0.9 \text{ assumed}$$

$$= \frac{1 + 1.5}{(1 + 0.9 \times 1.5)^2} = 1.89$$

$$81.82 = \frac{100}{1 + 0.44 \sqrt{\text{OLR}}}$$

$$\text{OLR} = 0.482 \text{ kg/m}^3/\text{d}$$

$$\text{OLR} = \frac{\text{kg of BOD applied to filter}}{\text{Volume of filter}} = \frac{Q_0 S_0}{V}$$

$$\frac{0.482 \text{ kg}}{\text{m}^3 \times \text{d}} = \frac{3.5 \times 10^6 \frac{\text{L}}{\text{d}} \times 165 \frac{\text{mg}}{\text{L}} \times 10^{-6} \frac{\text{kg}}{\text{mg}}}{V}$$

12

$$V = 1198.133 \text{ m}^3$$

depth of filter given, $H = 1.5 \text{ m}$, let ϕD is dia of filter

$$\therefore V = D^2 [0.785H + 0.11D]$$

$$1198.133 = D^2 [0.785 \times 1.5 + 0.11D]$$

$$D = \cancel{28.362 \text{ m}} \quad \underline{28.362 \text{ m}} < 60 \text{ m (Hence ok)}$$

D_{max}

Dimensions of HRTF

$$\rightarrow \text{Dia} = 28.362 \text{ m}$$

$$\text{Depth} = 1.5 + 0.3(\text{FB}) = \underline{1.8 \text{ m}}$$

(b) If the filter is designed as SRTF

$$\rightarrow \eta = \frac{100}{1 + 0.44 \sqrt{\text{OLR}}}$$

$$\text{as } F = \frac{1+R}{(1+0.1R)^2}$$

$$81.82 = \frac{100}{1 + 0.44 \sqrt{\text{OLR}}}$$

$$R = 0 \text{ for SRTF}$$

$$\Rightarrow F = 1$$

$$\text{OLR} = 0.255 \text{ kg/m}^3/\text{d}$$

$$\text{OLR} = \frac{Q_0 S_0}{V}$$

$$0.255 \text{ kg/m}^3/\text{d} = \frac{3.5 \times 10^6 \frac{\text{L}}{\text{d}} \times 165 \times 10^{-6} \frac{\text{kg}}{\text{L}}}{V}$$

$$V^1 = 2264.706 \text{ m}^3 \text{ (modified volume)}$$

$$2264.706 = D^1^2 [0.785 \times 1.5 + 0.011 D^1]$$

$$D^1 = \text{dia of SRTF}$$

$$D^1 = 37.713 \text{ m} < 60 \text{ m OK}$$

$$\% \text{ Change} = \frac{D^1 - D^0}{D^0} \times 100 = \frac{37.713 - 28.362}{28.362} \times 100 = 32.97\% \text{ (Ans)}$$

Dia of HRTF has to be increased by 32.97% if filter is designed as SRTF

- (a) (i) A coagulation-sedimentation water treatment plant treats 45 million litres of water per day. The dosage of filter alum required at the plant is 16 mg/l. The raw water has an alkalinity equivalent to 5 mg/l as CaCO_3 . Determine the annual quantity of filter alum required and the annual quantity of quicklime (containing 85% CaO) required for the plant. The molecular weights of the elements are given as: Al = 27, S = 32, O = 16, H = 1, Ca = 40, and C = 12.
- (ii) Explain the mechanism in brief occurring in slow sand filtration process.

(1) Water treated per day, $Q = 45 \text{ MLD}$ [12 + 8 = 20 marks]

$$\text{Dosage of filter alum} = 16 \text{ mg/L}$$

$$\text{Raw water alkalinity} = 5 \text{ mg/L as } \text{CaCO}_3$$

a) Annual quantity of filter alum

$$= \frac{16 \text{ mg}}{\text{L}} \times 10^{-6} \frac{\text{kg}}{\text{mg}} \times 45 \times 10^6 \frac{\text{L}}{\text{d}} \times \frac{365 \text{ d}}{\text{yr}}$$

$$= 262800 \frac{\text{kg}}{\text{year}} = 262.8 \text{ tonne/year (Ans)}$$

b) ∴ 1 g of alum required 0.45 g of alkalinity as CaCO_3 to treat water by gram equivalence concept.

⇒ 16 mg/L of alum required

$$\text{alkalinity} = 0.45 \times 16 = 7.2 \text{ mg/L as } \text{CaCO}_3$$

Additional alkalinity to be added
in water = $7.2 - 5 = 2.2 \text{ mg/L as CaCO}_3$

→ Amount of quick lime (purity 85% CaO)
required for alkalinity

$$= \frac{2.2 \text{ mg/L}}{\text{Equivalent wt of CaCO}_3} \times \frac{\text{Equivalent wt of CaCO}_3}{0.85} \text{ CaO}$$

$$= \frac{2.2 \text{ mg/L} \times 5}{50} = \frac{2.2 \text{ mg/L} \times 28}{50} \times \frac{1}{0.85}$$

$$= 1.45 \text{ mg/L}$$

Annual quantity of quick lime

$$= 1.45 \frac{\text{mg}}{\text{L}} \times 10^9 \frac{\text{tonne}}{\text{mg}} \times 45 \times 10^6 \frac{\text{L}}{\text{d}} \times \frac{365 \text{ d}}{\text{yr}}$$

$$= \underline{23.816 \text{ tonne/yr (Ans)}}$$

② Mechanism of slow sand filter.

→ Slow sand filter consisting fine gradation
of sand for filtering media. The size of
grains is approx 0.25-0.35 mm.

Slow sand filters provides high efficiency of
removal of solids & aims to produce
turbidity nearly zero in effluent. When
water after ~~flocculation tank~~ is applied PST
treatment applied with turbidity less than
10 mg/L → majority of impurities are blocked on
surface of filter and form swimdecke layer and
very less amount of impurity able to penetrate
whole filter media. The cleaning of slow
sand filter required only scraping of top sand
layer of about 1.5 to 3 cm thickness and for
better efficiency in 2-3 month cleaning is done.

Slow sand filters provide very low discharge rates with rate of filtration about $100-300 \text{ L/hr/m}^2$. They are not able to handle shock loading i.e. variation in discharge rates. They are suitable for rural areas where discharge flow rate requirement is less & no other treatment is available.

12 + 6

Q.7(b) A wastewater treatment plant discharges its treated effluent into a stream at a point designated as A. The characteristics of the stream at a location sufficiently upstream of point A, as well as those of the effluent being discharged, are given below.

		Effluent	Stream
Flow	m ³ /s	0.30	0.65
DO	mg/l	1.5	8.00
temperature	°C	27	23
BOD _{5/20°C}	mg/l	50	2

For the combined mixture of effluent and stream water, assume that the deoxygenation constant K_D at 20°C (base 10) is 0.087 day⁻¹ and the reoxygenation constant K_R at 20°C (base 10) is 0.174 day⁻¹. The equilibrium concentration of dissolved oxygen (C_s) for fresh water at different temperatures is provided below:

Temperature °C	18	20	22	23	24	25	26
C_s (mg/l)	9.54	9.17	8.99	8.83	8.53	8.38	8.22

The average velocity of the stream downstream of the discharge point A is 0.3 m/s. For temperature correction, use coefficients of 1.04 for the deoxygenation constant θ_D and 1.02 for the reoxygenation constant θ_R . Determine:

1. The critical oxygen deficit in the stream, and
2. The location downstream of point A at which this critical deficit occurs.

⇒

	Effluent	Stream
Q (m ³ /s)	0.3	0.65
DO	1.5 mg/L	8 mg/L
T (°C)	27	23
BOD _{5(20°C)}	50 mg/L	2 mg/L

[20 marks]

$K_D(20°C) = 0.087 \text{ day}^{-1}$ (base 10)
 $K_R(10°C) = 0.174 \text{ day}^{-1}$ (base 10)

(A) Dissolved oxygen in River water after mixing

$$\begin{aligned}
 (DO)_{\text{mix}} &= \frac{Q_w \times DO_w + Q_r \times DO_r}{Q_w + Q_r} \\
 &= \frac{0.3 \text{ m}^3/\text{s} \times 1.5 \text{ mg/L} + 0.65 \text{ m}^3/\text{s} \times 8 \text{ mg/L}}{0.3 + 0.65} \\
 &= 5.947 \text{ mg/L}
 \end{aligned}$$

$$\begin{aligned}
 (\text{Temp})_{\text{mix}} &= \frac{Q_w T_w + Q_r T_r}{Q_w + Q_r} \\
 &= \frac{0.3 \text{ m}^3/\text{s} \times 27^\circ\text{C} + 0.65 \frac{\text{m}^3}{\text{s}} \times 23}{0.3 + 0.65} \\
 &= 24.263^\circ\text{C}
 \end{aligned}$$

DO_{sat} = ?

T ^{°C}	DO _{sat} (mg/L)
24	8.53
25	8.38

$$\begin{aligned}
 \text{DO}_{\text{sat}} (T = 24.263^\circ\text{C}) &= 8.53 \frac{(24.263 - 24)}{(25 - 24)} (8.53 - 8.38) \\
 &= 8.4906 \text{ mg/L} \\
 &\approx 8.49 \text{ mg/L}
 \end{aligned}$$

→ Initial oxygen deficit

$$\begin{aligned}
 D_0 &= \text{DO}_{\text{sat}} - (D_0)_{\text{mix}} \\
 &= 8.49 - 5.947 \\
 D_0 &= 2.543 \text{ mg/L}
 \end{aligned}$$

$$\begin{aligned}
 K_D(T^\circ\text{C}) &= K_D(20) [1.04]^{T-20} \quad T > 20 \\
 K_R(T^\circ\text{C}) &= K_R(20) [1.02]^{T-20} \quad T > 20
 \end{aligned}$$

$$\begin{aligned}
 K_D(23^\circ\text{C}) &= 0.087 [1.04]^{23-20} \\
 &= 0.0979 \text{ day}^{-1}
 \end{aligned}$$

$$\begin{aligned}
 K_D(27^\circ\text{C}) &= 0.087 [1.04]^{27-20} \\
 &= 0.1145 \text{ day}^{-1}
 \end{aligned}$$

$$\begin{aligned}
 K_D(24.263^\circ\text{C}) &= 0.087 [1.04]^{24.263-20} \\
 &= 0.1028 \text{ day}^{-1}
 \end{aligned}$$

$$\begin{aligned}
 K_R(24.263^\circ\text{C}) &= 0.174 [1.02]^{24.263-20} \\
 &= 0.189 \text{ day}^{-1}
 \end{aligned}$$

① Ultimate BOD of waste & River

$$(\text{BOD})_w = \frac{(\text{BOD}_5)_{20^\circ\text{C}}}{1 - 10^{-k_{D20} \times 5}} = \frac{50 \text{ mg/L}}{1 - 10^{-0.087 \times 5}}$$

$$= 79.024 \text{ mg/L}$$

$$(\text{BOD})_r = \frac{2 \text{ mg/L}}{1 - 10^{-0.087 \times 5}} = 3.162 \text{ mg/L}$$

Ultimate BOD of River after mixing

$$l_0 = \frac{Q_w (\text{BOD})_w + Q_r (\text{BOD})_r}{Q_w + Q_r}$$

$$= \frac{0.3 \times 79.024 + 0.65 \times 3.162}{0.3 + 0.65}$$

$$l_0 = 27.118 \text{ mg/L}$$

② Critical oxygen deficit

$$F = \frac{K_R}{K_D} = \frac{0.189}{0.1028} = 1.838$$

$$\left[\frac{l_0}{D_c F} \right]^{F-1} = F \left[1 - (F-1) \frac{D_c}{l_0} \right]$$

$$= \left[\frac{27.118}{D_c \times 1.838} \right]^{1.838-1} = 1.838 \left[1 - (1.838-1) \frac{2.543}{27.118} \right]$$

$$D_c = 7.868 \text{ mg/L (Ans)}$$

③ Critical location = ?

$$\therefore D_c = \frac{K_D l_0 e^{-K_D t_c}}{K_R} \Rightarrow 7.868 = \frac{0.1028}{0.189} \times 27.118 e^{-0.1028 t_c}$$

$$t_c (\text{days}) = 6.113 \text{ days}$$

$$\text{Velocity} = 0.3 \text{ m/s}$$

Location of critical deficit beyond point A in

downstream = $V \times t_c$

$$L = \frac{0.3 \text{ m}}{\text{s}} \times \frac{6.113 \times 24 \times 3600 \text{ sec}}{10^3 \frac{\text{m}}{\text{km}}}$$

$$L_c = 158.449 \text{ km (Ans)}$$

- (c) (i) Explain the different type of settling observed in settling tanks of water / Sewage treatment plant.
- (ii) In a rectangular primary settling tank of size 4 m deep and 55 m long, if the horizontal flow velocity is 1.20 cm per sec. What would be the minimum size of particle to be removed effectively. Assume kinematic viscosity of water as $0.01 \text{ cm}^2/\text{sec}$. Specific gravity of the concerned particle is 2.65.

[10 + 10 = 20 marks]

⇒ (i) Based on the concentration of suspended matter and characteristics of particles, settling of particles are classified into four categories :-

I) Type 1 settling

In this settling, particles have little or no tendency to interact with each other or flocculate in dilute suspension. Such particles are called discrete particles. They settle as individual entities and there is no significant interaction betⁿ them.

Ex. Settling in Grit chamber

II) Type 2 settling

In the 2nd type, flocculent particles settle in dilute suspension. Particles agglomerate during settling which causes increase in size, shape and density results in settlement at a faster rate.

Ex. Settling primary sedimentation of wastewater treatment.

III) Type 3 settling

In the 3rd type, flocculent particles settle in intermediate concentration of particles. Due to proximity of particles with each other, they tend to remain at their fixed position with each other and settle as a whole mass rather than individual. This settling is known as zone settling or hindered settling.

Ex. Settling of B₅ sludge in secondary sedimentation tank after ASP.

(iv) Type IV settling

This settling is also known as Compression Settling.

→ In compression settling, ~~Compre~~ concentration of particles becomes very high such that particles are in direct contact with each other and form a structured mass. ~~lower~~ layers support weight of upper layers and any further settling results due to compression of whole mass.

It results in expulsion of water from voids between particles.

Ex. This type of settling generally occur at bottom of SST. ~~Ex~~ ^{like} deep bottom of sludge settlement in SST after ASP.

(ii) Given depth, $H = 4\text{ m}$
length, $L = 55\text{ m}$

Horizontal flow velocity, $V_H = 1.2\text{ cm/sec}$
size of particle $d = ?$

Kinematic viscosity $\nu = 0.01\text{ cm}^2/\text{s} = 0.01 \times 10^{-4}\text{ m}^2/\text{s}$
 $G = 2.68$

$$\therefore Dt = \frac{H}{V_o} = \frac{L}{V_H} = \frac{V}{Q}$$

where $V_o =$ surface
overflow
rate

$$V_o = \frac{H \times V_H}{L} = \frac{4}{55} \times 1.2 = 0.0873\text{ cm/s}$$

assuming the design particle is d_p and which is to be removed (100% \Rightarrow) surface ~~to~~ overflow rate is equal to settling velocity to remove this particle.

$$V_s = 0.0873\text{ cm/s}$$

assuming Stokes law valid

$$v_s = \frac{g}{18} (\rho_s - \rho) \frac{d^2}{\mu}$$

$$0.0873 \times 10^{-2} \frac{\text{m}}{\text{s}} = \frac{9.81 \text{ m/s}^2}{18} \frac{(\rho_s - \rho) d^2}{10^6 \text{ m}^2/\text{s}}$$

$$d = 3.116 \times 10^{-5} \text{ m} = 0.03116 \text{ mm} < 0.1 \text{ mm}$$

$$+ \text{Re (Reynold no.)} = \frac{v_s d}{\mu} = \frac{0.0873 \times 10^{-2} \times 0.03116 \times 10^{-3}}{10^{-6}} = 0.087 < 1$$

dia of particle

$$= 0.03116 \text{ mm (Ans)}$$

$$= 0.087 < 1 \leftarrow \text{Stokes law valid}$$

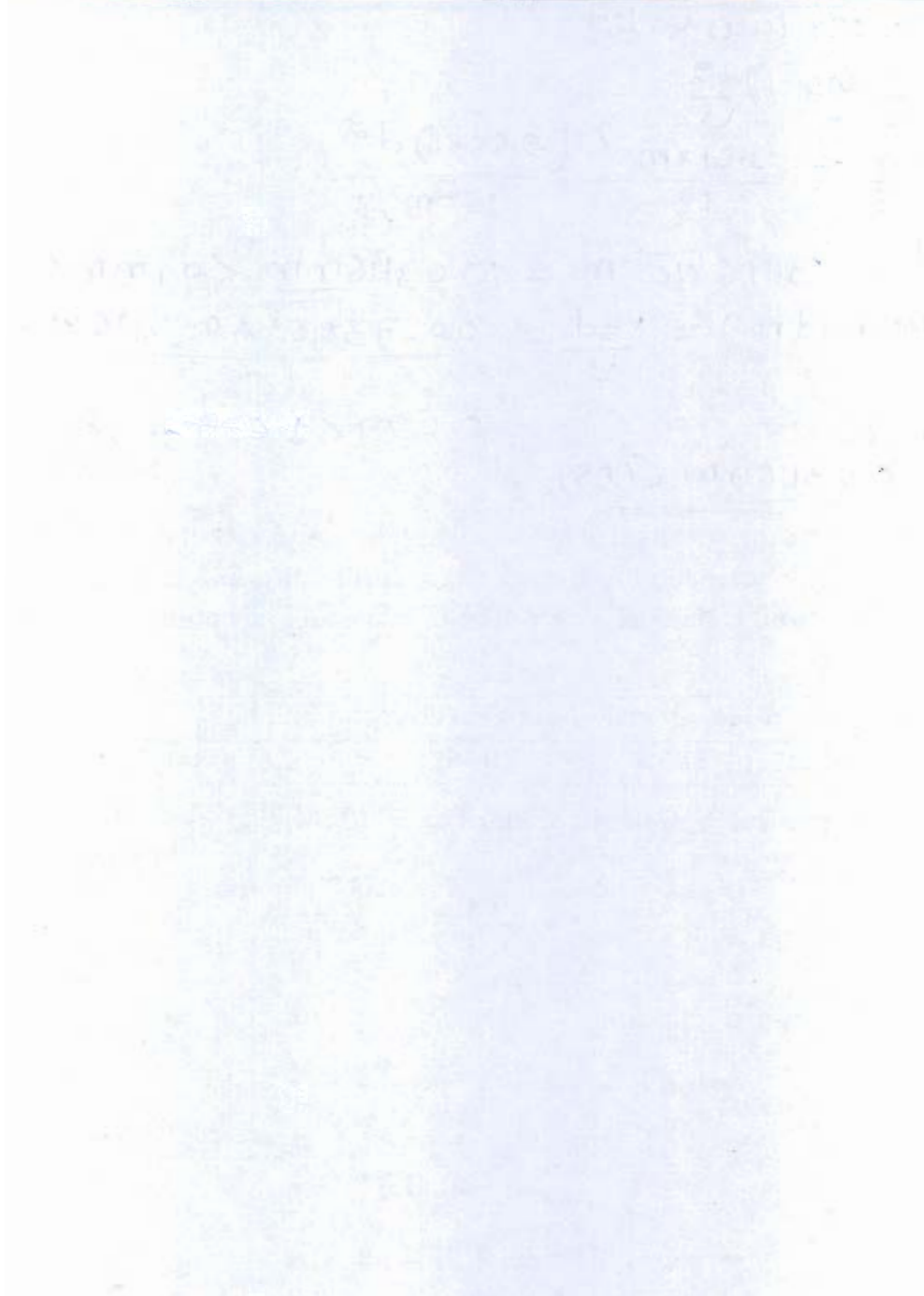
20

1) There is a thermal power plant of total capacity 915 MW with a load factor of 72.5 percent and an efficiency of 40 percent. Determine the amount of particulates, CO_2 and SO_2 that are generated annually if oil is the fuel source. The ultimate analysis of fuel are give below:

Moisture	Ash	Carbon	Hydrogen	Nitrogen+Oxygen	Sulphur
0.3%	0.04%	85.2%	11.3%	0.36%	2.8%

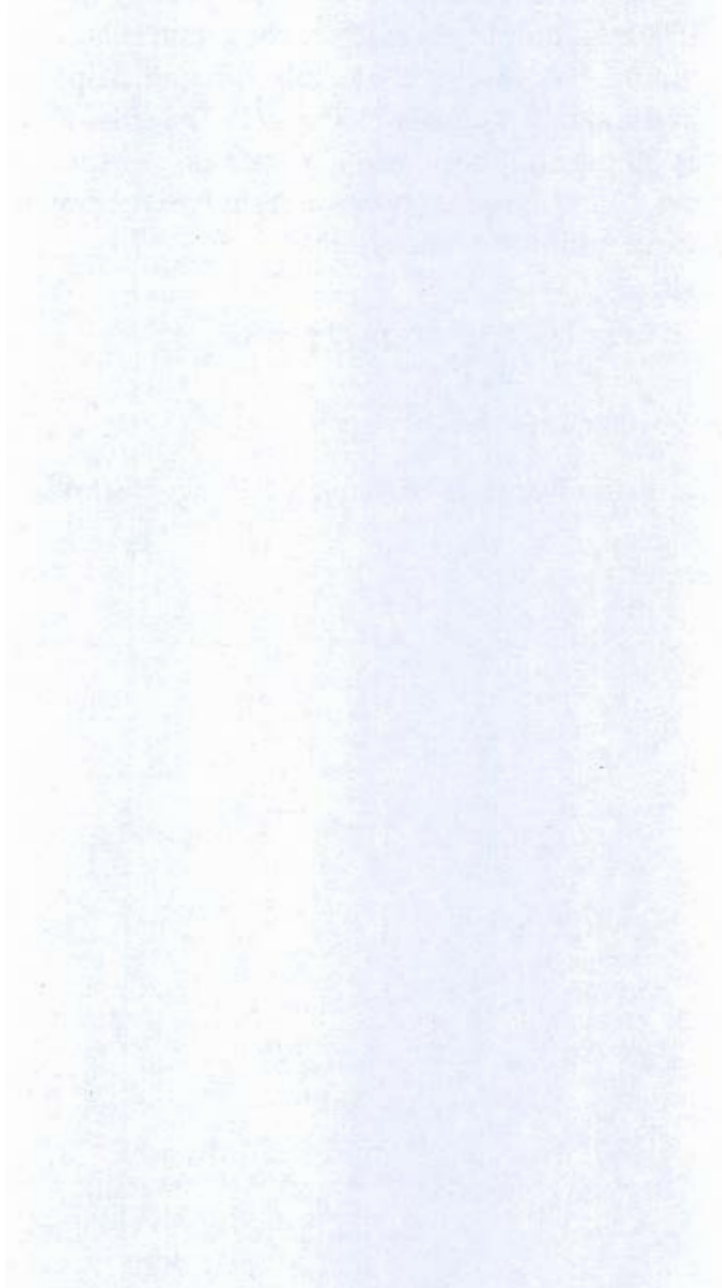
[Assume 80% of ash is particulate, Calorific value of fuel = 40.5MJ/kg]

[20 marks]



- Q) (i) An average operating data for a conventional activated sludge wastewater treatment plant are as follows. The wastewater flow rate is $40,000 \text{ m}^3$ per day and the volume of the aeration tank is $9,500 \text{ m}^3$. The influent BOD concentration is 240 mg/L , while the effluent BOD concentration is 18 mg/L . The mixed liquor suspended solids (MLSS) concentration in the aeration tank is 2480 mg/L . The effluent suspended solids concentration is 30 mg/L . The waste sludge has a suspended solids concentration of $9,700 \text{ mg/L}$, and the quantity of waste sludge withdrawn is 220 m^3 per day. Based on the above information, determine
- Aeration period in hours,
 - F/M ratio expressed as kg BOD per day per kg MLSS,
 - Sludge age in days.
 - Percentage efficiency of BOD removal
- (ii) Discuss the advantage and disadvantages of Activated Sludge treatment.

[12 + 8 = 20 marks]



- Q.8 (c) (i) Calculate the storage capacity required to meet the water demand given below, assuming that the inflow to the service reservoir is maintained at a uniform rate throughout the 24-hour period.

Time	00-04	04-08	08-12	12-16	16-20	20-24
Demand in million litres	0.36	0.86	1.70	1.36	0.74	0.42

- (ii) Write a short note over Water distribution network and it's type.

[12 + 8 = 20 marks]



○○○○

Space for Rough Work

Space for Rough Work
