

WORKDOOK 2025



Detailed Explanations of Try Yourself Questions

Instrumentation Engineering

Communication



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Amplitude Modulation

Detailed Explanation of Try Yourself Questions

T1. Sol.

The signal $s(t) = A_{C}[1 + \mu \cos(\omega_{m}t)] \cos(\omega_{c}t)$ The signal can be represented as $s(t) = \operatorname{Re}\left[A_{C}e^{j\omega_{c}t} + \frac{A_{C}\mu}{2}(e^{j(\omega_{c}+\omega_{m})t} + e^{j(\omega_{c}-\omega_{m})t})\right]$ $s(t)|_{\operatorname{complex}} = \left[A_{C}e^{j\omega_{c}t} + \frac{A_{C}\mu}{2}(e^{j(\omega_{c}+\omega_{m})t} + e^{j(\omega_{c}-\omega_{m})t})\right]$ $s(t)|_{c} = \left[s(t)_{c}e^{-j\omega_{c}t}\right]$ (where $e^{j(t)}$ the correction of $e^{j(t)}$ the correction of $e^{j(t)}$

(where, $s(t)|_{c}$ = the complex signal s(t) and $s(t)|_{ce}$ = the complex low pass equal of the signal s(t))

$$s(t)|_{ce} = A_C + \frac{A_C \mu}{2} [\cos \omega_m + j \sin \omega_m t] + \frac{A_C \mu}{2} [\cos \omega_m - j \sin \omega_m t]$$

Putting the conditions given in the questions we get:

$$S(t)|_{ce} = 1 + \frac{1}{8} [\cos \omega_m + j \sin \omega_m t] + \frac{1}{4} [\cos \omega_m - j \sin \omega_m t]$$
$$S(t)|_{ce} = 1 + \frac{3}{8} \cos \omega_m t - j \frac{1}{8} \sin(\omega_m t)$$
$$A \text{ envelop} = \left[\left(1 + \frac{3}{8} \cos(\omega_m t) \right)^2 + \left(\frac{1}{8} \sin(\omega_m t) \right)^2 \right]^{\frac{1}{2}}$$

T2. Sol.

...

Expression for AM signal

$$V_{AM}(t) = A_C \cos \omega_c t + A_C m_a \cos(\omega_c + \omega_m)t + A_C m_a \cos(\omega_c - \omega_m)t$$

$$P_C = 100 = \frac{A_C^2}{2}$$

$$A_C = 14.14 \text{ V}$$

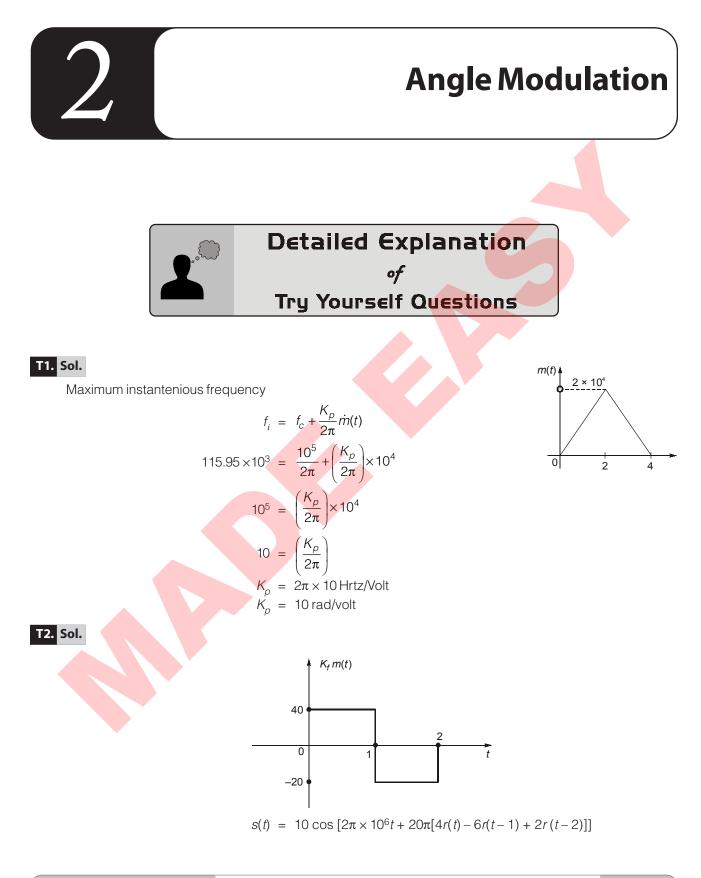
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 $\eta = \frac{m_a^2}{2 + m_a^2} = 40\%$ Also $0.8 + 0.4 m_a^2 = m_a^2$ $m_a = 1.154$ $B = A_C m_a/2 = 8.16$ or *:*.. T3. Sol. Þ $25 \, k\Omega$ $RC \leq \frac{1}{\omega_n} \frac{\sqrt{1-\mu^2}}{\mu}$ $C \leq \frac{1}{R\omega_n} \frac{\sqrt{1-\mu^2}}{\mu}$ $C \leq \frac{1}{10^4 \times 2\pi \times 25 \times 10^3} \cdot \frac{\sqrt{1 - (0.5)^2}}{0.5}$ $C \leq 1.1 \,\mathrm{nF}$ Т4. (с) $x(t) = m(t) + \cos \omega_c t$ $y(t) = 4(m(t) + \cos\omega_c t) + 10\left[m^2(t) + \cos^2\omega_c t + 2m(t)\cos\omega_c t\right]$ $= 4m(t) + 10m^{2}(t) + 4\cos\omega_{c}t + \frac{10}{2} + \frac{10}{2}\cos 2\omega_{c}t + 20m(t)\cos\omega_{c}t$ after passing through filter $y(t) = 4\cos\omega_c t + 20m(t)\cos\omega_c t$ $= 4[1 + 5 m(t)] \cos \omega_c t$ $\mu = 5 \times M$ $0.8 = 5 \times M$ $M = \frac{0.8}{5} = 0.16$





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Standard FM expression is given by:

$$s(t) = A_c \cos \left[2\pi fct + 2\pi k_f \int m(t)dt \right]$$

$$2\pi k_f \int m(t)dt = 20\pi \left(4r(t) - 6r(t-1) + 2r(t-2)\right)$$

$$k_f m(t) = 10[4 \ u(t) - 6u \ (t-1) + 2r \ (t-2)]$$

$$\Delta f = \max \left| k_f m(t) \right| = 40 \text{ Hz}$$

T3. Sol.

Maximum frequency deviation

$$\Delta f_{\max} = \frac{K_p}{2\pi} \left| \frac{d}{dt} m(t) \right|_{\max} = \frac{K_p}{2\pi} 2t e^{-t^2}$$
$$= \frac{8000}{2\pi} \cdot 2 \cdot \frac{1}{\sqrt{2}} \cdot e^{-1/2}$$
$$= 3.43 \text{ kHz}$$

$$\left(\because \max 2 + e^{-t^2} \text{ is at } t = \frac{1}{\sqrt{2}} \right)$$

T4. Sol.

Compairing the equation with the standard equation.

:..

$$s(t) = A \cos[\omega_{c}t + k_{p}m(t)]$$

$$k_{p}m(t) = 0.1 \sin(10^{3}\pi t)$$

$$m(t) = \frac{0.1}{k_{p}}\sin(10^{3}\pi t)$$

$$= 0.01 \sin(10^{3}\pi t)$$

Similarly

$$s(t) = A\cos\left[\omega_{c}t + K_{f}\int m(t)dt\right]$$

$$\int m(t) dt = 0.1 \sin(10^3 \pi t)$$

$$\int m(t) dt = \frac{0.1}{10\pi} \sin(10^3 \pi t) = \frac{0.1 \times 10^3 \pi}{10\pi} \cos(10^3 \pi t) = 10 \cos(10^3 \pi t)$$

T5. Sol.

 $A_m = 5 \text{ V}, f_m = 100 \text{ Hz} \} \Delta f = k_f A_m = 1 \text{ kHz}$ $A_m = 10 \text{ V}, f_m = 50 \text{ Hz} \} \Delta f = 2 \text{ kHz}$ To get $\Delta f = 30 \text{ kHz}$ frequency multiplication factor should be 15.

T6. (a)

$$BW = 2[\beta + 1]f_m$$

$$\beta = k_p A_m = 5$$

$$A_m \text{ is doubled} \Rightarrow \beta = 10 ; f_m = \frac{1}{2} \text{ kHz}$$

$$BW = 2[10 + 1] \cdot \frac{1}{2} = 11 \text{ kHz}$$



T7. Sol.

$$\beta_{f} = \frac{k_{f} \max \{m(t)\}}{f_{m}} = \frac{100 \text{ k} \times 1}{1 \text{ k}} = 100$$

$$BW_{f} = 2 (100 + 1) 1 \text{ k} = 202 \text{ kHz.}$$

$$\beta_{p} = k_{p} \max \{m(t)\}$$

$$= 10 \times 1 = 10$$

$$BW_{p} = 2 (10 + 1) 1 \text{ k} = 22 \text{ kHz}$$

Bandwidth required for channel

T8. Sol.

The phase modulated signal can be given by,

$$s(t) = A_c \cos[2\pi f_c t + k_p m(t)] = A_c \cos[\theta(t)]$$

The instantaneous frequency of the modulated signal,

$$f_i = \frac{1}{2\pi} \frac{d\theta(t)}{dt} = f_c + \frac{k_p}{2\pi} \frac{dm(t)}{dt}$$

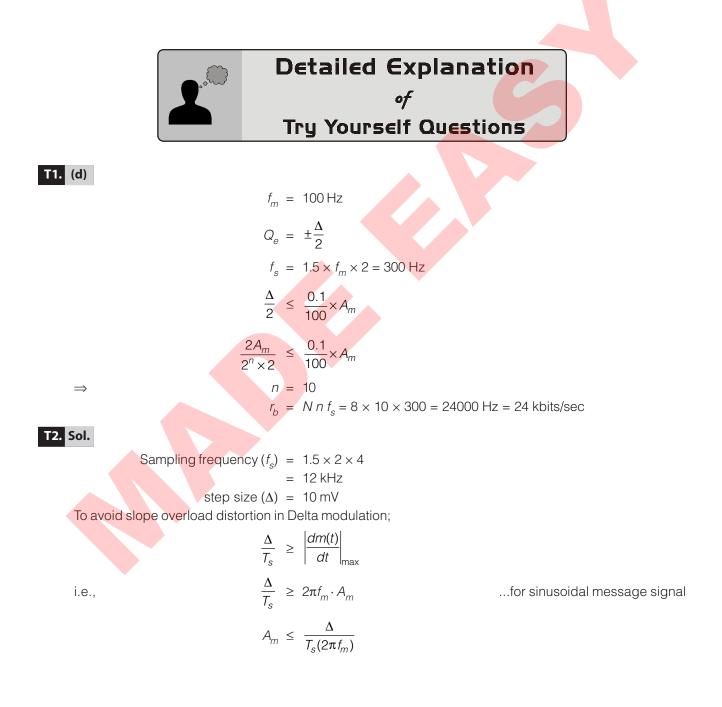
Given that,

$$m(t) = 100 \operatorname{sinc}(1000t) \, \mathrm{V} = 100 \frac{\operatorname{sin}(1000\pi t)}{1000\pi t}$$

$$\frac{dm(t)}{dt} = 100 \left[\frac{1000\pi \cos(1000\,\pi t)}{1000\,\pi t} - \frac{\sin(1000\,\pi t)}{1000\,\pi t^2} \right]$$

At
$$t = 1 \text{ ms}$$
,
So,
 $f_i = f_c + \frac{1}{2\pi}(-10^5 k_p) = 100 - \frac{100 \times 2}{2\pi} \text{ kHz}$
 $= 100 - \frac{100}{\pi} \text{ kHz} = 68.17 \text{ kHz}$

Sampling and Pulse Code Modulation





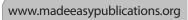
$$(A_m)_{\text{max}} = \frac{\Delta}{T_s(2\pi f_m)} = \frac{\Delta \cdot f_s}{2\pi f_m}$$
$$= \frac{10 \times 10^{-3} \times 12 \times 10^3}{2\pi \times 10^3} = 19.09 \times 10^{-3} \approx 19.1 \text{ mV}$$

T3. (c)

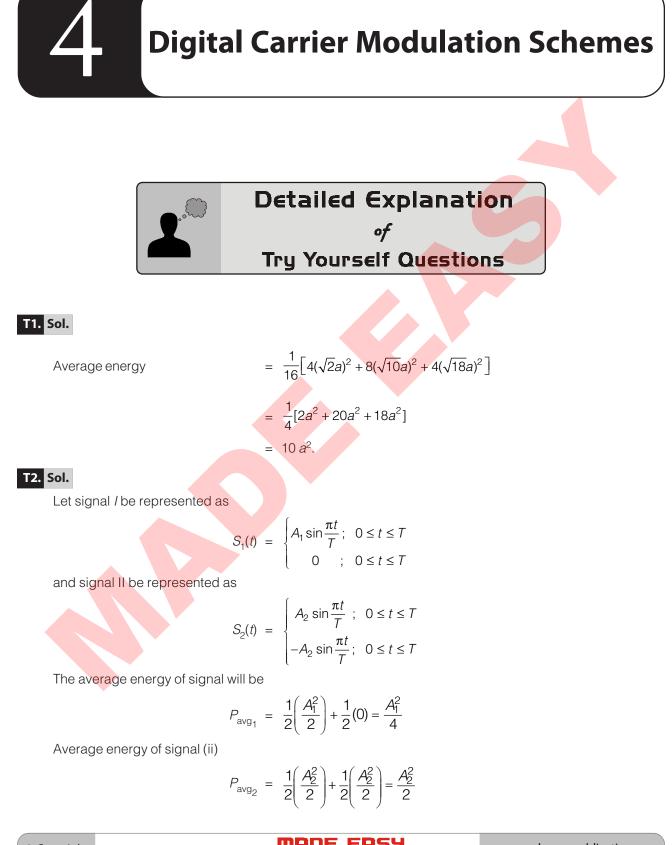
To prevent slope overload

$$\delta f_{s} \geq \max \left| \frac{dm(t)}{dt} \right|$$
$$\delta \times 200 \times 10^{3} \geq 2\pi A_{m} f_{m}$$
$$2 \times \pi \times (10 \times 10^{3})$$

$$\delta \geq \frac{2 \times \pi \times (10 \times 10^3) \times \frac{1}{2}}{200 \times 10^3}$$
$$\delta \geq 0.157 \text{ Volts}$$



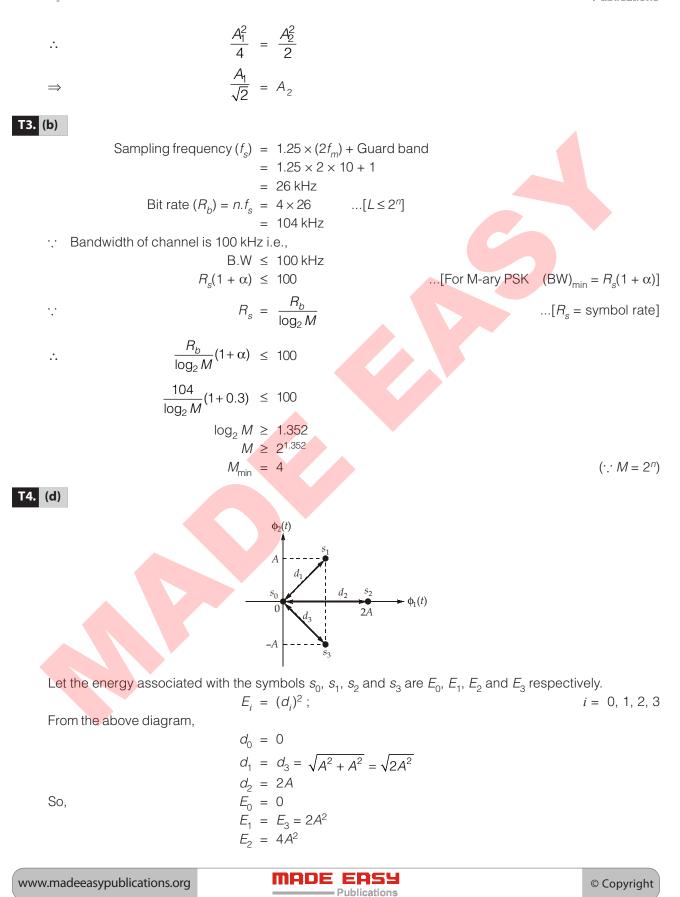




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The average symbol energy of the modulation scheme can be given as,

 $E_s = \sum_{i=0}^{3} E_i P(s_i)$; $P(s_i) = \text{probability of occurrence of the symbol } s_i$ $= 0(0.3) + 2A^2(0.2) + 4A^2(0.4) + 2A^2(0.1)$ $= (0.4 + 1.6 + 0.2)A^2$ $= 2.2 A^2$

