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## Electrical Machines (Synchronous Machine)

### ELECTRICAL ENGINEERING

Date of Test : 05/08/2023

#### ANSWER KEY >

- |        |         |         |         |         |
|--------|---------|---------|---------|---------|
| 1. (c) | 7. (b)  | 13. (b) | 19. (c) | 25. (d) |
| 2. (a) | 8. (b)  | 14. (b) | 20. (a) | 26. (b) |
| 3. (c) | 9. (c)  | 15. (a) | 21. (a) | 27. (c) |
| 4. (c) | 10. (b) | 16. (a) | 22. (c) | 28. (c) |
| 5. (d) | 11. (a) | 17. (b) | 23. (c) | 29. (b) |
| 6. (b) | 12. (b) | 18. (d) | 24. (a) | 30. (a) |

## DETAILED EXPLANATIONS

1. (c)

$$\text{Frequency, } f = \frac{PN}{120} = \frac{4 \times 1500}{120} = 50 \text{ Hz}$$

$$\begin{aligned} \text{Total number of stator conductor} &= \text{Number of slots} \times \text{conductor per slot} \\ &= 80 \times 6 = 480 \end{aligned}$$

$$\text{Stator conductor per phase, } Z_p = \frac{480}{3} = 160$$

$$\text{Winding factor, } k_w = 0.98$$

$$\begin{aligned} \text{Generated voltage per phase, } E_p &= 2.22 \times k_w \times f \times \phi \times Z_p \\ &= 2.22 \times 0.98 \times 50 \times 0.04 \times 160 \\ &= 696.19 \text{ V} \end{aligned}$$

$$\text{Generated line voltage, } E_L = \sqrt{3}E_p = 1205.83 \text{ V}$$

2. (a)

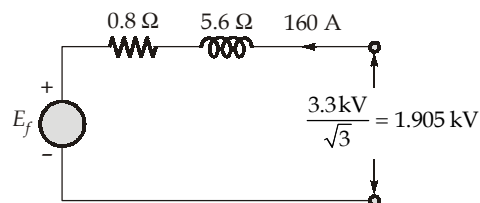
Given,

$$\text{Synchronous impedance, } X_s = 0.8 + j5.6 = 5.656 \angle 81.86^\circ \Omega$$

$$\text{Per phase voltage, } V_p = \frac{\text{Rated line voltage}}{\sqrt{3}} = \frac{3.3 \text{ kV}}{\sqrt{3}} = 1.905 \text{ kV}$$

$$\begin{aligned} \vec{E}_{f \text{ phase}} &= 1.905 - 5.656 \angle 81.86^\circ \times 0.16 \angle -36.9^\circ \\ &= 1.905 - 0.90496 \angle 44.96^\circ \\ &= 1.417 \angle -26.82^\circ \text{ kV or } 2.454 \text{ kV (line)} \end{aligned}$$

We can draw per phase diagram,



Mechanical power developed,

$$\begin{aligned} P_{\text{mech (dev)}} &= 3E_f I_p \cos(\phi + \delta) \\ &= 3 \times 1.417 \times 160 \cos(-36.9^\circ + 26.82^\circ) \\ &= 669.66 \text{ kW} \end{aligned}$$

$$\text{Shaft power output} = 669.66 - 30 = 639.66 \text{ kW}$$

$$\text{Power input} = \sqrt{3} \times 3.3 \times 160 \times 0.8 = 731.5 \text{ kW}$$

$$\eta = \frac{\text{Shaft power output}}{\text{Total input}} = \frac{639.66}{731.5} \times 100 = 87.44\%$$

**Alternate Solution :**

$$\begin{aligned} \text{Power input} &= \sqrt{3} \times 3.3 \times 160 \times 0.8 \\ &= 731618.26 = 731.618 \text{ kW} \end{aligned}$$

$$\begin{aligned} \text{Copper loss} &= 3I^2R = 3 \times (160)^2 \times R \\ &= 61.44 \text{ kW} \end{aligned}$$

$$\text{Power output} = 640.178 \text{ kW}$$

$$\eta = \frac{640.178}{731.618} \times 100 = 87.44\%$$

3. (c)

We know, terminal voltage,  $V_t = 1 \text{ p.u.}$

$$I_a = 1 \text{ p.u. } 0.8 \text{ p.f. lagging}$$

$$\phi = \cos^{-1} 0.8 = 36.86^\circ$$

Also,

$$X_d = 0.8 \text{ p.u.}$$

$$X_q = 0.6 \text{ p.u.}$$

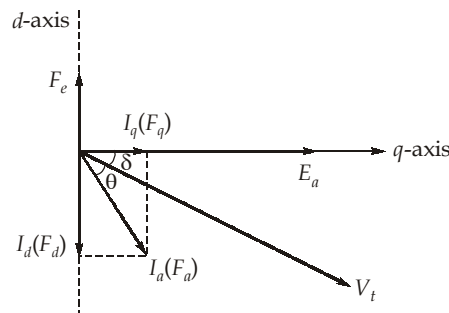
$$\tan \psi = \frac{V_t \sin \phi + I_a X_q}{V_t \cos \phi + I_a X_d} = \frac{1 \times 0.6 + 0.6 \times 1}{1 \times 0.8 + 0} = 1.5$$

$$\psi = \tan^{-1} (1.5) = 56.309^\circ$$

$$\begin{aligned} \text{Power angle, } \delta_1 &= \psi - \phi = 56.309^\circ - 36.86^\circ \\ &= 19.449^\circ \end{aligned}$$

$$\begin{aligned} E_f &= V_t \cos \delta + I_d X_d + I_a r_a = V_t \cos \delta + (I_a \sin \psi) X_d \\ &= 1 \times \cos 19.449 + (1 \times \sin 56.309) \times 0.8 \\ &= 0.9429 + 0.66563 \\ &= 1.60853 \text{ p.u.} \end{aligned}$$

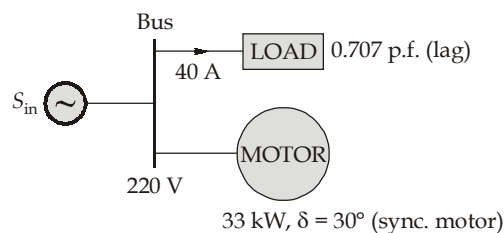
4. (c)



Thus by phasor we can conclude that

- $F_e$  leads  $F_a$  by angle  $(90 + \theta + \delta)$
- $F_q$  leads  $F_a$  by angle  $(\delta + \theta)$
- $F_d$  lags  $F_a$  by angle  $(90 - (\delta + \theta))$
- $F_e$  leads  $V_t$  by angle  $(90 + \delta)$ .

5. (d)



$$\begin{aligned} \vec{S}_{\text{Load}} &= \sqrt{3} \times 220 \times 40 \times \angle \cos^{-1}(0.707) \\ &= 15.242 \angle 45^\circ \text{ kVA} \\ &= (10.78 + j10.78) \text{ kVA} \end{aligned}$$

Using

$$\vec{S}_{\text{motor}} = P_{\text{motor}} + jQ_{\text{motor}}$$

$$P_{\text{motor}} = 33 \text{ kW}$$

$$P_{\text{motor}} = \frac{E_f \times 220}{1.27} \sin 30^\circ = 33 \times 10^3$$

$$E_f = (\sqrt{3} \times 220) = 381 \text{ V (L-L)}$$

$$Q_{\text{motor}} = \frac{220}{1.27} (-381 \cos 30^\circ + 220) = -19.047 \text{ kVAR (leading)}$$

$$\vec{S}_{\text{motor}} = (33 - j19.047) \text{ kVA}$$

$$\vec{S}_{\text{in}} = \vec{S}_{\text{motor}} + \vec{S}_{\text{Load}}$$

$$= (33 + 10.48) + j(10.78 - 19.047)$$

$$= 43.78 - j8.267$$

$$= 45.55 \angle -10.70^\circ \text{ kVA}$$

Power factor =  $\cos(-10.70) = 0.9826$  leading

6. (b)

At maximum power conditions,

$$\delta = \theta_s$$

$$\delta = \cos^{-1} \left[ \frac{0.4}{8} \right] = \cos^{-1}[0.05] = 87.134^\circ$$

$$E_f \angle \delta = V_t \angle 0 + I_a Z_s$$

$$E_f \text{ (per phase)} = \frac{12000}{\sqrt{3}} = 6928.20 \text{ V}$$

$$V_t \text{ (per phase)} = \frac{11000}{\sqrt{3}} = 6350.852 \text{ V}$$

$$E_f \cos \delta + j E_f \sin \delta = V_t + I_a \angle -\phi \cdot Z_s \angle \theta_s$$

$$= V_t + I_a Z_s \angle \theta_s - \phi$$

$$E_f \cos \delta + j E_f \sin \delta = V_t + I_a Z_s \cos(\theta_s - \phi) + j I_a Z_s \sin(\theta_s - \phi)$$

Comparing real and imaginary part,

$$E_f \cos \delta = V_t + I_a Z_s \cos(\theta_s - \phi)$$

$$E_f \sin \delta = I_a Z_s \sin(\theta_s - \phi)$$

$$6928.20 \times \cos 87.134 = 6350.85 + 8 I_a \cos(\theta_s - \phi)$$

$$346.411 = 6350.85 + 8 I_a \cos(\theta_s - \phi)$$

$$8 I_a \cos(\theta_s - \phi) = -6004.438$$

$$I_a \cos(\theta_s - \phi) = -750.554 \quad \dots(i)$$

Also  $8 I_a \sin(\theta_s - \phi) = 6928.20 \times \sin 87.134$

$$8 I_a \sin(\theta_s - \phi) = 6919.534$$

$$I_a \sin(\theta_s - \phi) = 864.941 \quad \dots(ii)$$

By squaring and adding equation (i) and (ii),

$$I_a = 1145.187 \text{ A}$$

Using equation (i),

$$I_a \cos(\theta_s - \phi) = -750.554$$

$$\cos(\theta_s - \phi) = -0.65539$$

$$\theta_s - \phi = 130.949$$

$$87.134 - \phi = 130.949$$

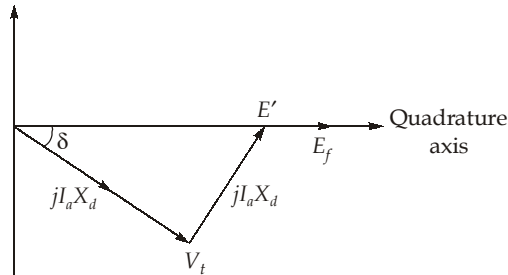
$$\phi = -43.815^\circ$$

$$\cos \phi = 0.7215$$

7. (b)

Power angle is the angle between  $E_f$  and  $V_t$

As  $E'$  and  $E_f$  are in phase, angle between  $E'$  and  $V_t$  is also equal to power angle,  $\delta$



Quadrature axis function,

$$I_a = 1 \angle 0^\circ \text{ p.u.}$$

$$X_q = 1.2 \text{ p.u.}$$

$$E' = V_t + jI_a X_q = 1 + j1 \times 1.2 = 1.562 \angle 50.19^\circ \text{ A}$$

$$\delta = 50.194^\circ$$

8. (b)

Emf equation synchronous motor is given as

$$\vec{E} = \vec{V}_t - \vec{I}_a \vec{Z}_s$$

Given that,

$$\vec{V}_t = 1 \angle 0^\circ \text{ p.u.}, \vec{I}_a = 1 \angle 90^\circ \text{ p.u.}, \vec{Z}_s = 0.5 \angle 90^\circ \text{ p.u.}$$

$$\vec{E} = 1 \angle 0^\circ - (1 \angle 90^\circ) \times (0.5 \angle 90^\circ)$$

$$= 1 - 0.5 \angle 180^\circ$$

$$\vec{E} = 1 + 0.5 \angle 0^\circ = 1.5 \text{ p.u.}$$

9. (c)

Given that,

$$V_t = 1.0 \text{ pu}, I_a = 1.0 \text{ pu}, 0.8 \text{ pf lagging}$$

$$\phi = \cos^{-1} 0.8 = 36.9^\circ$$

$$x_d = 0.8 \text{ pu}, x_q = 0.5 \text{ pu}$$

$$\tan \psi = \frac{V_t \sin \phi + I_a x_q}{V_t \cos \phi + I_a r_a} = \frac{1 \times 0.6 + 1 \times 0.5}{1 \times 0.8 + 0} = \frac{11}{8}$$

$$\psi = \tan^{-1} \left( \frac{11}{8} \right) = 53.97^\circ \simeq 54^\circ$$

Power angle,

$$\delta = \psi - \phi = 54^\circ - 36.9^\circ = 17.1^\circ$$

10. (b)

As we know,

$$I_{sc} \propto \frac{E_f}{X_s} \propto \frac{I_f \times f}{f} \quad (\because I_{sc} \propto I_f)$$

$$I_{sc2} = I_{sc1} \times \frac{I_{f2}}{I_{f1}} = 20 \times \frac{1.5}{1} = 30 \text{ A}$$

11. (a)

Since winding is double layer,

So, No. of coils = No. of slots

$$\text{No. of coils} = 36$$

Since each coil is passes 8 turns,

So total number of turns =  $36 \times 8 = 288$  turns

$$\text{Turns per phase} = \frac{\text{Total no. of turns}}{\text{No. of phases}} = \frac{288}{2} = 144 \text{ Turns/phase}$$

$$m = \frac{\text{Slot}}{\text{Pole} \times \text{Phase}} = \frac{36}{6 \times 2} = 3$$

$$\beta = \frac{180^\circ \times \text{Poles}}{\text{Slots}} = \frac{180^\circ \times 6}{36} = 30^\circ$$

$$\text{Distribution factor, } K_d = \frac{\sin\left(\frac{m\beta}{2}\right)}{m \sin\left(\frac{\beta}{2}\right)} = \frac{\sin(45^\circ)}{3 \sin(15^\circ)} = 0.91$$

$$\begin{aligned} \text{Emf per phase} &= 4.44 \phi_m f N_{ph} K_d = 4.44 \times 0.015 \times 50 \times 144 \times 0.91 \\ &= 436.36 \text{ volts/phase} \end{aligned}$$

$$E_{L(\text{rms})} = \sqrt{2} E_{\text{ph}(\text{rms})} = \sqrt{2} \times 436.36 = 617.11 \text{ volts}$$

12. (b)

$$\vec{I}_a = 1 \angle 36.86 \text{ p.u.}$$

$$\vec{V}_t = 1 \text{ p.u.}$$

$$\vec{Z}_s = j0.6 \text{ p.u.}$$

$$\begin{aligned} \vec{E}_f &= \vec{V}_t - \vec{I}_a \vec{Z}_s = 1 \angle 0 - 0.6 \angle 126.86^\circ \\ &= 1.44 \angle -19.44^\circ \text{ p.u.} \end{aligned}$$

$$\therefore \begin{aligned} E_f &= 1.44 \text{ p.u.}, \\ \delta &= -19.44^\circ \end{aligned}$$

As we know,

$$\text{Ful-load torque} = (\text{Maximum torque}) \cdot \sin \delta$$

$$\frac{\text{Maximum torque}}{\text{Full load torque}} = \frac{1}{\sin \delta} = \frac{1}{\sin 19.44} = 3.00$$

**Hint:** The ratio of two torque of a single machine can't be negative, don't put  $\delta$  to  $-\delta$ .

13. (b)

$$375 = \frac{120xf}{16} \Rightarrow f = 50 \text{ Hz}$$

$$\text{Slots per pole} = \frac{144}{16} = 9$$

$$\text{Slots per pole per phase, } m = \frac{144}{16 \times 3} = 3$$

$$\beta = \frac{180^\circ}{\text{slots per pole}} = 20^\circ$$

$$k_d = \frac{\sin \frac{m\beta}{2}}{m \sin \frac{\beta}{2}} \Rightarrow k_d = \frac{0.5}{3 \times 0.174} = 0.96$$

$$Z = \text{number of conductors in series per phase} = \frac{144 \times 10}{3} = 480$$

$$\begin{aligned} E_{\text{line}} &= \sqrt{3} \times 4.44 f N_{ph} \phi_m k_d \\ &= \sqrt{3} \times 4.44 \times 0.96 \times 0.03 \times \frac{480}{2} \times 50 \\ &= 2657.76 \text{ V} \end{aligned}$$

14. (b)

$$P_{sy} = \frac{EV}{X_s} \cos \delta$$

where  $P_{sy}$  = symmetrical power coefficient

$$P_{sy} \propto \text{stability} \propto \text{excitation}$$

At 'Q' the excitation is more than at 'P'.

So it is more stable at Q.

15. (a)

$$Z_{s(\text{adjusted})} = \frac{V_{\text{rated}} / \sqrt{3}}{I_{sc}} \quad \left| \text{At } I_f \text{ corresponding to } V_{oc} = V_{\text{rated}} \right.$$

Rated armature current,

$$\sqrt{3} V_{\text{rated}} I_{a(\text{rated})} = 10 \text{ MVA}$$

$$I_{a(\text{rated})} = \frac{10 \times 10^3}{\sqrt{3} \times 13.8} = 418.4 \text{ A}$$

$$I_{f(\text{rated})} = 842 \text{ A}$$

$$I_{sc} = \frac{418.4}{226} \times 842 = 1558.8 \text{ A}$$

$$Z_{s(\text{adjusted})} = \frac{13.8 \times 10^3 / \sqrt{3}}{1558.8} = 5.11 \Omega$$

$$\begin{aligned} X_{s(\text{adjusted})} &= \sqrt{Z_{s(\text{adjusted})}^2 - R_a^2} \\ &= \sqrt{5.11^2 - 0.75^2} = 5.054 \Omega \end{aligned}$$

$$X_{s(\text{pu})} = 5.054 \times \frac{10}{(13.8)^2} = 0.2654$$

16. (a)

$$\begin{aligned} Z_a &= (0.5 + j2) \Omega \\ &= 2.06 \angle 75.96^\circ \Omega; V_t = 415 \text{ V}, E_f = 500 \text{ V} \end{aligned}$$

$$\text{Maximum developed power} = \frac{E_f V_t}{Z_s} - \frac{E_f^2}{Z_s^2} \times R_a$$

$$\begin{aligned} P_{\text{dev}} &= \frac{500 \times 415}{2.06} - \left( \frac{500}{2.06} \right)^2 \times 0.5 \\ &= 71.272 \text{ kW} \end{aligned}$$

This is per phase power.

$$\begin{aligned} \therefore \text{Shaft power output} &= [3 \times 71.272 - 1] \text{ kW} \\ &= 212.81 \text{ kW} \end{aligned}$$

17. (b)

$$\begin{aligned} \text{Power (P)} &= \frac{VE_f}{X_s} \sin \delta \\ 0.75 &= \frac{1 \times 1.25}{0.7} \sin \delta \\ \delta &= 24.83^\circ \end{aligned}$$

Current is given by,

$$\begin{aligned} \vec{I} &= \frac{\vec{E}_f - \vec{V}}{jX} = \frac{1.25 \angle 24.83^\circ - 1 \angle 0^\circ}{j0.7} \\ I &= 0.77 \angle -14.36^\circ \end{aligned}$$

$$\text{Phase angle, } \phi = 14.36^\circ$$

$$\text{Power factor} = \cos \phi = 0.9688 \text{ (lagging)}$$

18. (d)

$$\text{Excitation emf, } (\vec{E}_f) = \vec{V} + \vec{I}_a Z_s$$

$$\text{Armature current, } I_a = \frac{20 \times 10^3}{\sqrt{3} \times 400} = 28.87 \text{ A}$$

$$\vec{E}_f = \frac{400}{\sqrt{3}} + (28.87 \angle 36.87^\circ) \times (0.5 + j3)$$

$$\vec{E}_f = 205.85 \angle 22.25^\circ \text{ V}$$

$$\begin{aligned} \text{Voltage regulation} &= \frac{|E_f| - |V|}{|V|} \times 100 \\ &= \frac{205.85 - \left( \frac{400}{\sqrt{3}} \right)}{\left( \frac{400}{\sqrt{3}} \right)} \times 100 = -10.86\% \end{aligned}$$



19. (c)

Power angle can be calculated as,

$$\vec{E}'_f = \vec{V}_t + j\vec{I}_a X_q$$

As rated load is being supplied at unity power factor,

$$\therefore \vec{I}_a = 1 \angle 0^\circ \text{ p.u.}$$

$$\begin{aligned} \vec{E}'_f &= 1.0 \angle 0^\circ + j1.0 \angle 0^\circ (0.8) \\ &= 1.28 \angle 38.65^\circ \text{ p.u.} \end{aligned}$$

$$\therefore \text{Power angle, } \delta = 38.65^\circ$$

20. (a)

$$\text{Full load current} = \frac{25 \times 10^3}{\sqrt{3} \times 400 \times 0.8} = 45.11 \text{ A}$$

$$\begin{aligned} \text{Excitation emf } \vec{E}_f &= \vec{V} - j\vec{I}_a X \\ &= \frac{400}{\sqrt{3}} - (45.11 \angle 36.87^\circ)(j7) \\ &= 490.5 \angle -31^\circ \text{ V} \end{aligned}$$

Rotor angle slip by 0.25 mechanical degree,

$$\theta_e = \frac{P}{2} \theta_m$$

$$\Delta\delta = \frac{4}{2} \times 0.25 = 0.5^\circ$$

$$\begin{aligned} \text{Synchronizing emf} &= 2E_f \sin \frac{\Delta\delta}{2} \\ &= 2 \times 490.5 \sin \left( \frac{0.5}{2} \right) = 4.28 \text{ V} \end{aligned}$$

$$\text{Synchronizing current} = \frac{4.28}{7} = 0.611 \text{ A}$$

21. (a)

For double layer winding,

$$\text{No. of slots} = \text{No. of coils}$$

$$\text{Total number of turns} = 60 \times 10 = 600$$

$$\text{Turns per phase} = \frac{600}{3} = 200$$

$$\text{Pitch factor } (K_c) = \cos 18^\circ = 0.951$$

$$\text{Distribution factor } (K_d) = \frac{\sin \frac{m\beta}{2}}{m \sin \frac{\beta}{2}}$$

$$m = \frac{60}{4} \times \frac{1}{3} = 5$$

$$\beta = \frac{180}{60/4} = 12^\circ$$

$$K_d = \frac{\sin \frac{5 \times 12}{2}}{5 \sin \frac{12}{2}} = 0.9567$$

$$\text{Induced emf, } E_{ph} = \sqrt{2} \pi K_w \phi f T_{ph}$$

$$E_{ph} = \sqrt{2} \pi \times 0.9567 \times 0.951 \times 0.015 \times 50 \times 200$$

$$E_{ph} = 606.33 \text{ V}$$

$$E_{L-L} = 1.05 \text{ kV}$$

22. (c)

Given,

$$V_t = 1.0 \text{ p.u.}$$

$$I_a = 1.0 \text{ p.u. at } 0.8 \text{ p.f. lagging}$$

$$\phi = \cos^{-1} 0.8 = 36.86^\circ$$

$$X_d = 0.8 \text{ p.u.}$$

$$X_q = 0.5 \text{ p.u.}$$

As we can use the relation,

$$\tan \psi = \frac{V_t \sin \phi + I_a X_q}{V_t \cos \phi + I_a r_a} \quad [ \because \text{Here } r_a = 0 ]$$

$$\tan \psi = \frac{1 \times 0.6 + 1 \times 0.5}{1 \times 0.8 + 0}$$

or

$$\tan \psi = 1.375$$

$$\psi = 53.97^\circ$$

$$\therefore \text{Power angle; } \delta = \psi - \phi \quad [\text{for generator}]$$

$$= 53.97^\circ - 36.86^\circ$$

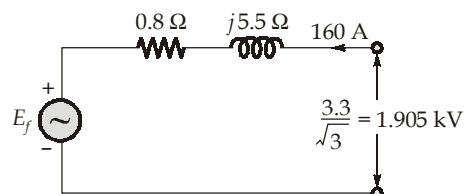
$$= 17.11^\circ$$

We can write,

$$\begin{aligned} \text{No load voltage; } E_f &= V_t \cos \delta + I_d X_d \\ &= V_t \cos \delta + (I_a \sin \psi) X_d \\ &= 1 \times \cos 17.11^\circ + (1 \times \sin 53.97^\circ) \times 0.8 \\ &= 1.602 \text{ p.u.} \approx 1.60 \text{ p.u.} \end{aligned}$$

23. (c)

Consider the following circuit;



$$\text{Full load current} = 160 \angle -36.86^\circ \text{ A}$$

$$\text{Synchronous impedance; } Z_s = (0.8 + j 5.5) \Omega$$

$$= 5.56 \angle 81.724^\circ \Omega$$

From circuit diagram we can write;

$$\vec{E}_f = 1.905 \times 10^3 \angle 0^\circ - 5.56 \angle 81.724^\circ \times 160 \angle -36.86^\circ$$

$$E_f = 1.42 \angle -26.22^\circ \text{ kV}$$

Now

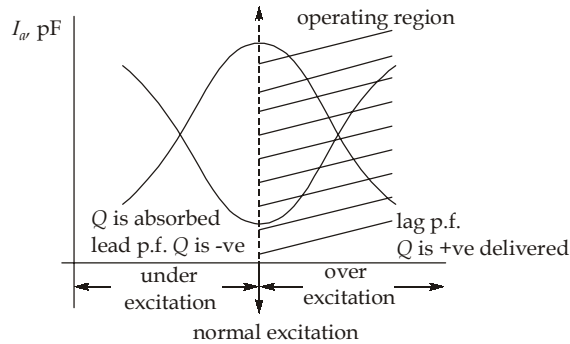
$$P_{\text{mech (dev)}} = 3 \times 1.42 \times 160 \cos (-36.86^\circ + 26.22^\circ) = 669.88 \text{ kW}$$

$$\text{shaft output} = 669.88 - 30 = 639.88 \text{ kW}$$

$$\begin{aligned} \text{Power input} &= \sqrt{3} \times 3.3 \times 160 \times 0.8 \\ &= 731.62 \text{ kW} \end{aligned}$$

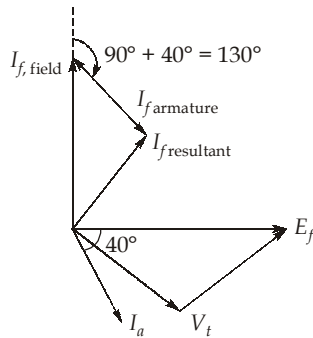
$$\eta_{\text{full load}} = \frac{\text{Output}}{\text{Input}} \times 100 = \frac{639.88}{731.62} \times 100 = 87.46\%$$

24. (a)



Feeds lagging KVAR to the bus but absorbs the leading KVAR.

25. (d)



26. (b)

$$\text{Synchronous impedance, } Z_s = (0.5 + j5)\Omega = 5.025 \angle 84.29^\circ \Omega$$

$$I_a = \frac{V \angle 0^\circ - E \angle -\delta}{Z_s \angle \theta}$$

$$S = VI_0^* = V \angle 0 \left[ \frac{V \angle 0 - E \angle -\delta}{Z_s \angle \theta} \right]^*$$

$$S = \frac{V^2}{Z_s} \angle \theta - \frac{EV}{Z_s} \angle \theta + \delta$$

So from above equation,

$$P = \frac{V^2}{Z_s} \cos\theta - \frac{EV}{Z_s} \cos(\theta + \delta)$$

$$900 \times 10^3 = \frac{2000^2}{5.025} (\cos 84.29^\circ) - \frac{2000 \times 3000}{5.025} \cos(84.29^\circ + \delta)$$

$$84.29^\circ + \delta = 133.426^\circ$$

$$\text{Power angle, } \delta = 49.13^\circ$$

27. (c)

Take,

$$V_t = 1 \angle 0^\circ \text{ p.u.}$$

So,

$$I_a = 1 \angle -\cos^{-1}(0.8) \text{ p.u.}$$

Alternator excitation emf,  $\vec{E}_f = \vec{V}_t + \vec{I}_a \vec{Z}_s$

$$\vec{E}_f = 1 \angle 0^\circ + [1 \angle -\cos^{-1}(0.8)] \times 1.25 \angle 90^\circ$$

$$\vec{E}_f = 1 + 1.25 \angle 53.13^\circ$$

$$\begin{aligned} |\vec{E}_f| &= \sqrt{(1 + 1.25 \cos 53.13^\circ)^2 + (1.25 \sin 53.13^\circ)^2} \\ &= 2.01 \text{ p.u.} \end{aligned}$$

When motor just fall out of step,

$$\delta \approx 90$$

Now for same excitation,

$$2.01 \angle 90^\circ = 1 \angle 0^\circ + I_a \times 1.25 \angle 90^\circ$$

$$\vec{I}_a = \frac{j2.01 - 1}{j1.25} = 1.608 + j0.8$$

$$\vec{I}_a = 1.8 \angle 26.45^\circ \text{ p.u.}$$

$$\text{Power factor} = \cos(26.45^\circ) = 0.895 \text{ leading}$$

28. (c)

$$E_f^2 = (V_E \cos \phi)^2 + (V_t \sin \phi + I_a X_s)^2$$

$$E_f^2 = V_t^2 \left[ 0.8^2 + \left( 0.6 + \frac{I_a X_s}{V_t} \right)^2 \right]$$

$$E_f^2 = V_t^2 [0.8^2 + (0.6 + 0.2)^2]$$

$$E_f = 1.13 V_t$$

$$\text{Voltage regulation} = \frac{E_f - V_t}{V_t} \times 100 = \frac{1.13V_t - V_t}{V_t} \times 100 = 13\%$$

29. (b)

$$S_{\text{load}} = 1200 \angle -\cos^{-1}(0.8) = 960 - j720$$

$$S_A = 750 \angle -\cos^{-1}(0.9) = 675 - j326.9$$

Now,

$$S_A + S_B = S_{\text{load}}$$

∴

$$\begin{aligned} S_B &= S_{\text{load}} - S_A \\ &= 960 - j720 - 675 + j326.9 \\ &= 285 - j393.1 \end{aligned}$$

$$S_B = 485.54 \angle -54.05^\circ$$

$$\cos \phi_B = \cos(-54.05) = 0.587 \text{ (lagging)}$$

30. (a)

Let, synchronous speed of motor =  $N_{sm}$

Also,

$$N_{sm} = \frac{120 \times f_m}{P_m}$$

∴

$$N_{sm} = \frac{120 \times 60}{P_m}$$

Synchronous speed of alternator,

$$N_{sg} = \frac{120 \times f_g}{P_g} = \frac{120 \times 25}{20} = 150 \text{ rpm}$$

Since alternator and motor are directly coupled

$$N_{sg} = N_{sm}$$

(or)

$$150 = \frac{120 \times 60}{P_m}$$

⇒

$$P_m = 48$$

