## HYDROLOGY

## CIVIL ENGINEERING

Date of Test : 31/07/2023

## ANSWER KEY

1. (c)
2. (d)
3. (a)
4. (a)
5. (b)
6. (d)
7. (b)
8. (a)
9. (c)
10. (b)
11. (c)
12. (c)
13. (d)
14. (a)
15. (b)
16. (b)
17. (c)
18. (c)
19. (c)
20. (a)
21. (c)
22. (b)
23. (a)
24. (c)
25. (c)
26. (b)
27. (a)
28. (c)
29. (c)
30. (d)

## DETAILED EXPLANATIONS

1. (c)

Double mass curve technique is used to check the consistency of rainfall data.
2. (d)

$$
\left.\begin{array}{rl}
\text { Rainfall, } P_{1} & =6 \mathrm{~cm} \\
\text { Runoff, } R_{1} & =3 \mathrm{~cm}
\end{array}\right] \begin{aligned}
& \therefore \quad \phi \text {-index, } \phi_{1}=\frac{6-3}{6}=\frac{1}{2} \mathrm{~cm} / \mathrm{hr}
\end{aligned}
$$

since,

$$
\begin{aligned}
& \phi_{1}=\phi_{2} \\
& \frac{1}{2}=\frac{12-R_{2}}{9} \\
& R_{2}=7.5 \mathrm{~cm}
\end{aligned}
$$

$$
\therefore \quad \frac{1}{2}=\frac{12-R_{2}}{9}
$$

3. (c)

| S.No. | Soil type | Infiltration Capacity (mm/h) | Remarks |
| :---: | :---: | :---: | :---: |
| 1. | Highly Clayey soils | 1.25 | Very Low |
| 2. | Clayey soils | 2.5 to 25 | Low |
| 3. | Sandy loam | 12.5 to 25 | Medium |
| 4. | Deep sands | $>25$ | High |

4. (b)

$$
\text { Equilibrium discharge, } \quad Q_{e}=2.778 \times \frac{300}{3}=277.8 \mathrm{~m}^{3} / \mathrm{s}
$$

7. (d)

$$
\text { Risk } \bar{R}=1-\left(1-\frac{1}{T}\right)^{n}
$$

Here,

$$
n=25 \text { years }
$$

$$
T=100 \text { years }
$$

$$
\therefore \quad \bar{R}=1-\left(1-\frac{1}{100}\right)^{25}=1-\left(\frac{99}{100}\right)^{25}
$$

8. (b)

Station $B$ is inoperative

$$
\begin{aligned}
N_{B} & =180 \mathrm{~cm} \\
1.1 N_{B} & =198 \mathrm{~cm} \\
0.9 N_{B} & =162 \mathrm{~cm} \\
N_{A} & =175 \mathrm{~cm} \quad N_{C}=165 \mathrm{~cm}
\end{aligned}
$$

Since, $N_{A}$ and $N_{C}$ are within $10 \%$ of $N_{B}$

$$
\therefore \quad P_{B}=\frac{P_{A}+P_{C}}{2}=\frac{150+135}{2}=142.5 \mathrm{~cm}
$$

9. (c)

IS 4987: 1968 recommendation are
In plains: 1 station per $520 \mathrm{~km}^{2}$
For $1040 \mathrm{~km}^{2}$, no of stations required $=\frac{1040}{520}=2$.
11. (b)

$$
\begin{aligned}
\text { Total rainfall, } P & =1.5+2.5+3.0+6.5+7.0+7.5+8.5+8.0+7.0+6.5+2.5+2.0 \\
& =62.5 \mathrm{~cm} \\
\text { Total runoff, } Q & =20.5 \mathrm{~cm} \\
t_{r} & =12 \mathrm{hr} \\
\therefore \quad W_{\text {index }} & =\frac{P-Q}{t_{r}}=\frac{62.5-20.5}{12}=3.5 \mathrm{~cm} / \mathrm{hr}
\end{aligned}
$$

For $\phi$-index, the values lesser than $3.5 \mathrm{~cm} / \mathrm{hr}$ are neglected i.e. 1.5, 2.5, 3, 2.5, 2.0 are neglected.

$$
\begin{aligned}
\therefore \quad \begin{aligned}
P & =6.5+7.0+7.5+8.5+8.0+7.0+6.5=51 \\
Q & =20.5 \mathrm{~cm} \\
t_{r} & =12-5=7 \mathrm{hr} \\
\therefore \quad \phi_{\text {index }} & =\frac{P-Q}{t_{r}}=\frac{51-20.5}{7}=4.357 \mathrm{~cm} / \mathrm{hr} \simeq 4.36 \mathrm{~cm} / \mathrm{hr} \\
\therefore & \left|W_{\text {index }}-\phi_{\text {index }}\right|
\end{aligned}=4.36-3.5=0.86 \mathrm{~cm} / \mathrm{hr}
\end{aligned}
$$

12. (a)

$$
k=0.60
$$

| Month | Temp.(F) | Percent sunshine $\mathrm{hr}\left(\mathrm{P}_{\mathrm{h}}\right)$ | $\Sigma P_{h} T_{f}$ |
| :---: | :---: | :---: | :---: |
| Nov | 60 | 2 | 120 |
| Dec | 55 | 8 | 440 |
| Jan | 50 | 7 | 350 |
| Feb | 60 | 6 | 360 |
|  |  |  | $\Sigma P_{h} T_{f}=1270$ |

$$
\begin{aligned}
\therefore \quad \text { PET } & =\frac{2.54 \mathrm{~K} \Sigma P_{h} T_{F}}{100}=\frac{2.54 \times 0.6 \times 1270}{100} \\
\text { PET } & =19.35 \mathrm{~cm}
\end{aligned}
$$

13. (a)

For the second 30 minutes,

Total infiltration,

$$
\begin{aligned}
t_{1} & =30 \mathrm{mins}=0.5 \mathrm{hr} \\
t_{2} & =60 \mathrm{mins}=1 \mathrm{hr} \\
F_{p} & =\int_{0.5}^{1}\left(4+e^{-2 t}\right) d t=\int_{0.5}^{1} 4 d t+\int_{0.5}^{1} e^{-2 t} d t \\
& =[4 t]_{0.5}^{1}+\left[-\frac{e^{-2 t}}{2}\right]_{0.5}^{1}=4 \times(1-0.5)+\frac{1}{2}\left[e^{-2 \times 0.5}-e^{-2 \times 1}\right]
\end{aligned}
$$

$$
\begin{aligned}
& =2+\frac{1}{2}\left[e^{-1}-e^{-2}\right] \\
& =2+\frac{1}{2}\left[\frac{1}{e}-\frac{1}{e^{2}}\right]=2+\frac{1}{2} \times 0.232=2+0.116=2.116 \mathrm{~cm}
\end{aligned}
$$

14. (a)

$$
\begin{array}{rlrl} 
& & \frac{U_{c}}{U_{m}} & =\frac{1 \mathrm{~cm}}{1 \mathrm{~mm}} \\
\Rightarrow & \frac{U_{c}}{U_{m}} & =\frac{1}{0.1} \\
\Rightarrow & U_{c} & =10 U_{m} \\
\therefore & U_{m} & =\frac{U_{c}}{10}
\end{array}
$$

15. (d)

Distribution graph is basically a D-hr unit hydrograph with ordinate showing the percentage of surface runoff occurring in successive period of equal time intervals of D-hr.
16. (c)

| Isohyet Interval | Average Isohyet Rainfall (mm) | Area between Isohyets $\left(\mathrm{km}^{2}\right)$ | $P A$ |
| :---: | :---: | :---: | :---: |
| $115-105$ | 110 | 120 | 13200 |
| $105-95$ | 100 | 150 | 15000 |
| $95-85$ | 90 | 200 | 18000 |
| $85-75$ | 80 | 250 | 20000 |
|  | $\Sigma A=720$ | $\Sigma P A=66200$ |  |

Average rainfall,

$$
P_{\mathrm{avg}}=\frac{\Sigma P A}{\Sigma A}=\frac{66200}{720}=91.94 \mathrm{~mm}
$$

$$
\begin{aligned}
\text { Volume of runoff } & =0.7 \times 720 \times 10^{6} \times 91.94 \times 10^{-3}=46.34 \times 10^{6} \mathrm{~m}^{3}=46.34 \mathrm{Mm}^{3} \\
\text { Volume of losses } & =(1-0.7) \times 720 \times 10^{6} \times 91.94 \times 10^{-3} \\
& =19.86 \times 10^{6} \mathrm{~m}^{3}=19.86 \mathrm{Mm}^{3}
\end{aligned}
$$

$\therefore$ Volume of runoff - Volume of losses $=46.34-19.86=26.48 \mathrm{Mm}^{3}$
17. (a)

In hydrologic routing, discharge is taken as a function of time.
19. (a)

As we know,

$$
\frac{(Q)_{\text {unsteady }}}{(Q)_{\text {steady }}}=\sqrt{1+\frac{d h / d t}{V_{w} \cdot S_{o}}}
$$

$\Rightarrow \quad(Q)_{\text {unsteady }}=160 \times \sqrt{1+\frac{11.2 \mathrm{~cm} / \mathrm{hr}}{2.0 \mathrm{~m} / \mathrm{s} \times 100 \times 3600 \times \frac{1}{3600}}}=164.42 \mathrm{~m}^{3} / \mathrm{s}$
20. (c)

Rainfall excess in 1st three hours, $R_{1}=0.5 \times 3=1.5 \mathrm{~cm}$
Rainfall excess in 2nd three hours, $R_{2}=1 \times 3=3 \mathrm{~cm}$

| $t(\mathrm{hr})$ | Ordinate of <br> 3hr UH | DRH due to <br> 1.5 cm ER | DRH due <br> to 3 cm ER | Ordinate of <br> final DRH | Base flow <br> $\left(\mathrm{m}^{3} / \mathrm{s}\right)$ | Ordinates of flood <br> hydrograph $\left(\mathrm{m}^{3} / \mathrm{s}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | $0 \times 1.5$ |  | 0 | 7 | 7 |
| 3 | 10 | $10 \times 1.5$ | $0 \times 3$ | 15 | 7 | 22 |
| 6 | 15 | $15 \times 1.5$ | $10 \times 3$ | 52.5 | 7 | 59.5 |
| 9 | 30 | $30 \times 1.5$ | $15 \times 3$ | 90 | 7 | 97 |
| 12 | 18 | $18 \times 1.5$ | $30 \times 3$ | 117 | 7 | 124 |
| 15 | 6 | $6 \times 1.5$ | $18 \times 3$ | 63 | 7 | 70 |
| 18 | 0 | $0 \times 1.5$ | $6 \times 3$ | 18 | 7 | 25 |
| 21 |  |  | $0 \times 3$ | 0 | 7 | 7 |

At $t=12 \mathrm{hr}$, ordinate of flood hydrograph is $124 \mathrm{~m}^{3} / \mathrm{s}$
21. (a)

Data normally required in the studies are
(i) Weather records in term of temperature, humidity and wind velocity
(ii) Precipitation data
(iii) Stream flow records
(iv) Evaporation and evapotranspiration data
(v) Infiltration characteristics of the study area
(vi) Soils of the area
(vii) Land use and land cover
(viii) Ground water characteristics
(ix) Physical and geological characteristics of the area
(x) Water quality data
22. (c)

Unit hydrograph $\Rightarrow R=1 \mathrm{~cm}=0.01 \mathrm{~m}$

$$
\begin{aligned}
\frac{1}{2} \times T_{B} \times 100 \times 3600 & =90 \times 10^{6} \times 0.01 \\
T_{B} & =50 \text { hours }
\end{aligned}
$$


23. (c)

In Western Ghat, Maharashtra, the flood peak will be given by Inglis formula, which is

$$
\begin{aligned}
Q_{p} & =\frac{124 A}{\sqrt{A+10.4}} \\
\Rightarrow \quad Q_{p} & =\frac{124 \times 53.6}{\sqrt{53.6+10.4}}=\frac{124 \times 53.6}{8}=830.8 \mathrm{~m}^{3} / \mathrm{s}
\end{aligned}
$$

24. (c)

$$
\begin{aligned}
\mu & =P_{a v .}=\frac{800+520+440+420}{4}=545 \mathrm{~mm} \\
\sigma_{n-1} & =\sqrt{\frac{\sum\left(P_{i}-P_{a v}\right)^{2}}{n-1}} \\
\Rightarrow \quad \sigma_{n-1} & =\sqrt{\frac{(800-545)^{2}+(520-545)^{2}+(440-545)^{2}+(420-545)^{2}}{4-1}} \\
\Rightarrow \quad \sigma_{\mathrm{n}-1} & =175.404 \mathrm{~mm} \\
\therefore \quad c_{v} & =\frac{\sigma_{n-1}}{\mu} \times 100=\frac{175.404}{545} \times 100=32.18 \%
\end{aligned}
$$

Now, $\quad$ No. of rainguages, $N=\left(\frac{c_{v}}{\varepsilon}\right)^{2}=\left(\frac{32.18}{6}\right)^{2}=28.77$
i.e.

$$
N=29
$$

$\therefore$ Additional raingauge stations required $=29-4=25$
25. (b)

$$
\begin{aligned}
\text { Total rainfall volume } & =0.015 \times 8 \times 1.5 \times 10^{6} \\
& =180,000 \mathrm{~m}^{3} \\
\text { Total infiltration volume } & =\text { Total rainfall }- \text { Runoff } \\
& =180,000-35000 \\
& =145000 \mathrm{~m}^{3} \\
\therefore \quad \text { Infiltration depth } & =\frac{145000}{1.5 \times 10^{6}}=0.0967 \mathrm{~m}=9.67 \mathrm{~cm}
\end{aligned}
$$

26. (b)

$$
\begin{aligned}
& \qquad \begin{aligned}
P & =\text { Input due to precipitation in } 10 \text { hours } \\
& =200 \times 100 \times 100 \times \frac{9}{100}=180000 \mathrm{~m}^{3} \\
R & =\text { Runoff }=2 \times 12 \times 3600=86400 \mathrm{~m}^{3} \\
\text { Water not available to runoff } & =180000-86400=93600 \mathrm{~m}^{3}
\end{aligned}, \$ \text {. }
\end{aligned}
$$

28. (a)

Relative humidity,

$$
R_{H}=\frac{e_{a}}{e_{s}}
$$

Also,
$\frac{v_{9}}{v_{2}}=\left(\frac{9}{2}\right)^{1 / 7}=1.24$
$\therefore \quad v_{9}=1.24 \times 12=14.88 \mathrm{kmph}$

So, daily evaporation,

$$
\begin{aligned}
E & =k_{m}\left(e_{s}-e_{a}\right)\left(1+\frac{v_{9}}{16}\right) \\
& =0.36(34-17)\left(1+\frac{14.88}{16}\right)=11.81 \mathrm{~mm} / \text { day }
\end{aligned}
$$

29. (c)

For the 1st hour rainfall, $\quad P=45 \mathrm{~mm}$

$$
\text { Effective rainfall }=\frac{12 \times(0)+7(45-30)+1(0)}{20}=5.25 \mathrm{~mm}
$$

For the second hour rainfall, $\quad P=55 \mathrm{~mm}$

$$
\begin{aligned}
\text { Effective rainfall } & =\frac{12(55-50)+7(55-30)+1(0)}{20}=11.75 \mathrm{~mm} \\
\therefore \quad & \text { Total effective rainfall }
\end{aligned}=5.25+11.75=17 \mathrm{~mm}
$$

30. (d)

Basin diameter,

$$
D=15 \mathrm{~km}
$$



Side of square around station $A=\frac{15}{2}=7.5 \mathrm{~km}$

$$
\text { Area of station } A=7.5 \times 7.5=56.25 \mathrm{~km}^{2}
$$

$$
\text { Total area of circular basin }=\frac{\pi}{4}(15)^{2}=176.7 \mathrm{~km}^{2}
$$

Area of station $B=$ Area of station $C=$ Area of station $D=$ Area of station $E$

$$
=\left(\frac{176.7-56.25}{4}\right)=30.11 \mathrm{~km}^{2}
$$

$$
\therefore \quad \text { Mean rainfall }=\frac{9 \times 56.25+30.11(7+10+11+8)}{176.7}
$$

$$
=8.99 \simeq 9 \mathrm{~cm}
$$

