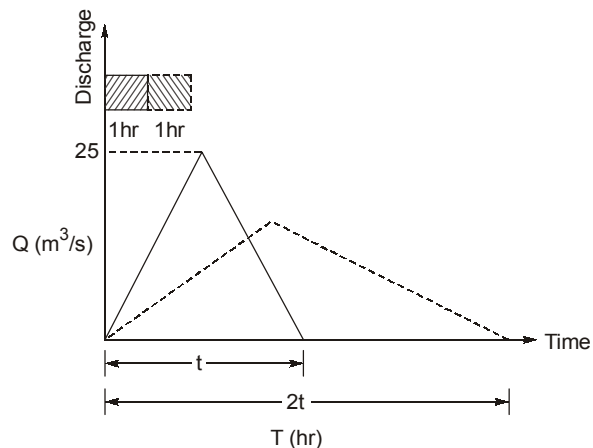


### ANSWER KEY > Engineering Hydrology

1. (b)	7. (c)	13. (c)	19. (b)	25. (d)
2. (d)	8. (a)	14. (a)	20. (b)	26. (c)
3. (a)	9. (d)	15. (c)	21. (a)	27. (d)
4. (a)	10. (c)	16. (d)	22. (d)	28. (a)
5. (a)	11. (c)	17. (b)	23. (c)	29. (c)
6. (a)	12. (a)	18. (b)	24. (c)	30. (c)

### DETAILED EXPLANATIONS

1. (b)



For 2-hr UH, the base time will increase, hence peak will go down.

2. (d)

Certain chemicals such as cetyl alcohol (hexadecanol) and stearyl alcohol (octadecanol) forms monomolecular layers on a water surface. These layers act as evaporation inhibitors by preventing the water molecules to escape past them.

4. (a)

Since variation is more than 10%,

$$P_x = \frac{105}{3} \left[ \frac{156}{155} + \frac{140}{150} + \frac{104}{120} \right]$$

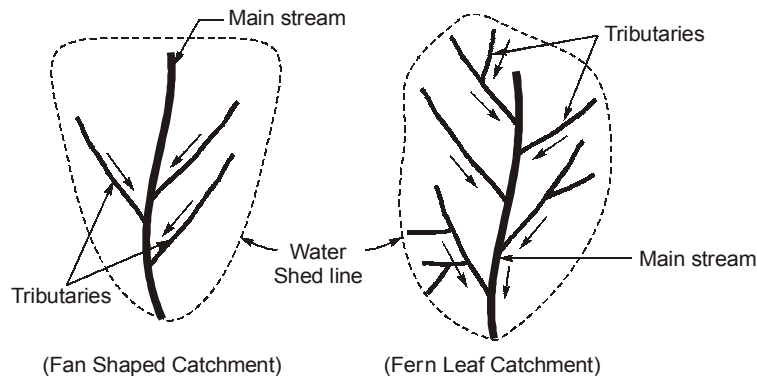
$$= 98.2 \text{ cm}$$

5. (a)

$$Q_{\text{equilibrium}} = 2.78 \frac{A}{T}$$

$$= 2.78 \times 360 \times \frac{1}{4} \approx 250 \text{ cumecs}$$

6. (a)



7. (c)

The limiting case of a UH of zero duration is known as IUH (Instantaneous Unit Hydrograph). The ordinate of one IUH at any time 't' is the slope of S-curve of intensity 1 cm/hr.

8. (a)

Isopleth is a line on a map connecting points having same numerical values of a certain quantity such as population figure or geographical measurement. Isobars are contour lines that connects different points with same constant pressure. Isochrones are lines on a map connecting points relating to equal time of travel of surface runoff or equal time of concentration.

11. (c)

$$\text{Peak of DRH} = 135 - 10 = 125 \text{ m}^3/\text{s}$$

$$P = 54 \text{ mm}, \quad \phi = 4 \text{ mm/hr}$$

$$\therefore n = P - \phi \times t = 54 - 4 \times 1 = 50 \text{ mm} = 5 \text{ cm}$$

$$\therefore \text{Peak of 1 hr. UH} = \frac{125}{5} = 25 \text{ m}^3/\text{s}$$

12. (a)

$$n = 2 + 3 = 5 \text{ cm}$$

For DRH,  $(\Sigma O) = (1 + 7 + 26 + 37 + 27 + 13 + 1) - 7 = 105$

$$n = \frac{0.36 \Sigma Ot}{A}$$

$$\Rightarrow A = \frac{0.36 \times 105 \times 1}{5} = 7.56 \text{ km}^2$$

13. (c)

$$P = 5 \times 2 = 10 \text{ cm}$$

$$= 10 \times 10^{-2} \times 100 \times 10^4 = 10^5 \text{ m}^3$$

$$R = 1 \text{ m}^3/\text{s} \times 10 \times 60 \times 60 = 36000 \text{ m}^3$$

$$\therefore \text{Runoff coefficient} = \frac{R}{P} = \frac{36000}{10^5} = 0.36$$

14. (a)

Time (hr)	4-h UH (m <sup>3</sup> /s)	S-curve addition	S-curve	Offset S-curve	$\Delta y$	6-h UH = ( $\Delta y \times 4/6$ )
0	0	—	0	—	0	0
2	9	—	9	—	9	6
4	20	0	20	—	20	13.33
6	35	9	44	0	44	29.33
8	43	20	63	9	54	36
10	22	44	66	20	46	30.67
		63		44		
		66		69		
				66		

15. (c)

(i) Mean rainfall,  $(\bar{P}) = \frac{\Sigma P}{n} = \frac{800 + 620 + 400 + 560}{4} = 595 \text{ mm}$

(ii) Standard deviation,  $\sigma = \sqrt{\frac{(P - \bar{P})^2}{n - 1}} = 165.23$

(iii) Coefficient of variation,  $c_v = \frac{100 \sigma}{\bar{P}} = \frac{100 \times 166.93}{595} = 27.77$

(iv) Optimum number of rain gauges,  $(N) = \left(\frac{c_v}{\epsilon}\right)^2 = \left(\frac{28.29}{10}\right)^2 \Rightarrow 7.7113 \approx 8 \text{ Nos}$

(v) Additional gauges required to be installed  
 = 8 – Existing 4 gauges  
 = 8 – 4 = 4

16. (d)

Time (1)	Total Stream flow in cumecs (2)	Base flow in cumecs (3)	Direct run off = column (2) – 4.8 (4)
0	4.8	4.8	0
2	5.1	4.8	0.3
4	6.5	4.8	1.7
6	7.4	4.8	2.6
8	10.2	4.8	5.4
10	8.8	4.8	4.0
12	7.4	4.8	2.6

Using Simpson's rule, the area enclosed by this discharge hydrograph

$$\begin{aligned}
 &= \frac{H}{3} \left[ \frac{1^{\text{st}} + \text{last ordinate}}{2} + 4 \times \text{Even ordinates} + 2 \times \text{odd ordinates} \right] \\
 &= \frac{2 \times 60 \times 60}{3} \left[ \frac{0 + 2.6}{2} + 4(0.3 + 2.6 + 4.0) + 2(1.7 + 5.4) \right] \\
 &= 103440 \text{ m}^3
 \end{aligned}$$

$$\therefore \text{Depth of water in the hydrograph} = \frac{103440}{400 \times 10^4} = 2.586 \times 10^{-2} \text{ m or } 2.586 \text{ cm}$$

$$\text{Rainfall} = 4 \text{ cm}$$

$$\text{Runoff} = 2.586 \text{ cm}$$

$$\therefore \text{Infiltration including basin recharge} = 4 - 2.586 = 1.414 \text{ cm}$$

$$t_r = 4 \text{ hr (given)}$$

$$\therefore \phi_{\text{index}} = \frac{1.414}{4} = 0.35 \text{ cm/hr}$$

17. (b)

$$\text{Loss} = \text{Rainfall} - \text{Runoff} = \frac{0.8}{100} \times 6 - \frac{256000}{8.6 \times 10^6} = 0.01823 \text{ m} = 1.823 \text{ cm}$$

$$\text{Rate of loss} = \frac{1.823}{6} = 0.304 \text{ cm/hr}$$

18. (b)

The probability of occurrence of an event ( $x \geq x_T$ ) at least once over a period of  $n$  successive years is called the risk,  $\bar{R}$ .

Hence, risk is given by

$$\begin{aligned}
 \bar{R} &= 1 - (\text{Probability of occurrence of the event } x \geq x_T \text{ in } n \text{ years}) \\
 &= 1 - \left(1 - \frac{1}{T}\right)^n = 1 - \left(1 - \frac{1}{50}\right)^{25} = 0.397 \approx 0.40
 \end{aligned}$$

where,

$$T = \text{Return period} = 50 \text{ years}$$

$$n = \text{Expected life} = 25 \text{ years}$$

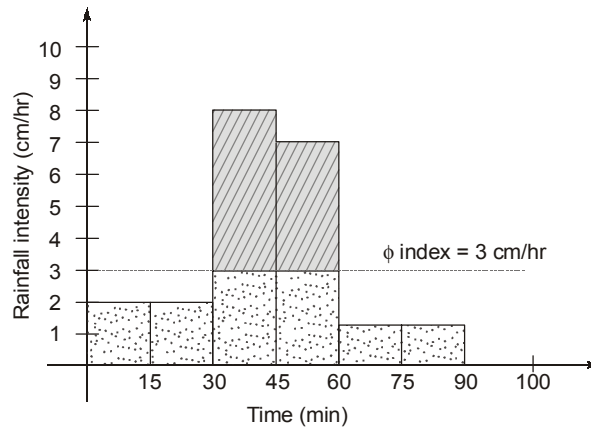
19. (b)

**Thiessen Polygon Method:** In this method, the rainfall recorded at each station is given a weightage on the basis of an area closest to the station.

$$P_{\text{avg}} = \frac{P_1 A_1 + P_2 A_2 + \dots + P_n A_n}{A_1 + A_2 + \dots + A_n}$$

where,  $P_1, P_2, \dots, P_n$  are the rainfall data of areas  $A_1, A_2, \dots, A_n$ .

20. (b)



Hatched portion shows the total runoff and dotted portion shows the total infiltration.

$$\therefore \text{Total runoff} = (8 - 3) \times \frac{15}{60} + (7 - 3) \times \frac{15}{60} = [(8 - 3) + (7 - 3)] \times \frac{15}{60} = 2.25 \text{ cm}$$

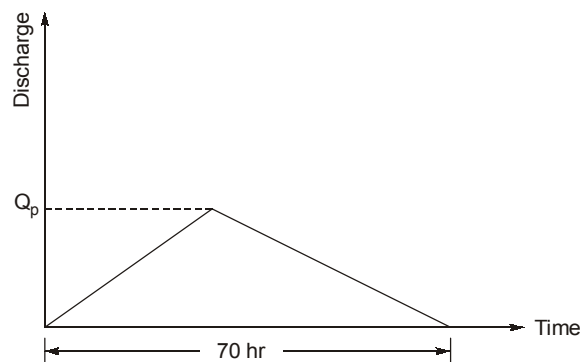
$$\begin{aligned} \text{Total precipitation} &= 2 \times \frac{15}{60} + 2 \times \frac{15}{60} + 8 \times \frac{15}{60} + 7 \times \frac{15}{60} + 1.25 \times \frac{15}{60} + 1.25 \times \frac{15}{60} \\ &= (2 + 2 + 8 + 7 + 1.25 + 1.25) \times \frac{15}{60} = 5.375 \text{ cm} \end{aligned}$$

$$\begin{aligned} W\text{-index} &= \frac{\text{Total precipitation} - \text{Runoff}}{\text{Duration of rainfall in hr}} = \frac{5.375 - 2.25}{90 / 60} \\ &= 2.083 \text{ cm/hr} \approx 2.08 \text{ cm/hr} \end{aligned}$$

24. (c)

Let the peak of the UH be  $Q_p$ .

The UH can be shown as



Area of DRH gives the volume of rainfall,

$$\frac{1}{2} \times 70 \times 60 \times 60 \times Q_p = \frac{1}{100} \times 756 \times 10^6$$

$$\Rightarrow Q_p = 60 \text{ m}^3/\text{s}$$

$$\therefore \text{Peak of DRH} = n \times \text{peak of UH} = 5 \times 60 = 300 \text{ m}^3/\text{s}$$

25. (d)

$$\text{Total rainfall} = 0.5 + 1.8 + 2.9 = 5.2 \text{ cm}$$

$$\text{Infiltration} = 5.2 - 2 = 3.2 \text{ cm}$$

$$\text{Excess rainfall duration, } t_e = 2 \times 3 = 6 \text{ hrs.}$$

$$\phi\text{-index} = \frac{3.2}{6} = 0.533 \text{ cm/hr}$$

This value being more than 0.5 cm/hr,

The excess rainfall duration will reduce by 2 hrs.

∴

$$t_e = 4 \text{ hrs.}$$

$$\text{Infiltration} = (1.8 + 2.9) - 2 = 2.7 \text{ cm}$$

$$\phi\text{-index} = \frac{2.7}{4} = 0.675 \text{ cm/hr}$$

26. (c)

$$\bar{x} = \frac{1}{n} \sum n_i = \frac{80 + 90 + 100 + 60 + 70}{5} = 80 \text{ cm}$$

The standard deviation of the rainfall is given by

$$\sigma = \sqrt{\frac{(x - \bar{x})^2}{n - 1}}$$

$$\sigma = 15.81$$

$$\Rightarrow C_V = \frac{\sigma}{\bar{x}} \times 100 = 19.76$$

$$N = \left( \frac{C_V}{\epsilon} \right)^2 = \left( \frac{19.76}{6} \right)^2 = 10.85 \approx 11$$

Thus, additional number of rainguages = 11 - 5 = 6

27. (d)

Time base of both the unit hydrographs is same. Let it be  $t$ .

$$\therefore \frac{1}{2} \times 30 \times t \times \frac{1}{235} = \frac{1}{2} \times 90 \times t \times \frac{1}{A_2}$$

$$\Rightarrow A_2 = 235 \times 3$$

$$\Rightarrow A_2 = 705 \text{ km}^2$$

28. (a)

The calculations are tabulated below:

Time (hr)	FH (m <sup>3</sup> /s)	Base Flow (m <sup>3</sup> /s)	DRH (m <sup>3</sup> /s)
Col. (1)	Col. (2)	Col. (3)	Col. (4)
0	5	5	0
12	15	5	10
24	40	5	35
36	80	5	75
48	60	5	55
60	50	5	45
72	25	5	20
84	15	5	10
96	5	5	0
			ΣO = 250

$$\text{Base flow} = 5 \text{ m}^3/\text{sec}$$

$$\text{Now, direct runoff depth, } DRD = \frac{0.36 \times \Sigma O \times t}{A}$$

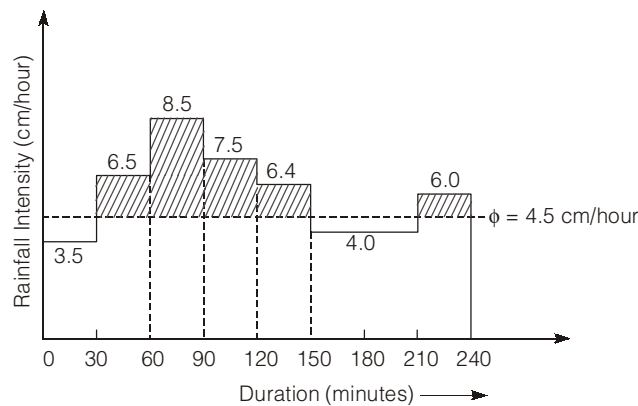
where

$$\Sigma O = 250 \text{ m}^3/\text{s}; t = 12 \text{ hr}; A = 450 \text{ km}^2$$

∴

$$DRD = \frac{0.36 \times 250 \times 12}{450} = 2.4 \text{ cm}$$

29. (c)



Rainfall excess is shown by hatched area.

Total rainfall

$$P = (3.5 + 6.5 + 8.5 + 7.5 + 6.4 + 4.0 + 4.0 + 6.0) \times \frac{30}{60} = 23.2 \text{ cm}$$

Total rainfall excess

$$R = [(6.5 - 4.5) + (8.5 - 4.5) + (7.5 - 4.5) + (6.4 - 4.5) + (6.0 - 4.5)] \times \frac{30}{60}$$

$$= (2 + 4 + 3 + 1.9 + 1.5) \times \frac{1}{2} = 6.2 \text{ cm}$$

$$W\text{-index} = \frac{P - R}{t} = \frac{23.2 - 6.2}{4} = 4.25 \text{ cm/hour}$$

30. (c)

Time(hr)	0	12	24	36	48
Inflow(m <sup>3</sup> /s)	100	750	780	470	270

$$Q_{\text{initial}} = 100 \text{ m}^3/\text{s}$$

$$k = 18 \text{ hours}$$

$$x = 0.3$$

$$2kx < \Delta t < k$$

$$2 \times 18 \times 0.3 < \Delta t < 18$$

$$\Delta t = 12 \text{ hrs}$$

Using Muskingham equation

$$C_0 = \frac{-kx + 0.5 \Delta t}{k(1-x) + 0.5 \Delta t} = \frac{-18 \times 0.3 + 0.5 \times 12}{18(1-0.3) + 0.5 \times 12} = 0.0323$$

$$C_1 = \frac{kx + 0.5 \Delta t}{k(1-x) + 0.5 \Delta t} = \frac{18 \times 0.3 + 0.5 \times 12}{18(1-0.3) + 0.5 \times 12} = 0.613$$

$$C_2 = \frac{k(1-x) - 0.5 \Delta t}{k(1-x) + 0.5 \Delta t} = \frac{18(1-0.3) - 0.5 \times 12}{18(1-0.3) + 0.5 \times 12} = 0.355$$

■■■■