## SOIL MECHANICS

## CIVIL ENGINEERING

Date of Test: 04/05/2023

## ANSWER KEY

1. (b)
2. (c)
3. (b)
4. (a)
5. (c)
6. (b)
7. (c)
8. (b)
9. (c)
10. (c)
11. (a)
12. (b)
13. (d)
14. (b)
15. (c)
16. (b)
17. (a)
18. (c)
19. (a)
20. (b)
21. (c)
22. (b)
23. (a)
24. (a)
25. (a)
26. (a)
27. (c)
28. (c)
29. (b)
30. (a)

## DETAILED EXPLANATIONS

1. (b)

$$
\begin{array}{lr}
\because & I_{D}=\frac{\frac{1}{\gamma_{d \min }}-\frac{1}{\gamma_{d}}}{\frac{1}{\gamma_{d \text { min }}}-\frac{1}{\gamma_{d \max }}} \\
\Rightarrow & 0.7=\frac{\frac{1}{14}-\frac{1}{\gamma_{d}}}{\frac{1}{14}-\frac{1}{17}} \\
\Rightarrow & \gamma_{d}=15.97 \mathrm{kN} / \mathrm{m}^{3} \\
\because & \gamma=\gamma_{d}(1+w) \\
\Rightarrow & \gamma=15.97(1+0.08) \\
\Rightarrow & \gamma=17.25 \mathrm{kN} / \mathrm{m}^{3}
\end{array}
$$

2. (b)

$$
\begin{array}{ll}
n=0.5 \\
\therefore & e=\frac{n}{1-n}=\frac{0.5}{0.5}=1 \\
\therefore & \gamma=\frac{(G+S e) \gamma_{w}}{1+e}=\frac{(2.7+0.7 \times 1) \times 10}{1+1}=17 \mathrm{kN} / \mathrm{m}^{3}
\end{array}
$$

3. (a)

$$
\because \quad q=K H \frac{N_{f}}{N_{D}}
$$

$K=6.67 \times 10^{-7} \mathrm{~m} / \mathrm{s}, H=6 \mathrm{~m}, N_{D}=18$,
$N_{f}=8-1=7(\because 8$ flow lines will correspond to 7 flow channels $)$

$$
\begin{aligned}
q & =6.67 \times 10^{-7} \times 6 \times \frac{7}{18} \\
& =6.67 \times 10^{-7} \times 6 \times \frac{7}{18} \times 60 \times 60 \times 24 \\
& =0.134 \mathrm{~m} / \mathrm{m} / \text { day }
\end{aligned}
$$

4. (b)

$$
\begin{aligned}
\sigma_{z} & =\frac{2 q}{\pi z}=\frac{2 \times 150}{\pi \times 5} \\
& =19.099 \mathrm{kN} / \mathrm{m}^{2}
\end{aligned}
$$

5. (c)

$$
\begin{aligned}
\text { Initial pore water pressure } & =110 \mathrm{kPa} \\
\text { Excess pore water pressure } & =100 \mathrm{kPa}
\end{aligned}
$$

After $40 \%$ consolidation, remaining excess porewater pressure $=100 \times(1-0.4)=60 \mathrm{kPa}$ So total pore pressure $=110+60=170 \mathrm{kPa}$
6. (a)

$$
\begin{aligned}
S_{i} & =q B\left(\frac{1-\mu^{2}}{E}\right) \cdot I_{f} \\
S_{i} & =\frac{500}{1.5 \times 1.5} \times 1.5\left[\frac{1-0.5^{2}}{2 \times 10^{3}}\right] \times 0.5 \\
& =0.0625 \mathrm{~m}=62.5 \mathrm{~mm}
\end{aligned}
$$

8. (c)

$$
A_{r}=\frac{160^{2}-145^{2}}{145^{2}} \times 100=21.78 \%
$$

Since area ratio is greater than $20 \%$ so the soil sample is disturbed.
10. (a)

$$
\begin{aligned}
k_{e q} & =\frac{z_{1}+z_{2}+z_{3}+z_{4}}{\frac{z_{1}}{k_{1}}+\frac{z_{2}}{k_{2}}+\frac{z_{3}}{k_{3}}+\frac{z_{4}}{k_{4}}} \\
& =\frac{3+2+4+1}{\frac{3}{2}+\frac{2}{1}+\frac{4}{4}+\frac{1}{3}}=2.07 \mathrm{~mm} / \mathrm{s}
\end{aligned}
$$

11. (b)

Total load, $Q=200 \times 4 \times 4=3200 \mathrm{kN}$
Divide this load in four equal squares of $2 \mathrm{~m} \times 2 \mathrm{~m}$ size, as shown in figure,
$\therefore$ Load in each part square $=\frac{3200}{4}=800 \mathrm{kN}$
The distance from $A$ to $O$ i.e. $A O=\sqrt{2} \mathrm{~m}$
By symmetry, the stress $\sigma_{z}$ at $O$ at 4 m depth is four times of that caused by one load.


So,

$$
\begin{aligned}
\sigma_{z} & =\frac{4 \times 800}{4^{2}} \times \frac{3}{2 \pi} \times\left[\frac{1}{1+\left(\frac{\sqrt{2}}{4}\right)^{2}}\right]^{5 / 2} \\
& =71.136 \mathrm{kN} / \mathrm{m}^{2} \\
& \simeq 71.14 \mathrm{kN} / \mathrm{m}^{2}
\end{aligned}
$$

12. (c)

$$
\begin{align*}
\beta & =9^{\circ}, \phi=27^{\circ} \\
K_{a} & =\cos \beta\left(\frac{\cos \beta-\sqrt{\cos ^{2} \beta-\cos ^{2} \phi}}{\cos \beta+\sqrt{\cos ^{2} \beta-\cos ^{2} \phi}}\right) \tag{i}
\end{align*}
$$

Putting values in (i), we get, $K_{a}=0.392$

$$
\begin{equation*}
K_{p}=\cos \beta\left(\frac{\cos \beta+\sqrt{\cos ^{2} \beta-\cos ^{2} \phi}}{\cos \beta-\sqrt{\cos ^{2} \beta-\cos ^{2} \phi}}\right) \tag{ii}
\end{equation*}
$$

Putting values in (ii), we get, $K_{p}=2.488$

$$
\therefore \quad \frac{K_{p}}{K_{a}}=\frac{2.488}{0.392}=6.35
$$

13. (b)

Designing as a floating raft,
Applied load + over burden + self weight $=$ weight of soil excavated

$$
\Rightarrow \frac{\left(1+0.3 \frac{B}{L}\right) C N_{C}+\gamma D_{f}-\gamma D_{f}+\text { over burden }}{F}=\gamma D_{f}
$$

$$
\Rightarrow \frac{\left(1+0.3 \times \frac{8}{10}\right) \times 15 \times 5.7+20}{1.5}=15 \times D_{f}
$$

$$
\Rightarrow \quad D_{f}=5.6 \mathrm{~m}
$$

14. (b)

$$
\begin{aligned}
\text { Ultimate pull } & =\alpha \bar{C} A_{s}+W_{P} \\
& =0.5 \times 120 \times(\pi \times 0.5 \times 12)+\frac{\pi}{4} \times 0.5^{2} \times 12 \times 25 \\
& =1189.88 \mathrm{kN}
\end{aligned}
$$

15. (d)

Negative skin friction in individual action $=n[\alpha \bar{c} A]$

$$
\begin{aligned}
& =9 \times 0.9 \times 20 \times 1.3 \times 3 \\
& =631.8 \mathrm{kN}
\end{aligned}
$$

Negative skin friction for pile group $=\alpha \bar{c}(4 B L)+$ weight of soil in negative zone

$$
\begin{aligned}
& =\alpha \bar{c}(4 B L)+\gamma A L \\
& =1 \times 20(4 \times 2.5 \times 3)+16 \times 2.5^{2} \times 3 \\
& =900 \mathrm{kN} \\
\text { So, } \quad Q & =900 \mathrm{kN}
\end{aligned}
$$

16. (c)

$$
\text { Shrinkage limit, } \quad \begin{aligned}
w s & =w_{1}-\Delta w \\
& =w_{1}-\frac{\Delta V \cdot \rho_{w}}{M_{S}} \\
& =\frac{M_{1}-M_{d}}{M_{d}}-\frac{\left(V_{1}-V_{d}\right) \rho_{w}}{M_{d}} \\
& =\frac{55.4-39.8}{39.8}-\frac{(29.2-21.1) \times 1}{39.8} \\
& =0.188 \\
\text { i.e. } \quad w_{s} & =18.8 \%
\end{aligned}
$$

17. (a)

As per Karman-Cozney relation

$$
\begin{array}{rlrl} 
& \because & k & =C D^{2}\left(\frac{\gamma_{w}}{\mu}\right)\left(\frac{e^{3}}{1+e}\right) \\
& \therefore & k & \propto \frac{e^{3}}{1+e} \\
\Rightarrow & \frac{k_{1}}{k_{2}} & =\frac{e_{1}^{3}}{1+e_{1}} \times \frac{1+e_{2}}{e_{2}^{3}} \\
\Rightarrow & \frac{k_{1}}{k_{2}} & =\frac{(0.27)^{3}}{1+0.27} \times \frac{1+0.15}{(0.15)^{3}} \\
& & k_{1} & =5.28 k_{2}
\end{array}
$$

$\therefore \quad$ Percentage change in permeability $=\frac{k_{2}-k_{1}}{k_{1}} \times 100$

$$
=\frac{k_{2}-5.28 k_{2}}{5.28 k_{2}} \times 100=-81.06
$$

$\therefore \quad$ Percentage change $=81.06 \%$
18. (c)

$$
\begin{aligned}
\mathrm{C}_{\mathrm{u} \text { (undisturbed) }} & =\frac{T}{\pi d^{2}\left[\frac{h}{2}+\frac{d}{6}\right]}=\frac{35 \times 1000}{\pi \times 60^{2} \times\left[\frac{100}{2}+\frac{60}{6}\right]} \\
& =0.05158 \mathrm{~N} / \mathrm{mm}^{2}=51.58 \mathrm{kN} / \mathrm{m}^{2} \\
\mathrm{C}_{\mathrm{u} \text { (remoulded) }} & =\frac{5 \times 1000 \times 10^{3}}{\pi \times 60^{2}\left[\frac{100}{2}+\frac{60}{6}\right]} \mathrm{kN} / \mathrm{m}^{2}=7.368 \mathrm{kN} / \mathrm{m}^{2}
\end{aligned}
$$

$\therefore \quad$ Sensitivity of the clay $=\frac{C_{u(\text { undisturbed })}}{C_{u(\text { remoulded })}}=\frac{51.58}{7.368}=7$
19. (a)

$$
\begin{aligned}
S \times e & =w G \\
\Rightarrow \quad e & =\frac{2.7 \times 0.2222}{1} \simeq 0.6 \\
\gamma_{\mathrm{sat}} & =\left(\frac{G+e}{1+e}\right) \gamma_{w}=\left(\frac{2.7+0.6}{1+0.6}\right) \times 10 \\
& =20.625 \mathrm{kN} / \mathrm{m}^{3}
\end{aligned}
$$

Effective stress at centre of clay layer

$$
\begin{aligned}
& \bar{\sigma}_{0}=(18-10) \times 2+(20.625-10) \times 0.5 \\
\Rightarrow \quad & \bar{\sigma}_{0}=21.31 \mathrm{kN} / \mathrm{m}^{2}
\end{aligned}
$$

Load distribution dimensions at the centre of clay layer $=2+0.75+0.75=3.5 \mathrm{~m}$ Increase in stress due to load,

$$
\begin{aligned}
\Delta \sigma & =\frac{200}{3.5 \times 3.5} \\
& =16.33 \mathrm{kN} / \mathrm{m}^{2} \\
\Delta H & =\frac{C_{c} H}{1+e} \log _{10}\left(\frac{\bar{\sigma}_{0}+\Delta \sigma}{\bar{\sigma}_{0}}\right) \\
& =\frac{0.4 \times 1}{1+0.6} \log _{10}\left(\frac{21.31+16.33}{21.31}\right) \\
& =0.06176 \mathrm{~m}=61.67 \mathrm{~mm}
\end{aligned}
$$

20. (c)

Samples obtained from auger are disturbed samples

| Degree of <br> expansiveness | DFS <br> percent |
| :--- | ---: |
| Low | $<20$ |
| Moderate | 20 to 35 |
| High | 35 to 50 |
| Very High | $>50$ |

21. (b)

$$
\begin{array}{rlrl}
i_{c r} & =\frac{G-1}{1+e}=(G-1)(1-n) \\
\Rightarrow & & i_{c r} & =(2.7-1)(1-0.3) \\
\Rightarrow & i_{c r} & =1.19 \\
& & i_{\text {allowable }} & =\frac{1.19}{\mathrm{FOS}} \\
\Rightarrow & i_{\text {allowable }} & =\frac{1.19}{1.5}=0.7933 \\
\therefore & (2+x) \times 0.7934 & =1.90 \\
\Rightarrow & 2+x & =2.395 \\
\Rightarrow & x & =0.395 \mathrm{~m} \simeq 0.4 \mathrm{~m}
\end{array}
$$

## Alternatively

Given,

$$
\begin{aligned}
n & =0.3, G_{s}=2.7 \\
H_{L} & =1.9 \mathrm{~m} \\
\text { FOS } & =1.5 \\
\text { FOS } & =\frac{\text { Buoyand weight }}{\text { Seepage force }} \\
& =\frac{\gamma_{\text {sub }}(2+x) A}{\gamma_{w} h_{L} A}=\frac{\left(\frac{G_{s}-1}{1+e}\right) \gamma_{w}(2+x)}{\gamma_{w} \times h_{L}} \\
& =\left(G_{s}-1\right) \frac{(1-n)(2+x)}{h_{L}}
\end{aligned}
$$

$$
\begin{aligned}
1.5 & =(2.7-1) \frac{(1-0.3)(2+x)}{1.9} \\
(2+x) & =\frac{1.5 \times 1.9}{1.7 \times 0.7} \\
x & =\frac{1.5 \times 1.9}{1.7 \times 0.7}-2 \\
& =0.395 \simeq 0.4 \mathrm{~m}
\end{aligned}
$$

22. (a)

Given, $w_{P}=35 \%, I_{p}=w_{L}-w_{P}=10 \%, w_{L}=\left(I_{p}+w_{p}=10+35\right)=45 \%$
We know that, $\frac{V_{L}-V_{P}}{w_{L}-w_{P}}=\frac{V_{P}-V_{d}}{w_{P}-w_{s}}$
Given

$$
\begin{aligned}
V_{d} & =(1-0.25) V_{p}=0.75 V_{p} \\
V_{d} & =(1-0.32) V_{L}=0.68 V_{L}
\end{aligned}
$$

$$
\therefore \quad w_{p}-w_{s}=\frac{\left(w_{L}-w_{p}\right)\left(V_{p}-V_{d}\right)}{\left(V_{L}-V_{p}\right)}=\frac{10\left(\frac{1}{0.75}-1\right) V_{d}}{\left(\frac{1}{0.68}-\frac{1}{0.75}\right) V_{d}}
$$

$$
\Rightarrow \quad w_{p}-w_{s}=24.28
$$

$$
\Rightarrow \quad w_{s}=35-24.28=10.72 \%
$$

Shrinkage ratio, $R=\frac{\left(V_{1}-V_{2}\right) / V_{d}}{w_{1}-w_{2}} \times 100=\frac{\left(V_{L}-V_{d}\right) / V_{d}}{w_{L}-w_{s}} \times 100$

$$
=\frac{\left(\frac{1}{0.68}-1\right)}{45-10.72} \times 100=1.372 \approx 1.37
$$

23. (a)


$$
\begin{aligned}
\phi & =30^{\circ} \\
\gamma_{t} & =20 \mathrm{kN} / \mathrm{m}^{3}
\end{aligned}
$$

FOS with seepage

$$
\frac{\gamma_{\text {sub }}}{\gamma_{\text {sat }}} \times \frac{\tan \phi}{\tan \beta}=\frac{(20-10)}{20} \times \frac{\tan \left(30^{\circ}\right)}{\tan \left(14^{\circ}\right)}=1.16
$$

24. (b)

$$
\begin{aligned}
\gamma_{\mathrm{sat}} & =\frac{G+e}{1+e} \times \gamma_{w}=\frac{2.65+1}{1+1} \times 9.81=17.9 \mathrm{kN} / \mathrm{m}^{3} \\
\gamma^{\prime} & =\gamma_{\mathrm{sat}}-\gamma_{w}=17.9-9.81=8.1 \mathrm{kN} / \mathrm{m}^{3}
\end{aligned}
$$

For sudden drawdown $\gamma=\gamma_{\text {sat }}$

$$
\begin{aligned}
& \phi_{w}=\frac{\gamma^{\prime}}{\gamma_{s a t}} \times \phi_{u}=\frac{8.1}{17.9} \times 15=6.8^{\circ} \\
& F_{C}=\frac{C_{u}}{S_{n} \times \gamma H}=\frac{12}{0.126 \times 17.9 \times 5}=1.06
\end{aligned}
$$

25. (c)

The Kaolinite structural unit consists a alternating layers of silica tetrahedral with the tips embedded in an alumina (gibbsite) octahedral unit as shown.


The combined silica-gibbsite sheet are held together by hydrogen bonding.
The structural unit montmorillonite mineral is composed of two silica sheets and one alumina (gibbsite) sheet as shown.


The interlayer bonding between the tops of silica sheets is mainly due to Vander walls' forces and is thus, very weak compared to hydrogen or other ion bonding.
Bentonite is a montmorillonite clay derived from volcanic ash. It is used in drilling oil wells and in soil exploration as a 'drilling mud' and as a clay grout.
26. (c)

- Local shear failure, generally occurs in soil having somewhat plastic stress-strain curve e.g., loose sand and soft clays.
- Cyclic pile load test is carried out when it is required to required to determine, skin friction and end bearing capacity separately for a pile load on a single pile.

27. (c)


Total axial frictional resistance

$$
\begin{aligned}
& =\frac{\gamma_{d} L_{1}+0}{2} \times k \times \tan \delta \times A_{1}+\gamma_{d} L_{1} \times k \times \tan \delta \times A_{2}+\frac{\left[\left(\gamma_{s a t}-\gamma_{w}\right) \times L_{2}\right]}{2} \times k \times \tan \delta \times A_{2} \\
& \Rightarrow P_{a}=\frac{18 \times 4+0}{2} \times 0.9 \times \tan 28^{\circ} \times 4 \times 2+72 \times 0.9 \times \tan 28^{\circ} \times 6 \times 2+\frac{[(20-9.81) \times 6]}{2} \times 0.9 \times \tan 28^{\circ} \times 6 \times 2 \\
& =726.82 \mathrm{kN}
\end{aligned}
$$

28. (b)

$$
\begin{aligned}
q_{z} & =q\left(1-\cos ^{3} \theta\right) \\
q & =6 \mathrm{kN} / \mathrm{m}^{2} \\
\cos \theta & =\frac{6}{7.81} \\
q_{z} & =6 \times\left[1-\left(\frac{6}{7.81}\right)^{3}\right] \\
& =3.28 \mathrm{kN} / \mathrm{m}^{2}
\end{aligned}
$$


29. (a)

30. (a)

As more than $50 \%$ is retained on $75 \mu$ IS sieve, the soil is coarse-grained.

$$
\begin{aligned}
\text { Coarse fraction } & =100-45=55 \% \\
\text { Gravel fraction } & =100-60=40 \% \\
\text { Sand fraction } & =55-40=15 \%
\end{aligned}
$$

As more than half the coarse fraction is larger than 4.75 mm sieve, the soil is gravel.
Also,

$$
\begin{aligned}
I_{P} & =w_{L}-w_{P}=40-12=28 \% \\
I_{P} & =0.73\left(w_{L}-20\right) \\
& =0.73(40-20)=14.6 \%
\end{aligned}
$$

$\because \quad I_{p}$ is above A-line, therefore the soil should be GC as per IS classification.

