## CPMT-PERT

## CIVIL ENGINEERING

Date of Test : 08/05/2023

## ANSWER KEY

1. (a)
2. (c)
3. (a)
4. (a)
5. (a)
6. (a)
7. (d)
8. (a)
9. (c)
10. (b)
11. (c)
12. (c)
13. (d)
14. (b)
15. (c)
16. (d)
17. (d)
18. (a)
19. (c)
20. (c)
21. (b)
22. (d)
23. (b)
24. (c)
25. (a)
26. (a)
27. (a)
28. (c)
29. (b)
30. (d)

## DETAILED EXPLANATIONS

1. (a)

Only $D$ is predecessor to activity $F$
2. (a)

| Activity | $1-2$ | $2-3$ | $2-4$ | $3-5$ | $2-5$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Expected time (in days) | 7 | 3 | 12 | 11 | 9 |

$T_{E}=10$

3. (c)

$$
\text { Cost slope }=\frac{8600-6000}{8-3}=520
$$

For duration of 5 days
Direct cost $=6000+520(8-5)=₹ 7560$
6. (a)

In bar charts, inter dependences between various activities is not shown.
7. (c)

Correct sequence of analysing a project will be as follows:

1. Work break down structure.
2. Network diagram.
3. Resource allocation and scheduling.
4. Project completion time.
5. Time cost study.
6. (d)

Project duration will be $4 T$ as there are four activities are in series but over all project duration will be $4 T$ $\pm 3 \sigma$.

$$
\begin{array}{rlrl} 
& & \sigma \text { for entire project } & =\sqrt{K^{2}+K^{2}+K^{2}+K^{2}} \\
\Rightarrow & & \sigma & =2 K \\
\therefore \quad & \text { Over all project duration } & =4 T \pm 6 K
\end{array}
$$

9. (c)

$$
\text { Cost slope }=\frac{c_{c}-c_{n}}{t_{n}-t_{c}}
$$


10. (d)

$$
\begin{aligned}
\mathrm{FDB} & =1-\left(\frac{c_{S}}{c_{i}}\right)^{1 / n} \\
& =1-\left(\frac{2000}{16000}\right)^{1 / 3}=0.5
\end{aligned}
$$

11. (d)

Cost of machine $=₹ 100000$
Rate of interest, $i=10 \%=0.1$

$$
\begin{aligned}
& \text { Capital recovery factor }(\mathrm{CRF})=\frac{i(1+i)^{n}}{(1+i)^{n}-1} \\
& \Rightarrow \quad \text { CRF }=\frac{0.1(1+0.1)^{20}}{(1+0.1)^{20}-1}=0.11746
\end{aligned}
$$

$\therefore$ The annual equipment cost $=100000 \times 0.11746$

$$
=₹ 11746
$$

12. (a)

For given network diagram,


Project completion time $=17$ weeks
Critical path $=1-3-5-7$
Slack of event $4=10$ weeks
Total float of activity 6-7 = 1 week
13. (a)

14. (a)


For given project,
Standard deviation $\sigma=\sqrt{9}=3$ days
Probability factor for $T_{S}=25, Z=\frac{25-28}{3}=-1$
Probability of completion within 25 days

$$
=100-84=16 \%
$$

For probability of completion after 31 days

$$
\begin{aligned}
\text { Probability factor, } Z & =\frac{31-28}{3}=1 \\
\text { Probability of completion } & =100-84=16 \% \\
\text { Total probability } & =16+16=32 \%
\end{aligned}
$$

15. (d)

During crashing of an activity, the duration of activity is reduced due to which:

1. Indirect cost decreases.
2. Direct cost increases.
3. (a)

| Activity | Crash limit (days) | Cost Slope (₹/day) |
| :---: | :---: | :---: |
| A | $4-3=1$ | $(105-80) /(4-3)=25$ |
| B | $6-4=2$ | $(250-180) /(6-4)=35$ |
| C | $8-5=3$ | $(320-200) /(8-5)=40$ |
| D | $10-6=4$ | $(530-350) /(10-6)=45$ |

Activity
A
B
Critical $-\quad \checkmark \quad \checkmark \quad \checkmark$
C
D
Critical - $\checkmark \quad \checkmark \quad \checkmark$

Since the critical activity $B$ has the lowest crash cost per day, it should be crashed first.
Hence, crash activity $B$ by 2 days


Critical path is still $B-C-D$
Project completion time = 22 days
Project cost $=810+(2)(35)=₹ 880$
17. (b)

Network diagram,


For activity 3-4,

$$
\begin{aligned}
\mathrm{EST} & =11 \\
\mathrm{EFT} & =11+10=21 \\
\mathrm{LFT} & =34 \\
\text { Total float } & =34-21=13 \text { days }
\end{aligned}
$$

For activity 3-6,

$$
\begin{aligned}
\text { EST } & =11 \\
\text { EFT } & =11+15=26 \\
\text { LFT } & =35 \\
\text { Total float } & =35-26=9 \text { days } \\
\text { Sum of total float } & =13+9=22 \text { days }
\end{aligned}
$$

18. (c)

For the given project, available paths are:
Available paths
(i) $1-2-3-5-6 \Rightarrow$ Time duration $=18$ days
(ii) $1-2-4-5-6 \Rightarrow$ Time duration $=18$ days

So both paths are critical.
Combination of activities to crash the path, and their respectively cost slopes are given below:
(i) only $A \quad \rightarrow$ ₹ 600/day
(ii) only $F \rightarrow$ ₹ 700/day
(iii) $B$ and $C \rightarrow 200+300=₹ 500 /$ day
(iv) $B$ and $E \quad \rightarrow \quad 200+200=₹ 400 /$ day
(v) $D$ and $C \quad \rightarrow \quad 300+300=₹ 600 /$ day
(vi) Dand $E \quad \rightarrow \quad 300+200=₹ 500 /$ day

So we will crash that combination of activity for which slope is minimum i.e. $B$ and $E$.
19. (a)

| Path available | Duration (days) | Standard deviation <br> (days) |
| :--- | :---: | :---: |
| $1-2-4-6$ | $5+8+17=30$ |  |
| $1-2-4-5-6$ | $5+8+5+18=36$ | 2.345 |
| $1-2-5-6$ | $5+13+18=36$ | 2.69 |
| $1-3-5-6$ | $4+11+18=33$ |  |

So, number of critical path $=2$
Path with more uncertainty $=1-2-5-6$
20. (c)

For given network diagram


After updating

21. (b)


Sum of slacks $=2+1=3$ days
22. (c)

23. (c)

There is an extra dummy between events (7) and (8).
There are two arrows joining events (2) and (4).
There is extra dummy connecting nodes (4) and (6).
The correct diagram will be


So there are two errors.
24. (b)

$$
\begin{aligned}
\text { Expected time } & =\frac{t_{0}+t_{p}+4 t_{m}}{6}=\frac{12+25+20 \times 4}{6} \\
& =\frac{117}{6} \text { minutes }
\end{aligned}
$$

Standard deviation, $\sigma=\frac{t_{p}-t_{0}}{6}=\frac{25-12}{6}=\frac{13}{6}$ minutes
Minimum time alloted, $t_{\text {min }}=t_{E}-3 \sigma$

$$
=\frac{117}{6}-\frac{3 \times 13}{6}=13 \text { minutes }
$$

25. (a)

For given relationship

26. (b)

Let $N$ be the number of unit
At breakdown point,
Fixed cost + Variable cost $=$ Total cost
$\Rightarrow \quad 1000000+100 \times N=5000000$
$\therefore \quad N=40000$ units
Suppose the selling price per unit be $₹ x$
Now, Margin of safety $=\frac{\text { Total sales }- \text { Sales at BEP }}{\text { Total sales }}$

$$
\left.\begin{array}{ll}
\Rightarrow & \frac{10}{100} \\
= & =\frac{5000000-40000 \times x}{5000000} \\
\therefore & x
\end{array}\right) ₹ 112.5
$$

27. (c)


Standard deviation of project,

$$
\begin{aligned}
& \sigma=\sqrt{4+16+4+1}=5 \text { days } \\
& Z=\frac{T_{S}-T_{E}}{\sigma}=\frac{31-36}{5}=-1
\end{aligned}
$$

Thus,

$$
\begin{aligned}
P(t \leq 31) & =P(Z \leq-1) \\
& =0.5-\phi(1)=0.5-(0.8413-0.5) \\
& =0.1587=15.87 \%
\end{aligned}
$$

28. (c)

From straight line method of depreciation

$$
\text { Depreciation, } \begin{aligned}
D & =\frac{c_{i}-c_{s}}{n} \\
D & =\frac{10000-1000}{5}=\text { Rs. } 1800 \\
\text { Book value, } B_{m} & =c_{i}-m D \\
B_{2} & =10000-2 \times 1800 \\
& =\text { Rs. } 6400
\end{aligned}
$$

29. (a)

| Project No. | Cost (₹) | No. of Cars | Unit Cost (₹) |
| :---: | :---: | :---: | :---: |
| 1. | 450000 | 150 | 3000 |
| 2. | 320000 | 80 | 4000 |
| 3. | 600000 | 120 | 5000 |
| 4. | 360000 | 90 | 4000 |
| 5. | 300000 | 60 | 5000 |
| 6. | 660000 | 220 | 3000 |
| 7. | 280000 | 70 | 4000 |
| 8. | 720000 | 180 | 4000 |

Forecast weighted unit cost,

$$
\begin{aligned}
& \qquad \begin{aligned}
U C & =\frac{A+4 B+C}{6} \\
\text { where, } \quad A & =₹ 5000 \\
B & =\frac{3000+4000+5000+4000+5000+3000+4000+4000}{8}=₹ 4000 \\
C & =₹ 3000 \\
\therefore \quad U C & =\frac{5000+4 \times 4000+3000}{6}=₹ 4000 \\
\text { Project cost } & =U C \times \text { Number of units } \\
& =4000 \times 135=₹ 540000
\end{aligned}
\end{aligned}
$$

30. (d)

$$
\begin{aligned}
\bar{X} & =17 \text { units } \\
\text { Variance, } \sigma^{2} & =9 \\
\text { Standard deviation, } \sigma & =3
\end{aligned}
$$

$$
Z=\frac{x-\bar{x}}{\sigma}
$$



For 22 days,

$$
Z=\frac{22-17}{3}=\frac{5}{3}=1.67
$$

$$
P(Z<1.67)=95.2 \%
$$

For 20 days,

$$
Z=\frac{20-17}{3}=\frac{3}{3}=1
$$

$$
P(Z<1)=84.13 \%
$$

$\therefore \quad P(Z<1.66)-P(Z<1)=95.2 \%-84.13 \%$
= 11.07\%

