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**METROLOGY+METAL CUTTING+MACHINE TOOL**

**MECHANICAL ENGINEERING**

**Date of Test : 31/08/2022**

**ANSWER KEY >**

- |        |         |         |         |         |
|--------|---------|---------|---------|---------|
| 1. (b) | 7. (c)  | 13. (c) | 19. (b) | 25. (b) |
| 2. (d) | 8. (c)  | 14. (c) | 20. (c) | 26. (c) |
| 3. (d) | 9. (a)  | 15. (c) | 21. (d) | 27. (c) |
| 4. (a) | 10. (b) | 16. (c) | 22. (a) | 28. (b) |
| 5. (b) | 11. (d) | 17. (c) | 23. (b) | 29. (b) |
| 6. (c) | 12. (b) | 18. (d) | 24. (d) | 30. (a) |

## DETAILED EXPLANATIONS

2. (d)

$$\begin{aligned} \text{Maximum interference} &= \text{Shaft}_{\max} - \text{Hole}_{\min} \\ &= 50.04 - 50.03 \\ &= 0.01 \text{ mm} \end{aligned}$$

5. (b)

From Taylor's tool life equation,

$$VT^n = \text{constant (K)}$$

$$\frac{V_1}{V_2} = \left(\frac{T_2}{T_1}\right)^n$$

or

$$n = \frac{\log_e\left(\frac{V_1}{V_2}\right)}{\log_e\left(\frac{T_2}{T_1}\right)} = \frac{\log_e\left(\frac{70}{100}\right)}{\log_e\left(\frac{49}{90}\right)} = 0.5866$$

∴  $K = 70 \times 90^{0.5866} = 980.52$

Now,

$$T^n = \frac{K}{V} = \frac{980.52}{90} = 10.8946$$

$$T = (10.8946)^{(1/0.5866)} = 58.638 \text{ min} \simeq 59 \text{ min}$$

6. (c)

Slip guage or guage blocks are used as standards for precision measurement.

7. (c)

$$T = \frac{L}{f \times N} = \frac{70}{0.3 \times 75} = 3.11$$

8. (c)

$$\sin\left(\frac{\alpha}{2}\right) = \tan\left(\frac{\alpha}{2}\right) = \frac{D-d}{2L} \quad (\alpha = 4^\circ)$$

$$\begin{aligned} \text{Tailstock offset} &= \frac{D-d}{2} = L \sin\left(\frac{\alpha}{2}\right) = 600 \sin 2^\circ \\ &= 20.94 \text{ mm} \end{aligned}$$

9. (a)

Broaching is a multipoint cutting tool operation in which a bar or rod type cutter with a series of cutting edges gradually increasing in size are used.

10. (b)

$$V = \frac{NL(1+m)}{1000} = \frac{20 \times 300 \left(1 + \frac{3}{4}\right)}{1000} = 10.5 \text{ m/min}$$

11. (d)

$$V = 10 \text{ m/min,}$$

$$\alpha = 35^\circ$$

$$l_c = 55 \text{ mm}$$

Assuming no expansion along width,

$$\therefore t_1 \cdot \pi D = l_c \cdot t_2$$

$$\therefore \frac{t_1}{t_2} = \frac{l_c}{\pi D} \Rightarrow \text{chip-thickness ratio}$$

$$\Rightarrow \frac{55}{\pi \times 30} \Rightarrow 0.5835$$

$$r = 0.5835$$

$$\therefore \tan \phi = \frac{r \cos \alpha}{1 - r \sin \alpha} = \frac{0.5835 \cos 35^\circ}{1 - 0.5835 \sin 35^\circ}$$

$$\tan \phi = 0.7184$$

$$\phi = 35.694$$

$$V_s = \frac{V \cos \alpha}{\cos(\phi - \alpha)} = \frac{10 \cos 35^\circ}{\cos(35.694^\circ - 35^\circ)} = 8.192 \text{ m/min}$$

12. (b)

For minimum power,

$$2\phi + \beta - \alpha = 90^\circ$$

$$\Rightarrow \beta - \alpha = 20^\circ \quad [ \because \phi = 35^\circ ]$$

$$\frac{F_T}{F_c} = \tan(\beta - \alpha) = \tan 20^\circ$$

$$\therefore \frac{F_c}{F_T} = 2.747$$

13. (c)

$$\text{Tool life } (T) \propto \frac{1}{\text{Flank wear}}$$

$$T \propto \frac{1}{\cot \alpha}$$

$$T \propto \tan \alpha$$

$$\frac{T_2}{T_1} = \frac{\tan \alpha_2}{\tan \alpha_1} = \frac{\tan 7^\circ}{\tan 10^\circ} = 0.7$$

$$T_2 = 0.7 T_1$$

Tool life will decrease by 30%.

14. (c)

For diameter step 18-30 mm

$$D = \sqrt{18 \times 30} = 23.23 \text{ mm}$$

$$\text{Tolerance unit (i)} = 0.45D^{1/3} + 0.001D = 1.284 + 0.02323 = 1.307 \text{ microns}$$

$$IT_8 = 26i = 26 \times 1.307$$

$$= 33.98 \approx 34$$

$$\text{Therefore, tolerance} = 34 \mu\text{m} = 0.034 \text{ mm}$$

$$\text{Tolerance for } 25H_8 = 0.034 \text{ mm}$$

$$\text{Hole size } 25H_8 = 25^{+0.034}_{+0.00} \text{ mm}$$

15. (c)

We know,

$$F = F_c \sin \alpha + F_t \cos \alpha = 450 \text{ N}$$

$$N = F_c \cos \alpha - F_t \sin \alpha = 900 \text{ N}$$

$$\mu = \frac{F}{N} = \frac{450}{900} = 0.5$$

16. (c)

Given :  $r = 0.5$ ;  $\alpha = 12^\circ$ ;  $v = 2.4 \text{ m/s}$

Now,

$$\tan \phi = \frac{r \cos \alpha}{1 - r \sin \alpha} = \frac{0.5 \cos 12^\circ}{1 - 0.5 \sin 12^\circ}$$

$$\phi = \tan^{-1}(0.5458) = 28.63^\circ$$

Shear velocity is,

$$v_s = \frac{v \cos \alpha}{\cos(\phi - \alpha)} = \frac{2.4 \cos 12^\circ}{\cos(28.63 - 12)} = 2.45 \text{ m/s}$$

$\therefore$  Shear strain rate =  $\frac{v_s}{t_s} = \frac{2.45}{25 \times 10^{-6}} = 9.8 \times 10^4 \text{ s}^{-1}$

17. (c)

$$2x + 0.03 + x = 0.05$$

$$3x = 0.02$$

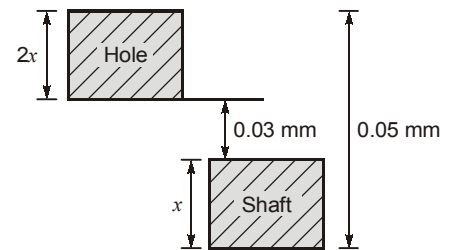
$$x = \frac{0.02}{3} = 6.66 \times 10^{-3}$$

$$= 0.00666 \text{ mm}$$

$$= 0.0067 \text{ mm}$$

Maximum limit of hole =  $40 + 2x = 40.0133 \text{ mm}$

Minimum limit of hole =  $40 \text{ mm}$



18. (d)

- Machining cost =  $\frac{C_m \pi DL}{1000 f V}$

$\Rightarrow$  Machining cost  $\propto \frac{1}{V}$

- Non productive cost is independent of velocity

- Tool changing cost =  $\frac{C_m \pi DL V^{\frac{1-n}{n}}}{1000 f C^{1/n}} \times T_c$

$\Rightarrow$  Tool changing cost increases with cutting velocity.

Here

$C_m$  = Machining cost per unit time

$T_c$  = Tool changing time per unit in min

$f$  = Feed rate in mm per revolution

$D$  = Diameter of work piece in mm

$L$  = Length of job to be machined in mm

$C$  = Constant from Taylor's tool life equation [ $VT^n = C$ ]

19. (b)

From the Merchant's circle,

$$F = R \sin \beta$$

$$F_c = R \cdot \cos(\beta - \alpha)$$

$$\text{Also, } R = \sqrt{F_t^2 + F_c^2} = \sqrt{539.55^2 + 245.25^2} = 592.67 \text{ N}$$

$$\text{Now, } F_c = R \cdot \cos(\beta - \alpha)$$

$$539.55 = 592.67 \times \cos(\beta - 10)$$

$$\beta = 34.44^\circ$$

$$\text{Now, } F = R \sin \beta = 592.67 \sin 34.44^\circ = 335.18 \text{ N}$$

20. (c)

 $\psi$  major cutting edge angle =  $60^\circ$  $\psi_1$  minor cutting edge angle = ? $\therefore$  Maximum height of roughness

$$\therefore H_{\max} = \frac{f}{(\tan \psi + \cot \psi_1)} \quad \dots (1)$$

$$R_a = \frac{H_{\max}}{4}$$

Given that

$$f = 0.05 \text{ mm}$$

$$R_a = 3 \times 10^{-3} \text{ mm}$$

So

$$R_a = \frac{f}{4(\tan \psi + \cot \psi_1)}$$

$$3 \times 10^{-3} = \frac{0.05}{4(\tan \psi + \cot \psi_1)}$$

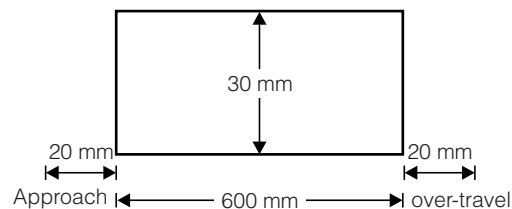
$$\tan \psi + \cot \psi_1 = \frac{50}{4 \times 3} = 4.1667$$

$$\tan 60^\circ + \cot \psi_1 = 4.1667$$

$$\cot \psi_1 = 4.1667 - \tan 60^\circ = 2.4346$$

$$\tan \psi_1 = 0.41074 = 22.33^\circ$$

21. (d)



$$\text{Total forward stroke length} = 20 + 600 + 20 = 640 \text{ mm}$$

$$\text{Forward time} = \frac{0.640}{8} \text{ min} = 0.08 \text{ min}$$

$$\text{Return time} = \frac{0.08}{2} = 0.04 \text{ min}$$

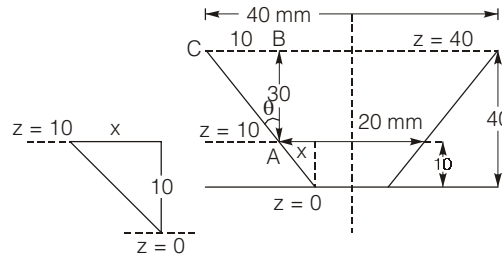
Total time in completing one stroke =  $0.08 + 0.04 = 0.12$  min

$$\text{Number of strokes} = \frac{30}{0.3} = 100 \text{ strokes}$$

Total machining time =  $0.12 \times 100 = 12$  min

22. (a)

$$\tan \theta = \frac{CB}{AB} = \frac{10}{30} = \frac{1}{3}$$



Now,

$$\tan \theta = \frac{x}{10}$$

$$\frac{1}{3} = \frac{x}{10}$$

⇒

$$x = \frac{10}{3} \text{ mm} = 3.33 \text{ mm}$$

So, diameter at  $z = 0$ ,

$$= 20 - 2x = 20 - 2 \times 3.33 = 13.334 \text{ mm}$$

23. (b)

$$\begin{aligned} \text{Minimum clearance} &= (\text{Hole})_{\text{minimum}} - (\text{Shaft})_{\text{maximum}} \\ &= 50.02 - 50.005 \end{aligned}$$

$$\text{Minimum clearance} = 0.015 \text{ mm}$$

24. (d)

$$X_{\text{max}} = 50.02 - (37.985 + 9.99) = 2.045 \text{ mm}$$

$$X_{\text{min}} = 49.98 - (38.015 + 10) = 1.995 \text{ mm}$$

$$\text{Tolerance} = X_{\text{max}} - X_{\text{min}} = 2.045 - 1.995 = 0.09 \text{ mm}$$

∴

$$X = 2 \pm 0.045 \text{ mm}$$

25. (b)

Maximum uncut chip thickness

$$t_{\text{max.}} = \frac{2f}{NZ} \sqrt{\frac{d}{D}}$$

where,

$N$  = rpm of cutter = 30 rpm

$d$  = depth of cut = 2 mm

$f$  = feed = 20 mm/min

$Z$  = number of teeth = 30

$D$  = cutter diameter = 80 mm

$$t_{\text{max.}} = \frac{2 \times 20}{30 \times 30} \sqrt{\frac{2}{80}} = 7.027 \mu\text{m}$$

27. (c)

$$\text{Breakthrough distance, } d = \frac{D}{2 \tan \alpha} = \frac{12}{2 \tan 60} = 3.464 \text{ mm}$$

$$\text{Drill point angle, } \alpha = 60$$

$$\text{Total length of travel} = 24 + 3.464 + 3 = 30.464 \text{ mm}$$

$$\text{Time required to drill a hole} = \frac{L}{fN} = \frac{30.464}{0.3 \times 350} \text{ min} = 17.408 \text{ sec.}$$

28. (b)

$$\begin{aligned} \frac{\text{Time}}{\text{Cut}} &= \frac{B}{fN} \\ &= \frac{300}{0.2} \times \frac{1}{10} = 150 \text{ min} \end{aligned}$$

29. (b)

$$\text{Given: } \quad \quad \quad 0.4 \text{ thread} \rightarrow 1 \text{ mm}$$

$$\text{then, } \quad \quad \text{pitch of lead screw (P)} = \frac{1}{0.4} = 2.5 \text{ mm}$$

Ratchet has 30 teeth

$$\therefore \text{ Pawl indexes } \frac{1}{30} \text{ revolution during each stroke}$$

$$\therefore \quad \quad \quad \text{feed} = \frac{1}{30} \times 2.5 = 0.083 \text{ mm}$$

30. (a)

$$D = 80 \text{ mm}, \quad \quad \quad z = 8$$

$$N = \frac{1000V}{\pi D} = \frac{1000 \times 20}{\pi \times 80} = 79.58 \text{ rpm}$$

$$V = 20 \text{ m/min}, \quad \quad \quad f = 160 \text{ mm/min}$$

$$d = 2 \text{ mm}$$

Maximum chip thickness,

$$\begin{aligned} t_{\max} &= \frac{2f_m}{Nz} \sqrt{\frac{d}{D}} \\ &= \frac{2 \times 160}{79.58 \times 8} \sqrt{\frac{2}{80}} = 0.079 \text{ mm} \end{aligned}$$

Minimum chip thickness,

$$t_{\min} = 0$$

$$t_{\text{avg}} = \frac{t_{\max} + t_{\min}}{2} = 0.0395 \text{ mm}$$

