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# INTERNAL COMBUSTION ENGINE

## MECHANICAL ENGINEERING

Date of Test : 21/09/2022

### ANSWER KEY >

- |        |         |         |         |         |
|--------|---------|---------|---------|---------|
| 1. (a) | 7. (c)  | 13. (d) | 19. (b) | 25. (b) |
| 2. (c) | 8. (b)  | 14. (a) | 20. (c) | 26. (a) |
| 3. (b) | 9. (b)  | 15. (b) | 21. (d) | 27. (a) |
| 4. (b) | 10. (d) | 16. (b) | 22. (c) | 28. (c) |
| 5. (a) | 11. (a) | 17. (d) | 23. (a) | 29. (b) |
| 6. (a) | 12. (c) | 18. (b) | 24. (c) | 30. (d) |

## DETAILED EXPLANATIONS

3. (b)

$$V_S = \frac{\pi}{4} d^2 L = \frac{\pi}{4} \times \frac{d^3}{1.1} = 245$$

$$d^3 = 343$$

 $\Rightarrow$ 

$$d = 7 \text{ cm}$$

$$L = \frac{d}{1.1} = \frac{7}{1.1} = 6.36 \text{ cm}$$

6. (a)

 $C_8H_{18} \rightarrow$  iso-octane

 $C_7H_{16} \rightarrow$  normal-heptane

 $C_{16}H_{34} \rightarrow$  normal-cetane

 $C_{11}H_{20} \rightarrow$   $\alpha$  - methyl naphthalene

7. (c)

Cam shaft runs at half the speed of crankshaft.

11. (a)

$$\frac{bp}{ip} = 0.8, \quad fp = 20 \text{ kW}$$

$$ip - bp = 20$$

$$ip - 0.8 \times ip = 20$$

or

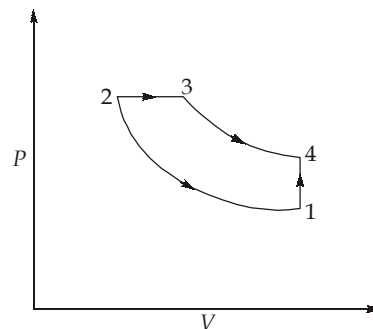
$$ip = 20 \times 5 = 100 \text{ kW}$$

$$bp = ip - fp = 100 - 20 = 80 \text{ kW}$$

12. (c)

SI engines are quantity governed engines.

18. (b)



Compression ratio,  $r = \frac{V_1}{V_2} = 15$

Expansion ratio,  $r_e = \frac{V_4}{V_3} = 10$

Cut-off ratio,  $r_c = \frac{r}{r_e} = \frac{V_1/V_2}{V_4/V_3} = \frac{V_3}{V_2} = \frac{15}{10} = 1.5$

$$[V_1 = V_4]$$

$$\begin{aligned} \text{Air standard efficiency, } \eta &= 1 - \frac{1}{\gamma} \frac{1}{r^{\gamma-1}} \left[ \frac{r_c^\gamma - 1}{r_c - 1} \right] = 1 - \frac{1}{1.4} \times \frac{1}{15^{0.4}} \left[ \frac{1.5^{1.4} - 1}{1.5 - 1} \right] \\ &= 0.6305 = 63.05\% \end{aligned}$$

19. (b)

$$\text{Indicated power, } IP = P_{\text{eff imep}} \times V_s \times \frac{(\text{Number of explosion})}{\text{Time of test}} \quad \dots (i)$$

Now, effective indicated mean effective pressure,

$$\begin{aligned} P_{\text{eff, imep}} &= P_{\text{imep}} - P_{\text{pumping mep}} \\ &= 6.4 - 0.6 = 5.8 \text{ bar} \end{aligned}$$

From equation (i),

$$\begin{aligned} IP &= 5.8 \times 10^5 \times \frac{\pi}{4} \times \frac{0.25^2 \times (1.9 \times 0.25) \times 3300}{1000 \times 40 \times 60} \\ &= 18.594 \text{ kW} \end{aligned}$$

$$\text{Brake power, } BP = (m_b \times g) \times r_d \times \left( \frac{2\pi \times \text{Number of revolution}}{\text{Time of test}} \right)$$

$$\begin{aligned} &= 90 \times 9.81 \times 0.8 \times \frac{2\pi \times 8080}{1000 \times 40 \times 60} \\ &= 14.941 \text{ kW} \end{aligned}$$

$$\text{Mechanical efficiency, } \eta_m = \frac{BP}{IP} = \frac{14.941}{18.594} = 0.8035 = 80.35\%$$

20. (c)

$$\text{Heat supplied/kg} = c_v (T_3 - T_2) + c_p (T_4 - T_3) \quad \dots (i)$$

$$\frac{T_2}{T_1} = \left( \frac{V_2}{V_1} \right)^{\gamma-1} = (10)^{1.4-1}$$

$$\begin{aligned} T_2 &= (10)^{0.4} \times 300 \\ &= 753.57 \text{ K} = 480.57^\circ\text{C} \end{aligned}$$

Now, from equation (i),

$$\begin{aligned} 878 &= 0.717 (987 - 480.57) + 1.004(T_4 - 987) \\ T_4 &= 1499.84^\circ\text{C} = 1772.84 \text{ K} \end{aligned}$$

$$\text{Cut-off ratio, } r_c = \frac{V_4}{V_3}$$

For constant pressure process (3-4)

$$\frac{V_4}{V_3} = \frac{T_4}{T_3}$$

$$\text{So, } r_c = \frac{T_4}{T_3} = \frac{1772.84}{1260} = 1.407 \quad [\because T_3 = 987^\circ\text{C} = 1260 \text{ K}]$$

21. (d)

$$\begin{aligned}
 V_s &= \frac{\pi}{4} \times 0.06^2 \times 0.1 \\
 &= 2.83 \times 10^{-4} \text{ m}^3/\text{cylinder} \\
 &= 283 \text{ cc/cylinder}
 \end{aligned}$$

$$\text{Compression ratio, } r = \frac{V_s + V_c}{V_c} = \frac{283 + 60}{60} = 5.72$$

$$\eta_{\text{air-std}} = 1 - \frac{1}{(r)^{\gamma-1}} = 0.5021 = 50.21\%$$

$$\begin{aligned}
 \eta_{\text{bth}} &= \eta_{\text{relative}} \times \eta_{\text{air-std}} = 0.5021 \times 0.52 \\
 &= 0.2611 = 26.11\%
 \end{aligned}$$

$$BP = \frac{2\pi NT}{60} = \frac{2\pi \times 3000 \times 65}{1000 \times 60} = 20.420 \text{ kW}$$

$$\eta_{\text{bth}} = \frac{BP(\text{Brake power})}{Q_s(\text{Heat supplied})} = \frac{BP}{\dot{m}_f \times CV}$$

$$\dot{m}_f = \frac{20.420 \times 3600}{0.2611 \times 43 \times 1000} = 6.547 \text{ kg/hr}$$

22. (c)

$$\text{Efficiency of Otto cycle} = 1 - \frac{1}{(r)^{\gamma-1}} \text{ (where, } r = \text{compression ratio)}$$

$$\eta_{\text{Otto}} = 1 - \frac{1}{(6)^{1.4-1}} = 0.5116 = 51.16\%$$

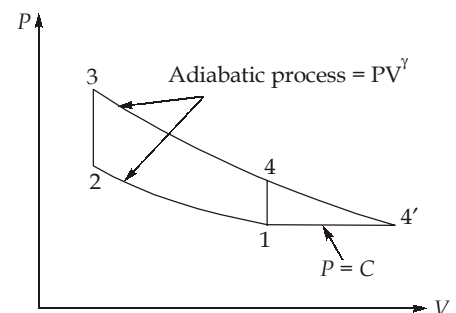
$$\begin{aligned}
 \text{Expansion ratio, (e)} &= \frac{V_4}{V_2} = \frac{V_4'}{V_3} = \left(\frac{P_3}{P_4'}\right)^{1/\gamma} = \left(\frac{P_3}{P_1}\right)^{1/\gamma} \\
 &= \left(\frac{20}{1}\right)^{1/1.4} = 8.497
 \end{aligned}$$

$$\text{Compression ratio, } r = 6$$

Efficiency of Atkinson cycle is given by

$$\begin{aligned}
 \eta_{\text{Atkinson}} &= 1 - \gamma \frac{(e-r)}{(e^\gamma - r^\gamma)} = 1 - 1.4 \frac{(8.497 - 6)}{(8.497^{1.4} - 6^{1.4})} \\
 &= 0.5466 = 54.66\%
 \end{aligned}$$

So, Difference in efficiencies = 54.66 - 51.16 = 3.5%



23. (a)

We know that, 
$$\eta_{bth} = \frac{BP}{m_f \times CV}$$

Given, 
$$\frac{m_f / hr}{BP} = 0.5 \text{ kg/kW-hr} = \frac{0.5}{3600} \text{ kg/sec-kW}$$

$$\eta_{bth} = \frac{1}{\frac{m_f}{BP} \times CV} = \frac{3600}{0.5 \times 43000} = 0.1674 = 16.74\%$$

$$\eta_m = \frac{\eta_{bth}}{\eta_{ith}}$$

$$\eta_{ith} = \text{Indicated thermal efficiency} = \frac{16.74}{0.8} = 0.20930 = 20.93\%$$

24. (c)

Work done per cycle,  $W = \text{Heat added} - \text{Heat Rejected}$   
 $= Q_S - Q_R$   
 $= C_v(T_3 - T_2) - C_v(T_4 - T_1)$

For isentropic compression and expansion processes

$$\frac{T_2}{T_1} = r^{\gamma-1}$$

and 
$$\frac{T_3}{T_4} = r^{\gamma-1}$$

Let  $\gamma - 1 = x$

So, 
$$W = C_v(T_3 - T_1 r^x) - C_v\left(\frac{T_3}{r^x} - T_1\right)$$

For maximum output:

$$\frac{dW}{dr} = 0$$

$$\Rightarrow -T_1 x r^{x-1} \times C_v - C_v \times T_3(-x) \times r^{-x-1} = 0$$

$$T_1 \times x = T_3 \frac{r^{-x-1}}{r^{x-1}} \times x$$

$$\frac{T_3}{T_1} = r^{2x}$$

$$r = \left(\frac{T_3}{T_1}\right)^{\frac{1}{2x}} = \left(\frac{T_3}{T_1}\right)^{\frac{1}{2(\gamma-1)}} = \left(\frac{T_3}{T_1}\right)^{\frac{1}{2(1.4-1)}} = \left(\frac{T_3}{T_1}\right)^{\frac{5}{4}}$$

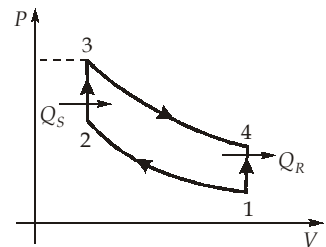
25. (b)

Compression ratio ( $r$ ) =  $\frac{V_1}{V_2} = \frac{400}{50} = 8$

So, efficiency of Otto cycle  $\eta_{Otto} = 1 - \frac{1}{(r)^{\gamma-1}} = 1 - \frac{1}{(8)^{1.4-1}} = 0.5647$

$$\eta_{Otto} = \frac{\text{Output power}}{\text{Heat Input}}$$

$$\text{Heat input} = \frac{100}{0.5647} = 177.077 \text{ kW}$$



26. (a)

For process 1-2:

$$\frac{T_2}{T_1} = \left( \frac{v_1}{v_2} \right)^{\gamma-1} = (r)^{\gamma-1} = 9^{0.4} = 2.408$$

$$T_2 = (90 + 273) \times 2.408 = 874.18 \text{ K}$$

$$\frac{P_2}{P_1} = \left( \frac{v_1}{v_2} \right)^{\gamma}$$

$$P_2 = 1 \times 9^{1.4} = 21.674 \text{ bar}$$

$$\frac{P_3}{P_2} = \frac{T_3}{T_2} \Rightarrow \frac{68}{21.674} = \frac{T_3}{874.18}$$

$$T_3 = 2742.65 \text{ K}$$

Heat added at constant volume ( $Q_{sv}$ ):

$$c_v(T_3 - T_2) = 0.71 (2742.65 - 874.18)$$

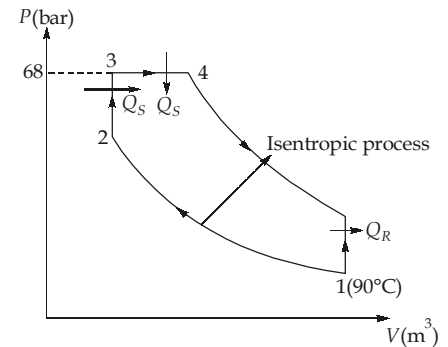
$$Q_{sv} = 1326.615 \text{ kJ/kg}$$

Total heat added = Heat added at constant pressure + Heat added at constant volume.

$$Q_{sp} = Q_s - Q_{sv} = 1750 - 1326.615 = 423.38 \text{ kJ/kg}$$

$$T_4 = T_3 + \frac{423.38}{c_p} = 2742.65 + \frac{423.38}{1.005}$$

$$= 3163.94 \text{ K}$$



27. (a)

Bore of the engine cylinder,  $D = 300 \text{ mm} = 0.3 \text{ m}$ Stroke length,  $L = 450 \text{ mm} = 0.45 \text{ m}$ Engine rpm,  $N = 300 \text{ rpm}$ Indicated mean effective pressure,  $P_{imep} = 6 \text{ bar} = 600 \text{ kPa}$ Net brake load,  $(W - S) = 1.5 \text{ kN}$ Diameter of brake drum,  $D_b = 1.8 \text{ m}$ Brake rope diameter,  $d = 2 \text{ cm} = 0.02 \text{ m}$ 

Indicated power, IP:

$$IP = \frac{P_{imep} L A N K}{120} \text{ kW} \quad \left[ \text{Here, } K = \frac{1}{2} \right]$$

$$IP = \frac{600 \times 0.45 \times \frac{\pi}{4} \times 0.3^2 \times 300}{120} = 47.71 \text{ kW}$$

Brake power, BP:

$$BP = \frac{(W - S)\pi(D_b + d)N}{60} = \frac{1.5 \times \pi(1.8 + 0.02) \times 300}{60} = 42.88 \text{ kW}$$

Mechanical efficiency:

$$\eta_m = \frac{BP}{IP} = \frac{42.88}{47.71} = 0.8987 \text{ or } 89.87\%$$

28. (c)

$$\frac{\text{Mass of air}}{\text{Mass of fuel}} = \frac{\dot{m}_{air}}{\dot{m}_{fuel}} = 30$$

$$T_1 = 27^\circ\text{C} = 27 + 273 = 300 \text{ K}$$

$$\gamma = 16$$

$$CV = 42000 \text{ kJ/kg}$$

From the process 1-2 :

$$T_2 = T_1 r^{\gamma-1} = 300 (16)^{0.4} = 909.4 \text{ K}$$

For constant pressure process 2-3,

$$\text{Heat supplied} = \dot{m}_{air} c_p (T_3 - T_2) = m_{fuel} \times CV$$

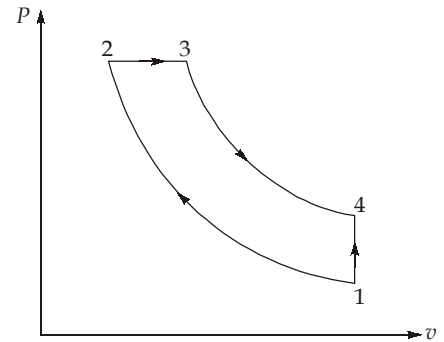
$$T_3 - T_2 = \frac{m_f}{m_a} \times \frac{CV}{c_p} = \frac{1}{30} \times \frac{42000}{1.005} = 1393$$

$$T_3 = 1393 + 909.4 = 2302.4 \text{ K}$$

$$\text{Cut-off ratio, } \rho = \frac{V_3}{V_2} = \frac{T_3}{T_2} = \frac{2302.4}{909.4} = 2.53$$

$$\eta_{th} = 1 - \frac{1}{r^{\gamma-1}} \left[ \frac{\rho^\gamma - 1}{\gamma(\rho - 1)} \right]$$

$$= 1 - \frac{1}{16^{0.4}} \left[ \frac{2.53^{1.4} - 1}{1.4 \times 1.53} \right] = 0.5892 \text{ or } 58.92\%$$



29. (b)

We know that,

$$\eta_m = \frac{\eta_{bth}}{\eta_{ith}} = \frac{\text{Brake thermal efficiency}}{\text{Indicated thermal efficiency}}$$

$$\eta_{bth} = 0.85 \times 0.6 = 0.51$$

and

$$\eta_{bth} = \frac{BP}{\dot{m}_f \times C.V.} \text{ or } \eta_{bth} = \frac{1}{SFC \times C.V.}$$

$$SFC = \frac{1}{\eta_{bth} \times C.V.} = \frac{1}{0.51 \times 40} = 0.049 \approx 0.05$$

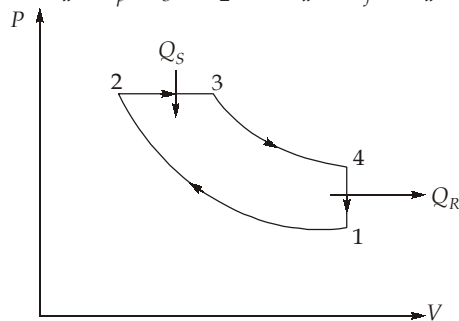
$$= 0.05 \text{ kg/MJ}$$

$$= \frac{0.05 \text{ kg/s}}{10^3 \text{ kJ/s}} = \frac{0.05 \times 3600 \text{ kg/hr}}{10^3 \text{ kW}} = 0.18 \text{ kg/kW-hr}$$

30. (d)

Heat addition at constant pressure,  $Q_s = (m_a + m_f) \times c_p (T_3 - T_2)$ 

$$m_f \times CV = m_a \times c_p (T_3 - T_2) (\because m_a + m_f \approx m_a)$$



$$CV \times \frac{m_f}{m_a} = c_p (T_3 - T_2)$$

$$\frac{CV}{AFR \times c_p} = (T_3 - T_2) \quad [\text{where, AFR is air fuel ratio}]$$

$$T_3 = T_2 + \frac{CV}{AFR \times c_p} = 800 + \frac{40 \times 10^3}{25 \times 1} = 2400 \text{ K}$$

$$\text{Cut-off ratio, } \rho = \frac{T_3}{T_2} = \frac{2400}{800} = 3$$

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