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# **ENGINEERING MECHANICS**

# CIVIL ENGINEERING

Date of Test: 01/05/2022

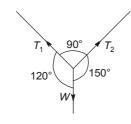
#### **ANSWER KEY** ➤

1.	(b)	7.	(b)	13.	(d)	19.	(c)	25.	(d)
2.	(b)	8.	(a)	14.	(c)	20.	(b)	26.	(d)
3.	(c)	9.	(b)	15.	(c)	21.	(c)	27.	(a)
4.	(b)	10.	(d)	16.	(c)	22.	(a)	28.	(a)
5.	(a)	11.	(d)	17.	(b)	23.	(d)	29.	(b)
6.	(a)	12.	(a)	18.	(c)	24.	(c)	30.	(a)

## **DETAILED EXPLANATIONS**

#### 1. (b)

Applying Lami's Theorem,



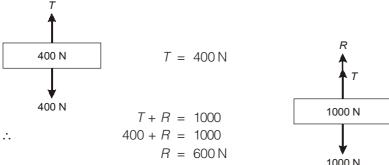
$$\frac{T_1}{\sin 150^{\circ}} = \frac{T_2}{\sin 120^{\circ}} = \frac{W}{\sin 90^{\circ}}$$

$$\therefore \qquad \frac{T_1}{T_2} = \frac{\sin 150^{\circ}}{\sin 120^{\circ}}$$

$$\therefore \frac{T_1}{T_2} = 0.577$$

## 2. (b)

Drawing free diagram of blocks, we have,



This is the reaction from the ground and it is the same force with which the 1000 N block press against the floor.

#### 3. (c)

$$\omega = (12 + 9t - 3t^{2})$$

$$\frac{d\omega}{dt} = 9 - 6t = 0, t = 1.5 \text{ s}$$

$$\omega_{\text{max}} = 12 + 9 \times 1.5 - 3 \times 1.5^{2}$$

$$= 12 + 13.5 - 6.75$$

$$= 18.75 \text{ rad/s}$$

#### 4. (b)

The velocity of point Q is zero, as the point Q is in contact with the surface.

#### 5. (a)

Torque, 
$$T = mg \times \frac{L}{2}$$
 
$$I_0 = \frac{mL^2}{3}$$
 
$$\alpha = \frac{T}{I_0} = \frac{mgL}{2} \times \frac{3}{mL^2} = \frac{1.5g}{L}$$

6. (a)

$$a = \frac{f}{m} = -\frac{bv}{m}$$

but,

$$a = V \frac{dV}{dx}$$

*:*.

$$\frac{vdv}{dx} = -\frac{bv}{m}$$

(at time infinity means steady state)

$$\int_{u}^{0} dv = -\frac{b}{m} \int_{0}^{x} dx$$

$$-u = -\frac{b}{m} \times x$$

x = mu/b

$$\Rightarrow$$

## 7. (b)

Resolving the forces in horizontal and vertical components.

Horizontal components,  $\Sigma F_{\chi} = 60 \cos 30^{\circ} - 80 \cos 45^{\circ} = -4.607$ 

Vertical components,  $\Sigma F_{Y} = 80 \sin 45^{\circ} + 60 \sin 30^{\circ} = 86.568$ 

Resultant, 
$$R = \sqrt{(\Sigma F_X)^2 + (\Sigma F_Y)^2} = \sqrt{(-4.607)^2 + (86.568)^2}$$
  
= 86.69 N

8. (a)

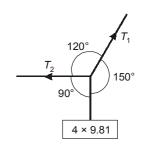
As the body is in equilibrium, using Lami's theorem

$$\therefore \frac{T_1}{\sin 90^\circ} = \frac{4 \times 9.81}{\sin (120^\circ)}$$

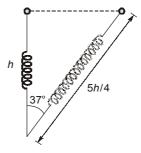
$$T_1 = 45.310 \,\mathrm{N}$$

$$\frac{T_2}{\sin 150^\circ} = \frac{4 \times 9.81}{\sin 120^\circ}$$

$$\Rightarrow$$
  $T_2 = 22.65 \,\mathrm{N}$ 



- 9. (b)
  - :. The kinetic energy of the ring will be given by the potential energy of spring.
  - $\therefore$  Let V be the speed of the ring when the spring becomes vertical



$$\frac{1}{2}mV^2 = \frac{1}{2}k[X]^2$$

$$X = \frac{5h}{4} - h = \frac{h}{4}$$

$$mV^2 = k \left\lceil \frac{h}{4} \right\rceil^2$$

$$V = \frac{h}{4} \sqrt{\frac{k}{m}}$$

Let *u*, *v*, *w* be the components of velocity in *x*, *y* and *z* direction respectively.

$$u = \frac{dx}{dt} = 2\cos t$$

Similarly,

$$v = -3 \sin t$$

$$W = \sqrt{5} \cos t$$

$$V = \sqrt{u^2 + v^2 + w^2}$$

$$= \sqrt{(2\cos t)^2 + (-3\sin t)^2 + (\sqrt{5}\cos t)^2}$$

$$V = \sqrt{4\cos^2 t + 9\sin^2 t + 5\cos^2 t}$$

$$V = \sqrt{9\left(\sin^2 t + \cos^2 t\right)} = 3 \text{ units}$$

#### 11. (d)

$$\omega_0 = 8000 \, \text{rpm} = 837.33 \, \text{rad/s}$$

$$t = 5 min = 300 s$$

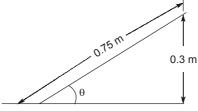
$$\theta = \omega_0 t + \frac{1}{2} \alpha t^2$$

$$\alpha = \frac{\omega - \omega_0}{t} = -\frac{837.33}{300} = -2.791 \text{ rad/s}^2$$

$$\theta = 837.33 \times 300 - 0.5 \times 2.791 \times (300)^2 = 125604 \text{ rad}$$

$$\therefore \text{ Number of revolutions } = \frac{\theta}{2\pi} = 19990.49 \approx 19991$$

#### 12. (a)



Coefficient of friction  $= \mu$ 

$$\mu = tan\theta$$

From figure,

$$\sin\theta = \frac{0.3}{0.75} = 0.4$$



$$\begin{array}{lll} \Rightarrow & \theta = sin^{-1}(0.4) \\ \therefore & \theta = 23.57^{\circ} \\ & \mu = tan\theta \\ & tan\,23.57^{\circ} = 0.436 \end{array}$$
 or

mg 
$$\sin \theta = (f_s)_{max} = \mu N$$
  
 $N = \text{mg } \cos \theta$   
 $\tan \theta = \mu$   
 $\mu = 0.436$ 

For no tipping or prevent overturning

$$Ph < \frac{Wb}{2}$$

where

 $W \rightarrow \text{weight of block}$ 

and

 $b \rightarrow \text{width of block}$ 

$$h < \frac{Wb}{2P} \qquad \dots (1)$$

and for slipping without tipping

P > f(force of friction)

$$P > \mu W$$
 ...(2)

From (1) and (2)

$$h < \frac{b}{2\mu}$$

∴.

$$h < \frac{60}{0.6}$$

$$h < 100 \, \text{mm}$$

Option (d) is correct.

#### 14. (c)

$$I = 2000 \times 0.25^2 = 125 \text{ kg-m}^2$$

for retardation,  $\omega = \omega_0 + \alpha t$ 

$$\omega = 0$$

$$\omega_0 = \frac{2\pi N}{60} = \frac{2\pi \times 3000}{60}$$

 $t = 10 \, \text{min} = 600 \, \text{sec}$ 

$$\alpha = \frac{2\pi \times 3000}{60 \times 600} = 0.5236 \text{ rad/s}$$

So, average frictional torque,

$$I\alpha = 65.44 \, \text{Nm}$$

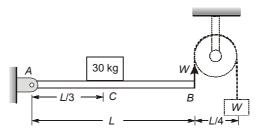
Resistance = 
$$mg + W = 200 \times 9.81 + 100$$
  
=  $2062 N$ 

$$\therefore \qquad a = \frac{2062}{200}$$

$$a = 10.31 \,\text{m/s}^2$$

$$\frac{V^2}{2a} = S = \frac{4^2}{2 \times 10.31} = 0.776 \text{ m}$$

# 16. (c)



W is the tension in the string.

Taking moments from end A

$$W \times L = 30 \times 9.81 \times L/3$$
$$W = 98.1 \,\text{N}$$

#### 17. (b)

*:*.

$$a = -t$$

$$dV = -tdt$$

$$V = -\frac{t^2}{2} + C_1$$

$$7.5 = 0 + C_1$$

$$C_1 = 7.5$$

$$V = -\frac{t^2}{2} + 7.5$$

$$V_{\text{at 3s}} = \frac{-3^2}{2} + 7.5 = 3 \text{ m/s}$$

$$V_{\text{at 3s}} = 3 \text{ m/s}$$

#### 18. (c)

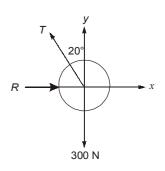
In xy direction

$$-T\sin 20^{\circ} i + T\cos 20j + Ri - 300j = 0$$

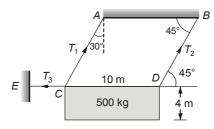
$$(R - T\sin 20^{\circ})i + (0.947 - 300)j = 0$$
then
$$R - T\sin 20^{\circ} = 0$$

$$0.94 T - 300 = 0$$

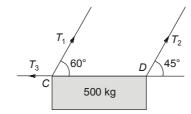
$$(Tension)T = \frac{300}{0.94} = 319.15 N$$



# 19. (c)



Considering free body diagram of the block.



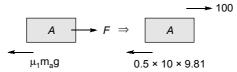
: The body is in equilibrium,

Now, taking moment about C

$$T_2 \sin 45^\circ \times 10 = 500 \times 5$$
  
 $T_2 = 353.55 \text{ kg}$ 

#### 20. (b)

Drawing free-body diagram of A and B.



Writing equation of motion for A.

$$100 - 0.5 \times 10 \times 9.81 = 10a$$

$$a = 5.095 \text{ m/s}^2$$

$$\mu_1 m_a g$$

$$B \Rightarrow B$$

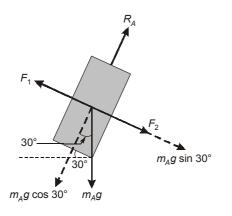
$$\mu_2 (m_a + m_b) g \leftarrow 0.1 \times 18 \times 9.81$$

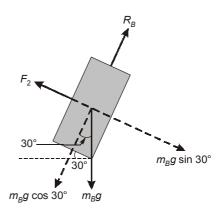
Writing equation of motion for B.

$$49.05 - 17.658 = 8 \ a$$
 
$$\Rightarrow \qquad \qquad a = 3.924 \ \text{m/s}^2$$
 After 0.1s, 
$$V_A = U_a + a_a t.$$
 
$$V_A = 0 + 5.095 \times 0.1$$
 
$$V_A = 0.5095 \ \text{m/s}$$
 Similarly, 
$$V_B = 0 + 3.924 \times 0.1$$
 
$$V_B = 0.3924$$
 
$$\therefore \text{ Relative velocity of } A \text{ wrt } B = V_A - V_B$$
 
$$= 0.5095 - 0.3924 = 0.117 \ \text{m/s}$$

#### 21. (c)

The FBD of the blocks A and B are shown below





Here  $F_1$  and  $F_2$  are the spring forces.

$$F = k\Delta z = k (x_0 - x_{\text{unstretched}})$$
  
 $F_1 = 1000 \times (0.3 - 0.25) = 50 \text{ N}$ 

and

$$F_2 = 1000 \times (0.28 - 0.25) = 30 \text{ N}$$

At equilibrium,

 $\Sigma$ Forces along the plane for mass A = 0

$$\Rightarrow -F_1 + F_2 + m_A g \sin 30^\circ = 0$$

$$\Rightarrow m_A = \frac{F_1 - F_2}{g \sin 30^\circ} = \frac{50 - 30}{9.81 \times 0.5} = 4.08 \text{ kg}$$

and  $\Sigma$ Forces along the plane for mass B = 0

$$\Rightarrow \qquad -F_2 + m_B g \sin 30^\circ = 0$$

$$m_{B} = \frac{F_{2}}{g \sin 30^{\circ}}$$

$$= \frac{30}{9.81 \times 0.5} = 6.12 \text{ kg}$$

# 22. (a)

K.E. = 
$$\frac{1}{2}I\omega^2$$
  

$$I = \frac{mr^2}{2} = \frac{20 \times (0.2)^2}{2} = 0.4 \text{ kgm}^2$$

$$\omega = \frac{2\pi N}{60} = \frac{2 \times 3.14 \times 500}{60} = 52.33 \text{ rad/s}$$
K.E. =  $\frac{1}{2} \times 0.4 \times 52.33^2 = 547.68 \text{ J}$ 

Let speed of car moving in opposite direction is V m/s.

From relative velocity approach

$$\frac{12}{V+50} = \frac{5}{60}$$

$$12 \times 60 = 5v + 250$$

$$V = 94 \, \text{km/hr}$$

# 24. (c)

: Velocities are in opposite directions,

 $\therefore$  I will lie between A and B,

$$\frac{IA}{IB} = \frac{V_a}{V_b} = \frac{5}{3}$$

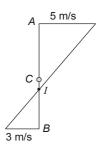
 $\Rightarrow$ 

$$\frac{0.5 - IB}{IB} = \frac{5}{3}$$

$$IB = 0.1875 \,\mathrm{m}$$

$$IA = 0.3125 \,\mathrm{m}$$

$$\omega = \frac{V_A}{IA} = \frac{5}{0.3125} = 16 \text{ rad/s}$$



## Alternatively,

$$\therefore V_A = V_C + R\omega$$

$$V_B = R\omega - V_C$$

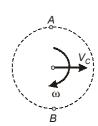
$$\therefore V_C + R\omega = 5$$

$$R\omega - V_C = 3$$

$$V_C + 0.25 \omega = 5$$

$$0.25 \omega - V_C = 3$$
 ...(b)

...(a)



On solving (a) and (b),

$$\omega = 16 \, \text{rad/s}$$

$$V_C = 1 \text{ m/s}$$

where  $V_C$  = velocity of centre C.

#### 25. (d)

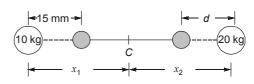
To keep centre of mass at C

$$m_1 x_1 = m_2 x_{2]}$$

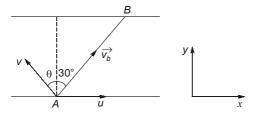
$$\rightarrow \qquad \text{(Let 10 kg} = m_1, 20 \text{ kg} = m_2\text{)}$$
and
$$m_1 (x_1 - 15) = m_2 (x_2 - d)$$

$$15 m_1 = m_2 d$$

$$d = \frac{15 \times 10}{20} = 7.5 \text{ mm}$$



Let v be the speed of boatman in still water



Resultant of u and v should be along AB. Components of  $\vec{v}_b$  (absolute velocity of boatman) along x and y-direction are:

$$v_x = u - v \sin \theta, \ v_y = v \cos \theta$$

$$\tan 30^\circ = \frac{v_y}{v_x}$$

$$0.577 = \frac{v \cos \theta}{u - v \sin \theta}$$

$$0.577 u - 0.577 v \sin \theta = v \cos \theta$$

$$v = \frac{0.577u}{0.577\sin\theta + \cos\theta}$$

$$v = \frac{(0.577 \times \cos 30^{\circ})u}{\sin 30^{\circ} \sin\theta + \cos 30^{\circ} \cos\theta}$$

$$v = \frac{0.49964}{\sin(\theta + 30^{\circ})}$$

$$v$$
 is minimum at  $\theta = 60^{\circ}$ ,  
 $v_{\text{min}} = 0.49964$ 

$$v_{\rm min} \simeq 0.54$$

#### 27. (a)

 $\Rightarrow$ 

Velocity of A is v along AB and velocity of particle B is along BC, its component

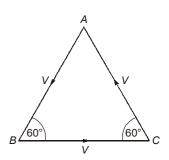
along BA is  $v\cos 60^\circ = \frac{v}{2}$ .

Thus separation AB decreases at the rate of

$$v + \frac{v}{2} = \frac{3v}{2}$$

Since this rate is constant, time taken in reducing separation from AB from d to zero is

$$t = \frac{d}{3v/2} = \frac{2d}{3v}$$



28. (a)

Here, 
$$\alpha = 45^{\circ}$$

We have: 
$$a = \frac{dV}{dt} \Rightarrow a = \frac{dV}{dx} \times \frac{dx}{dt}$$

$$\therefore \qquad \qquad a = \frac{dV}{dx} \times V$$

Also, 
$$a = \frac{mg\sin\alpha - \mu mg\cos\alpha}{m}$$

$$a = g[\sin \alpha - \mu \cos \alpha]$$

$$\therefore g[\sin \alpha - \mu \cos \alpha] = \frac{dV}{dx} \times V$$

$$\therefore g[\sin \alpha \cdot dx - 5x \cos \alpha dx] = V \cdot dV$$

On integrating,

$$g\left[\sin\alpha \cdot x - 5\cos\alpha \times \frac{x^2}{2}\right] = \left[\frac{V^2}{2}\right]_0^0$$
$$g\left[\sin\alpha \cdot x - 5\cos\alpha \times \frac{x^2}{2}\right] = 0$$

$$\Rightarrow \sin\alpha \cdot x = 5\cos\alpha \times \frac{x^2}{2}$$

$$x = \frac{2\tan\alpha}{5} \Rightarrow \frac{2\tan 45^\circ}{5} = 0.4 \,\text{m}$$

29. (b)

We have, Torque = 
$$I\alpha$$

$$\therefore 3F \sin 30^{\circ} \times 0.5 = I\alpha$$

$$3 \times 0.5 \times \frac{1}{2} \times 0.5 = 1.5 \times \frac{0.5^2}{2} \times \alpha$$

$$\therefore \qquad \qquad \alpha = 2 \, \text{rad/s}^{-1}$$

$$\therefore \qquad \qquad \omega \, = \, \omega_0 + \alpha t$$

$$\omega = 0 + 2 \times 1$$

$$\omega = 2 \text{ rad s}^{-1}$$

30. (a)

$$T = 2\pi \sqrt{\frac{L}{g}}$$

$$g = \frac{4\pi^2 L}{T^2}$$

In given problem 
$$T = \frac{36}{20} = 1.8 \text{ s}$$

$$g = \frac{4 \times \pi^2 \times 0.8}{1.8^2} = 9.74 \text{ m/s}^2$$

