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HEAT TRANSFER

MECHANICAL ENGINEERING

Date of Test : 13/09/2026

ANSWER KEY ➤

- | | | | | |
|--------|---------|---------|---------|---------|
| 1. (d) | 7. (b) | 13. (a) | 19. (c) | 25. (c) |
| 2. (d) | 8. (d) | 14. (b) | 20. (b) | 26. (d) |
| 3. (a) | 9. (c) | 15. (a) | 21. (c) | 27. (c) |
| 4. (d) | 10. (d) | 16. (a) | 22. (d) | 28. (c) |
| 5. (d) | 11. (b) | 17. (a) | 23. (a) | 29. (d) |
| 6. (a) | 12. (c) | 18. (a) | 24. (a) | 30. (c) |

DETAILED EXPLANATIONS

1. (d)

$$\eta = \frac{Q_{\text{actual}}}{Q_{\text{ideal}}} = \frac{\sqrt{hPkA}(T_b - T_{\infty})}{hA_{\text{fin}}(T_b - T_{\infty})} = \frac{\sqrt{hPkA}}{hPL} = \frac{1}{L} \sqrt{\frac{kA}{hP}}$$

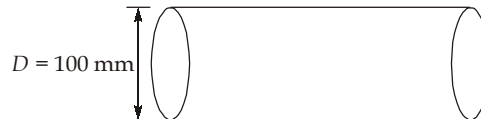
For circular fin

$$A = \frac{\pi}{4} d^2$$

$$P = \pi d$$

$$\eta = \frac{1}{L} \sqrt{\frac{kd}{4h}} = \frac{1}{2L} \sqrt{\frac{kd}{h}}$$

2. (d)



Diameter of steel pipe, $D = 100 \text{ mm}$

Nusselt number, $Nu = 20$

Thermal conductivity, $k = 0.06 \text{ W/mK}$

For horizontal pipe, $Nu = \frac{hD}{k}$

$$\Rightarrow 20 = \frac{h \times 0.1}{0.06}$$

Heat transfer coefficient, $h = 12 \text{ W/m}^2\text{K}$

3. (a)

$$v < \alpha$$

$$Pr = \frac{v}{\alpha}, \text{ so } Pr < 1$$

For $Pr < 1$, $\frac{\delta_t}{\delta_v} > 1$

$$\delta_t > \delta_v \text{ or } \delta_v < \delta_t$$

4. (d)

5. (d)

Critical radius of insulation, $r_c = \frac{k}{h_o}$

$$= \frac{0.5}{10} = 0.05 \text{ m} = 50 \text{ mm}$$

Maximum value of heat dissipation rate,

$$q_{\max} = \frac{\Delta T}{\frac{\ln\left(\frac{r_o}{r_i}\right)}{2\pi kL} + \frac{1}{hA_o}} = \frac{100 - 25}{\frac{\ln(50/0.5)}{2\pi \times 0.5 \times 1} + \frac{1}{2\pi \times \frac{50}{1000} \times 1 \times 10}} = 42.036 \text{ W/m}$$

6. (a)

Heat transfer rate through composite structural wall, $q_1 = -k_1 A \frac{\Delta T}{\delta_1} = -0.2 A \frac{\Delta T}{0.09}$

Heat transfer rate through masonry wall,

$$q_2 = -k_2 A \frac{\Delta T}{\delta_2} = -0.7 A \times \frac{\Delta T}{\delta_2}$$

As per given condition,

$$\begin{aligned} q_2 &= 0.6q_1 \\ \Rightarrow -0.7 A \times \frac{\Delta T}{\delta_2} &= 0.6 \times \left(-0.2 A \times \frac{\Delta T}{0.09} \right) \\ \delta_2 &= 0.525 \text{ m} = 525 \text{ mm} \end{aligned}$$

7. (b)

For parallel flow heat exchanger,

$$\varepsilon = \frac{1 - \exp(-NTU(1+C))}{1+C}$$

Put $C = 0$,

$$\begin{aligned} \varepsilon &= \frac{1 - \exp(-NTU)}{1} \\ \varepsilon &= 1 - \exp(-NTU) \end{aligned}$$

For counter flow heat exchanger,

$$\varepsilon = \frac{1 - \exp\{-NTU(1-C)\}}{1 - C \exp\{-NTU(1-C)\}}$$

Put $C = 0$,

$$\begin{aligned} \varepsilon &= \frac{1 - \exp\{-NTU(1-0)\}}{1 - 0 \times \exp\{-NTU(1-0)\}} \\ \varepsilon &= 1 - \exp(-NTU) \end{aligned}$$

So, expression:

$$\varepsilon = 1 - \exp(-NTU)$$

is valid for all the heat exchangers having zero capacity ratio.

8. (d)

The relative magnitude of the dimensionless parameter $\frac{Gr}{Re^2}$ governs the relative importance of natural convection in relation to forced convection where,

$$\frac{Gr}{Re^2} = \frac{g\beta(T_w - T_\infty)L}{U_0^2}$$

which represents the ratio of the buoyancy forces to inertia forces.

9. (c)

Reflectivity, $\rho = 0.4$

For opaque body,

$$\alpha + \rho = 1$$

$$\alpha + 0.4 = 1$$

$$\text{Absorptivity, } \alpha = 0.6 = \frac{G_{abs}}{G} = \frac{G_{abs}}{600}$$

Part of radiation absorbed,

$$G_{abs} = 0.6 \times 600 = 360 \text{ W/m}^2$$

10. (d)

For infinitely long fin,

$$\dot{q} = \sqrt{hPkA} (T_b - T_\infty)$$

For circular fin, $P = \pi D$

$$A = \frac{\pi D^2}{4}$$

So,

$$\dot{q} = \sqrt{h \times \pi D \times k \times \frac{\pi D^2}{4}} (T_b - T_\infty)$$

$$\dot{q} \propto \sqrt{k} D^{3/2}$$

$$\frac{\dot{q}_1}{\dot{q}_2} = \frac{\sqrt{k_1} D_1^{3/2}}{\sqrt{k_2} D_2^{3/2}} = \left(\frac{400}{250} \right)^{1/2} \left(\frac{D}{0.4D} \right)^{3/2} = 5$$

11. (b)

$$\frac{T(t) - T_\infty}{T_i - T_\infty} = e^{-bt}$$

$$\Rightarrow \frac{\frac{T_i + T_\infty}{2} - T_\infty}{T_i - T_\infty} = e^{-bt}$$

$$\Rightarrow \frac{1}{2} = e^{-bt}$$

Where $b = \frac{1}{\tau}$

$$\begin{aligned} \text{Time required, } t &= \frac{\ln 2}{b} \\ &= \tau \ln 2 = 10 \times 0.693 = 6.93 \text{ s} \end{aligned}$$

12. (c)

Mass flow rate of air, $\dot{m}_h = 1 \text{ kg/s}$

Specific heat at constant pressure of air, $c_{ph} = 1.005 \text{ kJ/kgK}$

$$\dot{m}_h c_{ph} = 1 \times 1.005 = 1.005 \text{ kW/K}$$

Mass flow-rate of water, $\dot{m}_c = 2 \text{ kg/s}$

$$c_{pc} = 4.18 \text{ kJ/kgK}$$

$$\dot{m}_c c_{pc} = 2 \times 4.18 = 8.36 \text{ kW/K}$$

Since, $\dot{m}_h c_{ph} < \dot{m}_c c_{pc}$

$$C_{\min} = \dot{m}_h c_{ph} = 1.005 \text{ kW/K}$$

Maximum heat transfer rate,

$$\begin{aligned} q_{\max} &= C_{\min}(T_{hi} - T_{ci}) \\ &= 1.005 \times (80 - 15) = 65.325 \text{ kW} \end{aligned}$$

13. (a)

Given : $c_p = 4.18 \text{ kJ/kgK}$; $D = 5 \text{ cm} = 0.05 \text{ m}$; $L = 20 \text{ m}$; $\dot{m} = 0.1 \text{ kg/s}$; $T_{bi} = 20^\circ\text{C}$; $T_{be} = 80^\circ\text{C}$;

$h = 1500 \text{ W/m}^2\text{K}$

For constant wall heat flux (q),

$$q = \dot{m} c_p (T_{be} - T_{bi}) = h A_s (T_{we} - T_{be})$$

$$\Rightarrow 0.1 \times (4.18 \times 10^3) \times (80 - 20) = 1500 \times (\pi \times 0.05 \times 20) (T_{we} - 80)$$

$$\begin{aligned} \Rightarrow T_{we} &= 80 + \frac{(0.1) \times (4.18 \times 10^3) (80 - 20)}{1500 \times (\pi \times 0.05 \times 20)} \\ &= 80 + 5.322 \\ &= 85.322^\circ \simeq 85.3^\circ\text{C} \end{aligned}$$

14. (b)

Without shield

Radiation heat transfer rate,

$$q = \frac{\sigma(T_1^4 - T_2^4)}{\frac{1}{\epsilon_1} + \frac{1}{\epsilon_2} - 1}$$

Let number of shields be N .

With shield

Radiation heat transfer rate,

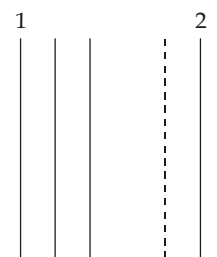
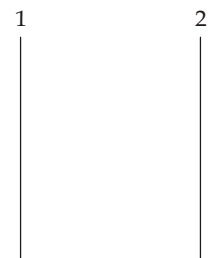
$$q' = \frac{\sigma(T_1^4 - T_2^4)}{\left(\frac{1}{\epsilon_1} + \frac{1}{\epsilon_2} - 1\right) + N\left(\frac{2}{\epsilon} - 1\right)}$$

As per the conditions,

$$q' = (1 - 0.9)q$$

$$\frac{q}{q'} = \frac{1}{0.1} = 10$$

$$\frac{\left(\frac{1}{\epsilon_1} + \frac{1}{\epsilon_2} - 1\right) + N\left(\frac{2}{\epsilon} - 1\right)}{\left(\frac{1}{\epsilon_1} + \frac{1}{\epsilon_2} - 1\right)} = 10$$

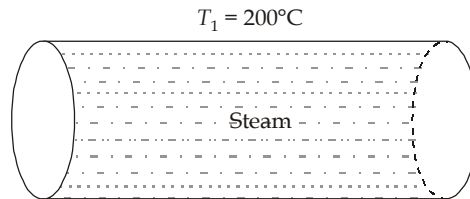


Shields

$$\frac{\left(\frac{1}{0.8} + \frac{1}{0.6} - 1\right) + N\left(\frac{2}{0.29} - 1\right)}{\left(\frac{1}{0.8} + \frac{1}{0.6} - 1\right)} = 10$$

$$\begin{aligned}\text{Number of shields, } N &= 2.925 \\ N &\simeq 3\end{aligned}$$

15. (a)



Heat transfer rate due to radiation,

$$\begin{aligned}q &= \epsilon \sigma (T_1^4 - T_2^4) \\ &= 0.8 \times 5.67 \times 10^{-8} \times [(200 + 273)^4 - (25 + 273)^4] = 1912.7638 \text{ W/m}^2 \\ &= h_r (T_1 - T_2)\end{aligned}$$

where,

h_r = Radiation heat transfer coefficient

$$\Rightarrow 1912.7638 = h_r \times (200 - 25)$$

$$h_r = 10.93 \text{ W/m}^2\text{K}$$

Convection heat transfer coefficient

$$h_c = 6 \text{ W/m}^2\text{-K}$$

So, combined heat transfer coefficient

$$= h_r + h_c = 10.93 + 6 = 16.93 \text{ W/m}^2\text{-K}$$

16. (a)

$$\begin{aligned}\text{Reynold's number, Re} &= \frac{\rho \times U_\infty \times D}{\mu} = \frac{1.5 \times 10 \times 0.02}{2.6 \times 10^{-5}} \\ &= 11538.46 > 2300\end{aligned}$$

So, the flow through the tube is turbulent flow.

$$\therefore \text{Nu} = \frac{\bar{h} \cdot D}{k}$$

$$\Rightarrow 35.44 = \frac{\bar{h} \times 0.02}{0.04}$$

$$\Rightarrow \bar{h} = 70.88 \text{ W/m}^2\text{K}$$

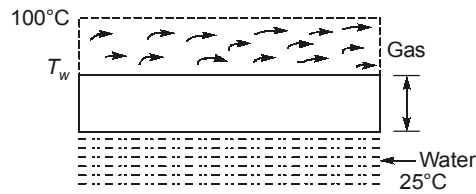
17. (a)

The heat transfer per unit length of tube is given by,

$$\frac{Q}{L} = h \times (\pi D) \times (T_w - T_b)$$

$$\begin{aligned}\Rightarrow \frac{Q}{L} &= 70.88 \times \pi \times 0.02 \times 20 \\ &= 89.07 \text{ W/m}\end{aligned}$$

18. (a)



$$\text{Rate of heat transfer} = \frac{T_g - T_w}{\Sigma R}$$

$$\Sigma R = \frac{1}{h_g} + \frac{L}{k} + \frac{1}{h_w} = \frac{1}{14500} + \frac{4 \times 10^{-3}}{95.5} + \frac{1}{2250}$$

$$\Sigma R = 5.553 \times 10^{-4} \text{ m}^2\text{K/W}$$

$$Q = \frac{100 - 25}{5.553 \times 10^{-4}} = 135063.4 \text{ W/m}^2$$

$$Q = (T_g - T_p)h_g$$

$$135063.4 = [100 - T_p]14500$$

$$T_p = 90.7^\circ\text{C}$$

19. (c)

Minimum heat capacity rate,

$$C_{\min} = \dot{m}_c c_{pc} = 3 \times 4.2 = 12.6 \text{ kW/K}$$

Overall heat transfer coefficient, $U = 1600 \text{ W/m}^2\text{°C}$ Heat transfer area, $A = 12 \text{ m}^2$

$$\text{NTU} = \frac{UA}{C_{\min}} = \frac{1600 \times 12}{12.6 \times 1000} = 1.5238$$

$$\text{Effectiveness, } \varepsilon = 1 - e^{-\text{NTU}} = 1 - e^{-(1.5238)} = 0.782$$

20. (b)

$$\text{For steady state, } \frac{\partial T}{\partial t} = 0$$

$$\therefore 0 = \frac{1}{r} \frac{\partial}{\partial r} \left(r \cdot \frac{\partial T}{\partial r} \right) + q$$

$$\frac{\partial}{\partial r} \left(r \cdot \frac{\partial T}{\partial r} \right) = -q \cdot r$$

On integration,

$$r \cdot \left(\frac{\partial T}{\partial r} \right) = \frac{-qr^2}{2} + A$$

$$\frac{\partial T}{\partial r} = \frac{-qr}{2} + \frac{A}{r}$$

$$T(r) = \frac{-qr^2}{4} + A \ln r + B$$

21. (c)

$\delta_H = 1.2 \text{ mm}$; $\mu = 20 \times 10^{-6} \text{ Pa-s}$; $c_p = 3 \text{ kJ/kgK}$ and $k = 0.05 \text{ W/mK}$

$$\text{Pr} = \frac{\mu c_p}{k} = \frac{20 \times 10^{-6} \times 3 \times 10^3}{0.05} = 1.2$$

$$\frac{\delta_H}{\delta_t} = 1.026 \times \text{Pr}^{1/3}$$

$$\begin{aligned} \Rightarrow \delta_t &= \frac{\delta_H}{1.026 \times \text{Pr}^{1/3}} \\ &= \frac{1.2}{1.026 \times (1.2)^{1/3}} = 1.1 \text{ mm} \end{aligned}$$

Note : It can be easily observed for the expression, the $\text{Pr} > 1$, so $\delta_t < \delta_H$ (1.2 mm).

So, option (c) will be correct.

22. (d)

Given : $A = 30 \text{ m}^2$; $U = 300 \text{ W/m}^2\text{K}$; $(c_p)_o = 3.5 \text{ kJ/kgK}$; $\dot{m}_o = 2 \text{ kg/s}$; $(c_p)_w = 4.18 \text{ kJ/kgK}$;

$\dot{m}_w = 1 \text{ kg/s}$

$$\text{Heat capacity rate; } c_{\text{oil}} = \dot{m}_o \times (c_p)_o = 2 \times (3.5 \times 10^3) = 7 \times 10^3 \text{ W/K}$$

$$c_{\text{water}} = \dot{m}_w \times (c_p)_w = 1 \times (4.18 \times 10^3) = 4.18 \times 10^3 \text{ W/K}$$

$$\begin{aligned} \text{Number of transfer units, NTU} &= \frac{U.A.}{C_{\min}} \\ &= \frac{300 \times 30}{(4.18 \times 10^3)} = 2.15311 \simeq 2.15 \end{aligned}$$

23. (a)

$$\text{Initially, } T_H = 1850 + 273 = 2123 \text{ K}$$

$$Q = 25 \text{ W, } T_L = 500 + 273 = 773 \text{ K}$$

$$25 = \sigma A (T_H^4 - T_L^4)$$

$$25 = \sigma A (2123^4 - 773^4)$$

$$\sigma A = \frac{25}{(2123^4 - 773^4)}$$

$$\text{After some time, } T_H = 1500 + 273 = 1773 \text{ K}$$

$$T_L = 750 + 273 = 1023 \text{ K}$$

$$Q = \sigma_1 A (T_H^4 - T_L^4)$$

$$Q = \frac{25(1773^4 - 1023^4)}{(2123^4 - 773^4)} = 11 \text{ Watt}$$

24. (a)

We know that,

$$Gr = \frac{g\beta\Delta TL_c^3}{\nu^2}$$

$$\beta = \frac{1}{T_{avg}} = \frac{1}{161 + 273} = 2.304 \times 10^{-3} \text{ K}^{-1} \quad \left(T_{avg} = \frac{25 + 297}{2} = 161^\circ\text{C} \right)$$

For horizontal plate:

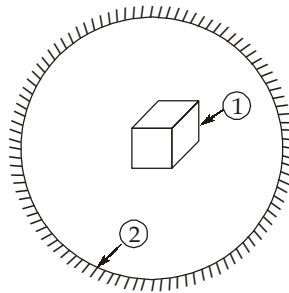
$$L_C = \frac{A_s}{p} = \frac{50 \times 50}{4 \times 50} = 12.5 \text{ cm or } 0.125 \text{ m}$$

So,

$$Gr = \frac{9.81 \times (2.304 \times 10^{-3}) \times 272 \times (0.125)^3}{(30 \times 10^{-6})^2}$$

$$= 133.184 \times 10^5$$

25. (c)

Given : $a = 10 \text{ mm}$; $d = 60 \text{ mm}$

$$A_1 = 6a^2 = 6 \times 10^2 = 600 \text{ mm}^2$$

$$A_2 = 4\pi \left(\frac{d}{2} \right)^2 = 4\pi \left(\frac{60}{2} \right)^2 = 3600\pi \text{ mm}^2$$

$$F_{11} = 0$$

Using summation rule;

$$F_{11} + F_{12} = 1$$

 $\Rightarrow$

$$F_{12} = 1$$

Using reciprocity relation;

$$A_1 F_{12} = A_2 F_{21}$$

 $\Rightarrow$

$$F_{21} = \frac{A_1}{A_2} \times F_{12} = \frac{600}{3600\pi} \times 1 = \frac{1}{6\pi}$$

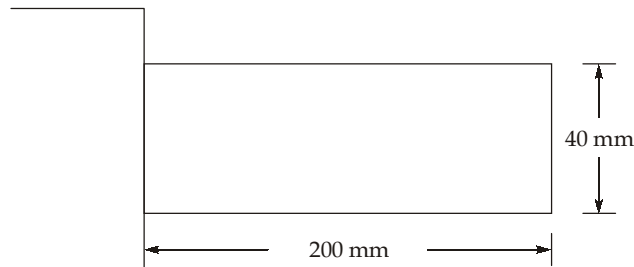
Using summation rule;

$$F_{21} + F_{22} = 1$$

 $\Rightarrow$

$$F_{22} = 1 - F_{21} = 1 - \frac{1}{6\pi}$$

26. (d)



Efficiency of fin, $\eta_{\text{fin}} = 40\%$
Diameter of fin, $d = 40 \text{ mm}$

$$\begin{aligned}\text{Cross-sectional area of fin, } A_b &= \frac{\pi}{4} d^2 \\ &= \frac{\pi}{4} \times 0.04^2 = 1.2566 \times 10^{-3} \text{ m}^2\end{aligned}$$

$$\begin{aligned}\text{Surface area of fin, } A_{\text{fin}} &= \pi d l \\ &= \pi \times 0.04 \times 0.2 = 0.02513 \text{ m}^2\end{aligned}$$

As we know,

$$\begin{aligned}\text{Effectiveness of fin, } \epsilon_{\text{fin}} &= \eta_{\text{fin}} \frac{A_{\text{fin}}}{A_b} \\ &= 0.4 \times \frac{0.02513}{1.2566 \times 10^{-3}} = 7.99\end{aligned}$$

27. (c)

Given : $D = 12 \text{ mm}$; $k_{\text{wire}} = 200 \text{ W/mK}$; $k_{\text{insulation}} = 0.16 \text{ W/mK}$; $h = 20 \text{ W/m}^2\text{K}$; $t = 1 \text{ mm}$

$$R = \frac{D}{2} = \frac{12}{2} = 6 \text{ mm}$$

$$\begin{aligned}\text{Critical radius of insulation, } r_c &= \frac{K_{\text{insulation}}}{h} = \frac{0.16}{20} \\ &= 0.008 \text{ m} = 8 \text{ mm}\end{aligned}$$

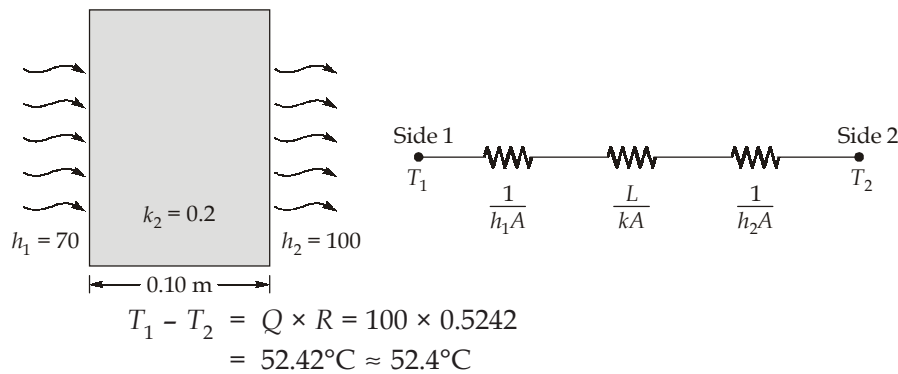
$$\begin{aligned}\text{Radius of insulation, } R_o &= R + t \\ &= 6 + 1 = 7 \text{ mm}\end{aligned}$$

As $R_o < r_c$, so on addition of further insulation of the same material, the heat loss will increase to maximum and then decreases continuously.

28. (c)

$$Q = \frac{\Delta T}{R} = \frac{T_1 - T_2}{R}$$

$$R = \frac{1}{h_1 A} + \frac{1}{kA} + \frac{1}{h_2 A} = \frac{1}{70} + \frac{0.1}{0.2} + \frac{1}{100} = 0.5242^\circ\text{C/W}$$



29. (d)

$$Q_1 = A_1 [F_{12}(J_1 - J_2) + F_{1-3}(J_1 - J_3)]$$

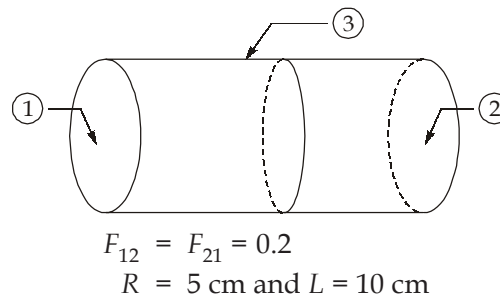
$$J_1 = \sigma 550^4 = 5188.4 \text{ W/m}^2\text{K}$$

$$J_2 = 7500 \text{ W/m}^2$$

$$J_3 = 3200 \text{ W/m}^2$$

$$Q = 9(0.2 \times (5188.4 - 7500) + 0.8 \times (5188.4 - 3200)) = 10.15 \text{ kW}$$

30. (c)



By summation rule:

$$F_{1-1} + F_{1-2} + F_{1-3} = 1 \text{ and} \quad \dots(i)$$

$$F_{3-3} + F_{3-2} + F_{3-1} = 1 \quad \dots(ii)$$

But,

$$F_{3-1} = F_{3-2} \quad \dots(iii)$$

Also,

$$F_{1-1} = F_{2-2} = 0 \quad \dots(iv)$$

From equation (i), we get

$$F_{1-3} = 1 - F_{1-1} - F_{1-2}$$

$$= 1 - 0 - 0.2 = 0.8$$

By reciprocity rule:

$$F_{1-3} \times A_1 = F_{3-1} \times A_3$$

So,

$$F_{3-1} = \frac{A_1}{A_3} \times F_{1-3}$$

$$F_{3-1} = \frac{\pi R^2}{2\pi RL} \times F_{1-3} = \frac{0.8 \times 5}{2 \times 10}$$

$$F_{3-1} = 0.2$$

From equation (ii), we get

$$F_{33} = 1 - F_{3-1} - F_{3-2}$$

$$= 1 - 2 \times F_{3-1} \quad [\text{From equation (iii)}]$$

$$= 1 - 2 \times 0.2 = 0.6$$

