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HYDRAULIC MACHINE

CIVIL ENGINEERING

Date of Test : 07/09/2026

ANSWER KEY ➤

1. (a)	7. (b)	13. (c)	19. (a)	25. (b)
2. (d)	8. (a)	14. (a)	20. (d)	26. (c)
3. (c)	9. (a)	15. (a)	21. (b)	27. (d)
4. (c)	10. (d)	16. (a)	22. (d)	28. (b)
5. (d)	11. (c)	17. (d)	23. (a)	29. (b)
6. (d)	12. (b)	18. (b)	24. (d)	30. (b)

DETAILED EXPLANATIONS

1. (a)

$$(F_r)_m = (F_r)_p$$

$$\left(\frac{V^2}{Lg}\right)_m = \left(\frac{V^2}{Lg}\right)_p$$

$$V_m = V_p \sqrt{\frac{L_m}{L_p}}$$

$$V_m = \frac{1}{\sqrt{36}} = \frac{1}{6} = 0.16 \text{ m/s}$$

2. (d)

Work done by jet on series of plates per second,

$$= F_x \times u$$

$$= \rho A V (V - u) \cdot u$$

[Where F_x = Force in x direction]

Kinetic energy of jet per second,

$$= \frac{1}{2} m V^2 = \frac{1}{2} \rho A V \cdot V^2 = \frac{1}{2} \rho A V^3$$

$$\text{Efficiency of jet} = \frac{\rho A V (V - u) \cdot u}{\frac{1}{2} \rho A V^3} = \frac{2(V - u) \cdot u}{V^2}$$

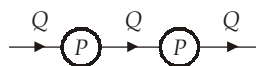
3. (c)

- Specific speed of turbine, $N_s = \frac{N\sqrt{P}}{H^{5/4}}$
- Specific speed of pump, $N_s = \frac{N\sqrt{Q}}{H^{3/4}}$

S.No.	Turbine	Specific speed
1.	Pelton - Single jet	Upto 30
	- Multijet jet	30 - 60
2.	Francis	60 - 300
3.	Propellar	300 - 600
4.	Kaplan	600 - 1000

- Draft tube is required at the exit of reaction turbine.
- Screw pump is used for pumping viscous oil.

4. (c)



Pumps in series

$$Q = Q_1 = Q_2 \dots$$

$$\text{and } H = H_1 + H_2 \dots$$

5. (d)

Depending upon the pump, a critical cavitation number of $\sigma < \sigma_c$ will result in cavitation and cause severe reduction in pump efficiency. Hence for operational purpose it should be seen that $\sigma \geq \sigma_c$

$$\text{i.e. NPSH} \geq \sigma_c H$$

$$\text{Hence minimum NPSH} = \sigma_c \times H$$

6. (d)

N_s or specific speed is related to the rpm (N), net head H and power P as:

$$N_s = \frac{N\sqrt{P}}{H^{5/4}}$$

$$\Rightarrow \sqrt{P} = \frac{N_s \times H^{5/4}}{N}$$

$$\Rightarrow \sqrt{P} = \frac{N_s^2 \times H^{5/2}}{N^2} = \frac{32^2 \times 256^{5/2}}{420^2} = 6087.97 \text{ W} \approx 6 \text{ kW}$$

7. (b)

8. (a)

The specific speed for turbines is given by

$$N_s = \frac{N\sqrt{Q}}{H^{5/4}}$$

The specific speed for pumps is given by

$$N_s = \frac{N\sqrt{Q}}{H^{3/4}}$$

9. (a)

$$P = T \times \omega$$

$$= 13900 \times \left(\frac{2\pi \times 600}{60} \right) = 873.632 \text{ kW}$$

10. (d)

Vapour pressure always play very important role in cavitation.

11. (c)

On splitting of jet into two stream, the larger discharge would be

$$Q_1 = \frac{Q}{2}(1 + \cos \theta)$$

$$\text{and smaller discharge would be, } Q_2 = \frac{Q}{2}(1 - \cos \theta)$$

$$\text{So, } \frac{\text{Smaller discharge}}{\text{Larger discharge}} = \frac{\frac{Q}{2}(1 - \cos \theta)}{\frac{Q}{2}(1 + \cos \theta)} = \frac{1 - \cos \theta}{1 + \cos \theta}$$

$$= \frac{1 - \cos(90 - 30^\circ)}{1 + \cos(90 - 30^\circ)} = \frac{1 - \frac{1}{2}}{1 + \frac{1}{2}} = \frac{1}{3}$$

12. (b)

$$u_1 = \frac{\pi DN}{60} = \frac{\pi \times 1.2 \times 450}{60} = 9\pi \text{ m/s}$$

From inlet velocity triangle,

$$\frac{V_1}{\sin 120^\circ} = \frac{u_1}{\sin 40^\circ}$$

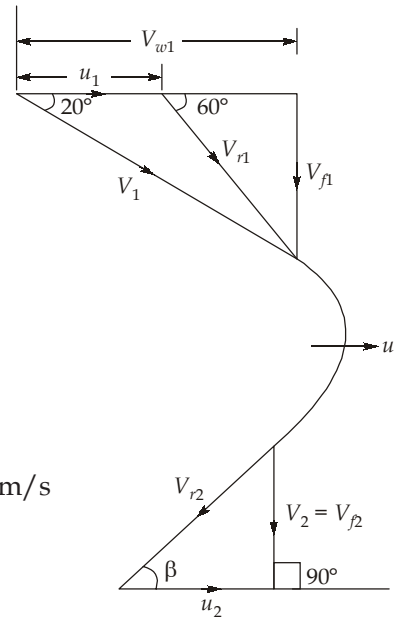
$$V_1 = 9\pi \times \frac{\sin 120^\circ}{\sin 40^\circ} = 38 \text{ m/s}$$

$$V_u = V_1 \cos 20^\circ = 35.7 \text{ m/s;}$$

$$V_{w2} = 0 \text{ (Radial exit)}$$

$$V_{f1} = V_1 \sin 20^\circ = 38 \times \sin 20^\circ = 12.99 \approx 13 \text{ m/s}$$

$$\begin{aligned} \text{So, Power developed} &= \rho Q(u_1 V_{w1} - u_2 V_{w2}) \\ &= 10^3 \times (0.4 \times 13) \times (9\pi) \times 35.7 \\ &= 5250 \text{ kW} \end{aligned}$$



13. (c)

Given,

$$h_{fs} = 0$$

$$h_{fd} = 0.5 \text{ m}$$

$$H_1 = 4 \text{ m}$$

$$H_2 = 15.5 \text{ m}$$

$$Q_1 = 5 \text{ lps} = 0.005 \text{ m}^3/\text{s}$$

$$Q_2 = 75 \text{ lps} = 0.075 \text{ m}^3/\text{s}$$

Efficiency of ram,

$$\eta = \frac{Q_1(H_2 + h_{fd})}{(Q_1 + Q_2)(H_1 - h_{fs})} \times 100$$

$$= \frac{0.005 \times (15.5 + 0.5)}{0.08 \times (4 - 0)} \times 100$$

$$= \frac{5 \times 10^{-3} \times 16}{8 \times 10^{-2} \times 4} \times 100$$

$$\eta = 25\%$$

14. (a)

Given: $Q = 0.05 \text{ m}^3/\text{s}$, $H = 30 \text{ m}$, $d = 15 \text{ cm} = 0.15 \text{ m}$, $l = 150 \text{ m}$, $f' = 0.014$, $\eta_o = 0.75$.

$$\therefore Q = A \times V$$

$$\Rightarrow V = 2.83 \text{ m/s}$$

Manometric head,

$$\begin{aligned} H_m &= H + \frac{4fLV^2}{2gD} + \frac{V^2}{2g} \\ &= 30 + \frac{4 \times 0.014 \times 150 \times (2.83)^2}{2 \times 9.81 \times 0.15} + \frac{(2.83)^2}{2 \times 9.81} \\ &= 53.267 \text{ m} \end{aligned}$$

$$\therefore \eta_o = \frac{\text{Water power}}{\text{Shaft power}}$$

$$\text{or, } 0.75 = \frac{\rho g Q H_m}{SP}$$

$$SP = \frac{1000 \times 9.81 \times 0.05 \times 53.267}{0.75} = 34.84 \text{ kW}$$

15. (a)

$$\text{Power} = T_1 \omega_1$$

$$75000 = T_1 \times \frac{2\pi \times 210}{60}$$

$$T_1 = 3410.463 \text{ Nm}$$

As we know,

$$\text{Unit torque, } T_u = \frac{T}{H}$$

$$\Rightarrow \frac{T_2}{T_1} = \frac{H_2}{H_1}$$

$$\frac{T_2}{3410.463} = \frac{10}{5}$$

$$T_2 = 6820.926 \text{ Nm}$$

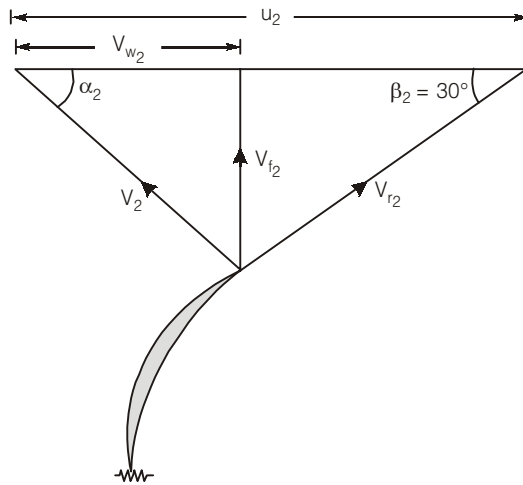
16. (a)

At the outlet

$$u_2 = \frac{\pi D_2 N}{60} = \frac{\pi \times 0.30 \times 1200}{60} = 18.85 \text{ m/s}$$

$$V_{f2} = 2.0 \text{ m/s and } \beta_2 = 30^\circ$$

From the outlet velocity triangle,



$$\tan \beta_2 = \frac{V_{f2}}{u_2 - V_{w2}}$$

$$\tan 30^\circ = \frac{2.0}{18.85 - V_{w2}}$$

$$18.85 - V_{w2} = 3.464; \text{ and hence } V_{w2} = 15.386 \text{ m/s}$$

Manometric efficiency

$$\eta_m = \frac{gH}{u_2 V_{w2}}$$

$$\text{Head developed, } H = \eta_m \frac{u_2 V_{w2}}{g} = \frac{0.85 \times 18.85 \times 15.386}{9.81} = 25.13 \text{ m}$$

17. (d)

$$N_s = \frac{N\sqrt{P}}{(H)^{5/4}} = \frac{100\sqrt{6400}}{(10)^{5/4}} = 450$$

$$N_s(450) > 250$$

Turbine is Kaplan.

18. (b)

The force on the jet is upward and to the left. The leftward component is supplied by the compression spring.

$$\begin{aligned} F_x &= \rho Q[(V_x)_2 - (V_x)_1] \\ &= 1000 \times \left(\frac{\pi}{4} \times (0.035)^2 \times 20 \right) \times (20 \cos 45^\circ - 20) \\ &= -112.7185 \text{ N} \end{aligned}$$

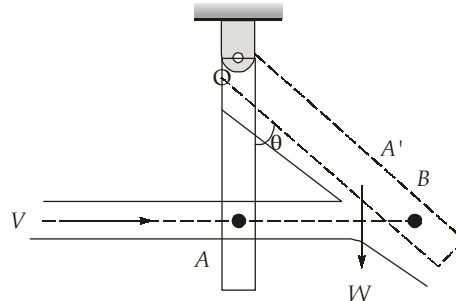
By Hooke's law,

$$\begin{aligned} F_x &= -k\Delta x \\ -112.7185 &= -1.8 \times 1000 (\Delta x) \\ \Delta x &= 62.62 \text{ mm} = 6.262 \text{ cm} \end{aligned}$$

19. (a)

$$\text{Area} = 10 \text{ cm}^2 = 10^{-3} \text{ m}^2$$

$$\text{Velocity of jet} = 50 \text{ m/s}$$



Force on an inclined stationary plate in normal direction to the plate,

$$F_n = \rho a v^2 \cdot \sin \theta$$

$$\text{Here } \theta' = 90 - \theta$$

$$\text{So, } F_n = \rho a v^2 \cos \theta$$

$$\text{Moment of } F_n \text{ about } O = F_n \times OB$$

$$= \rho a v^2 \times \frac{OA}{\cos \theta}$$

$$= \rho a v^2 (OA)$$

$$\text{For equilibrium position, } \Sigma M_O = 0$$

$$W \times \sin \theta \times OA = \rho a v^2 (OA)$$

$$\sin \theta = \frac{\rho a v^2}{W} \quad (\text{Since, } OA = OA')$$

$$\sin \theta = \frac{10^3 \times 10^{-3} \times (50)^2}{5 \times 10^3}$$

$$\sin \theta = \frac{1}{2}$$

$$\theta = 30^\circ$$

20. (d)

$$\text{We know, } \frac{Q_1}{N_1 D_1^3} = \frac{Q_2}{N_2 D_2^3}$$

$$N_2 = \left(\frac{Q_2}{Q_1} \right) \cdot \left(\frac{D_1}{D_2} \right)^3 \cdot N_1$$

Here,

$$D_1 = D_2$$

$$N_1 = 900 \text{ rpm}$$

$$Q_1 = 0.3 \text{ m}^3/\text{s}$$

$$Q_2 = 0.4 \text{ m}^3/\text{s}$$

$$N_2 = \left(\frac{0.4}{0.3} \right) (1)^3 \times 900$$

$$N_2 = 1200 \text{ rpm}$$

For corresponding head, $\frac{H_1}{D_1^2 N_1^2} = \frac{H_2}{D_2^2 N_2^2}$

$$H_2 = \left(\frac{N_2}{N_1}\right)^2 \left(\frac{D_2}{D_1}\right)^2 H_1$$

$$H_2 = \left(\frac{1200}{900}\right)^2 (1)^2 \times 15$$

$$H_2 = 26.67 \text{ m}$$

21. (b)

$$\frac{\text{Power}}{mg} = \frac{(V-u)(1+\cos\beta)u}{g} - \frac{k_1(V-u)^2}{2g}$$

β = blade angle

$\theta = 180 - \beta$ = bucket angle

θ = deflection angle

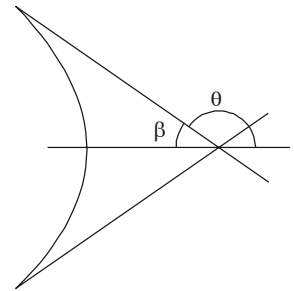
$$\Rightarrow \eta = \frac{(V-u)(1-\cos\theta)u - \frac{k_1(V-u)^2}{2}}{\frac{V^2}{2}}$$

$$\Rightarrow \eta = 2(1-\rho)\rho(1-\cos\theta) - k_1(1-\rho)^2$$

$$\frac{d\eta}{d\rho} = 2(1-\cos\theta)[1-2\rho] + 2k_1(1-\rho)$$

$$0 = (1-\cos\theta) + k_1 - \rho[k_1 + 2(1-\cos\theta)]$$

$$\rho = \frac{k_1 + (1-\cos\theta)}{k_1 + 2(1-\cos\theta)}$$



22. (d)

$$\text{B.P.} = \frac{mgh}{\eta_m} = \frac{80 \times 9.81 \times 30}{0.8} = 29.430 \text{ kW}$$

23. (a)

$$\frac{N_1}{\sqrt{H_1}} = \frac{N_2}{\sqrt{H_2}}$$

$$\therefore N_2 = N_1 \sqrt{\frac{H_2}{H_1}}$$

$$\therefore N_2 = 200 \sqrt{\frac{81}{100}}$$

$$N_2 = 200 \times \frac{9}{10} = 180 \text{ rpm}$$

$$\text{Also } P_2 = \left(\frac{H_2}{H_1}\right)^{3/2} \times P_1 = \left(\frac{81}{100}\right)^{3/2} \times 500 = 364.5 \text{ kW}$$

24. (d)

Characteristics of Pelton wheel

- (i) Impulse turbine
- (ii) High head turbine (300 – 2000 m)
- (iii) Low specific discharge turbine
- (iv) Axial flow turbine
- (v) Low specific speed turbine (4 – 70 rpm)

Characteristics of Francis turbine

- (i) Reaction turbine
- (ii) Medium head turbine (30 – 500 m)
- (iii) Medium specific discharge
- (iv) Radial flow turbine, but modern Francis turbine are mixed flow turbine
- (v) Medium specific speed turbine (60 m-400 rpm)

Characteristics of Kaplan turbine

- (i) Reaction turbine
- (ii) Low head turbine (2 m-70 m)
- (iii) High specific discharge
- (iv) Axial flow
- (v) High specific speed (300 –1100 rpm)

25. (b)

$$0.9 = \frac{72}{H}$$

$$\therefore H = 80 \text{ m}$$

$$\therefore \text{Pipe friction} = 100 - 80 = 20 \text{ m}$$

26. (c)

$$\sigma_c = \text{NPSH}/H$$

$$\therefore 0.144 = \frac{\text{NPSH}}{25}$$

$$\therefore \text{NPSH} = 3.6 \text{ m}$$

$$\text{NPSH} = H_{\text{atm}} - H_v - h_s - h_L$$

$$3.6 = 9.8 - 0.3 - h_s - 0.4$$

$$\therefore h_s = 5.5 \text{ m}$$

27. (d)

As flow rate increases frictional losses in the suction pipe increase, leading to higher NPSH requirement.

28. (b)

$$P = \eta_0 \rho Q g H$$

$$P \propto QH \quad \dots(i)$$

$$Q \propto D^2 \sqrt{H} \quad \dots(ii)$$

$$u \propto \sqrt{H} \alpha DN \quad \dots(iii)$$

Putting (ii) and (iii) in equation (i),

$$P \propto \frac{H^{5/2}}{N^2}$$

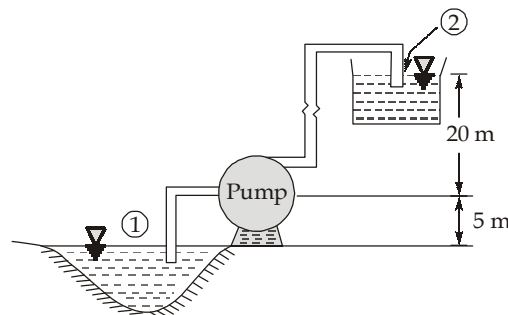
$$\Rightarrow \frac{PN^2}{H^{5/2}} = \text{Constant}$$

$$\left. \frac{PN^2}{H^{5/2}} \right|_P = \left. \frac{PN^2}{H^{5/2}} \right|_M$$

$$\frac{30 \times 100^2}{20^{2.5}} = \frac{40 \times N_m^2}{20^{2.5}}$$

$$N_m = \sqrt{\frac{30}{40}} \times 100 = 86.6 \text{ rpm} \simeq 87 \text{ rpm}$$

29. (b)



Applying energy conservation between (1) and (2)

$$H_p = 5 + 20 = 25 \text{ m}$$

$$\text{Power} = \frac{\rho Q g H_p}{\eta} = \frac{10^3 \times 3 \times 20 \times 10^{-4} \times g \times 25}{0.75} \times 10^{-3} \text{ kW}$$

$$= 2 \text{ kW}$$

30. (b)

$$N_s = \frac{N \sqrt{Q}}{H^{3/4}} = \frac{1500 \sqrt{2.25}}{(16)^{3/4}} = 281.25$$

