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ENGINEERING MECHANICS

CIVIL ENGINEERING

Date of Test : 18/03/2026

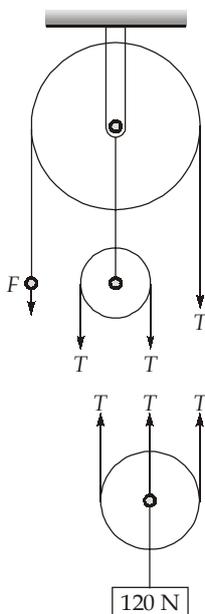
ANSWER KEY >

- | | | | | |
|--------|---------|---------|---------|---------|
| 1. (d) | 7. (b) | 13. (c) | 19. (d) | 25. (c) |
| 2. (b) | 8. (d) | 14. (c) | 20. (b) | 26. (b) |
| 3. (b) | 9. (b) | 15. (a) | 21. (d) | 27. (c) |
| 4. (c) | 10. (b) | 16. (d) | 22. (a) | 28. (b) |
| 5. (d) | 11. (c) | 17. (b) | 23. (d) | 29. (a) |
| 6. (d) | 12. (a) | 18. (b) | 24. (b) | 30. (c) |

DETAILED EXPLANATIONS

1. (d)

The rope is same all over the pulley tension (T) everywhere in the rope will be same.



Hence,
and

$$F = T$$

$$3T = 120$$

$$\Rightarrow F = T = \frac{120}{3} = 40 \text{ N}$$

2. (b)

The area under the force displacement curve will give the net work done by the force on the particle.

$$W_{\text{net}} = 10 \times 2 - \frac{1}{2} \times 10 \times 2 = 20 - 10 = 10 \text{ J}$$

Using work energy theorem,

$$W_{\text{net}} = \text{Change in kinetic energy}$$

$$10 = (KE)_f - KE_i$$

$$10 = \frac{1}{2} Mv^2 - 0$$

$$v = \sqrt{\frac{20}{M}} = \sqrt{\frac{20}{5}} = \sqrt{4} = 2 \text{ m/s}$$

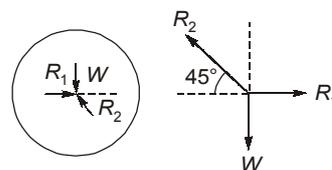
3. (b)

$$R_2 \cos 45^\circ = R_1$$

$$R_2 \sin 45^\circ = W$$

$$\Rightarrow R_2 = W\sqrt{2}$$

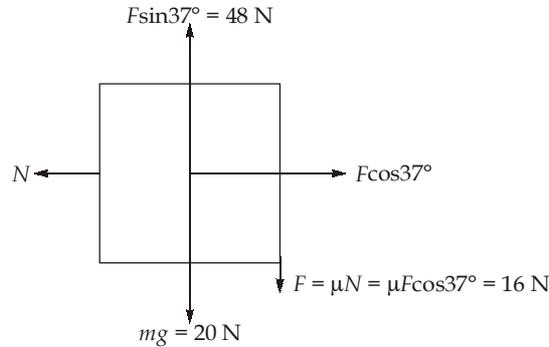
$$\therefore R_1 = W\sqrt{2} \times \frac{1}{\sqrt{2}} = W$$



$$\therefore \begin{aligned} W &= 50 \text{ N} \\ R_1 &= 50 \text{ N} \end{aligned}$$

4. (c)

Free-body diagram of the block is given as:



As the upward force [$F\sin 37^\circ = 48 \text{ N}$] is greater than the total downward force ($20 + 16 = 36 \text{ N}$) hence, it has an upward acceleration,

$$\begin{aligned} F_{\text{net}, y} &= ma \\ [48 - (20 + 16)] &= 2a \\ 48 - 36 &= 2a \\ a &= \frac{12}{2} = 6 \text{ m/s}^2 \end{aligned}$$

5. (d)

For no tipping or prevent overturning

$$Ph < \frac{Wb}{2}$$

where
and

$W \rightarrow$ weight of block
 $b \rightarrow$ width of block

$$h < \frac{Wb}{2P} \quad \dots(1)$$

and for slipping without tipping

$$\begin{aligned} P &> f(\text{force of friction}) \\ P &> \mu W \quad \dots(2) \end{aligned}$$

From (1) and (2)

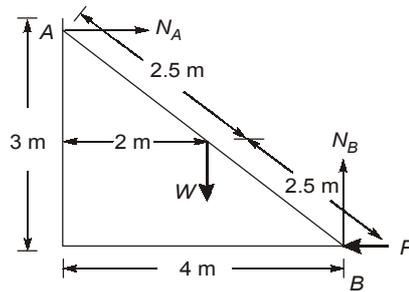
$$h < \frac{b}{2\mu}$$

$$\therefore h < \frac{60}{0.6}$$

$$\therefore h < 100 \text{ mm}$$

Option (d) is correct.

6. (d)



Considering equilibrium of ladder

$$N_A = P$$

$$W = N_B$$

$$\Sigma M_B = 0$$

$$N_A \times 3 - W \times 2 = 0$$

$$W = \frac{N_A \times 3}{2} = \frac{P \times 3}{2} = \frac{400 \times 3}{2} = 600 \text{ N}$$

$$[\because \vec{F}_H = 0]$$

$$[\because \vec{F}_V = 0]$$

8. (d)

For the mass m , $mg - T = ma$ For cylinder, $T \times R = I\alpha$

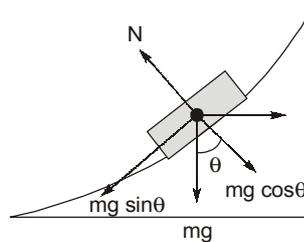
$$T \times R = mR^2 \times \frac{a}{R}$$

$$T = ma$$

$$\Rightarrow mg = 2ma$$

$$\Rightarrow a = \frac{g}{2} \text{ ms}^{-2}$$

9. (b)



$$\tan \theta = \frac{dy}{dx} = \frac{x^2}{2}$$

Now, $mg \sin \theta = \mu mg \cos \theta$

$$\Rightarrow \tan \theta = \mu$$

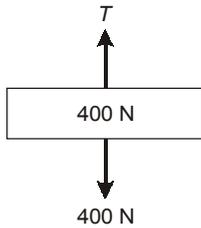
$$\Rightarrow \frac{x^2}{2} = 0.5$$

$$\Rightarrow x = 1$$

$$y = \frac{1}{6} \text{ m}$$

10. (b)

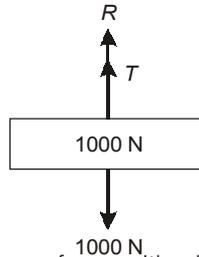
Drawing free diagram of blocks, we have,



$$T = 400 \text{ N}$$

∴

$$\begin{aligned} T + R &= 1000 \\ 400 + R &= 1000 \\ R &= 600 \text{ N} \end{aligned}$$



This is the reaction from the ground and it is the same force with which the 1000 N block press against the floor.

11. (c)

$$a = \frac{dv}{dt}$$

Let resisting force,

$$\Rightarrow F = Kv^2$$

Let m is mass of bullet

∴

$$a = \frac{F}{m} = \frac{Kv^2}{m}$$

$$\frac{dv}{dt} = \frac{Kv^2}{m}$$

$$\frac{1}{v^2} dv = \frac{K}{m} dt$$

$$\left[\frac{v^{-1}}{-1} \right]_u^v = \frac{K}{m} \int_0^t dt$$

$$\Rightarrow \left[\frac{v-u}{uv} \right] = \frac{K}{m} t$$

$$\Rightarrow t = \frac{(u-v)}{uv} \times \frac{-m}{K}$$

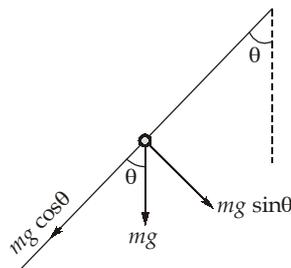
$$\therefore t \propto (u-v)(uv)^{-1}$$

12. (a)

Value of AB is given as,

$$AB = 2R \cos\theta$$

Free-body diagram of the bead is given by



Acceleration of bead along AB is given as

$$a = \frac{F_{net}}{m} = \frac{mg \cos \theta}{m} = g \cos \theta$$

Using 2nd equation of kinematics along AB,

$$S = ut + \frac{1}{2}at^2$$

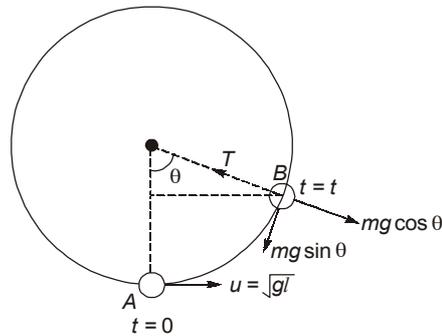
$$AB = \frac{1}{2}at^2$$

$$\therefore 2R \cos \theta = \frac{1}{2} \times g \cos \theta \times t^2$$

$$\therefore 2R = \frac{g}{2}t^2$$

$$t = 2\sqrt{\frac{R}{g}}$$

13. (c)



Let $T = mg$ at angle θ shown in figure

$$h = l(1 - \cos \theta) \quad \dots(1)$$

Apply conservation of mechanical energy between points A and B,

$$\frac{1}{2}m(u^2 - v^2) = mgh$$

$$u^2 = gl \quad \dots(2)$$

v = Speed of particle in position on B

$$v^2 = u^2 - 2gh \quad \dots(3)$$

$$T - mg \cos \theta = \frac{mv^2}{l}$$

$$mg - mg \cos \theta = \frac{mv^2}{l}$$

$$\Rightarrow v^2 = gl(1 - \cos \theta) \quad \dots(4)$$

Substituting the values of v^2 , u^2 and h from equations (4), (2) and (1) in equation (3).

$$gl(1 - \cos \theta) = gl - 2gl(1 - \cos \theta)$$

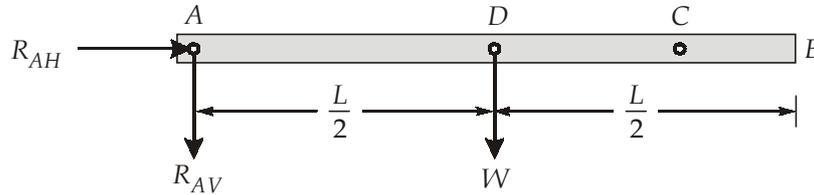
$$\cos \theta = \frac{2}{3}$$

$$\theta = \cos^{-1}\left(\frac{2}{3}\right)$$

Substituting $\cos \theta = \frac{2}{3}$ in equation (4),

$$v = \sqrt{\frac{gl}{3}}$$

14. (c)



Moment of inertia of the rod about point A,

$$I_A = \frac{W}{g} \frac{(L)^2}{12} + \frac{W}{g} \left(\frac{L}{2}\right)^2 = \frac{1}{3} \times \frac{W}{g} \times L^2$$

The net torque about point A,

$$\begin{aligned} \Sigma T_A &= I_A \alpha_A \\ W \times \frac{L}{2} &= \frac{1}{3} \times \frac{W}{g} \times L^2 \alpha_A \end{aligned}$$

$$\Rightarrow \alpha_A = \frac{3g}{2L}$$

Hence, the angular acceleration of the rod at the instant is $\frac{3g}{2L}$

Now, using Newton's second law of motion.

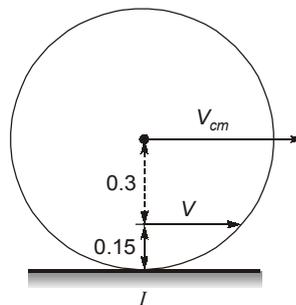
$$\begin{aligned} \Sigma F_{\text{external, vertical}} &= m a_{\text{cm, vertical}} \\ W - R_{AV} &= \left(\frac{W}{g}\right) \times r_{cm} \times \alpha \end{aligned}$$

$$\Rightarrow W - R_{AV} = \left(\frac{W}{g}\right) \times \frac{L}{2} \times \frac{3g}{2L}$$

$$\Rightarrow R_{AV} = W - \frac{3W}{4} = \frac{W}{4}$$

Hence, the vertical reaction at hinge point A at the instant is $\frac{W}{4}$.

15. (a)



$$V_{cm} = 0.45 \omega$$

$$\omega = \frac{3}{0.45} \text{ rad/s}$$

$$V = 0.15 \omega = \frac{0.15 \times 3}{0.45}$$

$$V = 1 \text{ m/s}$$

16. (d)

$$\omega_0 = 8000 \text{ rpm} = 837.33 \text{ rad/s}$$

$$t = 5 \text{ min} = 300 \text{ s}$$

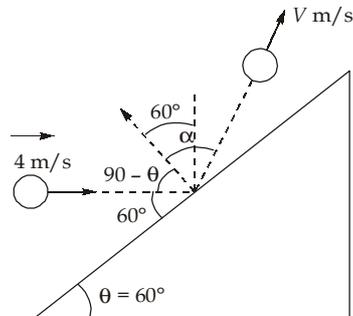
$$\theta = \omega_0 t + \frac{1}{2} \alpha t^2$$

$$\alpha = \frac{\omega - \omega_0}{t} = -\frac{837.33}{300} = -2.791 \text{ rad/s}^2$$

$$\theta = 837.33 \times 300 - 0.5 \times 2.791 \times (300)^2 = 125604 \text{ rad}$$

$$\therefore \text{Number of revolutions} = \frac{\theta}{2\pi} = 19990 \approx 20000$$

17. (b)



Since the impact is occurring normal to the incline, there will be no change in velocity along the incline so,

$$4 \cos(60^\circ) = V \sin \alpha$$

$$V \sin \alpha = 2$$

...(i)

Now,

$$\text{Coefficient of restitution} = \frac{\text{Velocity of separation along the line of impact}}{\text{Velocity of approach along the line of impact}}$$

$$e = \frac{V \cos \alpha}{4 \sin(60^\circ)}$$

$$0.5 = \frac{V \cos \alpha}{4 \sin(60^\circ)}$$

$$V \cos \alpha = 1.732$$

...(ii)

Dividing (i) by (ii)

$$\tan \alpha = \frac{2}{1.732}$$

$$\alpha = 49.1074^\circ$$

$$\text{Angle made with vertical} = 60 - 49.1074 = 10.8926^\circ$$

18. (b)

Apply virtual work method,

$$x = 2l \sin\left(\frac{\theta}{2}\right)$$

$$h = \frac{l}{2} \cos\left(\frac{\theta}{2}\right)$$

$$\Rightarrow dx = 2l \cos\left(\frac{\theta}{2}\right) \frac{d\theta}{2}$$

$$dh = -\frac{l}{2} \sin\left(\frac{\theta}{2}\right) \frac{d\theta}{2}$$

$$\Rightarrow \frac{dx}{\cos\left(\frac{\theta}{2}\right)} = -\frac{dh}{\sin\left(\frac{\theta}{2}\right)} \times 4$$

By principle of virtual work,

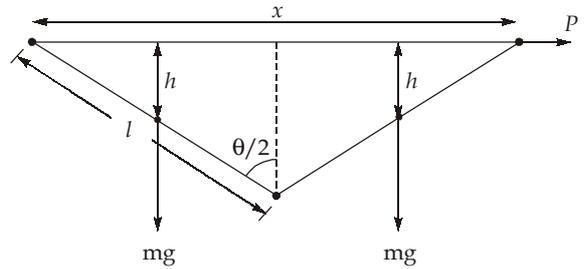
$$\Rightarrow Pdx + 2mgdh = 0 = \text{WD}$$

$$\Rightarrow P \times dx = 2mg \times \tan\left(\frac{\theta}{2}\right) \times \frac{dx}{4}$$

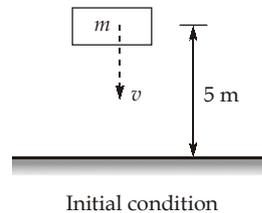
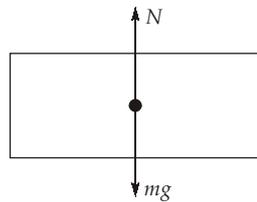
$$\Rightarrow \frac{2P}{mg} = \tan\left(\frac{\theta}{2}\right)$$

$$\Rightarrow \theta = 2 \times \tan^{-1}\left(\frac{2P}{mg}\right)$$

$$\theta = 90^\circ$$



19. (d)



$$\text{Velocity when block reaches the ground} = \sqrt{2gh}$$

$$= \sqrt{2 \times 10 \times 5} = 10 \text{ m/s}$$

By momentum conservation:

$$(F) \times dt = \text{Momentum just after striking the ground} - \text{momentum just before striking the ground}$$

$$(N - mg) \times dt = m \times 0 - (-m \times 10)$$

$$(N - mg) = \frac{m \times 10}{dt}$$

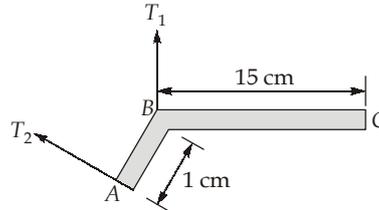
$$N = \frac{10 \times 10}{(1/10)} + 10 \times 10$$

Force of interaction, $N = 1100 \text{ N}$

20. (b)

Given: Coefficient of friction, $\mu_k = 0.20$, Contact angle, $\theta = \frac{240}{180}\pi = 4.189 \text{ rad}$, Torque, $\tau = 200 \text{ N-m}$

Since, the drum is rotating in the clockwise direction. The frictional resistance acting on the drum will be in the clockwise direction. Therefore, tension T_2 will act on the left end of the band and tension T_1 at the right end.



$$\begin{aligned} \text{Torque, } \tau &= (T_2 - T_1)r \\ 200 &= (T_2 - T_1) \times 0.25 \\ T_2 - T_1 &= 800 \text{ N} \quad \dots (i) \end{aligned}$$

Also,

$$\begin{aligned} \frac{T_2}{T_1} &= e^{\mu_k \theta} = e^{0.2 \times 4.189} \\ T_1 &= 0.433 T_2 \quad \dots (ii) \end{aligned}$$

Solving equation (i) and (ii),

$$T_2 = \frac{800}{(1 - 0.433)} = 1410.93 \text{ N}$$

Taking moment about the point B,

$$\Sigma M_B = 0,$$

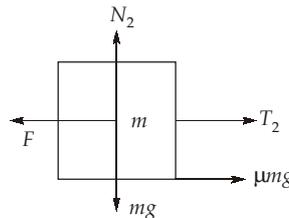
$$-T_2 \times 1 + P \times 15 = 0$$

$$P = \frac{T_2 \times 1}{15} = \frac{1410.93 \times 1}{15} = 94.06 \text{ N}$$

21. (d)

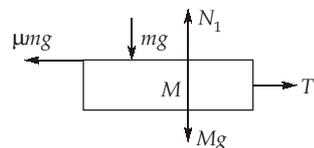
FBD for M:

$$\begin{aligned} \Rightarrow \Sigma F_x &= 0 \\ T_1 &= \mu mg \\ \Sigma F_x &= 0 \\ N_1 &= (M + m)g \end{aligned}$$



FBD for m:

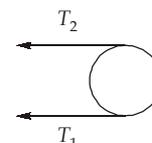
$$\begin{aligned} \Rightarrow \Sigma F_x &= 0 \\ F &= T_2 + \mu mg \end{aligned}$$



Pulley:

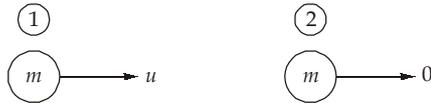
Since T_2 is tension at tight side,

$$\begin{aligned} \Rightarrow T_2 &= T_1 e^{\mu \pi} \\ \Rightarrow F &= e^{\mu \pi} \times \mu mg + \mu mg \\ \Rightarrow F &= \mu mg (1 + e^{\mu \pi}) \end{aligned}$$



22. (a)

Initially



Maximum kinetic energy will be recovered if collision is perfectly elastic ($e = 1$)



Momentum conservation: $mu = mv_1 + mv_2$

$$v_1 + v_2 = u \quad \dots(i)$$

$$e = 1$$

$$\Rightarrow e = \frac{v_2 - v_1}{u}$$

$$v_2 - v_1 = u \quad \dots(ii)$$

From (i) and (ii)

$$v_2 = u, v_1 = 0$$

$$KE_f = \frac{1}{2}mv_1^2 + \frac{1}{2}mv_2^2 = 0.5$$

$$\frac{1}{2} \times 0.1 \times u^2 = 0.5$$

$$u = \sqrt{10} \text{ m/s (Minimum)}$$

Minimum kinetic energy recovered if collision is perfectly inelastic ($e = 0$)

$$mu = mv_1 + mv_2$$

$$v_1 + v_2 = u \quad \dots(iii)$$

$$e = 0$$

$$\Rightarrow 0 = \frac{v_2 - v_1}{u}$$

$$v_2 = v_1 \quad \dots(iv)$$

From (iii) and (iv)

$$v_2 = v_1 = \frac{u}{2}$$

$$KE_f = \frac{1}{2}mv_1^2 + \frac{1}{2}mv_2^2 = 0.5$$

$$\frac{1}{2} \times m \left(\frac{u^2}{4} + \frac{u^2}{4} \right) = 0.5$$

$$\frac{u^2}{2} = 10$$

$$u = \sqrt{20} \text{ m/s (Maximum)}$$

So, $\frac{u_{\max}}{u_{\min}} = \sqrt{2} = 1.414$

23. (d)

Let the velocity of box as it reaches point D is v .
Energy conservation between A and D

$$mg \times 100 = mg \times 60 + \frac{1}{2}mv^2$$

$$v = 28.01 \text{ m/s}$$

As the box reaches the highest point after take off, it will have velocity,

$$v_h = v \cos \theta = 28.01 \times \cos(30)$$

$$v_h = 24.26 \text{ m/s}$$

Energy conservation between A and the highest point

$$mg \times 100 = mg \times h_{\max} + \frac{1}{2}m \times (24.26)^2$$

$$h_{\max} = 70 \text{ m}$$

24. (b)

$$mg(\sin \theta + \mu \cos \theta) = 3mg(\sin \theta - \mu \cos \theta)$$

$$(\sin 45^\circ + \mu \cos 45^\circ) = 3(\sin 45^\circ - \mu \cos 45^\circ)$$

$$\mu = 0.5$$

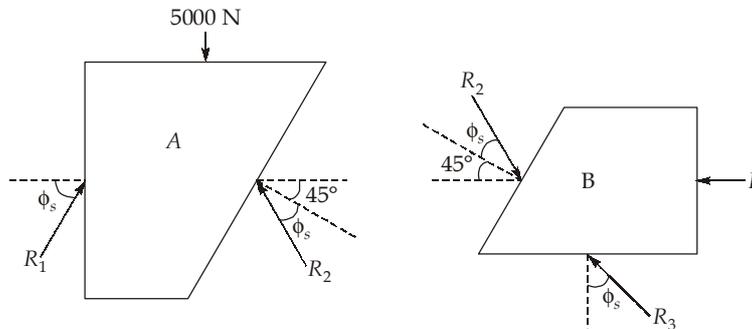
25. (c)

Coefficient of friction, $\mu_s = 0.2$.

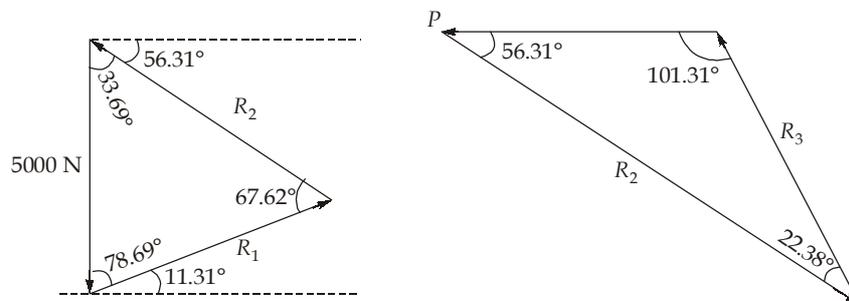
Here the force P is required to maintain the equilibrium. The direction of impending motion of the block A is downwards and that of block B is rightwards.

The free body-diagrams of the block are:

[Angle of friction: $\phi_s = \tan^{-1}\mu$, $\phi_s = \tan^{-1}(0.2)$, $\phi_s = 11.31^\circ$]



Making force triangles for A and B



Applying Lami's theorem for block A

$$\frac{5000}{\sin 67.62^\circ} = \frac{R_1}{\sin 33.69^\circ} = \frac{R_2}{\sin(78.69^\circ)}$$

$$\therefore R_2 = 5000 \times \frac{\sin(78.69^\circ)}{\sin(67.62^\circ)} = 5302.27 \text{ N}$$

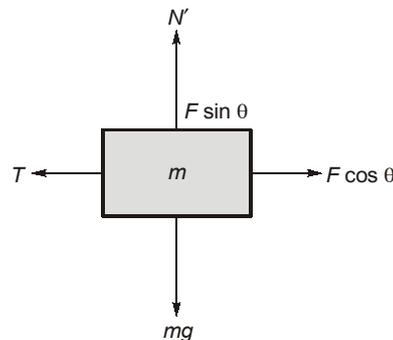
From Lami's theorem for block B

$$\frac{P}{\sin(22.38^\circ)} = \frac{R_3}{\sin(101.31^\circ)} = \frac{R_3}{\sin(56.31^\circ)}$$

$$\therefore P = R_2 \times \frac{\sin(22.38^\circ)}{\sin(101.31^\circ)}$$

$$P = 5302.27 \times \frac{\sin(22.38^\circ)}{\sin(101.31^\circ)} = 2058.81 \text{ N}$$

26. (b)



Considering free body diagram

$$F \cos \theta = T + \mu N'$$

$$T \cos \theta = \mu mg + \mu(mg - F \sin \theta)$$

$$[N' = mg - F \sin \theta]$$

$$\Rightarrow F = \frac{2\mu mg}{\cos \theta + \mu \sin \theta}$$

$$\Rightarrow \text{For } F_{\min} = \frac{2\mu mg}{\sqrt{1 + \mu^2}}$$

\therefore [Max value of $a \cos \theta + b \sin \theta$ is $\sqrt{a^2 + b^2}$]

27. (c)

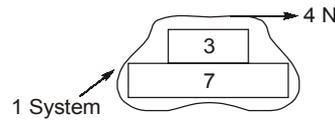
Drawing free body diagram of upper block,

$$10 - \mu_1 mg = m a$$

$$10 - 0.2 \times 2 \times 10 = 2 \times a$$

$$a_1 = 3 \text{ ms}^{-2}$$

for the 3 kg block, as frictional reaction from 2 kg will act in right, the 3 kg and 7 kg block will move simultaneously, since the 7 kg block is in contact with zero friction surface. There will be no tendency of relative motion between 3 kg and 7 kg and both will move as a same system due to the action of frictional force acting on the top of 3 kg by the 2 kg block



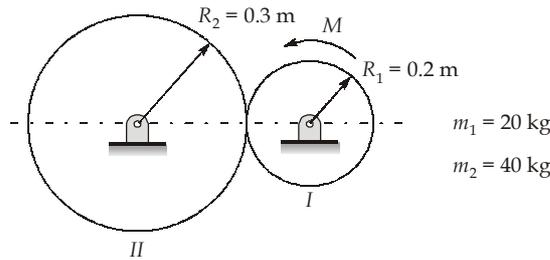
$$4 = 10a$$

$$a = 0.4$$

$$a_2 = 0.4 \text{ ms}^{-2}$$

$$a_3 = 0.4 \text{ ms}^{-2}$$

28. (b)



$$\text{Moment of inertia, } I_1 = \frac{m_1 R_1^2}{2} = \frac{20 \times 0.2^2}{2} = 0.4 \text{ kgm}^2$$

$$I_2 = \frac{m_2 R_2^2}{2} = \frac{40 \times 0.3^2}{2} = 1.8 \text{ kgm}^2$$

A force of friction F acts between disc I and II which drives disc II .

$$F \times R_2 = I_2 \alpha_2 \quad \dots(1)$$

$$R_1 \alpha_1 = R_2 \alpha_2$$

$$\Rightarrow 0.2 \times 8.33 = 0.3 \times \alpha_2$$

$$\alpha_2 = 5.55 \text{ m/s}^2$$

Put α_2 value in (1)

We get $F = 33.32 \text{ N}$

$$M - FR_1 = I_1 \alpha_1$$

$$\Rightarrow M - 33.32 \times 0.2 = 0.4 \times 8.33$$

$$M = 9.996 \approx 10 \text{ Nm}$$

29. (a)

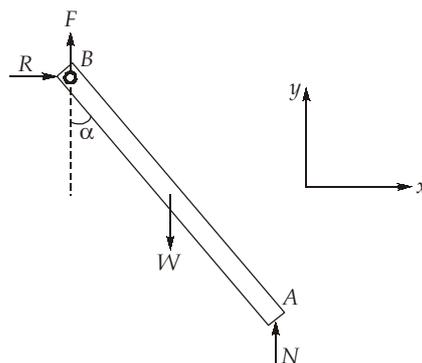
Mass of bar, $m = 4 \text{ kg}$

Length of bar, $L = 6 \text{ m}$

The elongation in the spring,

$$x = L - L \cos \alpha \quad \dots (i)$$

Free-body diagram of the bar is given as:



From equilibrium equations,

$$\Sigma F_x = 0, \quad R = 0$$

$$\Sigma F_y = 0, \quad F + N = W$$

$$\Sigma M_A = 0, \quad W \frac{L}{2} \sin \alpha - RL \cos \alpha - FL \sin \alpha = 0$$

as $R = 0$

$$W \frac{L}{2} \sin \alpha = FL \sin \alpha$$

$$\therefore F = \frac{W}{2} = \frac{4 \times 10}{2} = 20 \text{ N}$$

\therefore Putting this value of F in equation (i),

$$F = k(L)(1 - \cos \alpha)$$

$$k = \frac{F}{L(1 - \cos \alpha)} = \frac{20}{6(1 - \cos 30^\circ)}$$

$$k = 24.88 \text{ N/m}$$

30. (c)

$$W = f \times s \cos \theta$$

$$W = [200 + \mu(mg + N)] \times 10 \times \cos 180^\circ$$

$$W = -[200 + \mu(mg + 100)] \times 10$$

