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POWER SYSTEM-1

ELECTRICAL ENGINEERING

Date of Test : 30/09/2025

ANSWER KEY ➤

1. (a)	7. (a)	13. (c)	19. (b)	25. (b)
2. (b)	8. (d)	14. (c)	20. (b)	26. (b)
3. (d)	9. (a)	15. (a)	21. (a)	27. (b)
4. (c)	10. (b)	16. (d)	22. (d)	28. (b)
5. (d)	11. (a)	17. (b)	23. (b)	29. (c)
6. (b)	12. (a)	18. (b)	24. (c)	30. (a)

DETAILED EXPLANATIONS

1. (a)

$$\text{Average demand} = \frac{\text{Units generated/annum}}{\text{Hours in a year}}$$

$$= \frac{61.5 \times 10^6}{24 \times 365} = 7020.54 \text{ kW}$$

$$\text{Load factor} = \frac{\text{Average demand}}{\text{Maximum demand}} = \frac{7020.54 \text{ kW}}{20 \times 10^3 \text{ kW}}$$

$$\text{Load factor} = 0.35$$

2. (b)

No load receiving end voltage,

$$V_R = \frac{V_s}{A}$$

$$V_R = \frac{400}{0.8} = 500 \text{ kV}$$

$$\text{The sending end current} = I_s = CV_R$$

$$= (0.5 \times 10^{-6}) \left(\frac{500 \text{ kV}}{\sqrt{3}} \right) = 0.1443 \text{ A}$$

3. (d)

$$\text{Resistance per 100 m of distributor} = 2 \times 0.03 = 0.06 \Omega$$

$$\text{Resistance of AB, } R_{AB} = (0.06) \left(\frac{150}{100} \right) = 0.09 \Omega$$

$$R_{BC} = 0.06 \times \frac{50}{100} = 0.03 \Omega$$

$$R_{CA} = 0.06 \times \frac{100}{100} = 0.06 \Omega$$

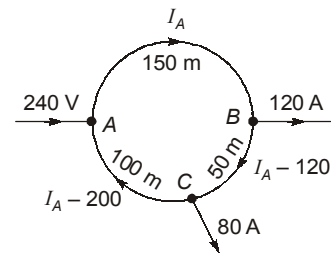
Applying KVL in the loop:

$$I_{AB} R_{AB} + I_{BC} R_{BC} + I_{CA} R_{CA} = 0$$

$$0.09 I_{AB} + 0.03 (I_{AB} - 120) + 0.06 (I_{AB} - 200) = 0$$

$$0.18 I_{AB} = 15.6$$

$$I_{AB} = \frac{15.6}{0.18} = 86.67 \text{ A}$$



4. (c)

$$\text{String efficiency, } \% \eta = \frac{V}{nV_n} \times 100$$

$$\text{Given, } n = 5,$$

$$V_5 = 0.25 \text{ V} = \text{voltage across the bottom most unit.}$$

$$\% \eta = \frac{V}{5 \times 0.25V} \times 100$$

$$\% \eta = 80\%$$

5. (d)

$$P_e = \frac{EV}{X} \sin \theta$$

$$\frac{P_1}{P_2} = \left(\frac{V_1}{V_2} \right)^2$$

$$\frac{20}{P_2} = \left(\frac{11}{33} \right)^2$$

$$\therefore P_2 = 180 \text{ MW}$$

6. (b)

$$\text{Insulation Resistance} = \frac{\rho}{2\pi l} \ln \left(\frac{R}{r} \right)$$

$$\text{Thus, } R_i \propto \frac{1}{l}$$

$$\therefore R_i = \frac{200}{5} = 40 \text{ M}\Omega$$

7. (a)

$$\begin{aligned} \text{Average load} &= \frac{\text{Energy generated in MWh during the day}}{24} \\ &= \frac{(6 \times 40) + (4 \times 50) + (2 \times 60) + (4 \times 50) + (4 \times 82) + (4 \times 40)}{24} \end{aligned}$$

$$\text{Average load} = \frac{1248}{24} = 52 \text{ MW}$$

$$\text{Load factor} = \frac{\text{Average load}}{\text{Maximum demand}} = \frac{52}{82} \times 100 = 63.41\%$$

8. (d)

Zero regulation always at leading power factor load and for zero regulation, we have

$$\phi_R = \theta = \tan^{-1} \left[\frac{X_L}{R} \right]$$

$$\text{Given : } R = X_L$$

$$\text{Therefore, } \phi_R = \tan^{-1} \left[\frac{X_L}{R} \right] = \tan^{-1} 1 = 45^\circ$$

$$\therefore \cos \phi_R = \cos 45^\circ = 0.707 \text{ leading}$$

Hence, the load will have 0.707 leading power factor.

9. (a)

$$C_n = 12 \mu\text{F}$$

$$C_n = \frac{12\mu\text{F}}{400\text{km}} = 0.03 \mu\text{F/km}$$

$$C_n = \frac{2\pi\epsilon}{\ln\frac{D}{r}} = \frac{55.631 \times 10^{-12}}{\ln\frac{D}{r}} \text{F/m} = \frac{55.631 \times 10^{-3}}{\ln\frac{D}{r}} \mu\text{F/km}$$

$$\Rightarrow \frac{55.631 \times 10^{-3}}{\ln\frac{D}{r}} = 0.03$$

$$\ln\frac{D}{r} = 1.854$$

$$\frac{D}{r} = 6.3877$$

$$r = \frac{1}{6.3877} = 15.65 \text{ cm}$$

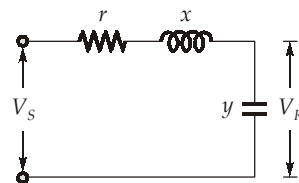
Now, Inductance per phase = $0.2 \ln\frac{D}{r'} \text{mH/km}$

$$= 0.2 \ln\frac{100}{0.7787 \times 15.65} = 0.42 \text{ mH/km}$$

10. (b)

In a SF_6 circuit breaker, the SF_6 gas is used at low velocity and low pressure due to which current chopping is prevented and capacitive currents are interrupted without restriking. Due to these reasons no switching resistor is required in these breakers. Hence, it is most suitable for short line fault without switching resistors.

11. (a)



Let length of line be l km,

$$|V_S| = |A||V_R|$$

When $I_R = 0$ at no load.

$$|A| = \frac{220}{235} = 0.936$$

For receiving end condenser

$$|A| = |1 + YZ|$$

$$Y = j2.8 \times 10^{-6} l$$

$$Z = j0.4l$$

$$|A| = |1 + YZ|$$

$$YZ = j0.4l \times j2.8 \times 10^{-6} l$$

$$YZ = -1.12 \times 10^{-6} l^2$$

$$|A| = |1 + YZ| = |1 - 1.12 \times 10^{-6} l^2|$$

$$0.936 = 1 - 1.12 \times 10^{-6} l^2$$

$$l^2 = \frac{1 - 0.936}{1.12 \times 10^{-6}} = \frac{400000}{7}$$

$$l = 239.04 \text{ km}$$

12. (a)

Since the generators are in parallel, they will operate at the same frequency at steady load.

Let load on generator 1 (200 MW) = x MW

load on generator 2 (400 MW) = $(600 - x)$ MW

and reduction in frequency = Δf

$$\therefore \frac{\Delta f}{x} = \frac{0.04 \times 50}{200} \quad \dots (i)$$

$$\text{and} \quad \frac{\Delta f}{600 - x} = \frac{0.05 \times 50}{400} \quad \dots (ii)$$

Equating Δf in (i) and (ii),

$$x = 230.769 \approx 231 \text{ MW (load on generator-1)}$$

$$600 - x = 369 \text{ MW (load on generator-2)}$$

$$\therefore \text{System frequency} = 50 - \frac{0.04 \times 50}{200} \times 231 = 47.69 \text{ Hz.}$$

13. (c)

$$\text{Given,} \quad |V_s| = |V_R| = 275 \text{ kV,} \quad \alpha = 5^\circ, \beta = 75^\circ$$

Since the power is received at unity power factor, therefore

$$Q_R = 0$$

$$\text{Now,} \quad Q_R = \frac{|V_s| |V_R|}{|B|} \sin(\beta - \delta) - \frac{|A| |V_R|^2}{|B|} \sin(\beta - \alpha)$$

$$\text{or,} \quad 0 = \frac{275 \times 275}{200} \sin(75^\circ - \delta) - \frac{0.85}{200} \times 275^2 \sin(75^\circ - 5^\circ)$$

$$\text{or,} \quad 378 \sin(75^\circ - \delta) = 302$$

$$\text{or,} \quad \sin(75^\circ - \delta) = 0.798$$

$$\text{or,} \quad \delta = 22^\circ$$

$$\begin{aligned} \text{Now,} \quad P_R &= \frac{|V_s| |V_R|}{|B|} \cos(\beta - \delta) - \frac{|A| |V_R|^2}{|B|} \cos(\beta - \alpha) \\ &= \frac{275 \times 275}{200} \cos(75^\circ - 22^\circ) - \frac{0.85 \times 275^2}{200} \cos 70^\circ \end{aligned}$$

$$\text{or,} \quad P_R = 117.63 \text{ MW}$$

14. (c)

$$C = \frac{2\pi \epsilon_0 \epsilon_r}{\ln\left(\frac{R}{r}\right)} \text{ F/m} = \frac{2\pi \times 8.854 \times 10^{-12} \times 2.4}{\ln\left(\frac{15}{10}\right)} \text{ F/m}$$

$$= 0.329 \text{ } \mu\text{F/km}$$

$$\therefore \text{Total cable capacitance} = 0.329 \times 2.5 \quad (\text{Since } l = 2.5 \text{ km})$$

$$= 0.8225 \mu F$$

$$\text{So, dielectric loss, } P_d = V_{ph}^2 \omega C \tan \delta$$

$$= (11000)^2 \times (100 \pi) (0.8225 \times 10^{-6}) (0.031)$$

$$\text{or, } P_d = 969 \text{ W}$$

15. (a)

$$\text{Radius, } r = \frac{1}{2} \times 21 \times 10^{-3} = 10.5 \times 10^{-3} \text{ m}$$

$$D_{eq} = (3 \times 5 \times 3.6)^{1/3} \approx 3.78 \text{ m}$$

$$r' = 0.7788 r = 0.7788 \times 10.5 \times 10^{-3} = 8.177 \times 10^{-3} \text{ m}$$

Inductance per phase,

$$L = 2 \times 10^{-7} \ln \frac{D_{eq}}{r} \text{ H/m}$$

$$= 2 \times 10^{-7} \ln \frac{3.78}{8.177 \times 10^{-3}} = 12.272 \times 10^{-4} \text{ H/km}$$

\therefore Inductive reactance per phase per km is:

$$X_L = 2\pi fL = 2\pi \times 50 \times 12.272 \times 10^{-4} = 0.386 \Omega/\text{km}$$

16. (d)

Number of units = 3

Voltage across the second unit, $V_2 = 15 \text{ kV}$

Voltage across the third unit, $V_3 = 20 \text{ kV}$

$$\frac{V_3}{V_2} = \frac{V_1(1+3K+K^2)}{V_1(1+K)}$$

$$\frac{20}{15} = \frac{1+3K+K^2}{1+K}$$

$$20K + 20 = 15 + 45K + 15K^2$$

$$15K^2 + 25K - 5 = 0$$

$K = 0.18$ by ignoring the negative value.

17. (b)

$$\Delta f = \frac{-\Delta P}{\frac{1}{R_1} + \frac{1}{R_2} + B}$$

On a common base of 1000 MVA

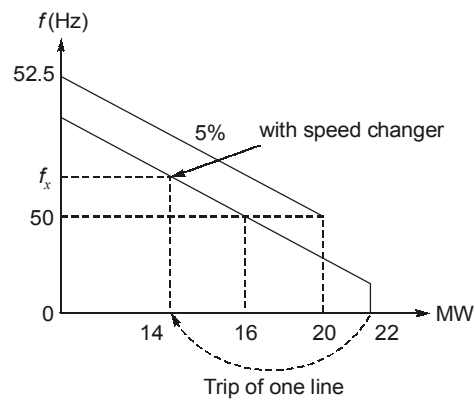
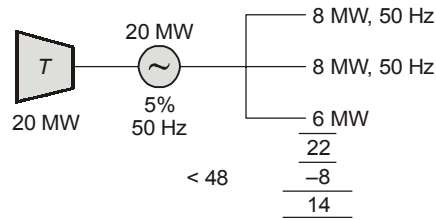
$$R_1 = (0.04) \left(\frac{1000}{400} \right) = 0.1$$

$$R_2 = (0.05) \left(\frac{1000}{800} \right) = 0.0625$$

$$\Delta f = \frac{-130/1000}{\frac{1}{0.1} + \frac{1}{0.0625}} = -5 \times 10^{-3} \text{ p.u.}$$

$$f = f_0 + \Delta f = 50 - (5 \times 10^{-3}) (50) \\ = 49.75 \text{ Hz}$$

18. (b)



From droop characteristic,

$$\frac{\Delta f_1}{\Delta P_1} = \frac{\Delta f_2}{\Delta P_2}$$

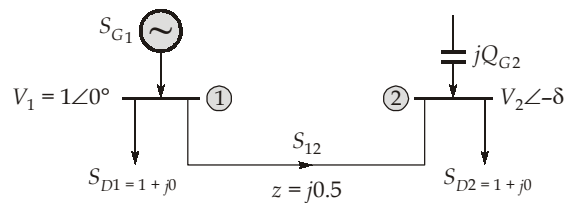
$$\frac{2.5}{20} = \frac{\Delta f_2}{2}$$

 \Rightarrow

$$\Delta f_2 = 0.25$$

$$f_x = 50 + 0.25 = 50.25 \text{ Hz}$$

19. (b)



$$P_S = \frac{V_1 V_2}{X_L} \sin \delta$$

$$1 = \frac{1 \times 1}{0.5} \sin(0 - \delta)$$

$$\delta = -30^\circ$$

$$Q_R = \frac{V_S V_R}{X_L} \cos \delta - \frac{V_R^2}{X_L}$$

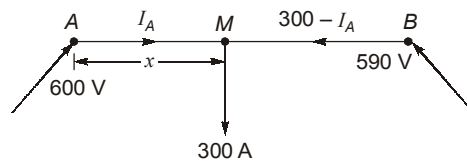
$$= -0.268 \text{ pu}$$

$$Q_C = Q_{G2} = -Q_R = -(-0.268)$$

$$= 0.268 \text{ pu}$$

20. (b)

Let minimum potential occurs at point M at a distance x km from substation A. Let I_A amperes be the current supplied by the substation A. The current supplied by substation B is $300 - I_A$.



Resistance of track per km = 0.04Ω

Resistance of section AM = $0.04 x \Omega$

Resistance of section MB = $0.04 (6 - x) \Omega$

Potential at M, $V_M = V_A - I_A R_{AM}$... (i)

Potential at M, $V_M = V_B - (300 - I_A) R_{MB}$... (ii)

Equating equations (i) and (ii),

$$V_A - I_A R_{AM} = V_B - (300 - I_A) R_{MB}$$

$$600 - 0.04x I_A = 590 - [(300 - I_A) \times 0.04 (6 - x)]$$

$$I_A = 341.67 - 50x$$

Now substituting the value of I_A in equation (i) we get,

$$V_M = V_A - (341.67 - 50x) \times 0.04x$$

$$V_M = 600 - 13.667x + 2x^2$$

For V_M to be minimum, its differential coefficient w.r.t. x must be zero.

$$\frac{d}{dx}(2x^2 - 13.667x + 600) = 0$$

$$4x - 13.667 = 0$$

$$x = \frac{13.667}{4} = 3.417 \text{ km}$$

i.e., minimum potential occurs at a distance 3.417 km from substation A.

21. (a)

System capacitance upto circuit breaker,

$$C = \frac{B}{2\pi f} = \frac{9 \times 10^{-5}}{2\pi \times 50}$$

$$= 2.8647 \times 10^{-7} \text{ F}$$

System inductance upto circuit breaker,

$$L = \frac{X_L}{2\pi f} = \frac{18}{2\pi \times 50} = 0.05729 \text{ H}$$

Natural frequency of oscillation,

$$f_n = \frac{1}{2\pi\sqrt{LC}}$$

$$f_n = \frac{1}{2\pi\sqrt{(2.8647 \times 10^{-7}) \times (0.05729)}}$$

$$f_n = 1.242 \text{ kHz}$$

22. (d)

Inductance per loop meter is

$$L = 4 \times 10^{-7} \ln\left(\frac{d}{r'}\right) \text{ H/m}$$

$$= 4 \times 10^{-4} \ln\left(\frac{d}{r'}\right) \text{ H/km}$$

When distance between the wires is increased as square of original distance, then new inductance per loop km is

$$L' = 4 \times 10^{-4} \ln\left(\frac{d^2}{r'}\right) \text{ H/km}$$

When distance between the wire is doubled new inductance per loop km is

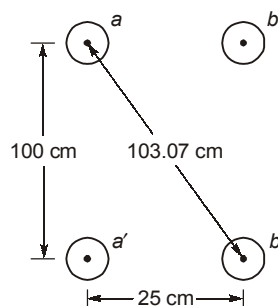
$$L' = 4 \times 10^{-4} \ln\left(\frac{2d}{r'}\right) \text{ H/km}$$

When, distance between the wire is increased four fold, new inductance per loop km is

$$= 4 \times 10^{-4} \ln\left(\frac{4d}{r'}\right) \text{ H/km}$$

So, none of these is correct.

23. (b)



$$\text{GMR of conductor} = 0.7788 \times r$$

$$= 0.7788 \times 0.5 = 0.3894 \text{ cm}$$

Self GMD of aa' combination is,

$$D_s = \sqrt[4]{D_{aa} \cdot D_{aa'} \cdot D_{a'a'} \cdot D_{a'a}}$$

$$= \sqrt[4]{(0.3894)^2 \cdot (100)^2} = 6.2402 \text{ cm}$$

Mutual GMD between a and b ,

$$\begin{aligned} &= D_m = \sqrt[4]{D_{ab} \cdot D_{ab'} \cdot D_{a'b} \cdot D_{a'b'}} \\ &= \sqrt[4]{(25)^2 \times (103.07)^2} = 50.76 \text{ cm} \end{aligned}$$

Inductance per conductor per meter,

$$\begin{aligned} &= 2 \times 10^{-7} \log_e \left(\frac{D_m}{D_s} \right) \\ &= 2 \times 10^{-7} \log_e \left(\frac{50.76}{6.2402} \right) = 0.42 \times 10^{-6} \text{ H} \end{aligned}$$

\therefore loop inductance per km of the line

$$= 2 \times 0.42 \times 10^{-6} \times 1000 = 0.84 \text{ mH}$$

24. (c)

Transmission line parameters,

$$V_s = AV_r + BI_r \quad \dots(i)$$

There is no load current but current flowing through the shunt inductor is I_L .

Now equation (i) becomes,

$$V_s = AV_r + BI_L$$

Dividing the above equation with I_L on both sides.

$$\frac{V_s}{I_L} = A \frac{V_r}{I_L} + B \frac{I_L}{I_L}$$

Since,

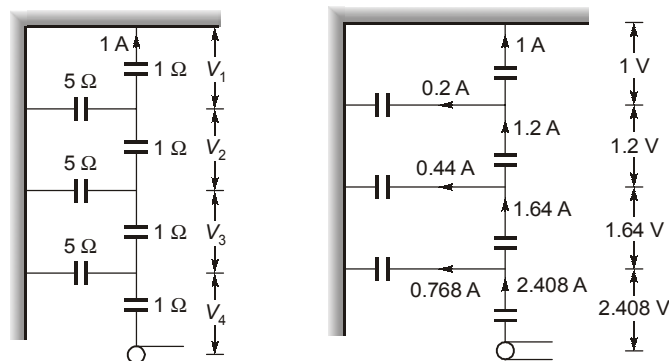
$$\begin{aligned} V_s &= V_R \\ X_L &= AX_L + B \\ X_L(1 - A) &= B \end{aligned}$$

$$X_L = \frac{B}{1 - A} = \frac{160}{1 - 0.95} = 3200 \Omega$$

25. (b)

The ratio of self capacitance (c) to pin-earth capacitance (c_1) is $\frac{c}{c_1} = 5$. Suppose $X_c = 1 \Omega$, then

$X_{c1} = 5 \Omega$. Suppose the voltage V across the string is such that current in the top insulator is 1 A as shown below then the potential across various insulators will be as shown below,



The voltage obtained across the string is

$$V = 1 + 1.2 + 1.64 + 2.408$$

$$V = 6.248 \text{ V}$$

$$\therefore \text{String efficiency} = \frac{6.248}{4 \times 2.408} \times 100$$

$$\eta = 64.86\%$$

26. (b)

Reactive power injected into transmission line by generator = Q_t

$$Q_t = \frac{V_1^2}{X} - \frac{V_1 V_2}{X} \cos \delta$$

$$P_t = \frac{V_1 V_2}{X} \sin \delta$$

$$2 = \frac{1}{0.1} \sin \delta$$

$$\Rightarrow \sin \delta = 0.2$$

$$\Rightarrow \cos \delta = \sqrt{0.96} \approx 0.98$$

$$Q_t = 10 - 10 \times 0.98 = 0.20 \text{ p.u.}$$

Active power delivered by generator is

$$P_s = P_{D1} + P_{D2} = 3 \text{ p.u.}$$

Reactive power delivered by generator is

$$Q_s = Q_{D1} + Q_t = 1.2020 \text{ p.u.}$$

$$\text{So, pf of generator} = \frac{P}{\sqrt{P^2 + Q^2}} = \frac{3}{\sqrt{3^2 + 1.20^2}} = 0.9284 \text{ lag}$$

27. (b)

At no-load,

$$I_R = 0$$

$$A = \frac{|V_S|}{|V_R|} = \frac{|220|}{|242|} = \frac{10}{11}$$

and

$$A \approx 1 + \frac{YZ}{2}$$

$$\frac{10}{11} = 1 + \frac{l^2(yz)}{2} = 1 + \frac{l^2(j0.4 \times j2.8 \times 10^{-6})}{2}$$

$$\frac{10}{11} = 1 - 0.56 \times 10^{-6} l^2$$

$$l \approx \sqrt{\frac{1}{11 \times 0.56 \times 10^{-6}}} = 402.91 \text{ km}$$

28. (b)

Mutual inductance, $L_m = 0.2 \ln \frac{1}{D} \text{ mH/km}$

$D \rightarrow$ Distance between the conductors

$$\begin{aligned} L_m &= 0.2 \ln \frac{1}{4} = -0.4 \ln 2 \\ &= -0.4 \times 0.69 = -0.276 \text{ mH/km} \end{aligned}$$

29. (c)

$$\begin{aligned} \frac{\Delta P_D}{\Delta f} &= -\left(B + \frac{1}{R}\right) \\ &= -\left(2 + \frac{1}{0.025}\right) \quad \begin{cases} R = \text{speed regulation parameters} \\ B = \text{load frequency constant} \end{cases} \\ \text{Slope} = \frac{\Delta P_D}{\Delta f} &= -\left(2 + \frac{1000}{25}\right) = -42 \text{ MW/Hz} \end{aligned}$$

30. (a)

For short term planning problem, losses can be found out by using approximate loss formula given by (for a two bus system)

$$P_{\text{loss}} = B_{11}P_1^2 + 2B_{12}P_1P_2 + B_{22}P_2^2$$

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