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REFRIGERATION & AIR CONDITIONING

MECHANICAL ENGINEERING

Date of Test : 20/09/2025

ANSWER KEY ➤

- | | | | | |
|--------|---------|---------|---------|---------|
| 1. (c) | 7. (a) | 13. (b) | 19. (b) | 25. (d) |
| 2. (b) | 8. (a) | 14. (a) | 20. (c) | 26. (a) |
| 3. (b) | 9. (a) | 15. (b) | 21. (b) | 27. (b) |
| 4. (d) | 10. (c) | 16. (a) | 22. (a) | 28. (a) |
| 5. (c) | 11. (b) | 17. (b) | 23. (b) | 29. (c) |
| 6. (c) | 12. (b) | 18. (c) | 24. (a) | 30. (a) |

DETAILED EXPLANATIONS

1. (c)

$$\begin{aligned}\text{Net heat loss, } Q &= 60000 - 4000 \\ &= 56000 \text{ kJ/h} \\ &= 15.555 \text{ kW}\end{aligned}$$

$$\text{COP} = \frac{Q}{W} = 2.5$$

$$\text{Power required, } W = \frac{Q}{2.5} = \frac{15.555}{2.5} = 6.22 \text{ kW}$$

2. (b)

$$\begin{aligned}\text{COP} &= \frac{\text{Refrigeration Effect}}{W_{\text{compressor}} - W_{\text{turbine}}} = \frac{T_1 - T'_4}{(T'_2 - T_1) - (T_3 - T'_4)} \\ &= \frac{263 - 197}{(467 - 263) - (313 - 197)} = 0.75\end{aligned}$$

5. (c)

The heat rejection ratio is the ratio of heat rejected to the heat absorbed,

$$\text{HRR} = \frac{Q_c}{Q_e} = \frac{Q_e + W_c}{Q_e} = 1 + \frac{1}{\text{COP}}$$

For a fixed condenser temperature, as the evaporator temperature increases, the COP increases and the heat rejection ratio decreases.

Thus, option (c) is correct.

6. (c)

To produce ultra-low temperature the compression ratio will increase thereby decreasing the volumetric efficiency.

7. (a)

$$(\text{COP})_{\text{cascade}} = \frac{(\text{COP})_1 \times (\text{COP})_2}{1 + (\text{COP})_1 + (\text{COP})_2} = \frac{3.4 \times 6.1}{1 + 3.4 + 6.1} = 1.975$$

8. (a)

$$\text{Heat rejection ratio (HRR)} = \frac{Q_{\text{condenser}}}{RE}$$

$$\text{HRR} = \frac{h_2 - h_3}{h_1 - h_4} = \frac{200 - 50}{150 - 50} = \frac{150}{100} = 1.5$$

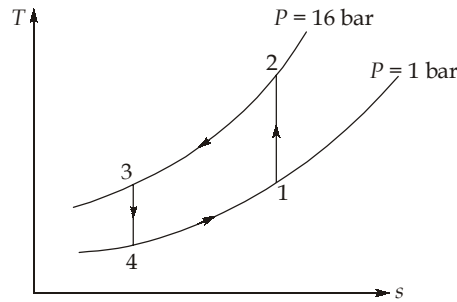
10. (c)

$$\text{CMM} = 10 \times \frac{3}{60} = 0.5 \text{ m}^3/\text{min}$$

$$\Delta T = 20 \text{ K}$$

$$\begin{aligned}\text{SHL} &= 0.0204 \times \text{CMM} \times \Delta t \\ &= 0.0204 \times 0.5 \times 20 = 0.20 \text{ kW}\end{aligned}$$

11. (b)



$$T_1 = -5^\circ\text{C} = 268 \text{ K}$$

$$T_3 = 30^\circ\text{C} = 303 \text{ K}$$

$$\frac{T_2}{T_1} = \frac{T_3}{T_4} = (r_p)^{(\gamma-1)/\gamma} = (16)^{0.4/1.4} = 2.208$$

$$T_2 = 591.74 \text{ K}, T_4 = 137.22 \text{ K}$$

$$\begin{aligned} \text{Refrigeration effect} &= h_1 - h_4 = c_p (T_1 - T_4) \\ &= 1.005(268 - 137.22) \\ &= 131.43 \text{ kJ/kg} \end{aligned}$$

$$\text{Mass flow rate} = \frac{\text{Refrigeration capacity}}{\text{Refrigeration effect}} = \frac{33.5}{131.43} = 0.2548 \text{ kg/s}$$

$$\begin{aligned} \dot{V}_{\text{compressor}} &= \frac{\dot{m}RT_1}{P_1} = \frac{0.2548 \times 0.287 \times 268}{100} \\ &= 0.196 \text{ m}^3/\text{s} = 11.76 \text{ m}^3/\text{min} \end{aligned}$$

12. (b)

$$(\text{COP})_A = (\text{COP})_B$$

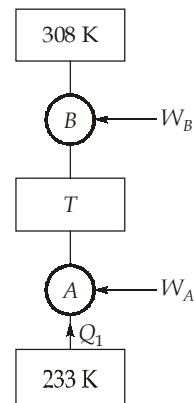
$$\frac{T_L}{T - T_L} = \frac{T}{T_H - T}$$

$$\begin{aligned} T_L T_H - T_L T &= T^2 - T_L T \\ T^2 &= T_L T_H \end{aligned}$$

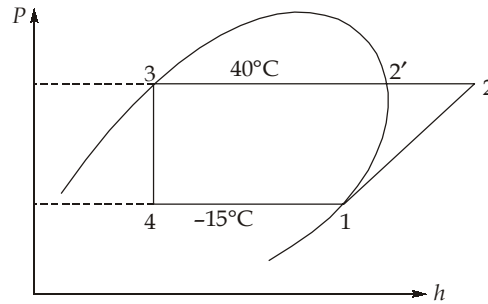
$$T = \sqrt{T_L T_H} = \sqrt{308 \times 233} = 267.88 \text{ K}$$

$$(\text{COP})_A = \frac{233}{267.88 - 233} = 6.68$$

$$\begin{aligned} W_A &= \frac{Q_1}{(\text{COP})_A} = \frac{3}{6.68} \\ &= 0.449 \text{ kJ/s} \simeq 0.45 \text{ kJ/s} \end{aligned}$$



13. (b)



For process 1 - 2,

$$s_1 = s_2$$

$$5.7550 = 5.1558 + 2.1897 \ln\left(\frac{T_2}{40 + 273}\right)$$

$$T_2 = 411.55 \text{ K}$$

$$h_2 = h'_2 + c_{p_v} (T_2 - T'_2)$$

$$h_2 = 1473 + 2.1897 [411.55 - (40 + 273)]$$

$$h_2 = 1688.79 \text{ kJ/kg}$$

$$\text{Theoretical COP} = \frac{\text{Desired effect}}{W_{\text{input}}} = \frac{h_1 - h_4}{h_2 - h_1} = \frac{1433 - 371.5}{1688.79 - 1433}$$

$$\text{COP} = 4.149 \approx 4.15$$

14. (a)

We know, efficiency of Brayton cycle working with pressure ratio r_p is

$$\eta = 1 - \frac{1}{(r_p)^{\frac{\gamma-1}{\gamma}}} \quad \dots (i)$$

and COP of Bell-Coleman cycle working between same pressure ratio of r_p is,

$$\text{COP} = 1 - \frac{1}{(r_p)^{\frac{\gamma-1}{\gamma}} - 1} \quad \dots (ii)$$

From equation (i), we have,

$$\frac{1}{(r_p)^{\frac{\gamma-1}{\gamma}}} = 1 - \eta$$

$$\Rightarrow (r_p)^{\frac{\gamma-1}{\gamma}} = \frac{1}{1 - \eta}$$

Put value in equation (ii), we get

$$\begin{aligned} \text{COP} &= \frac{1}{\left(\frac{1}{1 - \eta}\right) - 1} = \frac{1}{\left(\frac{1 - 1 + \eta}{1 - \eta}\right)} \\ &= \frac{1 - \eta}{\eta} = \frac{1}{\eta} - 1 \end{aligned}$$

$$\Rightarrow \frac{1}{\eta} = 1 + \text{COP}$$

$$\Rightarrow \eta = \frac{1}{1 + \text{COP}}$$

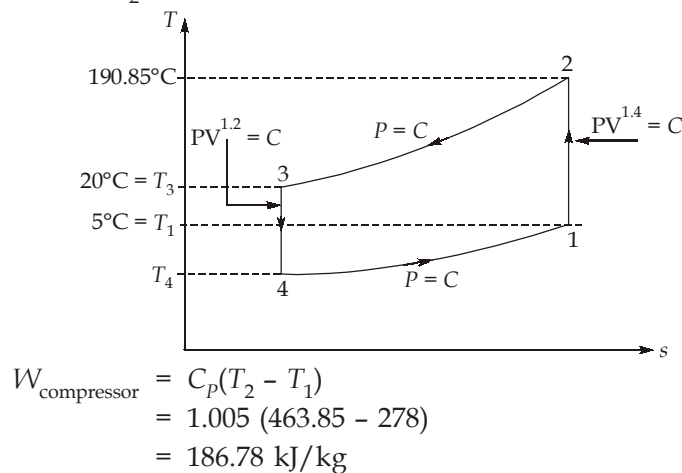
15. (b)

Given: $P_1 = 1$ bar, $C_{p \text{ air}} = 1.005$ kJ/kgK, $P_2 = 6$ bar, $\gamma_{\text{air}} = 1.4$, $P_4 = 1$ bar, $T_1 = 5^\circ\text{C} = 278$ K, $T_3 = 20^\circ\text{C} = 293$ K

For process 1-2 (Isentropic compression)

$$\frac{T_2}{T_1} = \left(\frac{P_2}{P_1} \right)^{\frac{\gamma-1}{\gamma}} = \left(\frac{6}{1} \right)^{\frac{1.4-1}{1.4}}$$

$$T_2 = 463.85 \text{ K}$$



For process 3-4 (Polytropic expansion)

$$\therefore \frac{T_3}{T_4} = \left(\frac{P_3}{P_4} \right)^{\frac{n-1}{n}} = \left(\frac{P_2}{P_1} \right)^{\frac{n-1}{n}} \quad [\because P_3 = P_2 \text{ and } P_4 = P_1]$$

$$\frac{T_3}{T_4} = (6)^{\frac{1.2-1}{1.2}} = 1.348$$

$$T_4 = 217.35 \text{ K}$$

and

$$W_{\text{expander}} = \left(\frac{n}{n-1} \right) mR(T_3 - T_4)$$

$$= \left(\frac{1.2}{1.2-1} \right) (1)(0.287)(293 - 217.35) \quad [\because m = 1 \text{ kg assumed}]$$

$$= 130.27 \text{ kJ/kg}$$

$$\text{Refrigerating effect} = C_p(T_1 - T_4)$$

$$= 1.005 (278 - 217.35)$$

$$= 60.95 \text{ kJ/kg}$$

$$\therefore \text{COP} = \frac{RE}{W_{\text{input}}} = \frac{60.95}{W_C - W_T}$$

$$= \frac{60.95}{186.78 - 130.27} = 1.078$$

16. (a)

Heat delivered by heat pump is the heating effect (Q_1) and heat absorbed by refrigerator is the cooling effect (Q_2).

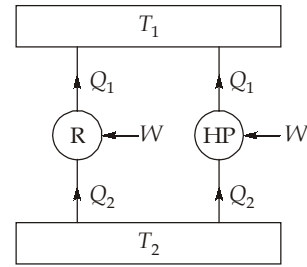
Given: $(COP)_R = 4$; $W = 1 \text{ kW}$

$$(COP)_{HP} = (COP)_R + 1$$

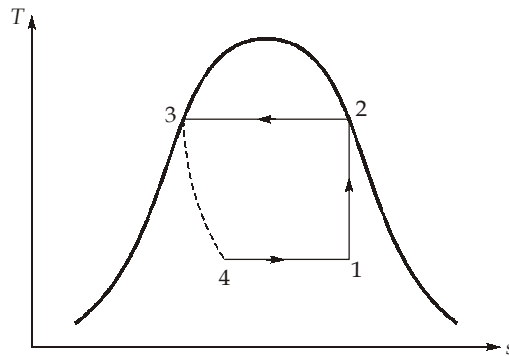
$$(COP)_{HP} = 4 + 1 = 5$$

$$\Rightarrow \frac{Q_1}{W} = 5$$

$$\Rightarrow Q_1 = 5 \text{ kW}$$



17. (b)



As per given data,

$$h_2 = h_{f3} + h_{fg} = 81.25 + 121.6 = 202.85 \text{ kJ/kg}$$

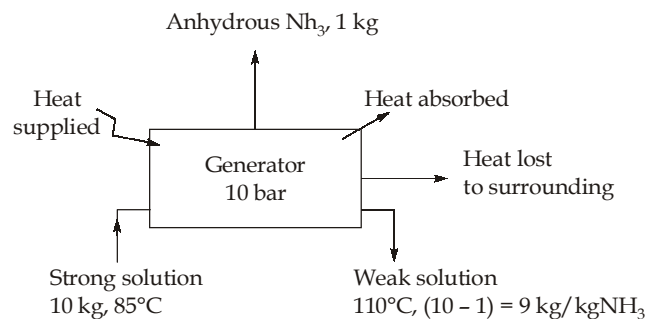
$$h_3 = h_4 = 81.25 \text{ kJ/kg}$$

$$\begin{aligned} h_1 &= h_{f4} + xh_{fg} \\ &= -7.53 + 0.6 \times 245.8 \\ &= 139.95 \text{ kJ/kg} \end{aligned}$$

$$\therefore (COP)_{ideal} = \frac{h_1 - h_4}{h_2 - h_1} = \frac{139.95 - 81.25}{202.88 - 139.95} = 0.933$$

$$\therefore (COP)_{act} = 0.7 \times 0.933 = 0.65$$

18. (c)



Energy balance: Heat of strong ammonia-aqua + Heat from heating source = Heat of anhydrous NH_3 vapour + Heat of weak solution + heat absorbed + heat lost to surrounding.

$$10 \times [200 + 4.8(85 - (-50))] + Q_s = 1910 + 9 \times [200 + 4.8 \times (110 - (-50))] + 479.1 + 100$$

$$Q_s = 2721.1 \text{ kJ/kgNH}_3$$

19. (b)

As per given data, $P = 85 \text{ kPa}$, $\text{DBT} = 30^\circ\text{C}$, $P_{vs} = 4.24 \text{ kPa}$, $\phi = 0.55$

$$\therefore \phi = \frac{P_v}{P_{vs}} \Rightarrow 0.55 = \frac{P_v}{4.24}$$

$$\therefore P_v = 2.332 \text{ kPa}$$

$$\begin{aligned} \therefore \text{Humidity ratio, } \omega &= \frac{0.622 P_v}{P - P_v} = \frac{0.622 \times 2.332 \times 1000}{85 - 2.332} \\ &= 17.54 \text{ g/kgd.a.} \end{aligned}$$

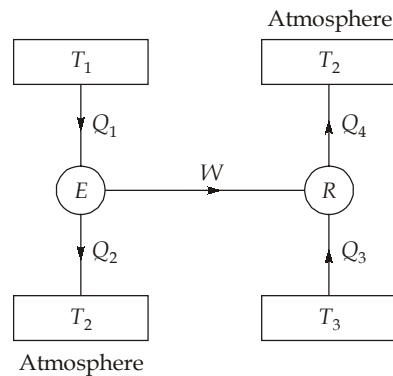
20. (c)

Given: $Q_3 = 40 \times 3.5 = 140 \text{ kW}$

$$(\text{COP})_{\text{act}} = 0.7(\text{COP})_{\text{ideal}}$$

$$(\eta_E)_{\text{act}} = 0.5(\eta_E)_{\text{ideal}}$$

$$T_1 = 1273 \text{ K}, T_2 = 303 \text{ K}, T_3 = 263 \text{ K}$$



Heat supplied ' Q_1 ' is given by

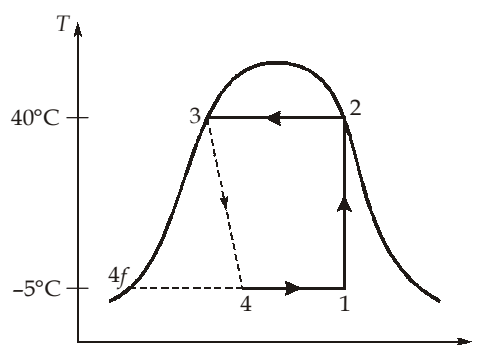
$$\begin{aligned} Q_1 &= \frac{Q_3}{(\text{COP})_{\text{act}} \times (\eta_E)_{\text{act}}} = \frac{140}{0.7 \left(\frac{T_3}{T_2 - T_3} \right) \times 0.5 \left(\frac{T_1 - T_2}{T_1} \right)} \\ &= \frac{140 \times 1273 \times (303 - 263)}{0.7 \times 0.5 \times 263(1273 - 303)} = 79.84 \text{ kW} \end{aligned}$$

$$\therefore (\text{COP})_{\text{overall}} = \frac{Q_3}{Q_1} = \frac{140}{79.84} = 1.75$$

21. (b)

$$\begin{aligned} \text{Refrigerating effect, R-E} &= h_1 - h_4 = (h_1 - h_{4f}) - (h_4 - h_{4f}) \\ &= T(S_1 - S_{4f}) - (h_3 - h_{4f}) \end{aligned}$$

$$[\because h_3 = h_4]$$



Here,

$$\begin{aligned}
 S_1 - S_{4f} &= (S_1 - S_3) + (S_3 - S_{4f}) \\
 S_1 - S_{4f} &= \left(\frac{h_{fg}}{T} \right)_{40^\circ\text{C}} + c_p \ln \left(\frac{T_3}{T_{4f}} \right) \quad [\because S_1 = S_2] \\
 &= \left(\frac{203.2}{273 + 40} \right) + 0.963 \ln \left(\frac{273 + 40}{273 - 5} \right) \\
 &= 0.649 + 0.149 = 0.798
 \end{aligned}$$

and

$$\begin{aligned}
 h_3 - h_{4f} &= C_{pl} (T_3 - T_{4f}) \\
 \therefore \text{R.E.} &= 268 \times 0.798 - 0.963 \times (313 - 268) \\
 &= 170.53 \text{ kJ/kg}
 \end{aligned}$$

22. (a)

Given : $t = 28^\circ\text{C}$; $p = 1 \text{ bar}$; $\phi = 67\%$; $P_{vs} = 3.778 \text{ kPa}$

$$\phi = \frac{P_v}{P_{vs}}$$

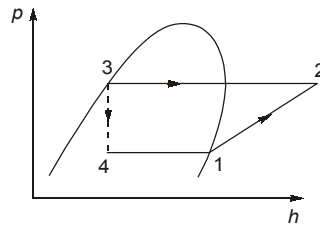
$$\Rightarrow 0.67 = \frac{P_v}{3.778}$$

$$\Rightarrow P_v = 2.53126 \text{ kPa}$$

$$\omega = \frac{0.622 P_v}{p - P_v} = \frac{0.622 \times 2.53126}{100 - 2.53126} = 0.016 \text{ kg/kg of dry air}$$

$$\begin{aligned}
 h &= 1.005t + \omega(2500 + 1.88t) \\
 &= 1.005 \times 28 + 0.016 (2500 + 1.88 \times 28) \\
 &= 68.98 \text{ kJ/kg}
 \end{aligned}$$

23. (b)



Given: $h_1 = 1200 \text{ kJ/kg}$, $h_2 = 1700 \text{ kJ/kg}$, $h_4 = h_3 = 400 \text{ kJ/kg}$

$$\text{Compressor work} = \dot{m}[h_2 - h_1]$$

$$\Rightarrow \dot{m} = \frac{W_c}{h_2 - h_1} = \frac{50 \times 1000}{(1700 - 1200) \times 1000} = 0.1 \text{ kg/s}$$

$$\begin{aligned}
 \text{Capacity of plant} &= \frac{\dot{m}(h_1 - h_4)}{3.5} \text{ Tons} \\
 &= \frac{0.1(1200 - 400)}{3.5} = 22.86 \text{ Tons}
 \end{aligned}$$

24. (a)

Given data: Total pressure, $p = 736 \text{ mm Hg}$, Saturation pressure, $p_{vs} = 18 \text{ mm Hg}$,

$$\text{Relative humidity, } \phi = \frac{p_v}{p_{vs}} = 0.68$$

$$0.68 = \frac{p_v}{18}$$

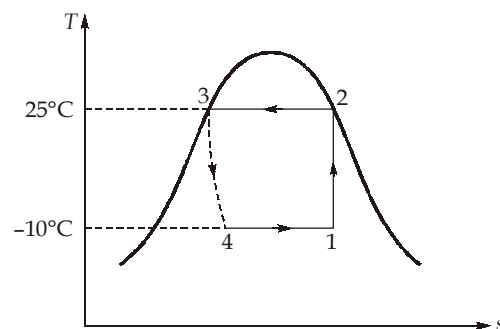
Partial pressure of water vapour, $p_v = 12.24$ mm Hg

We know that humidity ratio,

$$\begin{aligned}\omega &= \frac{0.622 p_v}{p - p_v} \text{ kg}_{W.V.}/\text{kg of d.a.} \\ &= \frac{0.622 \times 12.24}{736 - 12.24} = 0.01052 \text{ kg}_{W.V.}/\text{kg of d.a.} \\ &= 10.52 \text{ g}_{W.V.}/\text{kg d.a.}\end{aligned}$$

25. (d)

Given: $P_2 = 10$ bar, $P_1 = 3$ bar, $\dot{m} = 6$ kg/min



$$s_2 = (s_g)_{25^\circ\text{C}} = 5.0391 \text{ kJ/kgK}$$

$$s_2 = s_1 = (s_g)_{-10^\circ\text{C}} + x(s_{fg})_{-10^\circ\text{C}}$$

$$5.0391 = 0.5443 + x(5.4770 - 0.5443)$$

$$x = 0.9112$$

So,

$$\begin{aligned}h_1 &= (h_f)_{-10^\circ\text{C}} + x(h_{fg})_{-10^\circ\text{C}} \\ &= (130.37) + 0.9112 (1380.50 - 130.37)\end{aligned}$$

$$h_1 = 1269.51 \text{ kJ/kg}$$

$$h_2 = (h_g)_{25^\circ\text{C}} = 1450.80 \text{ kJ/kg}$$

$$h_3 = (h_f)_{25^\circ\text{C}} = 285.98 \text{ kJ/kg} \quad (\because \text{Process 3-4 is Isenthalpic})$$

$\Rightarrow$

$$h_3 = h_4 = 285.98 \text{ kJ/kg}$$

Now, Refrigeration capacity = $\dot{m}(h_1 - h_4) = 6(1269.51 - 285.98)$

$$\text{RC} = 5901.23 \text{ kJ/min}$$

$$\text{RC} = 98.35 \text{ kW}$$

26. (a)

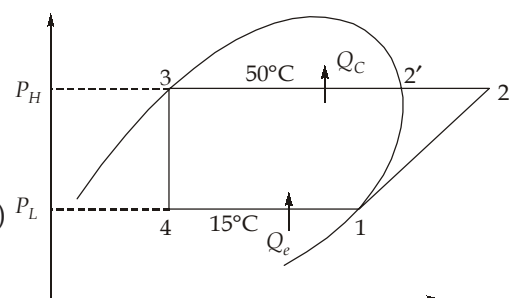
For discharge temperature, $s_1 = s_2 = s'_2 + c_{p_v} \ln\left(\frac{T_2}{T'_2}\right)$

$$1.72 = 1.7072 + 1.246 \ln\left(\frac{T_2}{273 + 50}\right)$$

$$T_2 = 326.33 \text{ K}$$

Enthalpy at discharge, $h_2 = h'_2 + c_{p_v} (T_2 - T'_2)$

$$h_2 = 423.4 + 1.246 (326.33 - 323)$$



$$= 427.55 \text{ kJ/kg}$$

Heat rejection in condenser,

$$Q_C = \dot{m}(h_2 - h_3)$$

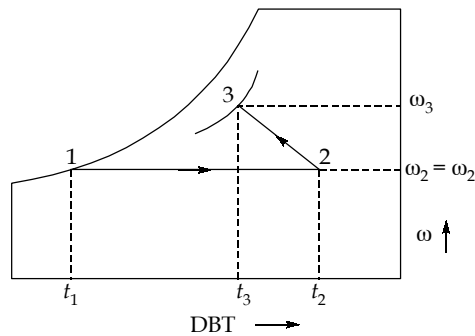
$$\frac{100000}{3600} = \dot{m}(427.55 - 271.62)$$

Mass flow rate of refrigerant, $\dot{m} = 0.178 \text{ kg/s}$

Theoretical piston displacement of compressor,

$$\begin{aligned}\dot{V} &= \dot{m}v_1 = 0.178 \times 0.04185 \\ &= 7.455 \times 10^{-3} \text{ m}^3/\text{s}\end{aligned}$$

27. (b)



At state 3,

$$\begin{aligned}t_3 &= 12^\circ\text{C} \\ [P_{\text{sat}}]_{12^\circ\text{C}} &= 2.34 \text{ kPa} \\ \phi &= 0.5\end{aligned}$$

So,

$$P_{v3} = \phi P_{\text{sat}} = 0.5(2.34) = 1.17 \text{ kPa}$$

So,

$$\omega_3 = 0.622 \frac{P_{v3}}{P_{\text{atm}} - P_{v3}} = 0.622 \frac{1.17}{101.3 - 1.17}$$

$$\omega_3 = 7.267 \times 10^{-3} \text{ kg/kg of d.a.}$$

At state 1,

$$\begin{aligned}t_1 &= 2^\circ\text{C} \\ \phi &= 100\% \text{ (Saturated air)} \\ P_{v1} &= [P_{\text{sat}}]_{\text{at } 2^\circ\text{C}} = 0.7156 \text{ kPa}\end{aligned}$$

Now,

$$\omega_1 = 0.622 \frac{P_{v1}}{P_{\text{atm}} - P_{v1}} = 0.622 \frac{0.7156}{101.3 - 0.7156}$$

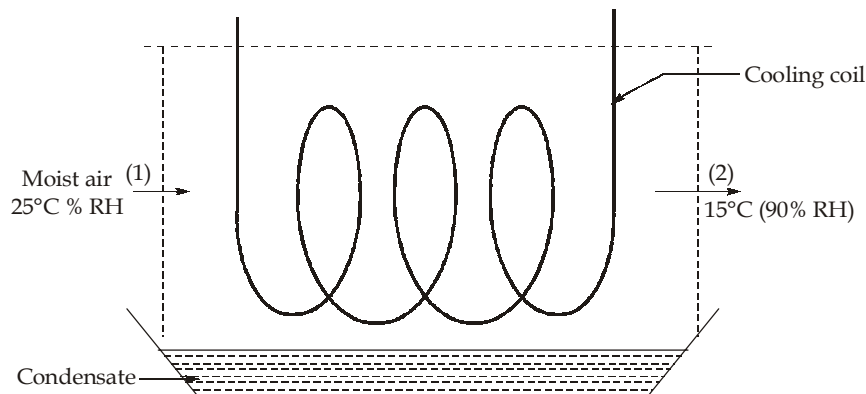
$$\omega_1 = 4.425 \times 10^{-3} \text{ kg/kg of d.a.}$$

Specific volume of dry air at room temperature,

$$v_3 = \frac{RT_3}{(P_{\text{air}})_3} = \frac{0.287(273 + 12)}{(101.3 - 1.17)} = 0.816 \text{ m}^3/\text{kg}$$

$$\begin{aligned}\text{Spray water} &= \frac{(\Delta\omega)}{v_3} = \frac{(7.267 - 4.425)}{0.816} \times 10^{-3} \text{ kg/m}^3 \\ &= 3.482 \text{ g/m}^3\end{aligned}$$

28. (a)



By continuity equation for moisture balance.

$$\dot{m}_{\text{water}} = \dot{m}_{\text{air}} \times (\omega_1 - \omega_2)$$

Here, For ω_1 and ω_2 ,

$$P_{v_1} = \phi_1 P_{s1} = 0.80 \times 4.246 = 3.397 \text{ kPa}$$

$$P_{v_2} = 0.90 \times (1.7051) = 1.5346 \text{ kPa}$$

So,

$$\begin{aligned} \omega_1 &= 0.622 \times \frac{P_{v_1}}{P_{\text{atm}} - P_{v_1}} = 0.622 \times \left(\frac{3.397}{101.325 - 3.397} \right) \\ &= 0.02131 \text{ kg/kg d.a.} \end{aligned}$$

and

$$\omega_2 = \frac{0.622 \times 1.5346}{101.325 - 1.5346} = 0.00949 \text{ kg/kg d.a.}$$

So, amount of moisture condensed per kg of d.a.

$$\begin{aligned} \dot{m}_{\text{water}} &= \omega_1 - \omega_2 \\ &= 0.02131 - 0.00949 \\ &= 0.01182 \text{ kg/kg d.a.} \end{aligned}$$

29. (c)

The refrigerator operates on ideal Carnot cycle

$$\text{COP} = \frac{T_L}{T_H - T_L} = \frac{-8 + 273}{28} = 9.464$$

Amount of cooling or heat extracted from the refrigerant space,

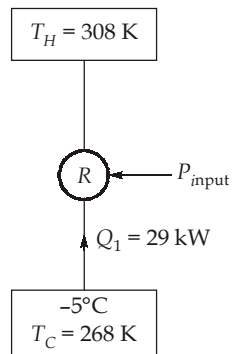
$$Q_L = \text{COP} \times W_{\text{in}} = 9.464 \times 15 = 141.96 \text{ kJ}$$

Amount of refrigerant that vaporizes during heat absorption is

$$\begin{aligned} m_{\text{evap}} \times h_{fg} &= Q_L \\ \Rightarrow m_{\text{evap}} \times 204.52 &= 141.96 \text{ kJ} \\ \Rightarrow m_{\text{evap}} &= 0.694 \text{ kg} \end{aligned}$$

$$\text{Fraction of mass that vaporises} = \frac{m_{\text{evap}}}{m_{\text{total}}} = \frac{0.694}{0.8} = 0.868 \approx 0.87$$

30. (a)



$$\text{Actual COP} = \frac{1}{3} \times \text{ideal COP} = \frac{1}{3} \times \left(\frac{T_C}{T_H - T_C} \right) = \frac{1}{3} \left(\frac{268}{308 - 268} \right)$$

$$(\text{COP})_{\text{actual}} = 2.23$$

$$(\text{COP})_{\text{actual}} = \frac{\text{Desired effect}}{P_{\text{input}}}$$

$$P_{\text{input}} = \frac{29}{2.23} = 13.00 \text{ kW}$$

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