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NETWORK THEORY

EC-EE

Date of Test : 13/08/2025

ANSWER KEY ➤

- | | | | | |
|--------|---------|---------|---------|---------|
| 1. (b) | 7. (c) | 13. (a) | 19. (a) | 25. (c) |
| 2. (a) | 8. (a) | 14. (b) | 20. (a) | 26. (a) |
| 3. (c) | 9. (c) | 15. (c) | 21. (a) | 27. (b) |
| 4. (a) | 10. (d) | 16. (d) | 22. (b) | 28. (b) |
| 5. (a) | 11. (d) | 17. (d) | 23. (a) | 29. (c) |
| 6. (c) | 12. (d) | 18. (b) | 24. (a) | 30. (c) |

DETAILED EXPLANATIONS

1. (b)

Since the network is passive, current I is due to the two sources V_1 and V_2 .
By principle of superposition,

$$I = K_1 V_1 + K_2 V_2$$

$$1 = 4K_1 + 0$$

$$K_1 = 0.25$$

and

$$-1 = 0 + 5K_2$$

$$K_2 = \frac{-1}{5} = -0.2$$

Given,

$$V_1 = 10 \text{ V}$$

and

$$V_2 = 5 \text{ V}$$

$$\text{Current, } I = (10 \times 0.25) + (5 \times -0.2)$$

$$I = 2.5 - 1 = 1.5 \text{ A}$$

2. (a)

We have:

$$\vec{I}_3 = \vec{I}_1 - \vec{I}_2$$

$$= 6 \angle 30^\circ - 2 \angle 20^\circ$$

$$= 4.045 \angle 34.92^\circ \text{ A}$$

\therefore

$$I_{3 \text{ max}} = \sqrt{2} \times I_{\text{rms}}$$

$$= \sqrt{2} \times 4.045 = 5.72 \text{ A}$$

Here,

$$\phi = 34.92^\circ$$

and

$$\omega = 2\pi f = 2\pi \times 60 = 377 \text{ rad/sec}$$

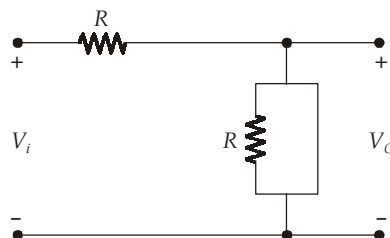
\therefore Instantaneous current

$$i_3 = 5.72 \sin (377t + 34.92^\circ) \text{ A}$$

3. (c)

At $\omega \rightarrow \infty$, Capacitor \rightarrow short circuited

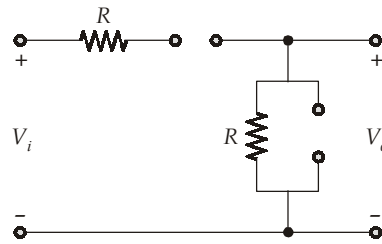
Circuit looks like,



$$\frac{V_o}{V_i} = 0$$

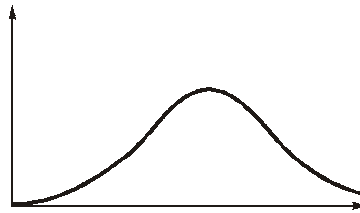
At $\omega \rightarrow 0$, Capacitor \rightarrow open circuited

Circuit looks like



$$\frac{V_o}{V_i} = 0$$

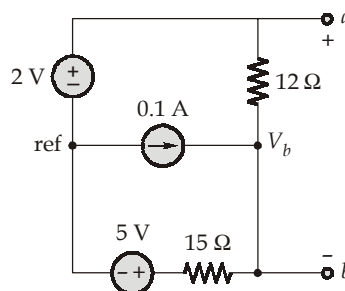
So frequency response of the circuit will be,



So the circuit is Band pass filter

4. (a)

Removing terminal C the circuit can be rearranged as,



V_{Th} is the voltage dropped by 12Ω resistor

$$V_{Th} = V_a - V_b = 2 - V_b$$

Apply KCL at node b

$$\frac{V_b - V_a}{12} - 0.1 + \frac{V_b - 5}{15} = 0$$

By solving, we get

$$V_b = 4\text{ V}$$

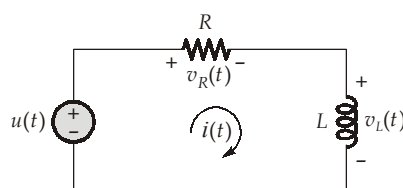
$$V_{Th} = -2\text{ V}$$

$$R_{Th} = \frac{12 \times 15}{12 + 15} = 6.667\Omega$$

and

$$I_N = \frac{V_{Th}}{R_{Th}} = -0.3\text{ A}$$

5. (a)



$$i(t) = 1 - e^{-t/\tau}$$

where,

$$\tau = \frac{L}{R}$$

$$v_R(t) = i(t) \cdot R$$

$$v_R(t) = (1 - e^{-t/\tau})R$$

$$v_L(t) = L \frac{di}{dt} = L \cdot \frac{1}{\tau} e^{-t/\tau}$$

$$v_L(t) = R e^{-t/\tau}$$

Let $t = t_1$ when $v_R(t) = v_L(t)$

$$\Rightarrow (1 - e^{-t_1/\tau})R = R e^{-t_1/\tau}$$

$$\Rightarrow 2e^{-t_1/\tau} = 1$$

$$\Rightarrow e^{-t_1/\tau} = \frac{1}{2}$$

$$\Rightarrow -\frac{t_1}{\tau} = \ln \frac{1}{2} = -\ln 2$$

$$\Rightarrow t_1 = \tau \ln 2$$

6. (c)

We apply KVL in the loop,

$$-12 + 4i + 2V_0 - 4 + 6i = 0$$

Put, $V_0 = -6i$

$$-12 + 4i - 12i - 4 + 6i = 0$$

$$-2i = 16$$

$$i = -8 \text{ A}$$

$$V_0 = -6 \times -8 = 48 \text{ V}$$

7. (c)

Current in a capacitor leads voltage by 90° ,

Voltage across capacitor, $V_c = 10 \sin 2\pi t$

$$\text{Capacitor current} = \frac{V_c}{X_c} = \frac{10}{X_c} \sin \left(2\pi t + \frac{\pi}{2} \right)$$

$$= \frac{10}{X_c} \cos 2\pi t$$

$$\text{Power in capacitor} = V_c(t) i_c(t)$$

$$\text{Energy stores in capacitor} = \int_0^{0.5} V_c(t) i_c(t) dt$$

$$E_C = \int_0^{0.5} \frac{100}{X_C} \sin 2\pi t \cos 2\pi t dt$$

$$= \frac{50}{X_C} \int_0^{0.5} \sin 4\pi t dt = \frac{50}{X_C} \left[\frac{-\cos 4\pi t}{4\pi} \right]_0^{0.5}$$

$$E_C = \frac{50}{4\pi X_C} [-\cos 2\pi + \cos 0] = 0 \text{ J}$$

8. (a)

Here, Line voltage, $V_L = 1100$ V

Line current, $I_L = 80$ A

Power supplied, $P = 100$ kW

∴ power factor of the circuit,

$$\cos \phi = \frac{P}{\sqrt{3}V_L I_L} = \frac{100 \times 10^3}{\sqrt{3} \times 1100 \times 80} = 0.656 \text{ leading}$$

Impedance of the load per phase,

$$Z = \frac{V_{ph}}{I_{ph}} = \frac{\frac{V_L}{\sqrt{3}}}{I_L} = \frac{\frac{1100}{\sqrt{3}}}{80} = 7.94 \Omega$$

Resistance of the load per phase,

$$R = Z \cos \phi = 7.94 \times 0.656 = 5.208 \Omega \approx 5.21 \Omega$$

Reactance of the load per phase,

$$X_C = \sqrt{Z^2 - R^2} = \sqrt{(7.94)^2 - (5.21)^2} = 5.99 \Omega$$

Capacitance of the load per phase,

$$C = \frac{1}{2\pi f X_C}$$

$$\frac{1}{2\pi \times 50 \times 5.99} = 531.4 \mu\text{F}$$

9. (c)

The transfer function is,

$$H(s) = \frac{V_0(s)}{V_i(s)} = \frac{R \parallel \frac{1}{sC}}{sL + R \parallel \frac{1}{sC}} = \frac{R}{s^2 RLC + sL + R}$$

or

$$H(j\omega) = \frac{R}{-\omega^2 RLC + j\omega L + R}$$

Since

$$H(0) = 1 \text{ and } H(\infty) = 0$$

∴ The circuit is a second-order low pass filter.

10. (d)

When all the resistances are present:

$$P = \frac{3V_{ph}^2}{R} = 3 \left(\frac{V_L}{\sqrt{3}} \right)^2 \times \frac{1}{R} = \frac{V_L^2}{R}$$

When one of the phase resistances is removed,

$$P = 2 \left(\frac{V_L}{2} \right)^2 \times \frac{1}{R} = \frac{V_L^2}{2R}$$

$$\therefore \text{Reduction in power} = \frac{\frac{V_L^2}{R} - \frac{V_L^2}{2R}}{\frac{V_L^2}{R}} \times 100 = 50\%$$

11. (d)

Applying KVL in primary and secondary loops,

$$V_1 = I_1 j\omega L_1 - I_2 j\omega M \quad \dots(i)$$

$$0 = -I_1 j\omega M + I_2 (100 + j\omega L_2) \quad \dots(ii)$$

$$\text{Input impedance} = Z_{in} = \frac{V_1}{I_1} = j\omega L_1 - \frac{I_2}{I_1} j\omega M$$

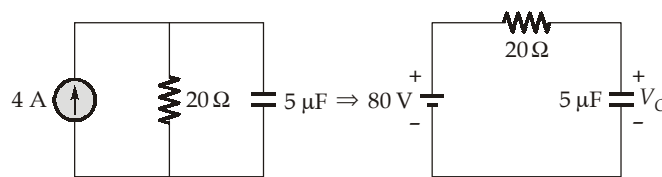
From equation (ii), we get

$$\frac{I_2}{I_1} = \frac{j\omega M}{100 + j\omega L_2}$$

Substituting the above expression in equation (i), we get

$$\begin{aligned} Z_{in} &= j\omega L_1 - \frac{(j\omega M)^2}{100 + j\omega L_2} \\ &= (j1000) + \frac{(1000)^2 \times 4}{100 + j4000} \quad [\because M^2 = L_1 L_2] \\ Z_{in} &= 25 \angle 1.43^\circ \Omega \end{aligned}$$

12. (d)

The circuit that exists for $t < 0$ is,

$$V = IR = 4 \times 20 = 80 \text{ V}$$

 \therefore

$$V_c(0^+) = V_c(0^-) = 80 \text{ V}$$

$$\text{Time constant, } \tau = RC = 20 \times 5 \times 10^{-6} = 10^{-4} \text{ s}$$

After $t = 0$,

$$\begin{aligned} V_c(t) &= V_\infty - (V_\infty - V_0) e^{-t/\tau} \\ &= 0 - (0 - 80) e^{-t/\tau} \end{aligned}$$

$$V_c(t) = 80e^{-10^4 t}$$

The half of initial voltage,

$$\frac{80}{2} = 40 \text{ V}$$

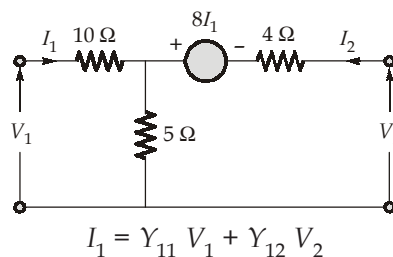
 \therefore

$$40 = 80e^{-10^4 t}$$

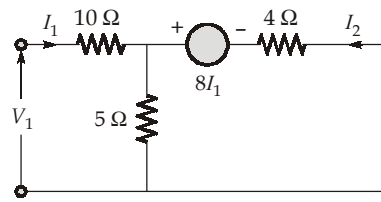
$$0.5 = e^{-10^4 t}$$

$$\text{Time, } t = 69.3 \mu\text{s}$$

13. (a)



Short-circuiting port-2 i.e. $V_2 = 0$, we get



Applying KVL in both loops, we get

$$V_1 = 10I_1 + 5I_1 + 5I_2 \quad \dots(i)$$

and $4I_2 + 5I_2 + 5I_1 - 8I_1 = 0$

$$\Rightarrow 9I_2 = 3I_1$$

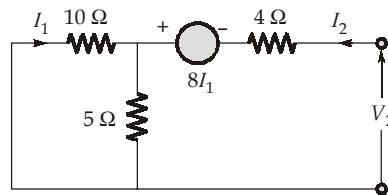
$$\Rightarrow I_2 = \frac{I_1}{3} \quad \dots(ii)$$

From equations (i) and (ii); we get

$$V_1 = 10I_1 + 5I_1 + \frac{5I_1}{3} = 15I_1 + \frac{5I_1}{3} = \frac{50I_1}{3}$$

$$\Rightarrow \left. \frac{I_1}{V_1} \right|_{V_2=0} = Y_{11} = \frac{3}{50} \text{ mho}$$

Short circuiting port-1; i.e. $V_1 = 0$, we get



Applying KVL in both loops; we have

$$10I_1 + 5I_1 + 5I_2 = 0$$

$$15I_1 = -5I_2$$

$$\Rightarrow I_2 = -3I_1 \quad \dots(iii)$$

and $V_2 = 4I_2 - 8I_1 + 5I_1 + 5I_2$

$$\Rightarrow V_2 = 9I_2 - 3I_1$$

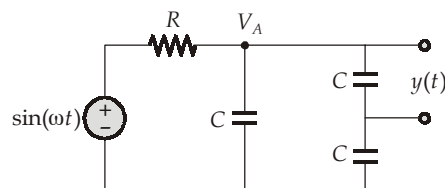
$$\Rightarrow V_2 = 9(-3I_1) - 3I_1$$

$$\Rightarrow V_2 = -30I_1$$

[Using equation (iii)]

$$\therefore \left. \frac{I_1}{V_2} \right|_{V_1=0} = Y_{12} = -\frac{1}{30} \text{ mho}$$

14. (b)



Applying KCL at node A, we get

$$\frac{V_A - \sin \omega t}{R} + \frac{V_A}{\frac{1}{j\omega C}} + \frac{V_A}{\frac{2}{j\omega C}} = 0 \quad \dots(i)$$

$$V_A \left[\frac{1}{R} + j\omega C + \frac{j\omega C}{2} \right] = \frac{\sin \omega t}{R} = \frac{1 \angle 0^\circ}{R}$$

$$V_A = \frac{2}{2 + 3RC \cdot j\omega}$$

...(ii)

Also

$$Y = \frac{V_A}{2} = \frac{1}{2 + 3j\omega RC}$$

...(iii)

$$\therefore |A(\omega)| = \frac{1}{4} = 0.25$$

$$\therefore \frac{1}{4} = \frac{1}{\sqrt{4 + 9\omega^2 (RC)^2}}$$

$$\text{or, } \omega = \frac{2}{\sqrt{3} RC}$$

15. (c)

rms value of the waveform,

$$= \sqrt{\frac{1}{T} \int_0^T x(t)^2 dt} = \sqrt{\frac{1}{T} \int_0^T \left[\left(\frac{10}{T} \right) t \right]^2 dt}$$

Since the line passing through origin is,

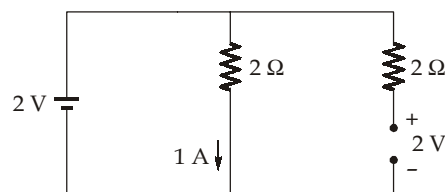
$$y = mx$$

$$y = \left(\frac{10 - 0}{T} \right) t$$

$$\text{RMS} = \sqrt{\frac{10^2}{T^3} \left[\frac{t^3}{3} \right]_0^T} = \frac{10}{\sqrt{3}} = 5.77$$

16. (d)

The circuit in the steady state with switch 's' is closed

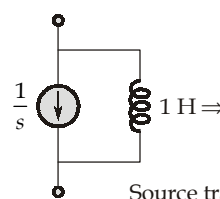
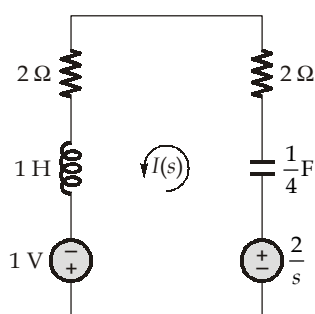


$$i(0^+) = i(0^-) = 1 \text{ A}$$

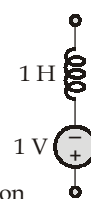
$$V_c(0^+) = V_c(0^-) = 2 \text{ V}$$

and

Changing the circuit in s-domain



Source transformation



$$V = \frac{1}{S} \times SL(s) = 1 \times 1 = 1 \text{ V}$$

KVL in the loop gives:

$$\frac{2}{s} + 1 = \left(\frac{4}{s} + 4 + s \right) I(s)$$

$$I(s) = \frac{s+2}{(s+2)^2} = \frac{1}{s+2}$$

Taking inverse laplace, we get

$$i(t) = e^{-2t}$$

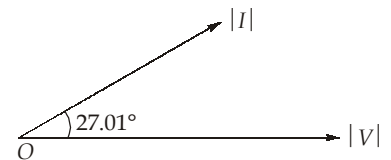
17. (d)

$$Y_{eq} = \frac{1}{50} + \frac{1}{j(2\pi \times 50 \times 0.15)} + j(2\pi \times 50 \times 100 \times 10^{-6})$$

$$Y_{eq} = 0.0224 \angle 27.01^\circ \text{ U}$$

$$Z_{eq} = 44.64 \angle -27.01^\circ \Omega$$

$$I = \frac{100 \angle 0^\circ}{44.64 \angle -27.01^\circ} = 2.24 \angle 27.01^\circ \text{ A}$$



The input power factor = $\cos(27.01^\circ) = 0.89$ leading

18. (b)

When the switch is at position 1,

$$V_C(0^-) = 100 \text{ V}$$

Voltage across capacitor at $t > 0$

$$V_C = V_\infty - (V_\infty - V_0)e^{-t/\tau}$$

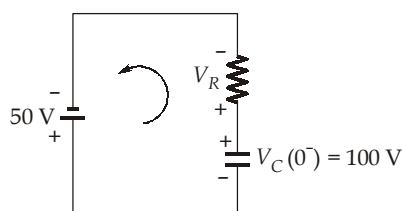
Where,

$$\tau = RC = 5000 \times 1 \times 10^{-6} = 5 \text{ msec}$$

$$V_C = (-50) - (-50 - 100)e^{-200t}$$

$$V_C = (150 e^{-200t} - 50) \text{ V}$$

Applying KVL in the loop

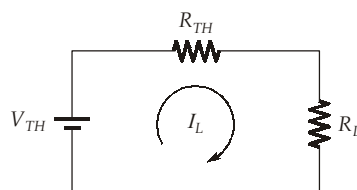


$$-V_C + V_R - 50 = 0$$

$$V_R = V_C + 50 = 150 e^{-200t} - 50 + 50$$

$$V_R = 150 e^{-200t} \text{ V}$$

19. (a)



For first case,

$$P = 20 \text{ kW and } R_L = 50 \Omega$$

$$\begin{aligned}
 \text{Power, } P &= I_L^2 R_L \\
 \text{or, } 20 \times 10^3 &= I_L^2 \times 50 \\
 \text{or, } I_L &= 20 \text{ A} \\
 \text{and } V_{TH} &= 20 \cdot R_{TH} + 1000 \quad \dots (i)
 \end{aligned}$$

For second case

$$\begin{aligned}
 \text{Power, } P &= 20 \text{ kW and } R_L = 200 \Omega \\
 \therefore I_L &= \sqrt{\frac{P_L}{R_L}} = \sqrt{\frac{20 \times 10^3}{200}} = 10 \text{ A} \\
 \text{and } V_{TH} &= 10 R_{TH} + 2000 \quad \dots (ii)
 \end{aligned}$$

From equation (i) and (ii), we get

$$V_{TH} = 3000 \text{ V and } R_{TH} = 100 \Omega$$

Thus, the maximum power transfer to the load

$$P_L = \frac{V_{TH}^2}{4R_{TH}} = \frac{(3000)^2}{4 \times 100} = 22.5 \text{ kW}$$

20. (a)

$$V_{ab} = V_{Th}$$

By applying KCL,

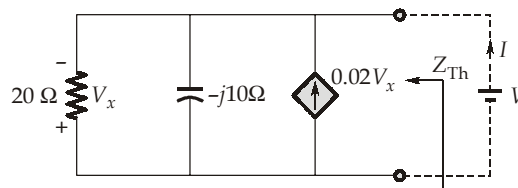
$$\frac{V_{Th} - 100}{20} + \frac{V_{Th}}{-j10} = 0.02 V_x$$

Where,

$$V_x = 100 - V_{Th}$$

$$\frac{V_{Th} - 100}{20} + \frac{V_{Th}}{-j10} = 0.02(100 - V_{Th})$$

$$V_{Th} = \frac{7}{0.07 + j0.1} = 57.34 \angle -55^\circ \text{ V}$$



$$Z_{Th} = \frac{V}{I}$$

By apply KCL in the circuit gives,

$$\frac{V}{20} + \frac{V}{-j10} - 0.02V_x = I$$

$$\text{and, } V_x = -V$$

$$\therefore \frac{V}{20} + \frac{V}{-j10} + 0.02V = I$$

$$\begin{aligned}
 Z_{Th} &= \frac{V}{I} = \left[\frac{1}{\frac{1}{20} + \frac{1}{-j10} + 0.02} \right] \\
 &= (4.7 - j6.7) \Omega
 \end{aligned}$$

21. (a)

Given,

$$V_1 = 4V_2 - 20I_2 \quad \dots(i)$$

$$I_1 = 0.1 V_2 - 2I_2 \quad \dots(ii)$$

We need to find the Thevenin impedance Z_{th}

At the input port, $V_1 = -10I_1 \quad \dots(iii)$

(For Thevenin impedance calculation voltage source is replaced by short circuit)

Put equation (iii) in equation (i),

$$-10I_1 = 4V_2 - 20I_2$$

$$I_1 = -0.4 V_2 + 2I_2 \quad \dots(iv)$$

Equating equation (ii) and (iv),

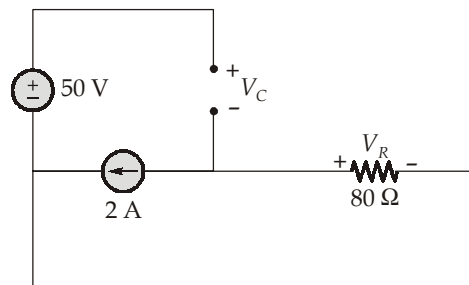
$$0.1 V_2 - 2I_2 = -0.4 V_2 + 2I_2$$

$$0.5 V_2 = 4I_2$$

$$Z_{th} = \frac{V_2}{I_2} = 8 \Omega$$

22. (b)

For $t < 0$;



$$V_R(0^-) = -160 \text{ V}$$

$$V_{2A} = 160 \text{ V}$$

$$V_C(0^+) = 210 \text{ V}$$

$$V_C(0^-) = V_C(0^+) = 210 \text{ V}$$

and

23. (a)

Total impedance is

$$Z = Z_3 + (Z_1 \parallel Z_2)$$

$$= (30 + jX) + \left(\frac{(20 + j10)(10 - j30)}{20 + j10 + 10 - j30} \right)$$

$$= 30 + jX + \frac{500 - j500}{30 - j20}$$

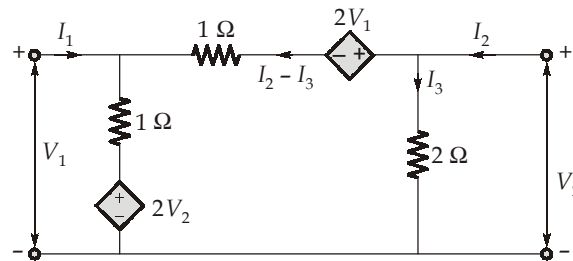
$$= 30 + jX + 19.23 - 3.846 i$$

At resonance, the imaginary part is zero

$$\therefore X = 3.846 \Omega \approx 3.85 \Omega$$

24. (a)

Transforming the dependent current source in to voltage source, the network is shown as,



Let I_3 be the current through $2\ \Omega$

Apply KVL in outer loop,

$$-V_2 + 2V_1 + I_2 - I_3 + V_1 = 0$$

$$-V_2 + 3V_1 + I_2 - I_3 = 0$$

...(i)

Also,

$$-V_1 + I_1 + I_2 - I_3 + 2V_2 = 0$$

...(ii)

$$V_1 = I_1 + I_2 - I_3 + 2V_2$$

From equation (i) and (ii), we get

$$5V_2 + 3I_1 + 4I_2 - 4I_3 = 0$$

Where,

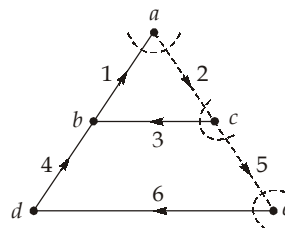
$$I_3 = \frac{V_2}{2}$$

$$V_2 = -I_1 - \frac{4}{3}I_2$$

Hence,

$$Z_{21} = \left. \frac{V_2}{I_1} \right|_{I_2=0} = -1\ \Omega$$

25. (c)

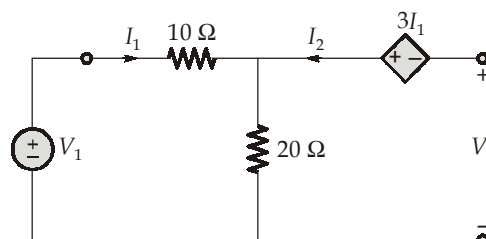


$C_1(1, 2)$: This separates the node-a and direction of both branch is opposite to each other.

$C_2(2, 3, 5)$: This separates node-C and direction of branch - 2 is opposite to branch - 3 and branch - 5.

26. (a)

To determine A and C, we leave the output port open as in figure. So that $I_2 = 0$ and place a voltage source V_1 at the input port.



$$V_1 = (10 + 20)I_1 = 30I_1$$

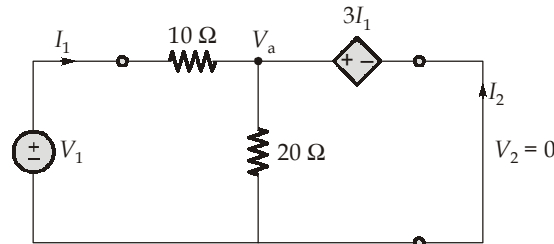
$$V_2 = 20I_1 - 3I_1 = 17I_1$$

Thus,

$$A = \frac{V_1}{V_2} = \frac{30I_1}{17I_1} = 1.765$$

$$C = \frac{I_1}{V_2} = \frac{I_1}{17I_1} = 0.0588 \text{ S}$$

To obtain B and D , we short circuit the output port so that,



But,

$$V_a = 3I_1$$

and

$$I_1 = \frac{(V_1 - V_a)}{10}$$

$$V_1 = 13I_1$$

Applying KCL at node a ,

$$I_1 - \frac{3I_1}{20} + I_2 = 0$$

$$\frac{17}{20}I_1 = -I_2$$

Therefore,

$$B = -\frac{V_1}{I_2} = \frac{-13I_1}{\left(-\frac{17}{20}\right)I_1} = 15.29 \Omega$$

$$D = \frac{20}{17} = 1.176$$

$$\begin{bmatrix} A & B \\ C & D \end{bmatrix} = \begin{bmatrix} 1.765 & 15.29 \\ 0.0588 & 1.176 \end{bmatrix}$$

27. (b)

$$Z_{Th} = (40 - j30) \parallel j20$$

$$= \frac{j20(40 - j30)}{j20 + 40 - j30} = (9.412 + j22.35) \Omega$$

By voltage division,

$$V_{th} = \frac{j20}{j20 + 40 - j30} (150 \angle 30^\circ)$$

$$= 72.76 \angle 134^\circ \text{ V}$$

The value of R_L that will absorb the maximum average power is

$$R_L = |Z_{th}| = \sqrt{(9.412)^2 + (22.35)^2} = 24.25 \, \Omega$$

The current through the load is,

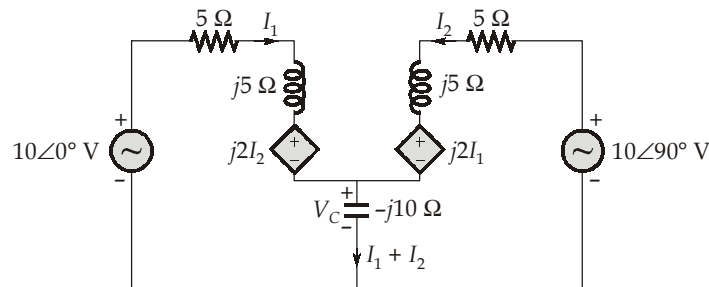
$$I = \frac{V_{th}}{Z_{th} + R_L} = \frac{72.76 \angle 134^\circ}{33.66 + j22.35} = 1.8 \angle 100.416^\circ$$

The maximum average power absorbed by R_L is

$$\begin{aligned} P_{\max} &= \frac{1}{2} |I|^2 R_L = \frac{1}{2} (1.8)^2 (24.25) \\ &= 39.285 \approx 39.29 \text{ W} \end{aligned}$$

28. (b)

Using de-coupled technique,



Applying KVL in loop-1,

$$\begin{aligned} 10 \angle 0^\circ &= I_1(5 + j5 - j10) + I_2(j2 - j10) \\ &= (5 - j5)I_1 + (-j8)I_2 \end{aligned} \quad \dots(i)$$

Applying KVL in loop-2,

$$\begin{aligned} 10 \angle 90^\circ &= I_2(5 + j5 - j10) + I_1(j2 - j10) \\ 10 \angle 90^\circ &= I_2(5 - j5) + (-j8)I_1 \end{aligned} \quad \dots(ii)$$

Now adding equation (i) and (ii),

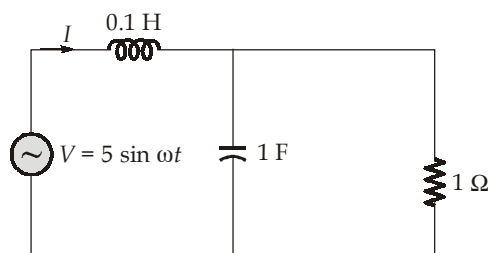
$$10 + j10 = I_1(5 - j13) + I_2(5 - j13)$$

$$I_1 + I_2 = \frac{10 + j10}{5 - j13}$$

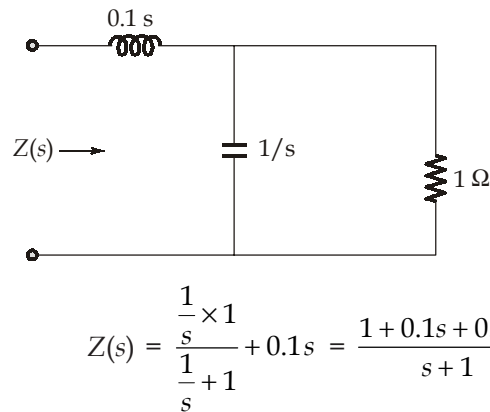
$$V_C = -jX_C(I_1 + I_2)$$

$$= -j10 \times \frac{10 + j10}{5 - j13} = 10.15 \angle 24^\circ \text{ V}$$

29. (c)



For V and I in phase imaginary part of $Z(s)$, should be zero,



multiplying numerator and denominator by $(s - 1)$

$$Z(s) = \frac{(0.1s^2 + 0.1s + 1)(s - 1)}{(s + 1)(s - 1)} = \frac{0.1s^3 + 0.1s^2 + s - 0.1s^2 - 0.1s - 1}{s^2 - 1}$$

Put $s = j\omega$

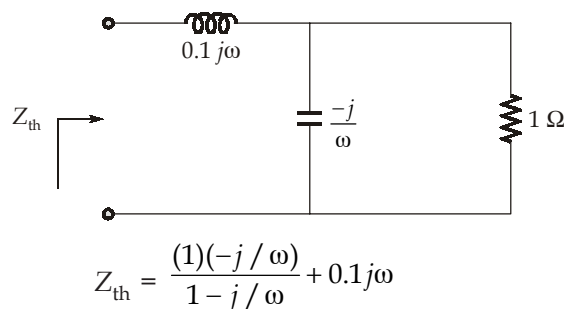
$$Z(j\omega) = \frac{0.1(j\omega)^3 + 0.9(j\omega) - 1}{(j\omega)^2 - 1} = \frac{j(0.9\omega - 0.1\omega^3) - 1}{-\omega^2 - 1}$$

Equating imaginary part to zero,

$$\begin{aligned} 0.9\omega - 0.1\omega^3 &= 0 \\ \omega^2 &= 9 \\ \omega &= \pm 3 \text{ rad/sec} \end{aligned}$$

Alternative Solution:

In frequency domain,



$$\Rightarrow \frac{j}{j - \omega} + 0.1j\omega = 0$$

$$\Rightarrow \frac{j(j + \omega)}{(j - \omega)(j + \omega)} + 0.1j\omega = 0$$

$$\Rightarrow \frac{1 - j\omega}{1 + \omega^2} + 0.1j\omega = 0$$

For V and I in phase, imaginary term = 0

$$\text{Thus, } \frac{-\omega}{1 + \omega^2} + 0.1\omega = 0$$

$$\Rightarrow \omega = 3 \text{ rad/s}$$

30. (c)

$$M = K\sqrt{L_1 L_2} = 0.5\sqrt{36}$$

$$= 3 \text{ H}$$

The total energy stored in the system,

$$W(t) = \frac{1}{2}L_1 [i_1(t)]^2 + \frac{1}{2}L_2 [i_2(t)]^2 - M[i_1(t)i_2(t)]$$

$$= \frac{1}{2} \times 4 [5 \cos(50t - 30^\circ)]^2 + \frac{1}{2} \times 9 [2 \cos(50t - 30^\circ)]^2$$

$$- 3 [5 \cos(50t - 30^\circ) \times 2 \cos(50t - 30^\circ)]$$

at $t = 0$,

$$W(t) = 28.5 \text{ J}$$

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