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REINFORCED CEMENT CONCRETE

CIVIL ENGINEERING

Date of Test : 07/08/2025

ANSWER KEY >

1. (c)	7. (c)	13. (b)	19. (a)	25. (c)
2. (c)	8. (b)	14. (a)	20. (a)	26. (d)
3. (b)	9. (d)	15. (d)	21. (c)	27. (d)
4. (a)	10. (d)	16. (c)	22. (b)	28. (a)
5. (b)	11. (a)	17. (a)	23. (d)	29. (a)
6. (b)	12. (c)	18. (d)	24. (d)	30. (b)

DETAILED EXPLANATIONS

1. (c)

As per IS 456:2000, the pH of water shall not be less than 6. Here water source having pH = 6 may also be used but pH = 7 is most suitable.

2. (c)

Case I : (D.L. + L.L.) combination

$$P_1 = 1 \times 60 + 1 \times 90 = 150 \text{ kN}$$

Case II : (D.L. + W.L. or E.L.) combination

As E.L. is more so take E.L. directly no need to check for WL

$$P_2 = 1 \times 60 + 150 \times 1 = 210 \text{ kN}$$

Case III: (D.L. + 0.8 (L.L.) + 0.8 (W.L. or E.Q.) combination

$$P_3 = 1 \times 60 + 0.8 \times 90 + 0.8 \times 150 = 252 \text{ kN}$$

So, design load for serviceability = 252 kN

3. (b)

$$\begin{aligned} \therefore E_c &= 5000\sqrt{f_{ck}} = 5000 \times \sqrt{25} \\ &= 25000 \text{ N/mm}^2 \\ &= 25 \text{ kN/mm}^2 \end{aligned}$$

As per Cl. 6.2.3.1 of **IS 456 : 2000**, the actual measured value may differ by $\pm 20\%$ from the above value.

$$\begin{aligned} \text{So, range} &= 0.8 \times 25 \text{ to } 1.2 \times 25 \\ &= 20 \text{ to } 30 \text{ kN/mm}^2 \end{aligned}$$

4. (a)

$$\begin{aligned} \text{Bearing strength for WSM} &= 0.25 \times f_{ck} && (\text{Cl. 34.4 of IS 456 : 2000}) \\ &= 0.25 \times 25 \\ &= 6.25 \text{ N/mm}^2 \end{aligned}$$

5. (b)

$$\begin{aligned} \text{B.M. at support next to the end support} &= \frac{1}{10} w_d L^2 + \frac{1}{9} \times w_l l^2 \quad (\text{Table 12 of IS 456 : 2000}) \\ &= \frac{1}{10} \times 6 \times 4.5^2 + \frac{1}{9} \times 3 \times 4.5^2 \\ &= 18.9 \text{ kN-m} \end{aligned}$$

6. (b)

Development length for HYSD bars in compression

$$\begin{aligned} L_d &= \frac{0.87 f_y \phi}{4 \tau_{bd} \times (1.6 \times 1.25)} \\ &= \frac{0.87 \times 415 \times 20}{4 \times 1.4 \times 1.6 \times 1.25} \\ &= 644.73 \text{ mm} \end{aligned}$$

7. (c)

In general, bond strength is enhanced when the following measures are adopted:

- (i) Deformed bars are used instead of plain bars.
- (ii) Smaller bar diameters are used.
- (iii) Higher grade of concrete is used.
- (iv) Increased cover is provided around each bar.
- (v) Increased length of embedment, bends and hooks are provided.
- (vi) Mechanical anchorages are employed.
- (vii) Stirrups with increased area, reduced spacing and/or higher grade of steel is used.

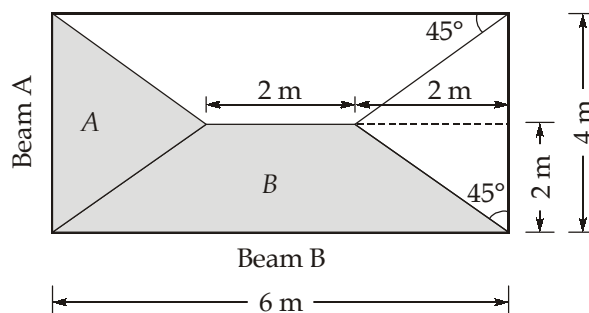
8. (b)

Creep increases when:

- Cement content is high
- Water cement ratio is high
- Aggregate content is low
- Air entrainment is high
- Relative humidity is low
- Temperature is high
- Loading occurs at an early age
- Loading sustained over a long period.

9. (d)

As per IS 456 : 2000, load distribution for a two way slab is given as



Load carried by beam A = Shaded area A

$$= \frac{1}{2} \times 4 \times 2 \times 10 = 40 \text{ kN}$$

$$\text{i.e., } \frac{40}{4} = 10 \text{ kN/m}$$

Load carried by beam B = Shaded area B

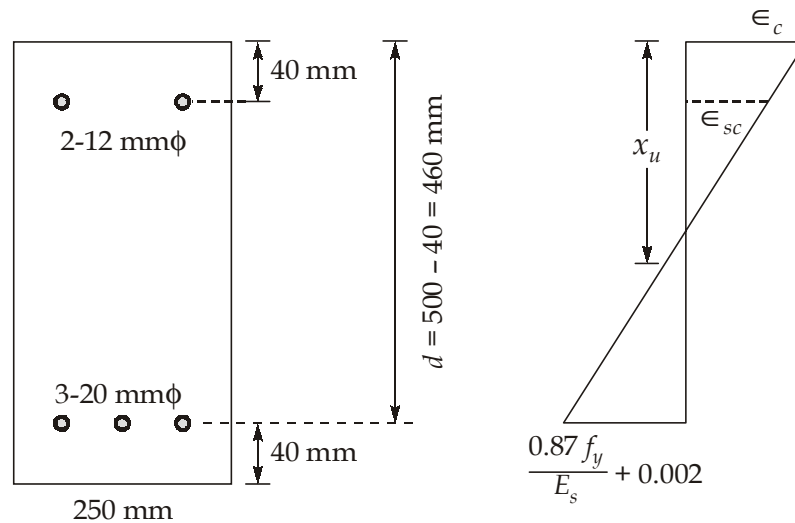
$$= \frac{1}{2} (6 + 2) \times 2 \times 10 = 80 \text{ kN}$$

$$\text{i.e., } \frac{80}{6} = 13.3 \text{ kN/m}$$

10. (d)

As per Cl. 26.2.5 of IS 456 : 2000, splices in flexural members should not be provided where bending moment is more than 50 percent of the moment of resistance.

11. (a)



$$A_{sc} = 2 \times \frac{\pi}{4} \times 12^2 = 226.19 \text{ mm}^2$$

$$A_{st} = 3 \times \frac{\pi}{4} \times 20^2 = 942.48 \text{ mm}^2$$

For Fe415, $x_{u,lim} = 0.48 \times d = 0.48 \times 460 = 220.8 \text{ mm}$

Actual depth of neutral axis can be computed as,

$$C = T$$

$$\Rightarrow 0.36 f_{ck} B x_u + (f_{sc} - 0.45 f_{ck}) A_{sc} = 0.87 f_y A_{st} \quad (\text{Assuming tension steel as yielded})$$

$$\Rightarrow 0.36 \times 20 \times 250 \times x_u + (345 - 0.45 \times 20) \times 226.19 = 0.87 \times 415 \times 942.48$$

$$\Rightarrow x_u = 146.82 \text{ mm} < x_{u,lim} (220.8 \text{ mm}) \Rightarrow \text{Under reinforced section}$$

\therefore Section is under reinforced, maximum strain in extreme concrete fibre 0.0035 will be

From similar triangle concrete

$$\frac{\epsilon_{sc}}{x_u - d_c} = \frac{0.0035}{x_u}$$

$$\epsilon_{sc} = \frac{0.0035}{146.82} \times (146.82 - 40) = 2.54 \times 10^{-3} \simeq 0.00255$$

12. (c)

$|\delta|$ = Downward defection due to UDL

- Upward defection due to pre-stressing force

$$\text{Deflection due to UDL } (\delta_1) = \frac{5}{384} \frac{wl^4}{E_c I_c}$$

$$E_c = 5000 \sqrt{f_{ck}} = 5000 \times \sqrt{35} \text{ N/mm}^2 = 29580.399 \text{ N/mm}^2$$

$$I_c = \frac{bd^3}{12} = \frac{500 \times 750^3}{12} = 1.758 \times 10^{10} \text{ mm}^4$$

$$\delta_1 = \frac{5}{384} \frac{wl^4}{E_c I_c} = \frac{5}{384} \times \frac{85(6000)^4}{(29580.399)(1.758 \times 10^{10})} = 2.76 \text{ mm } (\downarrow)$$

Upward deflection due to prestressing force

$$\begin{aligned}\delta_2 &= \frac{5}{48} \times \frac{Pe l^2}{E_c I_c} \\ &= \frac{5}{48} \times \frac{(1620 \times 10^3)(145)(6000)^2}{(29580.399)(1.758 \times 10^{10})} = 1.69 \text{ mm } (\uparrow)\end{aligned}$$

$$\therefore \delta = \delta_1 - \delta_2 = 2.76 - 1.69 = 1.07 \text{ mm } (\downarrow)$$

13. (b)

Column is fixed at one end and pinned at other end.

$$\begin{aligned}e_{\min} &= \frac{L_0}{500} + \frac{D}{30} \\ &= \frac{3200}{500} + \frac{400}{30} \\ &= 19.73 \text{ mm} < 0.050D = 20 \text{ mm} \quad (\text{OK})\end{aligned}$$

$$\therefore l_{\text{eff}} = 0.8 \times 3.2 = 2.56 \text{ m}$$

$$\lambda = \frac{256}{40} = 6.4 < 12$$

\therefore It is a short column

$$P_u = 0.4 f_{ck} A_c + 0.67 f_y A_{sc}$$

$$\Rightarrow 1200 \times 10^3 = 0.4 \times 20 \times \left[\frac{\pi}{4} \times 400^2 - A_{sc} \right] + 0.67 \times 415 \times A_{sc}$$

$$\Rightarrow 1200 \times 10^3 = 1005309.65 - 8A_{sc} + 278.05 A_{sc}$$

$$\Rightarrow A_{sc} = 720.94 \text{ mm}^2$$

Check: Minimum steel = 0.8% of gross area

$$= \frac{0.8}{100} \times \frac{\pi}{4} \times 400^2 = 1005.31 \text{ mm}^2 > A_{sc}$$

So provide $A_{sc} = 1005.31 \text{ mm}^2$

14. (a)

Given: $b = 200 \text{ mm}, d = 350 \text{ mm}$

$$\begin{aligned}\text{Pre-stressing force} &= 3 \times 60 \times 1100 \times 10^{-3} \text{ kN} \\ &= 198 \text{ kN}\end{aligned}$$

Eccentricity, $e = \frac{350}{2} - 90 = 85 \text{ mm}$

$$m = 6$$

$$\begin{aligned}\text{Stress at the level of tendons} &= \frac{P}{A} + \frac{Pe^2}{I} \\ &= \frac{198 \times 10^3}{200 \times 350} + \frac{198 \times 10^3 \times 85^2}{\frac{200 \times 350^3}{12}} = 2.83 + 2.00 = 4.83 \text{ N/mm}^2\end{aligned}$$

$$\begin{aligned}\text{Loss of stress due to elastic deformation} &= m.f_c \\ &= 6 \times 4.83 = 28.98 \text{ N/mm}^2\end{aligned}$$

$$\text{Loss of prestressing force} = \frac{28.98 \times 3 \times 60}{1000} \text{ kN} = 5.22 \text{ kN} \approx 5.2 \text{ kN}$$

15. (d)

For axially loaded column,

$$\begin{aligned}e_{\min} &= \max \left\{ \frac{L}{500} + \frac{B \text{ or } D}{30} < 0.05 (B \text{ or } D) \right. \\ &\quad \left. 20 \text{ mm} \right\} \\ &= \max \left\{ \frac{3000}{500} + \frac{400}{30} = 19.33 < 0.05 (B \text{ or } D) = 20 \text{ mm} \right. \\ &\quad \left. 20 \text{ mm} \right\}\end{aligned}$$

 \therefore

$$P_u = 0.4 f_{ck} A_c + 0.67 f_y A_{sc}$$

$$P_v = 0.4 f_{ck} [A_g - A_{sc}] + 0.67 f_y A_{sc}$$

where

 A_c = Area of concrete A_g = Gross area of column A_{sc} = Area of compression steel

$$1650 \times 10^3 = 0.4 \times 20 [400^2 - A_{sc}] + 0.67 (500) A_{sc}$$

$$1650 \times 10^3 = 1280000 - 8 A_{sc} + 335 A_{sc}$$

$$A_{sc} = 1131.498 \text{ mm}^2 \approx 1131.50 \text{ mm}^2$$

But as per IS 456, $(A_{sc})_{\min} = 0.8\%$ of cross-sectional area

$$= \frac{0.8}{100} \times 400^2 = 1280 \text{ mm}^2$$

 \therefore

$$A_{sc} = 1280 \text{ mm}^2$$

16. (c)

Let,

 A_c = Area of concrete

$$\frac{75}{500} = \frac{y}{500 - x_u}$$

 \Rightarrow

$$y = 75 \left(\frac{500 - x_u}{500} \right)$$

Width of section at neutral axis i.e., $b_{NA} = 250 + 2y$

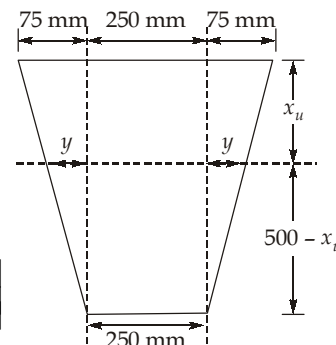
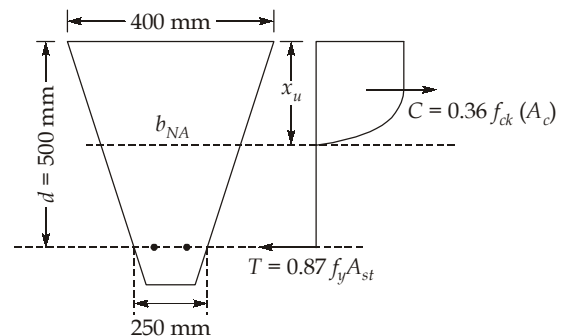
$$b_{NA} = 250 + 150 \left(\frac{500 - x_u}{500} \right)$$

Average width of beam section is compression

$$= \frac{1}{2} (400 + b_{NA})$$

$$= \frac{1}{2} \left[650 + 150 \left(\frac{500 - x_u}{500} \right) \right]$$

$$= (400 - 0.15x_u)$$

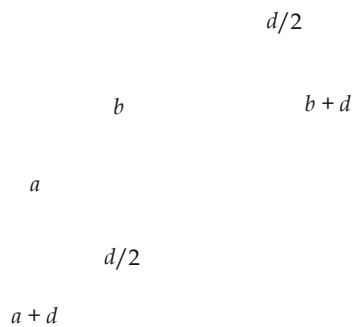


$$\begin{aligned}
 C &= T \\
 \Rightarrow 0.36 f_{ck} b_{avg} x_u &= 0.87 f_y A_{st} \\
 \Rightarrow 0.36 \times 25 \times (400 - 0.15x_u)x_u &= 531826.65 \\
 \Rightarrow x_u^2 - 2666.7 x_u + 393945.67 &= 0 \\
 \therefore x_u &= 157 \text{ mm} = 15.7 \text{ cm}
 \end{aligned}$$

17. (a)

$$(\tau_{ve})_{\text{developed}} = \frac{P_o - w_o [(a+b)(b+d)]}{2(a+d+b+d) \times d}$$

\therefore Critical section for two way shear will be at $\frac{d}{2}$ distance from column face



$$\begin{aligned}
 (\tau_{ve})_{\text{developed}} &= \frac{1300 - 205 [(0.4 + 0.75)(0.5 + 0.75)]}{2 [0.75 \times (0.4 + 0.75 + 0.5 + 0.75)]} \text{ kN/m}^2 \\
 &= 0.279 \text{ N/mm}^2 \simeq 0.28 \text{ N/mm}^2
 \end{aligned}$$

18. (d)

$$P_L = P_o [kx + \mu \alpha]$$

$$\alpha = \frac{4h}{l}$$

$$\tan \alpha = \frac{4 \times 250}{12000} = 0.0833 \quad (\therefore \alpha = 4.76^\circ = 0.0831 \text{ radian})$$

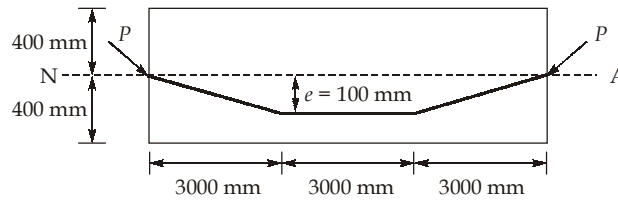
Given, $k = 0.15 \text{ per } 1000 \text{ m} = \frac{0.15}{1000} \text{ per m}$

$x = 6.0 \text{ m}$ {as loss is asked at mid-span of beam}

$$\therefore P_L = 1200 \left[\frac{0.15}{1000} \times 6.0 + 0.35 \times 0.0831 \right]$$

$$\Rightarrow P_L = 35.982 \text{ kN} \simeq 36 \text{ kN}$$

19. (a)



The given trapezoidal cable profile of prestressing wire reflects the bending moment diagram due to the two point loads.

Given: $Q = 40 \text{ kN}$, $e = 100 \text{ mm}$
 $L = 9 \text{ m}$
 $P = \text{Prestressing force}$

For balancing the bending effect,

$$P \times e = \frac{QL}{3}$$

$$\Rightarrow P \times 100 = \frac{40 \times 10^3 \times 9000}{3}$$

$$\Rightarrow P = 1200 \text{ kN}$$

20. (a)

Loss of stress due to creep = $\epsilon_{cc} f_c E_s$

where, $f_c = f_{c1} + \frac{2}{3}(f_{c2} - f_{c1})$

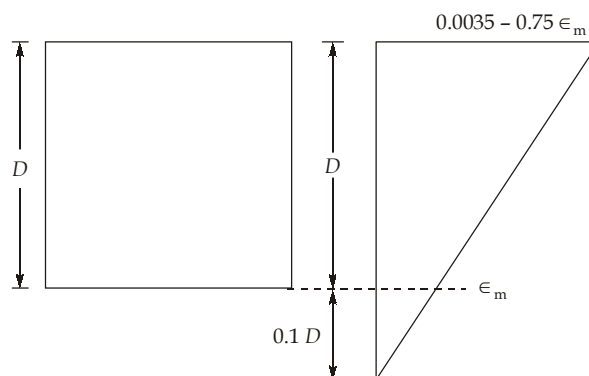
$$f_{c1} = 8 \text{ MPa}$$

$$f_{c2} = 14 \text{ MPa}$$

$$\therefore f_c = 8 + \frac{2}{3}(14 - 8) = 8 + \frac{2}{3} \times 6 = 12 \text{ MPa}$$

$$\therefore \text{Loss of stress} = 30 \times 10^{-6} \times 12 \times 210 \times 10^3 = 75.6 \text{ MPa}$$

21. (c)



$$\frac{0.0035 - 0.75 \epsilon_m}{1.1D} = \frac{\epsilon_m}{0.1D}$$

$$\Rightarrow 11.75 \epsilon_m = 0.0035$$

$$\Rightarrow \epsilon_m = \frac{0.0035}{11.75}$$

∴ Strain in extreme compression fibre,

$$\epsilon = 0.0035 - 0.75 \epsilon_m$$

$$\Rightarrow \epsilon = 0.0035 - 0.75 \times \frac{0.0035}{11.75}$$

$$\Rightarrow \epsilon = 0.003276596$$

$$\Rightarrow \epsilon = 3276.596 \mu$$

22. (b)

$$V_u = 80 \times 10^3 \text{ kN}$$

$$P_t = \frac{100 \times 4 \times \frac{\pi}{4} \times 12^2}{250 \times 400} = 0.452\%$$

Using the table to get τ_c corresponding to

$$P_t = 0.452\%$$

$$\frac{0.48 - 0.36}{0.5 - 0.25} = \frac{0.48 - x}{0.5 - 0.452}$$

$$\Rightarrow x = \tau_c = 0.457 \text{ MPa}$$

$$\tau_v = \frac{80 \times 10^3}{250 \times 400} = 0.8 \text{ MPa}$$

We see that

$$\tau_c < \tau_v$$

∴

$$\begin{aligned} V_{us} &= V_u - \tau_c b d \\ &= 80 \times 10^3 - 0.457 \times 250 \times 400 = 34300 \text{ N} \end{aligned}$$

Since vertical stirrups,

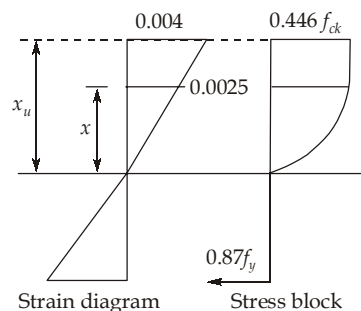
$$S_v = \frac{0.87 f_y A_{sv} d}{V_{us}}$$

$$\therefore 280 = \frac{0.87 \times 250 \times 2 \times \frac{\pi}{4} \phi^2 \times 400}{34300}$$

$$\Rightarrow \phi = 8.38$$

Let us provide 10 mm dia. stirrups.

23. (d)



From strain diagram,

$$\frac{0.004}{x_u} = \frac{0.0025}{x}$$

$$\Rightarrow x = \frac{0.0025}{0.004} x_u$$

$$\Rightarrow x = \frac{5}{8} x_u$$

∴ Total compressive force,

$$C = C_{\text{linear}} + C_{\text{parabolic}}$$

$$\Rightarrow C = 0.446 f_{ck} \times (x_u - x) \times b + \frac{2}{3} \times 0.446 f_{ck} \times x \times b$$

$$\Rightarrow C = 0.446 f_{ck} \left(x_u - \frac{5}{8} x_u \right) \times b + 0.185 f_{ck} b \left(\frac{5}{8} x_u \right)$$

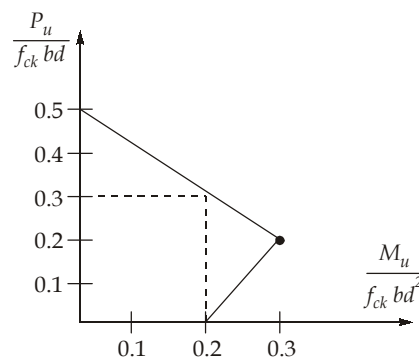
$$\Rightarrow C = 0.167 f_{ck} b x_u + 0.185 f_{ck} b x_u$$

$$\Rightarrow C = 0.352 f_{ck} b x_u = 0.352 \times 25 \times b x_u$$

$$\Rightarrow C = 8.8 b x_u$$

24. (d)

$$\frac{P_u}{f_{ck} b d} = \frac{540 \times 10^3 \text{ N}}{20 \times 300 \times 300} = 0.3$$



For $\frac{P_u}{f_{ck} b d} = 0.3$, $\frac{M_u}{f_{ck} b d^2} = 0.2$ from interaction curve diagram

Hence,

$$M_u = 0.2 \times 20 \times 300 \times 300^2 \text{ Nmm}$$

$$= 108 \text{ kNm}$$

25. (c)

Determining the depth of N.A.

Let N.A. lies in the flange i.e.

$$x_u \leq D_f$$

$$\therefore C = T$$

$$\Rightarrow 0.36 f_{ck} b x_u = 0.87 f_y A_{st}$$

$$\Rightarrow x_u = \frac{0.87 \times 415 \times 4 \times \frac{\pi}{4} \times 20^2}{0.36 \times 20 \times 800}$$

$$= 78.77 \text{ mm} \leq D_f (= 80 \text{ mm})$$

Hence, N.A. lies in flange

For Fe415, $x_{u,lim} = 0.48 \times 400 = 192 \text{ mm} > x_u (= 78.77 \text{ mm})$ OK

So, section is underreinforced

$$\begin{aligned}\therefore \text{MOR} &= 0.87 f_y A_{st} (d - 0.42 x_u) \\ &= 0.87 \times 415 \times 4 \times \frac{\pi}{4} \times 20^2 \times (400 - 0.42 \times 78.77) \text{ Nmm} \\ &= 166.47 \text{ kNm}\end{aligned}$$

26. (d)

$$\text{Initial stress in wires} = \frac{300 \times 10^3 \text{ N}}{200 \text{ mm}^2} = 1500 \text{ N/mm}^2$$

$$\text{For post tensioned beam, total residual shrinkage strain} = \frac{2 \times 10^{-4}}{\log(t+2)} = \frac{2 \times 10^{-4}}{\log(18+2)} = 1.537 \times 10^{-4}$$

$$\text{Loss of stress} = 210 \times 10^3 \times 1.537 \times 10^{-4} = 32.277 \text{ MPa}$$

$$\text{Percentage loss of stress} = \frac{32.277}{1500} \times 100 = 2.15\%$$

27. (d)

28. (a)

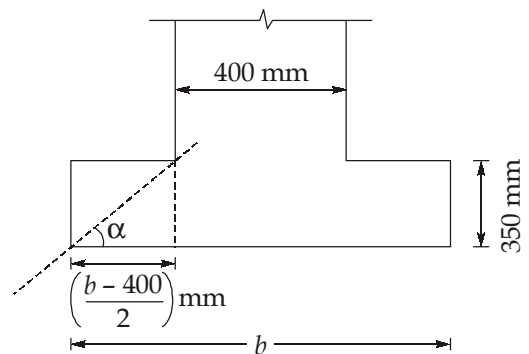
Fundamental time period of vibration as per Cl. 7.6.2 (c) of IS 1893 : 2016 (part-I) is.

$$T = \frac{0.09H}{\sqrt{D}} \quad (\text{Here, } H = 70 \text{ m, } D = 16 \text{ m in short direction})$$

$$\Rightarrow T = \frac{0.09 \times 70}{\sqrt{16}} = 1.575 \text{ sec} \approx 1.6 \text{ sec}$$

29. (a)

$$\begin{aligned}\tan \alpha &\leq 0.9 \sqrt{\frac{100 \times q_0}{f_{ck}} + 1} \\ \Rightarrow \frac{350}{\frac{b-400}{2}} &\leq 0.9 \sqrt{\frac{100 \times 6}{25} + 1} \\ \Rightarrow \frac{700}{b-400} &\leq 4.5 \\ \Rightarrow 155.56 &\leq b - 400 \\ \Rightarrow b &\leq 555.56 \text{ mm}\end{aligned}$$



30. (b)

The maximum strain in concrete at outermost compression fibre is flexural compression is 0.0035.

