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MACHINE DESIGN

MECHANICAL ENGINEERING

Date of Test : 15/07/2025

ANSWER KEY ➤

- | | | | | |
|--------|---------|---------|---------|---------|
| 1. (d) | 7. (a) | 13. (d) | 19. (c) | 25. (c) |
| 2. (d) | 8. (b) | 14. (c) | 20. (a) | 26. (a) |
| 3. (b) | 9. (c) | 15. (c) | 21. (d) | 27. (a) |
| 4. (c) | 10. (d) | 16. (a) | 22. (c) | 28. (d) |
| 5. (a) | 11. (d) | 17. (b) | 23. (c) | 29. (b) |
| 6. (c) | 12. (d) | 18. (c) | 24. (c) | 30. (d) |

DETAILED EXPLANATIONS

1. (d)

$$k_a = 0.79, k_b = 0.85, k_c = 0.897$$

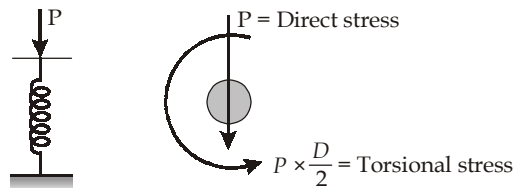
$$k_d = \frac{1}{k_f} = \frac{1}{1.5} = 0.67, S_e = 320 \text{ MPa}$$

So,

$$S_e' = k_a k_b k_c k_d S_e$$

$$S_e' = 129.14 \text{ MPa}$$

2. (d)



3. (b)

$$k_b = 1.5, k_t = 2$$

$$M_b = 500 \text{ kN-m}, M_t = 400 \text{ kN-m}$$

$$\text{Equivalent torsional moment, } (T_e) = \sqrt{(k_b M_b)^2 + (k_t M_t)^2}$$

$$T_e = \sqrt{(1.5 \times 500)^2 + (2 \times 400)^2}$$

$$T_e = 1096.58 \text{ kN-m}$$

4. (c)

$$P = \frac{W}{l \times d}$$

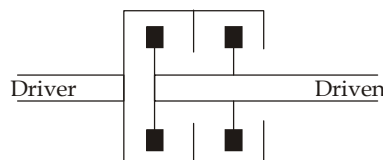
$$W = \frac{2 \times 10^6 \times 0.075 \times 0.12}{1000} = 18 \text{ kN}$$

$$H = f \times W \times v$$

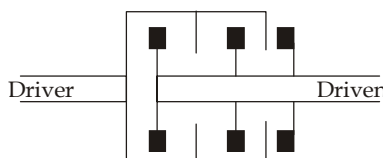
$$H = \frac{0.03 \times 18 \times 10^3 \times (\pi \times 0.075 \times 1200)}{60 \times 1000} = 2.545 \text{ kW}$$

5. (a)

For 3 driver and 2 driven disks we will have $(3 + 2 - 1) = 4$ contact surfaces.



For 3 driver and 3 driven disks we will have $(3 + 3 - 1) = 5$ contact surfaces.



So, torque transmission capacity would increase by $\frac{5-4}{4} \times 100 = 25\%$.

6. (c)

$$\begin{aligned} \text{Bending stress, } \sigma &= \frac{M}{\pi \times r^2 \times t} \\ 140 &= \frac{2486}{\pi \times t \times 25^2} \\ t &= 9.04 \times 10^{-3} \text{ m} \\ t &= 9.04 \text{ mm} \end{aligned}$$

$$\begin{aligned} \text{Size of weld, } h &= \frac{t}{0.707} \\ h &= 12.786 \text{ mm} \\ h &\simeq 13 \text{ mm} \end{aligned}$$

7. (a)

The result came from guest's theory and hencky, both are suitable for ductile material but hencky's results are safer and more economical.

8. (b)

9. (c)

$$\begin{aligned} \sigma_1 &= 360 \text{ MPa} \\ \sigma_2 &= 140 \text{ MPa} \\ \sigma_{\text{eff}} &= \sqrt{\sigma_1^2 - \sigma_1 \sigma_2 + \sigma_2^2} \\ &= \sqrt{(360)^2 - 140 \times 360 + 140^2} \\ \sigma_{\text{eff}} &= 314.32 \text{ MPa} \end{aligned}$$

10. (d)

$$\begin{aligned} \sigma_1 &= -200 \text{ MPa} \\ \sigma_2 &= -150 \text{ MPa} \\ \sigma_3 &= 0 \\ \tau_{\text{max}} &= \frac{S_{yt}}{2 \times \text{FOS}} \\ \tau_{\text{per}} &= \text{maximum of } \left\{ \left| \frac{\sigma_1 - \sigma_2}{2} \right|, \left| \frac{\sigma_2 - \sigma_3}{2} \right|, \left| \frac{\sigma_3 - \sigma_1}{2} \right| \right\} \\ &= \left| \frac{-200 - (-150)}{2} \right| = 25 = \left| \frac{-150 - 0}{2} \right| = 75 \\ &= \frac{0 - (-200)}{2} = 100 \\ \frac{S_{yt}}{\text{FOS}} &= 2 \times 100 \\ \text{FOS} &= \frac{S_{yt}}{200} = \frac{430}{200} = 2.15 \end{aligned}$$

11. (d)

$$\text{Corrected endurance limit, } S_e' = \frac{S_e}{K_f}$$

$$K_f = 2.2$$

$$S_e' = 66.3636 \text{ MPa}$$

$$\text{So, } \sigma_a = \frac{S_e'}{FOS} = \frac{66.3636}{2} = 33.1818 \text{ MPa} \quad (\text{where factor of safety is 2})$$

$$\text{So, } \sigma_a = \frac{P}{(50t)}$$

$$t = \frac{P}{50\sigma_a} = \frac{50 \times 10^3}{50 \times 33.1818} = 30.137 \text{ mm}$$

$$t_{\min} = 31 \text{ mm}$$

12. (d)

$$\text{Shear stress, } \tau = \frac{P}{2A}$$

$$A = \frac{\pi}{4} \times d^2$$

$$\tau = \frac{4P}{2 \times \pi d^2}$$

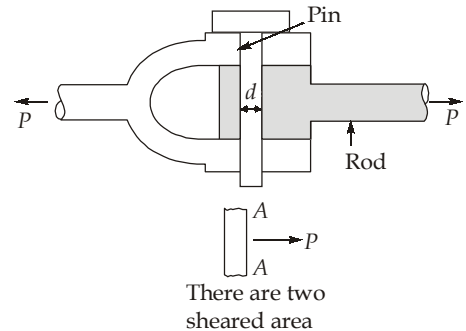
According to distortion energy theory, $\tau_{\max} = 0.577 S_{yt}$
(where S_{yt} is 380 MPa)

$$\tau_{\max} = 219.26 \text{ N/mm}^2$$

$$\text{Now, } \tau \leq \frac{\tau_{\max}}{N}$$

$$\frac{4 \times 25 \times 10^3}{2 \times \pi \times d^2} \leq \frac{219.26}{2.5}$$

$$d \geq 13.471 \text{ mm}$$



13. (d)

$$A = [3, \log_{10}(0.9 \times 650)]$$

$$= (3, 2.7671)$$

$$B = [6, \log_{10}(300)]$$

$$= (6, 2.4771)$$

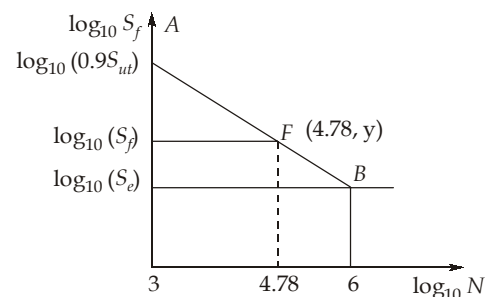
$$F = [\log_{10}(60000), y] = (4.78, y)$$

Equation of AB

$$(y - 2.7671) = \frac{(2.4771 - 2.7671)(4.78 - 3)}{6 - 3}$$

$$y = 2.595$$

$$S_f = 393.58 \text{ MPa}$$



14. (c)

$$\text{Mean force, } F_m = \frac{F_{\max} + F_{\min}}{2} = \frac{(25.2 + 10.8)}{2} = 18 \text{ N}$$

$$\text{Alternating force, } F_a = \frac{F_{\max} - F_{\min}}{2} = \frac{(25.2 - 10.8)}{2} = 7.2 \text{ N}$$

$$\text{Moment of inertia, } I = \frac{bh^3}{12} = \frac{1}{12} \times (1.25) \times (0.16)^3 \text{ cm}^4 = 4.27 \times 10^{-12} \text{ m}^4$$

$$\sigma_m = \frac{M_m \times y}{I} = \frac{F_m L \times y}{I} = \frac{18 \times 6 \times 0.08 \times 10^{-4}}{4.27 \times 10^{-12} \times 10^6} = 202.34 \text{ MPa}$$

$$\sigma_a = \frac{M_a \times y}{I} = \frac{F_a L \times y}{I} = \frac{7.2 \times 6 \times 0.08 \times 10^{-4}}{4.27 \times 10^{-12} \times 10^6} = 80.937 \text{ MPa}$$

Goodman eq.

$$\frac{1}{N} = \frac{\sigma_a}{S_e} + \frac{\sigma_m}{S_{ut}} = \frac{80.937}{229} + \frac{202.34}{595}$$

$$N = 1.44$$

15. (c)

$$\sigma_t = \frac{S_{ut}}{f_s} = \frac{300}{2.5} = 120 \text{ N/mm}^2$$

Tensile stress due to axial load of 15 kN will be

$$\sigma_a = \frac{P}{A} = \frac{15000}{t \times 5t} = \frac{3000}{t^2} \text{ N/mm}^2$$

Tensile stress due to moment of (15 kN × 7.5t) will be

$$\sigma_b = \frac{P \times y}{I} = \frac{15000 \times 7.5t \times 2.5t}{\frac{1}{12}(t)(5t)^3} = \frac{27000}{t^2} \text{ N/mm}^2$$

So, total tensile stress at the crosssection is

$$\sigma = \sigma_a + \sigma_b = \frac{30000}{t^2}$$

$$120 = \frac{30000}{t^2}$$

$$t = 15.81 \text{ mm}$$

16. (a)

$$P_1 = 55 \text{ MPa, Principal stress}$$

$$\sigma_{ut} = 150 \text{ MPa, } \sigma_{uc} = -500 \text{ MPa}$$

Mohr's theory used for materials which have different compressive and tensile strength like cast iron.

Governing equation, by Mohr's theory,

$$\frac{P_1}{\sigma_{ut}} + \frac{P_2}{\sigma_{uc}} = 1$$

$$\frac{55}{150} + \frac{P_2}{-500} = 1$$

$$P_2 = -316.67 \text{ MPa}$$

17. (b)

$$d = 6\sqrt{t} = 6\sqrt{30} = 32.863 \text{ mm}$$

Shear strength of one rivet

$$P_s = 1.875 \left(\frac{\pi}{4} \times d^2 \tau \right)$$

$$P_s = 95423.824 \text{ N}$$

Crushing strength of one rivet = $(dt) \cdot \sigma_c$

$$(P_c) = 32.863 \times 30 \times 120 = 118306.8 \text{ N}$$

Tensile strength of the plate in outer row

$$P_t = (w - d) \times t \times \sigma_t = (250 - 32.863) \times 30 \times 80 = 521128.8 \text{ N}$$

$$\therefore P_s < P_c$$

$$\therefore 521128.8 = n \times 95423.824$$

$$n = 5.46$$

$$n \approx 6$$

18. (c)

$$D = 0.2 \text{ m}, \quad d = 0.15 \text{ m}$$

$$\mu = 0.2, \quad 2\alpha = 30^\circ$$

$$\alpha = 15^\circ$$

$$P = P_{\max} = 0.1 \text{ N/mm}^2$$

$$= 0.1 \text{ MPa}$$

$$\begin{aligned} \text{We know that, } M_t &= \frac{\mu \times \pi \times P}{\sin \alpha \times 12} (D^3 - d^3) = \frac{0.2 \times \pi \times 0.1 (200^3 - 150^3)}{\sin 15^\circ \times 12 \times 1000} \\ &= 93.565 \text{ N-m} = 93.565 \times 1000 \text{ N-mm} = \frac{93.565 \times 1000}{1000} \text{ kN-mm} \end{aligned}$$

$$M_t = 93.565 \text{ kN-mm}$$

19. (c)

$$\text{Given, } (L_{80})_1 = 380 \text{ MR}$$

$$(P_e)_1 = 12 \text{ kN}$$

We know that,

$$L_{80} = 1.90 L_{90}$$

$$(L_{90})_1 = \frac{(L_{80})_1}{1.90} = \frac{380}{1.90} = 200 \text{ MR}$$

Rated life of bearing is bearing life with 90% reliability

$$L_{90} \propto \left(\frac{1}{P_e} \right)^3$$

$$\frac{(L_{90})_1}{(L_{90})_2} = \left[\frac{(P_e)_2}{(P_e)_1} \right]^3$$

$$\frac{(L_{90})_1}{(L_{90})_2} = (2)^3$$

$$(L_{90})_2 = \frac{200}{8} = 25 \text{ MR}$$

$$\therefore \frac{L_{80}}{L_{90}} = \left[\frac{\ln(1/0.8)}{\ln(1/0.9)} \right]^{1/1.17}$$

$$\therefore (P_e)_2 = 2(P_e)_1$$

20. (a)

$$\text{Sommerfeld number, } S = \left(\frac{D}{C} \right)^2 \frac{Zn}{P}$$

$$\text{Pressure, } P = \frac{W}{LD} = \frac{5 \times 10^3}{0.05 \times 0.05} = 2 \times 10^6 \text{ Pa}$$

$$Z = \frac{11.62}{100} \times \frac{1}{10} = 0.01162 \text{ Ns/m}^2$$

$$\text{So, } S = \left(\frac{0.05}{50 \times 10^{-6}} \right)^2 \times \frac{0.01162 \times 1000}{60 \times 2 \times 10^6}$$

$$S = 0.096833$$

21. (d)

As per St. Venant's theory (maximum principal strain theory)

$$(\sigma_1 - \mu\sigma_2) \leq \left(\frac{\sigma_{yt}}{\text{F.O.S.}} \right)$$

Von-mises and hencky's theory (maximum distortion energy theory)

$$\sigma_1^2 + \sigma_2^2 - \sigma_1\sigma_2 \leq \left(\frac{\sigma_{yt}}{\text{F.O.S.}} \right)^2$$

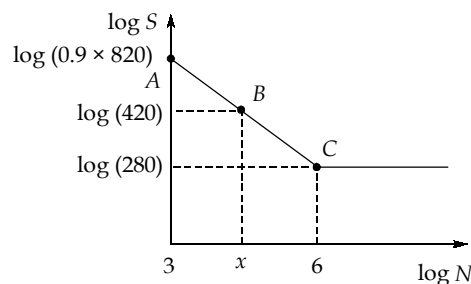
Rankine theory (maximum principal stress theory)

$$\sigma_1 \leq \left(\frac{\sigma_{yt}}{\text{F.O.S.}} \right)$$

Haigh's theory (Total strain energy theory)

$$\sigma_1^2 + \sigma_2^2 - 2\mu\sigma_1\sigma_2 \leq \left(\frac{\sigma_{yt}}{\text{F.O.S.}} \right)^2$$

22. (c)



Since ABC is a straight line, so slope of AC = slope of BC

$$\frac{\log(0.9 \times 820) - \log(280)}{3 - 6} = \frac{\log(420) - \log(280)}{x - 6}$$

$$x = 4.7448$$

$$\log N = 4.7448 \Rightarrow N = 55576.32 \text{ cycles}$$

23. (c)

24. (c)

Shaft is under pure torsion, so

$$\sigma_1 = -\sigma_2 = \frac{16T}{\pi d^3}$$

$$\sigma_1 = \frac{16 \times 95 \times 10^3}{\pi d^3} = \frac{483.831 \times 10^3}{d^3}$$

So,
$$\sigma_2 = \frac{-483.831 \times 10^3}{d^3}$$

As per M.D.E.T.

$$\sigma_1^2 + \sigma_2^2 - \sigma_1 \sigma_2 \leq \left(\frac{\sigma_{yt}}{\text{F.O.S.}} \right)^2$$

$$\sigma_1^2 + (-\sigma_1)^2 - \sigma_1 \times (-\sigma_2) \leq \left(\frac{\sigma_{yt}}{\text{F.O.S.}} \right)^2$$

$$3\sigma_1^2 \leq \left(\frac{\sigma_{yt}}{\text{F.O.S.}} \right)^2$$

$$3 \left(\frac{483.831 \times 10^3}{d^3} \right)^2 \leq \left(\frac{240}{2} \right)^2$$

$$d \geq 19.11 \text{ mm} \simeq 20 \text{ mm}$$

25. (c)

$$(M_b)_{\max} = 150 \times 100 = 15000 \text{ Nmm}$$

$$(M_b)_{\min} = -50 \times 100 = -5000 \text{ Nmm}$$

$$\begin{aligned} (M_b)_m &= \frac{1}{2} [(M_b)_{\max} + (M_b)_{\min}] = \frac{1}{2} [15000 + (-5000)] \\ &= 5000 \text{ Nmm} \end{aligned}$$

$$\begin{aligned} (M_b)_a &= \frac{1}{2} [(M_b)_{\max} - (M_b)_{\min}] = \frac{1}{2} [15000 - (-5000)] \\ &= 10000 \text{ Nmm} \end{aligned}$$

Based on soderberg criterion,

$$\frac{\sigma_a}{S_e} + \frac{\sigma_m}{S_{yt}} = 1$$

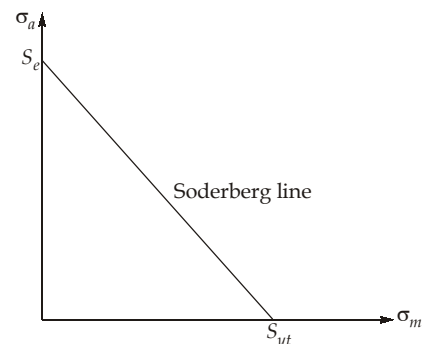
$$\sigma = \frac{32M_b}{\pi d^3}$$

$$\frac{32(M_b)_a}{\pi d^3 \times 125} + \frac{32(M_b)_m}{\pi d^3 \times 380} = 1$$

$$\frac{32 \times 10000}{\pi d^3 \times 125} + \frac{32 \times 5000}{\pi d^3 \times 380} = 1$$

$$814.8733 + 134.0252 = d^3$$

$$d = 9.82 \text{ mm}$$



26. (a)

$$\begin{aligned}\tau &= 0.75 (S_{ut}) \\ &= 0.75 \times 1350 \\ \tau &= 1012.5 \text{ MPa}\end{aligned}$$

Shear stress correction factor,

$$k_s = \left(1 + \frac{0.5}{C}\right) \quad \left[C = \frac{D}{d}\right]$$

$$\begin{aligned}k_s &= 1 + \frac{0.5}{5} \quad [C = 5] \\ &= 1.1\end{aligned}$$

$$\tau = k_s \frac{8PC}{\pi d^2}$$

$$1012.5 = 1.1 \times \frac{8 \times (498) \times (5)}{\pi d^2}$$

$$d = 2.62 \approx 3 \text{ mm}$$

$$D = 3 \times 5 = 15 \text{ mm}$$

Actual spring rate

$$k_{\text{actual}} = \frac{Gd^4}{8D^3N} = \frac{75750 \times 3^4}{8 \times 15^3 \times 38} = 5.98 \text{ N/mm}$$

27. (a)

$$\tau = \frac{M_t}{2\pi r^2}$$

$$140 = \frac{2500 \times 1000}{2\pi \times t(25)^2}$$

$$t = 4.55 \text{ mm}$$

$$\text{Size of weld, } h = \frac{t}{0.707} = 6.43 \text{ mm}$$

$$h = 7 \text{ mm}$$

28. (d)

$$C = 22 \text{ kN}$$

$$F_{\text{max radial}} = Pe$$

$$L_{90} = \left[\frac{C}{Pe}\right]^3$$

$$L_{90} = 2000 \times 60 \times 600$$

$$L_{90} = 72 \times 10^6 \text{ revolution}$$

$$72 = \left[\frac{22}{Pe}\right]^3$$

$$Pe = 5.29 \text{ kN}$$

29. (b)

$$\begin{aligned}\text{Beam strength } S_b &= \sigma_b b m Y \\ &= \sigma_b \times 36 \times 3 \times 0.3 \\ d_g &= m \times t_g = 3 \times 16 = 48 \text{ mm} \\ M_t &= \frac{3 \times 1000}{2\pi \times 20} \text{ N-m} \\ M_t &= \frac{3 \times 10^3}{2\pi \times 20} \times 10^3 \text{ N-mm} \\ &= 23873.241 \text{ N-mm}\end{aligned}$$

Tangential force due to torque,

$$\begin{aligned}P_t &= \frac{2 \times 23873.241}{48} = 994.718 \text{ N} \\ P_{\text{eff}} &= P_t \times C_V = 994.718 \times 1.5 \\ &= 1492.0775 \text{ N} \\ 1492.0775 &= \sigma_b \times 36 \times 3 \times 0.3 \\ \sigma_b &= 46 \text{ MPa}\end{aligned}$$

30. (d)

$$\begin{aligned}E &= \frac{1}{2} m k^2 (\omega_1^2 - \omega_2^2) \\ \omega_1 &= \frac{2\pi N_1}{60} = \frac{2\pi \times 350}{60} = 36.65 \text{ rad/sec} \\ \omega_2 &= 0 \\ m &= \frac{\pi}{4} d^2 \times t \times \rho = \frac{\pi}{4} \times (1^2) \times 0.2 \times 7200 = 1130.97 \text{ kg}\end{aligned}$$

Radius of gyration (k) of a solid disk about its axis of rotation is $\left(\frac{d}{\sqrt{8}}\right)$

$$\begin{aligned}k &= \frac{d}{\sqrt{8}} \\ k &= \frac{1}{\sqrt{8}} \\ \Rightarrow k^2 &= \frac{1}{8} \\ E &= \frac{1}{2} \times (1130.97) \times \frac{1}{8} \times (36.65)^2 \\ E &= 94.946 \text{ kJ}\end{aligned}$$

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