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INDUSTRIAL ENGINEERING

MECHANICAL ENGINEERING

Date of Test : 22/03/2025

ANSWER KEY ➤

- | | | | | |
|--------|---------|---------|---------|---------|
| 1. (a) | 7. (c) | 13. (b) | 19. (b) | 25. (a) |
| 2. (c) | 8. (d) | 14. (a) | 20. (a) | 26. (c) |
| 3. (c) | 9. (c) | 15. (b) | 21. (a) | 27. (b) |
| 4. (b) | 10. (b) | 16. (a) | 22. (a) | 28. (c) |
| 5. (a) | 11. (a) | 17. (b) | 23. (c) | 29. (c) |
| 6. (a) | 12. (c) | 18. (b) | 24. (a) | 30. (c) |

DETAILED EXPLANATIONS

1. (a)

$$\lambda = 0.01 \text{ per hour}$$

$$T = 150 \text{ hours}$$

$$R = \exp(-\lambda t) = e^{(-0.01 \times 150)} = 0.223130 = 22.31\%$$

2. (c)

$$p_a = 0.5034$$

$$p' = 0.01$$

$$\begin{aligned} \text{AOQ} &= 0.5034 \times 0.01 \times \left(\frac{1000 - 25}{1000} \right) \\ &= 0.490815 \times 10^{-2} \\ &= 0.491\% \end{aligned}$$

3. (c)

4. (b)

$$\text{Cost saving after Value engineering} = 1950 - 1660 = 290$$

$$\text{Annual saving} = 1320 \times 290 = 382800$$

5. (a)

$$\begin{aligned} \text{Incremental cost per day} &= \frac{\text{Crash cost} - \text{Normal cost}}{\text{Normal time} - \text{Crash time}} \\ &= \frac{700 - 500}{12 - 8} = \frac{200}{4} = 50 \end{aligned}$$

6. (a)

$$T_{ei} = \frac{a + 4m + b}{6}$$

a = Optimistic time, m = Most likely time, b = Pessimistic time

$$T_{ei} = \frac{4 + 4 \times 6 + 8}{6} = 6$$

$$\text{Variance} = \left(\frac{b - a}{6} \right)^2 = \left(\frac{8 - 4}{6} \right)^2 = 0.4445$$

$$\frac{T_{ei}}{\text{Variance}} = \frac{6}{0.4445} = 13.5$$

7. (c)

'€' should be allocated to minimum cost cell, but it does not form a closed loop.

Firstly, it should be allocated to 2, but it forms a closed loop.

Hence, it is allocated to cost cell having transportation cost 7.

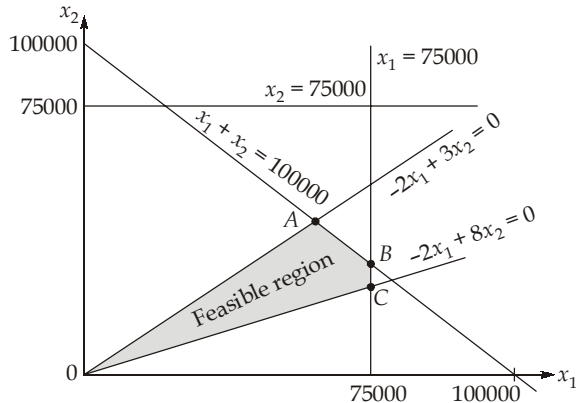
8. (d)

9. (c)

10. (b)

11. (a)

Unique solution



Point	x_1	x_2	z
0	0	0	0
A	60000	40000	14000
B	75000	25000	12500
C	75000	18750	11250

So, optimal solution is at A.

12. (c)

The given problem is maximization type converting it into minimization type.

	I	II	III	IV
A	20	70	50	0
B	60	100	70	80
C	30	25	30	20
D	40	45	60	30

Using Hungarian method.

	I	II	III	IV
A	20	70	50	0
B	0	40	10	20
C	10	5	10	0
D	10	15	30	0

	I	II	III	IV
A	20	65	40	0
B	0	35	0	20
C	10	0	0	0
D	10	10	20	0

	I	II	III	IV
A	10	55	30	0
B	0	35	0	20
C	10	0	0	10
D	0	0	10	0

Sales men	Territory	Sales
A	IV	220
B	III	160
C	II	190
D	I	175

745

This is a case of multiple optimal solution. Alternate optimal solution is

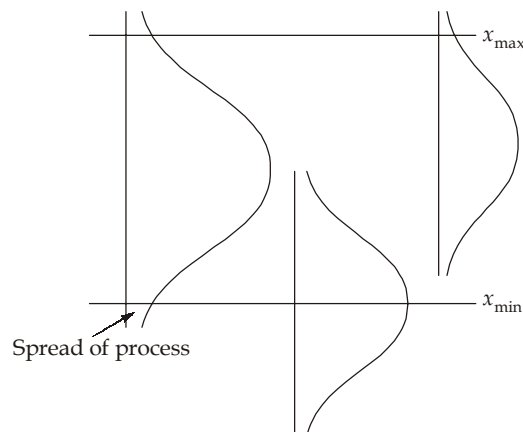
Sales men	Territory	Sales
A	IV	220
B	III	150
C	II	195
D	I	180

745

13. (b)

Spread of process = $6\sigma'$

Specified tolerance = $X_{\max} - X_{\min}$



Defective parts will be always there so, rejections are high.

14. (a)

$$IF_{ij} = \text{Max} \{0, ES_{jk} - LF_{ni} - t_{ij}\}$$

15. (b)

The allocation of units using north west corner rule is

	Warehouse			
	D	E	F	Supply
A	6(20)	4(30)	1	50
Plant B	3	8(40)	7	40
C	4	4(25)	2(35)	60
Demand	20	95	35	

16. (a)

$$\text{Demand} = D = 10000 \text{ units/year}$$

$$\text{Ordering cost} = C_o = ₹ 10/\text{order}$$

$$\text{Unit price} = C = ₹ 20/\text{unit}$$

$$\text{Holding cost} = C_h = 0.2 \times C = ₹ 0.2 \times 20 = ₹ 4/\text{unit/year}$$

$$\text{Back order cost} = c_b = 0.25 \times C = ₹ 0.25 \times 20 = ₹ 5/\text{unit/year}$$

$$Q_o = \sqrt{\frac{2DC_o}{C_h}} \sqrt{\frac{C_h + C_b}{C_b}} = \sqrt{\frac{2 \times 10000 \times 10}{4}} \sqrt{\frac{4 + 5}{5}} = 300 \text{ units/order}$$

$$\text{Maximum quantity to be back-ordered} = S_o = Q_o - M_o$$

$$\text{where } M_o = \sqrt{\frac{2DC_o}{C_h}} \sqrt{\frac{C_b}{C_h + C_b}} = \sqrt{\frac{2 \times 10000 \times 10}{4}} \sqrt{\frac{5}{4 + 5}} = 167 \text{ units}$$

$$S_o = 300 - 167 = 133 \text{ units}$$

17. (b)

	Fixed cost (₹)	Hourly cost of operating machine (₹)	Time to setup machine (minute)	Time per piece (minute)
Alternate-I	100000	100	30	4
Alternate-II	290000	500	45	0.2

Number of units produce in 1 hour

$$\text{For alternate I} = \frac{60}{4} = 15$$

$$\text{Cost per piece} = \frac{100}{15} = ₹ 6.667$$

$$\text{For alternate II} = \frac{60}{0.2} = 300$$

$$\text{Cost per piece} = \frac{500}{300} = ₹ 1.667$$

Set up cost alternate I:

$$100 \times \frac{30}{60} = ₹ 50$$

Set up cost alternate II:

$$500 \times \frac{45}{60} = ₹ 375$$

$$(\text{Fixed cost} + \text{Variable cost})_{\text{alternate-I}} = (\text{Fixed cost} + \text{Variable cost})_{\text{alternate-II}}$$

Let x be the minimum quantity.

$$100000 + 50 + 6.667x = 290000 + 375 + 1.667x$$

$$100050 + 6.667x = 290375 + 1.667x$$

$$5x = 190325$$

$$x = 38065 \text{ units}$$

Above 38065 units alternate II will be cheaper.

18. (b)

$$\begin{aligned}\text{Weighted score for location 1} &= 25 \times 3 + 25 \times 4 + 25 \times 3 + 15 \times 1 + 10 \times 5 \\ &= 75 + 100 + 75 + 15 + 50 = 315\end{aligned}$$

$$\begin{aligned}\text{Weighted score for location 2} &= 25 \times 5 + 25 \times 3 + 25 \times 3 + 15 \times 2 + 10 \times 3 \\ &= 125 + 75 + 75 + 30 + 30 = 335\end{aligned}$$

Since weighted score of location 2 is more so it is best.

19. (b)

Plotting the break even point.

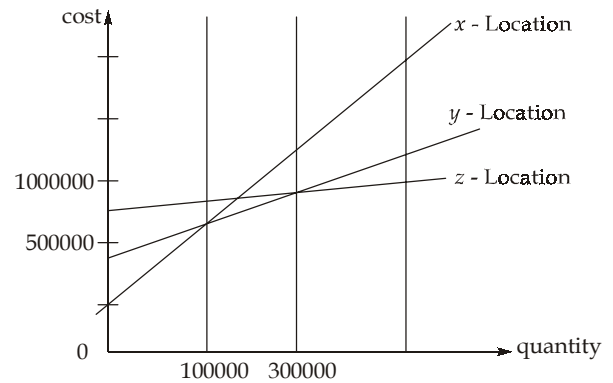
Solving for cross over between x and y ,

$$\begin{aligned}10q + 150000 &= 8q + 350000 \\ q &= 100000 \text{ units}\end{aligned}$$

Solve for cross over between y and z

$$\begin{aligned}8q + 350000 &= 6q + 950000 \\ q &= 300000 \text{ units}\end{aligned}$$

From graph for 130000 units y is best location.



20. (a)

p_i = Probability of failure of bulb in i^{th} week

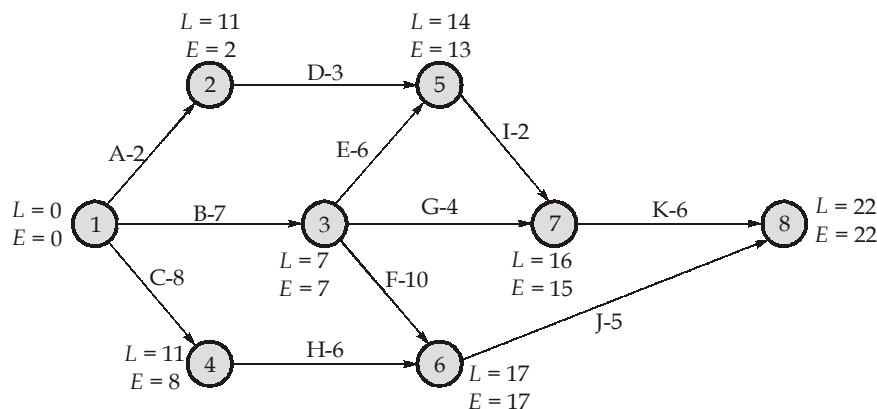
$$\begin{aligned}p_0 &= 0, & p_1 &= 0.1, \\ p_2 &= 0.2, & p_3 &= 0.4, \\ p_4 &= 0.3\end{aligned}$$

$$\text{Average life of bulb} = \sum_{i=1}^4 i p_i = 1 \times 0.1 + 2 \times 0.2 + 3 \times 0.4 + 4 \times 0.3 = 2.9 \text{ weeks}$$

$$\text{Average number of failures} = \frac{300}{2.9} = 103.4482 \approx 103$$

Cost of individual replacement of bulb = $2 \times 103 = ₹206$ per week.

21. (a)



Free float for G is $15 - 11 = 4$

Independent float for G is $15 - 7 - 4 = 4$

$$\text{Difference} = 4 - 4 = 0$$

22. (a)

Setting the problem in standard form,

Maximize, $w = 0x_1 + 0x_2 + 0x_3 + 0s_1 + 0s_2 + A_1 + A_2$

Subject to,

$$\begin{aligned} 3x_1 + 2x_2 + x_3 + 4x_4 + s_1 &= 6 \\ 2x_1 + x_2 + 5x_3 + x_4 + s_2 &= 4 \\ 2x_1 + 6x_2 - 4x_3 + 8x_4 + A_1 &= 0 \\ x_1 + 3x_2 - 2x_3 + 4x_4 + A_2 &= 0 \\ x_1, x_2, x_3, x_4, s_1, s_2, A_1, A_2 &\geq 0 \end{aligned}$$

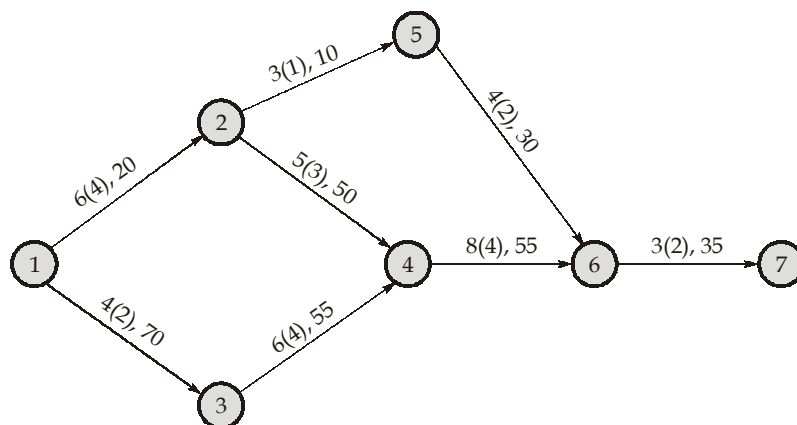
For finding the basic feasible solution,

$$\begin{aligned} x_1 = x_2 = x_3 = x_4 &= 0, \\ s_1 &= 6, & s_2 &= 4, \\ A_1 &= 0, & A_2 &= 0 \\ w &= 0 \end{aligned}$$

Since, $w = 0$ and A_1 and $A_2 = 0$, so phase I is not required and we can solve directly phase II and LPP has feasible solution.

Constraints 4 is half of constraint 3 so, it shows the presence of redundancy in constraints.

23. (c)



Activity	1 - 2	1 - 3	2 - 4	2 - 5	3 - 4	4 - 6	5 - 6	6 - 7
Crash cost/ day	20	70	50	10	55	55	30	35

Critical path is 1 - 2 - 4 - 6 - 7

Normal duration = 22 days

To crash project by 1 day, we crash activity 1 - 2, as it has minimum cost of crashing.

Cost of crashing = 20

Direct cost = 470

Indirect cost = $10 \times 21 = 210$

Total cost = 700

24. (a)

Period	Actual demand (D)	F	$F_t = F_{t-1} + \alpha[(D_{t-1}) - (F_{t-1})]$
1	10	10	10
2	12	10	$10 + 0.3 \times (10 - 10) = 10$
3	8	10.6	$10 + 0.3(12 - 10) = 10.6$
4	11	9.82	$10.6 + 0.3(8 - 10.6) = 9.82$
5	9	10.174	$9.82 + 0.3(11 - 9.82) = 10.174$

25. (a)

$$\begin{aligned}\lambda &= 6 \text{ cust/hr}, & t &= 30 \text{ min} = 0.5 \text{ hr} \\ n &= 4, \\ \lambda t &= 6 \times 0.5 = 3\end{aligned}$$

$$\text{Probability} = \frac{(\lambda t)^n \cdot e^{-\lambda t}}{n!} = \frac{(3)^4 \cdot e^{-3}}{4!} = 0.168$$

26. (c)

Weekly demand, $R = 400$ units/weekOrdering cost, $C_3 = ₹75$ per orderCarrying cost, $C_1 = 7.5\%$ per year of product cost

$$\begin{aligned}C_1 &= \left(\frac{7.5}{100} \times 50 \right) \text{ per unit per year} \\ &= \left(\frac{7.5}{100} \times \frac{50}{52} \right) \text{ per unit per week} \\ &= \frac{3.75}{52} \text{ per unit per week}\end{aligned}$$

$$\begin{aligned}\text{Total cost of inventory} &= 400 \times 50 + \sqrt{2C_1C_3R} \\ &= 400 \times 50 + \sqrt{2 \times \frac{3.75}{52} \times 75 \times 400} \\ &= 20000 + 65.78 = ₹20065.78 \text{ per week} \\ \text{Profit} &= 55 \times 400 - 20065.78 = ₹1934.22\end{aligned}$$

27. (b)

$$\text{Cycle time} = \frac{480}{20} = 24 \text{ minutes/unit}$$

$$\text{Minimum number of workstation} = \frac{80}{24} = 3.22 \approx 4$$

$$\text{Balance efficiency} = \frac{80}{24 \times 4} \times 100 = 83.33\%$$

28. (c)
P, R, S are correct and Q is incorrect as objective function is measurable in quantitative terms.

29. (c)
According to shortest processing rule

Job	Processing time t_i (minutes)	Job flow time
4	3	3
1	4	7
3	6	13
2	8	21

$$\text{Total job flow time} = 3 + 7 + 13 + 21 = 45$$

$$\text{Mean flow time} = \frac{44}{4} = 11 \text{ minutes}$$

According to earliest due date rule

Job	Processing time	Job flow time
2	8	8
1	5	13
3	6	19
4	3	22

$$\text{Total job flow time} = 8 + 13 + 19 + 22 = 62$$

$$\text{Mean flow time} = \frac{62}{4} = 15.5$$

$$\text{Ratio} = \frac{11}{15.5} = 0.71$$

30. (c)

$$F_t = F_{t-1} + \alpha(D_{t-1} - F_{t-1})$$

$$F_{14} = 75; D_{14} = 100; \alpha = 0.5$$

$$F_{15} = 75 + 0.5(100 - 75) = 87.5$$

$$F_{16} = 87.5 + 0.5(100 - 87.5) = 93.75$$

Now,

$$(\text{Error})_{14} = 25$$

$$(\text{Error})_{15} = 12.5$$

$$(\text{Error})_{16} = 6.25$$

$$\text{BIAS} = (\text{Mean forecast error})$$

$$= \frac{25 + 12.5 + 6.25}{3} = 14.583$$

