MADE EASY

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Leading Institute for ESE, GATE & PSUs

ESE 2025 : Mains Test Series

UPSC ENGINEERING SERVICES EXAMINATION

Mechanical Engineering

Test-2 : Strength of Materials + Machine Design + Engineering Mechanics

Name : ....

Roll No :

Test Centres			Student's Signature
Delhi ☑	Bhopal ☐	Jaipur ☐	
Pune ☐	Kolkata ☐	Hyderabad ☐	

Instructions for Candidates

1. Do furnish the appropriate details in the answer sheet (viz. Name & Roll No).
2. There are Eight questions divided in TWO sections.
3. Candidate has to attempt FIVE questions in all in English only.
4. Question no. 1 and 5 are compulsory and out of the remaining THREE are to be attempted choosing at least ONE question from each section.
5. Use only black/blue pen.
6. The space limit for every part of the question is specified in this Question Cum Answer Booklet. Candidate should write the answer in the space provided.
7. Any page or portion of the page left blank in the Question Cum Answer Booklet must be clearly struck off.
8. There are few rough work sheets at the end of this booklet. Strike off these pages after completion of the examination.

FOR OFFICE USE

Question No.	Marks Obtained
Section-A	
Q.1	20
Q.2	—
Q.3	40
Q.4	—
Section-B	
Q.5	38
Q.6	—
Q.7	36
Q.8	09
Total Marks Obtained	143

Signature of Evaluator .... Cross Checked by ....

IMPORTANT INSTRUCTIONS

CANDIDATES SHOULD READ THE UNDERMENTIONED INSTRUCTIONS CAREFULLY. VIOLATION OF ANY OF THE INSTRUCTIONS MAY LEAD TO PENALTY.

DONT'S

1. Do not write your name or registration number anywhere inside this Question-cum-Answer Booklet (QCAB).
2. Do not write anything other than the actual answers to the questions anywhere inside your QCAB.
3. Do not tear off any leaves from your QCAB, if you find any page missing do not fail to notify the supervisor/invigilator.
4. Do not leave behind your QCAB on your table unattended, it should be handed over to the invigilator after conclusion of the exam.

DO'S

1. Read the Instructions on the cover page and strictly follow them.
2. Write your registration number and other particulars, in the space provided on the cover of QCAB.
3. Write legibly and neatly.
4. For rough notes or calculation, the last two blank pages of this booklet should be used. The rough notes should be crossed through afterwards.
5. If you wish to cancel any work, draw your pen through it or write "Cancelled" across it, otherwise it may be evaluated.
6. Handover your QCAB personally to the invigilator before leaving the examination hall.

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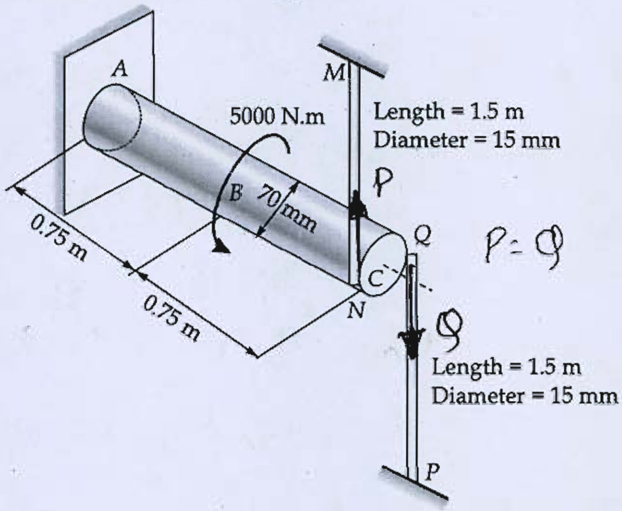
Section A : Strength of Materials + Machine Design + Engineering Mechanics

Q.1 (a) A steel shaft *ABC*, of constant circular cross-section and of diameter 70 mm, is clamped at the left end *A*, loaded by a twisting moment of 5000 Nm at its midpoint *B*, and elastically restrained against twisting at the right end *C* as shown in the figure.

At end C the bar *ABC* is attached to vertical steel bars each of 15 mm diameter. The upper bar *MN* is attached to the end *N* of a horizontal diameter of the 70 mm bar *ABC* and the lower bar *PQ* is attached to the other end *Q* of this same horizontal diameter as shown in the figure. For all materials *E* = 200 GPa and *G* = 80 GPa. Determine the peak shearing stress in bar *ABC* as well as the tensile stress in the bar *MN*.



[12 marks]

T_A → 5kN-m → ← T_c

Let θ be angular rotation of c

then deformation in bar $= \frac{d\theta}{2} = \frac{70\theta}{2}$

$= 35\theta$ mm — (1)

(3)

$$3\theta = \frac{PL}{AE} = \frac{P\times10^3\times1.5\times10^3}{\frac{\pi}{4}\times15^2\times2\times10^5}$$

$$3\cdot\frac{T_c\times750}{80\times10^3\times\frac{\pi}{32}\times70^4} = \frac{P\times10^3\times1.5\times10^3}{\frac{\pi}{4}\times15^2\times2\times10^5}$$

$$3\times\frac{P\times10^3\times70\times750}{80\times10^3\times\frac{\pi}{32}\times70^4} = P$$

$$\theta_c = \frac{T_c \times L}{GJ} + \frac{(T_c - 5)L}{GJ}$$

$$= \frac{750}{80\times10^3 \times \frac{\pi}{32}\times 70^4} \times 10^6 \left[T_c + T_c - 5\right]$$

$$= 3.97722\times10^{-3}(2T_c - 5) \quad —②$$

$$T_c = P.d = P\times70\times10^3$$

$$= 7\times10^4 P \quad —③$$

$$\theta_c = 3.97722\times10^{-3}(14\times10^4 P - 5) \quad \text{putting ③ in ②}$$

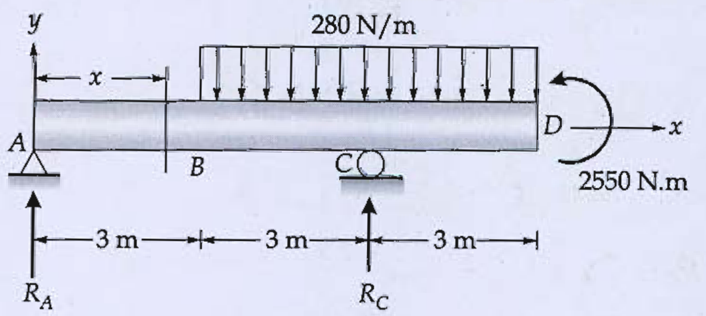
—④

putting ④ in ①

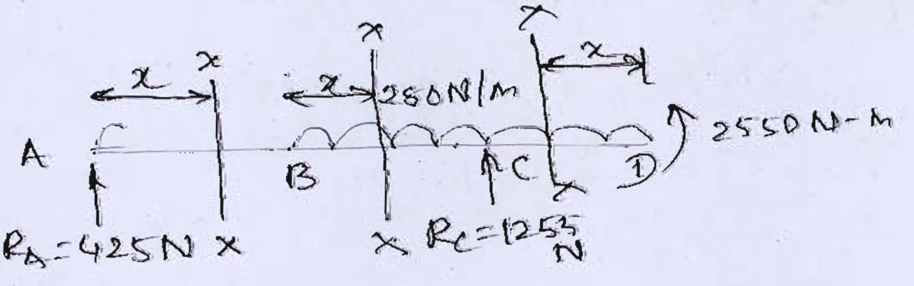
$$35\times 3.97722\times10^{-3}(14\times10^4\times P - 5)$$

$$= \frac{P\times1.5\times10^3\times10^3}{\frac{\pi}{4}\times15^2\times2\times10^5}$$

Q.1 (b) The beam AC is simply supported at A and C and subjected to the uniformly distributed load of 280 N/m and the couple of magnitude 2550 Nm as shown in the figure. Write the equations for shearing force and bending moment and make sketches of these equations.



[12 marks]



$\Sigma M_A = 0$

$$R_C = \frac{280 \times 6 \times (3+3) - 2550}{6}$$

$= 1255$ N

$\Sigma F_V = 0 \Rightarrow R_A = 280 \times 6 - 1255$

$= 425$ N

Do not write in this margin

→ AB

x from A & considering left of the section

$SF_x = 425\ N$

$SF_A = SF_B = SF(x = 3^-) = 425$

$BM_x = 425x$

$BM(x=0) = BM_A = 0$

$BM(x=3) = 425 \times 3$

$= 1275\ N\text{-}m$

→ For BC

x from B (Left side)

$SF_x = 425 - 280x$

$SF(x = 0^+) = SF_B = 425\ N$

$SF(x = 3^-) = SF_C = 425 - 280 \times 3$

$= -415\ N$

$BM_x = 425(x+3) - \frac{280x^2}{2}$

$BM(x = 0^+) = BM_B = 1275\ N\text{-}m$

$BM(x = 3^-) = BM_C = 425(3+3) - \frac{280 \times 3^2}{2}$

$= 1290\ N\text{-}m$

for CD

x from D (Right side)

$SF_x = 280x$

$SF(x=0) = SF_D = 0$

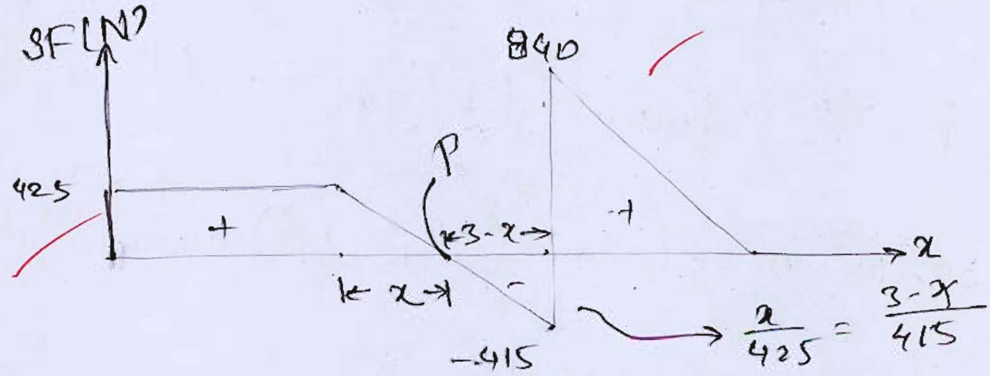
$SF(x=3) = 280 \times 3$

$SF_D = 840$

$BM_x = 2550 - \frac{280x^2}{2}$

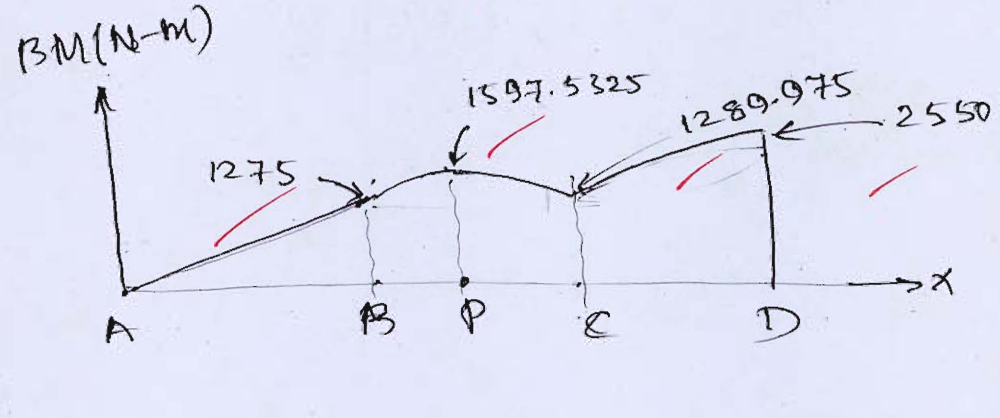
$BM(x=0) = BM_D = 2550$

$BM(x=3) = 990 N$



$\frac{x}{425} = \frac{3-x}{415}$

$x = 1.5178 m$

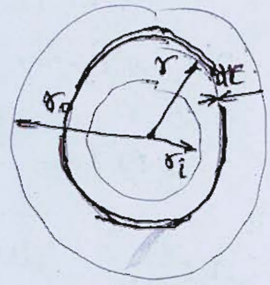


12

Q.1 (c) A plate clutch consists of one pair of contacting surface and transmits 30 kW power at 900 rpm. The ratio of outer diameter to inner diameter is 2. The coefficient of friction is 0.3 and the permissible intensity of pressure is 1.5 N/mm². Assuming uniform wear, calculate the inner and outer diameters.

[12 marks]

$df = \mu \cdot 2\pi r\,dr\,\frac{C}{r}$



$\int_0^T dT = 2\pi\mu C\int_{r_i}^{r_o} r\,dr$

2

$T = 2\pi\mu P_{max} r_i \times \frac{r_o^2 - r_i^2}{2}$

multiplying both side by ω.

$P = \mu P_{max} r_i (r_o^2 - r_i^2) \cdot \frac{2\pi N}{60}$

$30\times10^6 = 0.3\times1.5\times r_i (4r_i^2 - r_i^2) \times \frac{\pi\times900}{30}$

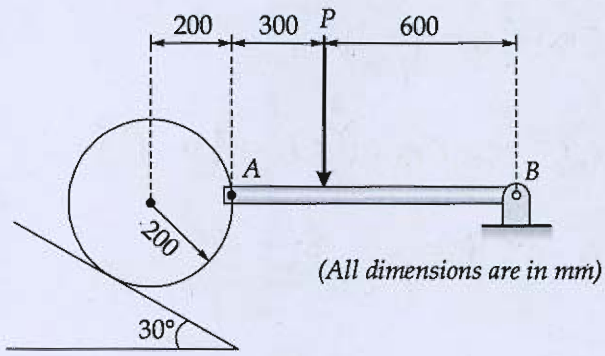
$r_i = 61.78\,mm$

$r_o = 2r_i = 123.56\,mm.$

Q.1 (d) A pair of spur gears with 20° full depth involute teeth consists of a 22 teeth pinion meshing with a 44 teeth gear. The module is 3 mm while the face width is 45 mm. The material for pinion as well as gear is steel with an ultimate tensile strength of 600 N/mm^2. The gears are heat treated to a surface hardness of 400 BHN. The pinion rotates at 1500 rpm and the service factor for the application is 1.75. Assume that velocity factor accounts for the dynamic load and the factor of safety is 2. Determine the rated power that the gears can transmit. Take Lewis form factor (Y) = 0.33 for 20° full depth involute system and $\sigma_b = 0.33\ s_{ut}$.

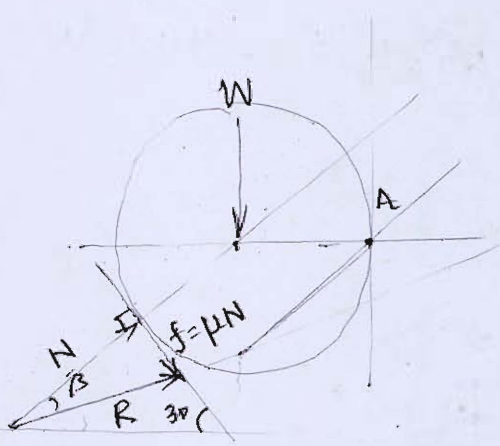
[12 marks]

Q.1 (e) A 40 kg disc rests on an inclined surface for which $\mu_s = 0.3$ as shown in the figure. Determine the maximum vertical force P that may be applied to link AB without causing the disc to slip at C.



(All dimensions are in mm)

[12 marks]



$W = 40 \times 9.81$

$= 392.4\,N$

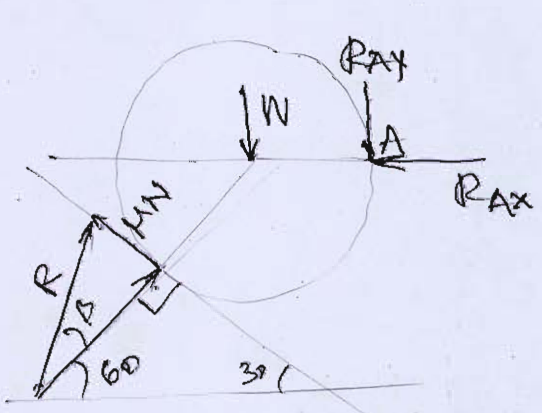
$\beta = \tan^{-1} 0.3$

$= 16.7°$

$\Sigma M_A = 0$

$W \times 200$

(3)



For disc.

$\Sigma M_A = 0$

$W \times 200 = \mu N \times 200$

$W = \mu N$

$N = \dfrac{392.4}{0.3} = 1308\,N$

$R = \sqrt{N^2 + (\mu N)^2}$

$= 1365.592\,N.$

$\Sigma F_x = 0$

$R_{Ax} = R\cos(60+\beta)$

$= 1365.6\cos(60° + 16.7°)$

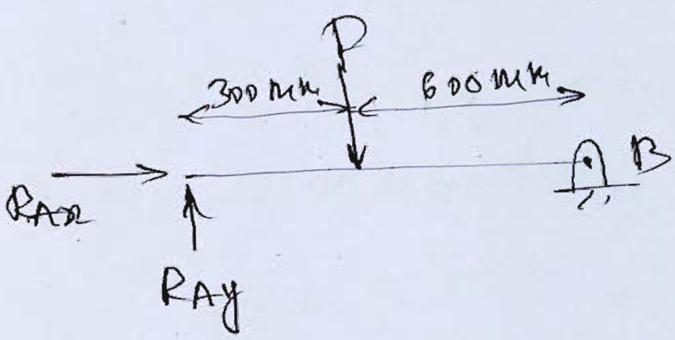
$= 314.16$ N.

$\Sigma F_y = 0$

$R_{Ay} = R\sin(60+\beta) - W$

$= 1365.6\sin(60° + 16.7°) - 392.4$

$= 936.573$ N



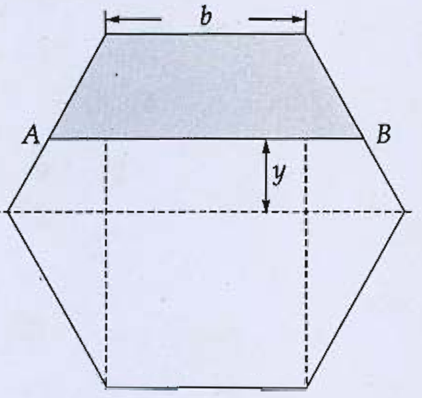
$\Sigma M_B = 0$

$P = \dfrac{936.573 \times 900}{600}$

$= 1404.86$ N

$P = 1404.86$ N Ans

Q.2 (a) A bar of hexagonal cross-section of side length b mm is used as a cantilever with one of its diagonal being horizontal. Derive an expression for the shear stress τ at the fibre AB in terms of b and y. Determine the shear stress when $y = 10$ mm, $b = 30$ mm and shear force applied is 6 kN. Also plot the shear stress distribution plot across the depth of the hexagonal section.



[20 marks]

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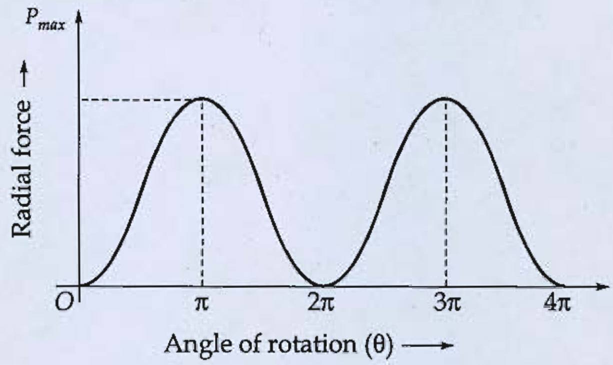
Q.2 (b) A ball bearing is subjected to a radial force which varies in sinusoidal way as shown in the figure. The direction of force remains fixed. The amplitude of the force is 2000 N and the speed of rotation is 750 rpm. Determine the dynamic load capacity of the bearing for the expected life of 9000 hr.



[20 marks]

Q.2 (c) If the density of a hemisphere varies as the distance from the bounding plane, show that the distance of the centre of gravity from that plane is $\frac{8}{15}^{\text{th}}$ of its radius.

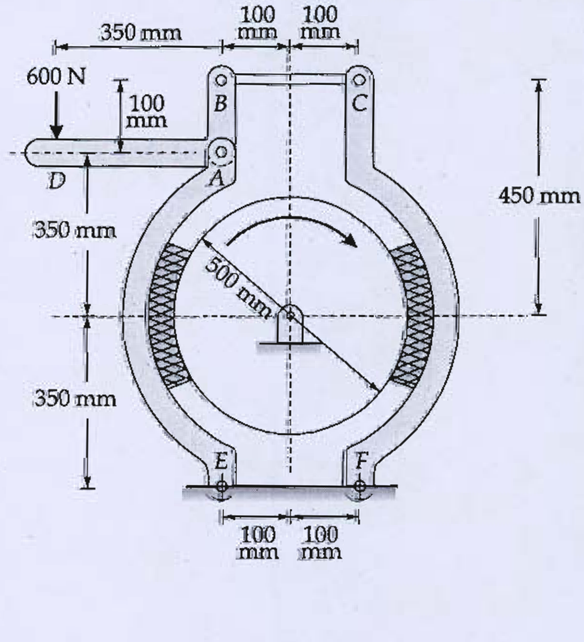
[20 marks]

Q.3 (a) A double block brake is as shown in the figure. The brake drum rotates in clockwise direction and the actuating force is 600 N. The coefficient of friction between the blocks and the drum is 0.3 Calculate.

(i) The torque absorbing capacity of the brake.

(ii) The dimensions of the blocks, if the intensity of pressure between the blocks and brake drum is 1.2 N/mm^2.

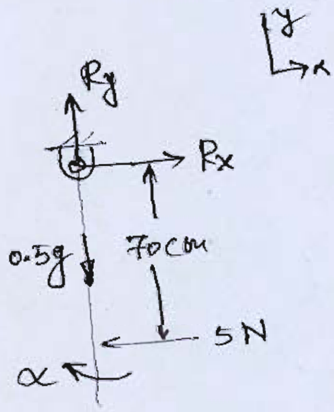
Assume that the blocks are identical and the length of each block is twice its width.



[20 marks]

Q.3 (b) A wooden metre stick AB of 500 grams mass and length 1 m hangs vertically as shown in figure. If a horizontal force of 5 N is applied at a point that is 30 cm from the bottom end B, determine (a) the angular acceleration of the stick, (ii) the components of reaction at the hinge at A. In addition, determine the point of application of the horizontal force at which the horizontal component of the reaction at A is zero.

[20 marks]

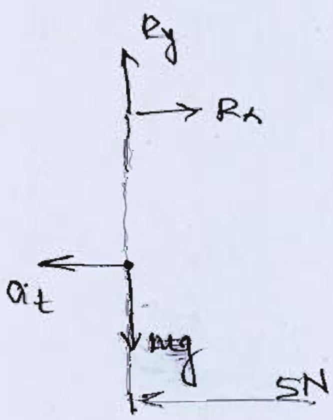


$I_{Hing} = \frac{ML^2}{3} = \frac{1}{6}\ kg\text{-}m^2$

$\Sigma T_{Hing} = I\alpha$

$5 \times 0.7 = \frac{1}{6} \cdot \alpha$

$\alpha = 21\ rad/s$ Ans.



$\Sigma F_y = 0 \quad \because a_y = 0$

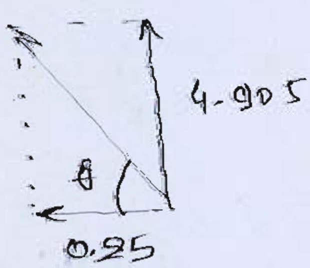
$R_y = 0.5g = 4.905\ N$

$\Sigma F_x = m a_x$

$5 - R_x = 0.5 \times 0.5 \times 21$

$R_x = -0.25\ N$

Reaction.



$R = \sqrt{R_x^2 + R_y^2}$

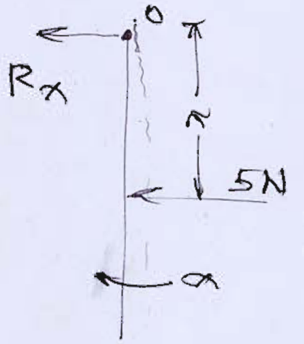
$= 4.91\ N$ Ans.

$\theta = \tan^{-1}\left(\frac{F_y}{F_x}\right)$

$= 87.1^\circ$

Do not write in this margin

For zero reaction.



$$\Sigma T_0 = I\alpha$$

$$5 \cdot x = \frac{1}{6}\alpha$$

$$\alpha = 30x$$

$$\Sigma F_x = m a_x$$

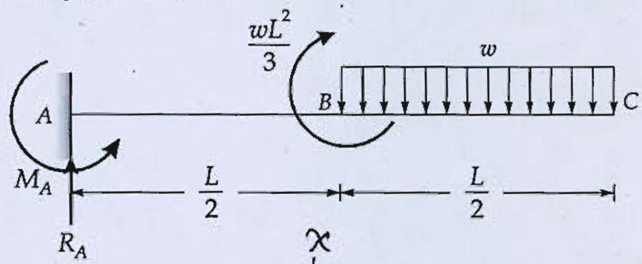
$$R_x^{\,0} + 5 = 0.5 \times 30x \times 0.5$$

$$x = 0.6667\,m$$

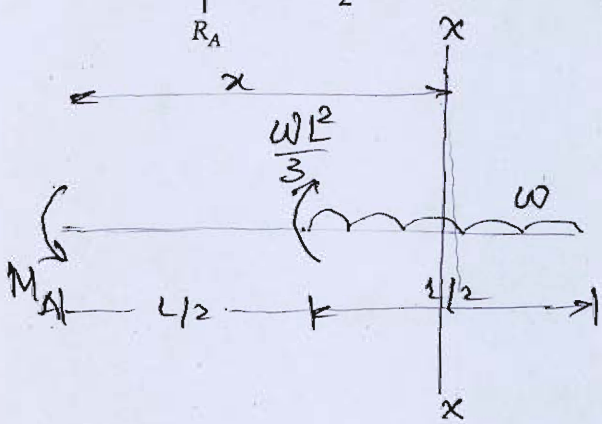
$= 66.67\,cm$ from top **Ans**

20

Q.3 (c) The cantilever beam *ABC* as shown below is subjected to a uniform load w per unit length distributed over its right half, together with a concentrated couple $\frac{wL^2}{3}$ applied at *B*. Using Macaulay's method determine and the maximum deflection of the beam.



[20 marks]



$\Sigma M_A = 0$

$M_A = \frac{wL^2}{3} + w\frac{L}{2}\left(\frac{L}{2} + \frac{L}{4}\right)$

$= \frac{17wL^2}{24}$

$\Sigma F_v = 0 \Rightarrow R_A = \frac{wL}{2}$

considing left of section

$$M_x = -\frac{17wL^2}{24}(x)^0 + \frac{wL^2}{3}\left(x-\frac{L}{2}\right)^0 - \frac{w\left(x-\frac{L}{2}\right)^2}{2}$$

$$+ \frac{wL}{2}x$$

$$EI\frac{d^2y}{dx^2} = \frac{wL}{2}x - \frac{17wL^2}{24}x^0 + \frac{wL^2}{3}\left(x-\frac{L}{2}\right)^0$$

$$- \frac{w\left(x-\frac{L}{2}\right)^2}{2}$$

$$EI\frac{dy}{dx} = \frac{wLx^2}{4} - \frac{17wL^2}{24}x + \frac{wL^2}{3}\left(x-\frac{L}{2}\right)$$

$$- \frac{w\left(x-\frac{L}{2}\right)^3}{6} + C_1$$

at $x = 0$; $\frac{dy}{dx} = 0 \Rightarrow C_1 = 0$

$$EI\,y = \frac{wLx^3}{12} - \frac{17wL^2x^2}{48} + \frac{wL^2\left(x-\frac{L}{2}\right)^2}{6}$$

$$- \frac{w\left(x-\frac{L}{2}\right)^4}{24} + C_2$$

at $x = 0$; $y = 0 \Rightarrow C_2 = 0$

$$y_{max} = y(x = L)$$

$$= \frac{wL^4}{EI}\left[\frac{1}{12} - \frac{17}{48} + \frac{1}{6}\left(\frac{1}{2}\right)^2 - \frac{1}{24}\left(\frac{1}{2}\right)^4\right]$$

$$= -\frac{89wL^4}{384EI}$$

$\therefore$ downward def^n of free end $= \frac{89wL^4}{384EI}$

20

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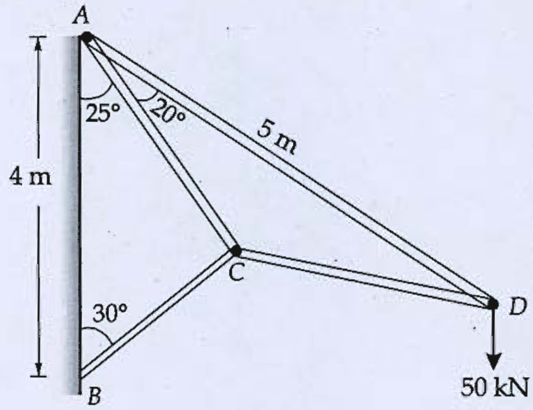
Q.4 (a) Find the force its nature in member *AD* and *BC* for given cantilever truss loaded by 50 kN as shown in the figure below.

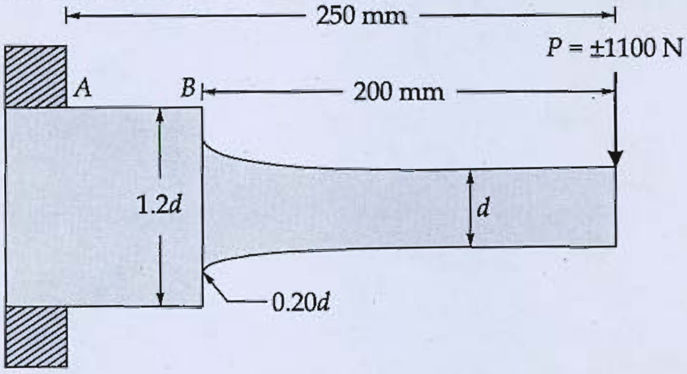


[20 marks]

Q.4 (b) A long thin bar of length L and rigidity EI is pinned at end A, and at B rotation is resisted by a restoring moment of magnitude λ per radian of rotation at that end. Derive the equation for the axial buckling load P. Neither A nor B can displace in the y-direction, but A is free to approach B.

[20 marks]

Q.4 (c) A cantilever beam made of cold draw steel having surface finish factor (k_a) 0.78 and S_{ut} = 540 N/mm^2 is subjected to a completely reversed load of 1100 N as shown in the figure. The notch sensitivity factor q at the fillet can be taken as 0.85 and the expected reliability is 90%. Determining the diameter d of the beam for a life cycle of 11000 cycles.



Take, reliability factor, k_c = 0.897 for 90% reliability and size factor k_b = 0.85.

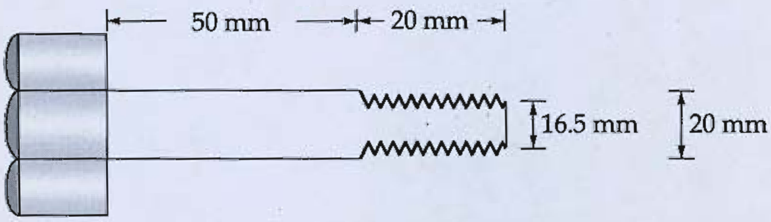
[Use Stress Concentration Factor Chart attached at the end]

[20 marks]

Section B : Strength of Materials + Machine Design + Engineering Mechanics

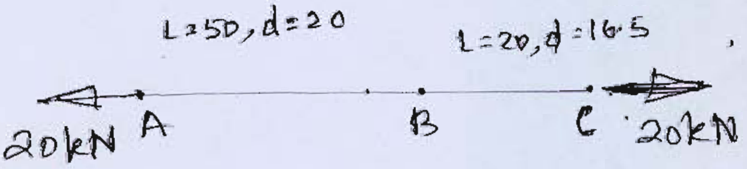
Q.5 (a) Calculate the strain energy of the bolt as shown in the figure under a tensile load of 20 kN. Show that the strain energy is increased for the same maximum stress, by turning down the shark of the bolt to the root diameter of the thread.

Take $E = 2 \times 10^5$ N/mm^2



Assuming that the load is distributed evenly over the core of screwed portion.

[12 marks]



All dia^s are in mm

$U = U_{AB} + U_{BC}$

$= \left(\frac{P^2 L}{AE}\right)_{AB} + \left(\frac{P^2 L}{AE}\right)_{BC}$

$$= \frac{P^2}{E}\left[\left(\frac{L}{A}\right)_{AB} + \left(\frac{L}{A}\right)_{BE}\right]$$

$$= \frac{(20\times10^3)^2}{2\times10^5}\left[\frac{50}{\frac{\pi}{4}\times 20^2} + \frac{20}{\frac{\pi}{4}\times 16.5^2}\right]$$

= ~~789.655 N-mm.~~ = 505.379 N-mm

$$\sigma_{max} = \frac{P}{A_{BC}} = \frac{20\times10^3}{\frac{\pi}{4}\times16.5^2}$$ = ~~116.92 MPa.~~ 93.53 MPa.

d = 16.5 mm, l = 70 m

A ———————— C

$$U_{AC} = \frac{\sigma_{max}^2}{2E}\left(\frac{\pi d^2}{4} L\right)$$

$$= \frac{(116.92)^2}{2\times2\times10^5}\times\left(\frac{\pi\times16.5^2}{4}\times 70\right)$$

=

Q.5 (b) A golf ball is launched with an initial velocity of 75 m/s at an angle of 15° with horizontal. Determine the radius of curvature of the trajectory and the time rate of change of the speed of the ball

(a) just after launch, and (b) at apex

Neglect aerodynamic drag.

[12 marks]

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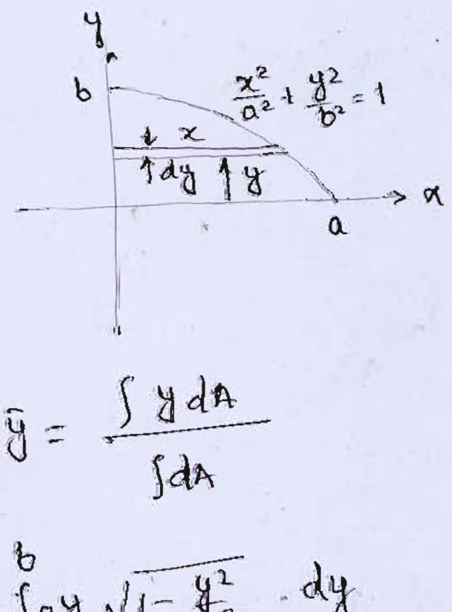
Q.5 (c) Determine the centroid of quadrant of an ellipse, whose equation is $\frac{x^2}{a^2}+\frac{y^2}{b^2}=1$.

[12 marks]



$x = \sqrt{a^2\left(1-\frac{y^2}{b^2}\right)}$

$dA = x\,dy$

$= \sqrt{a^2\left(1-\frac{y^2}{b^2}\right)}\,dy$

$\int_A dA = A = \frac{\pi ab}{4}$

$\bar{y} = \frac{\int y\,dA}{\int dA}$

$I = \int_0^b ay\sqrt{1-\frac{y^2}{b^2}}\cdot dy$

$1-\frac{y^2}{b^2} = t^2 \Rightarrow -\frac{2y}{b^2}\,dy = 2t\,dt$

$y\,dy = -b^2 t\,dt$

$$I = a\int t\cdot(-b^2 t\,dt)$$

$$= -\frac{ab^2}{3}\cdot t^3 \qquad t^2 = x^{1/2}$$

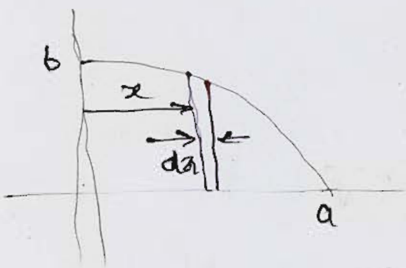
$$= -\frac{ab^2}{3}\left[1-\frac{y^2}{b^2}\right]^{3/2}\Bigg|_0^b$$

$$= -\frac{ab^2}{3}\left[0-1\right]$$

$$= \frac{ab^2}{3}$$

$$\bar{y} = \frac{\int y\,dA}{\int dA} = \frac{ab^2}{3}\times\frac{4}{\pi ab} = \frac{4}{3\pi}b$$

similiarly



$$dA = y\,dx$$

$$= \left(\left(1-\frac{x^2}{a^2}\right)b^2\right)^{1/2}dx$$

$$dA = b\left(1-\frac{x^2}{a^2}\right)^{1/2}dx$$

12

$$I_2 = \int_0^a x\cdot dA \qquad\qquad 1-\frac{x^2}{a^2} = u^2$$

$$= b\int_0^a x\left(1-\frac{x^2}{a^2}\right)^{1/2}dx \qquad 2u\,du = -2\frac{x}{a^2}dx$$

$$x\,dx = -a^2u\,du$$

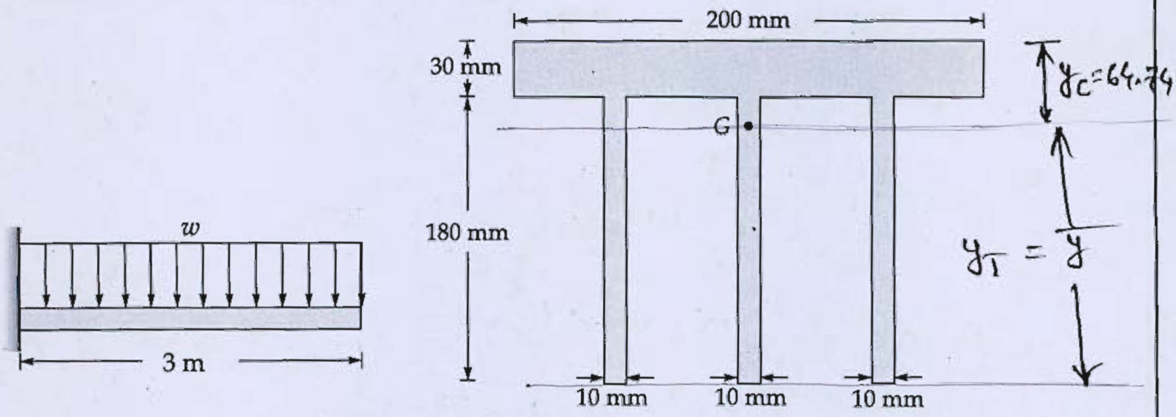
$$= b\int -a^2u^2\,du$$

$$= -\frac{ba^2}{3}u^3 = -\frac{ba^2}{3}\left[1-\frac{x^2}{a^2}\right]^{3/2}\Bigg|_0^a$$

$$= \frac{ba^2}{3}$$

$$\bar{x} = \int x\,dA\Big/\int dA = \frac{ba^2}{3}\times\frac{4}{\pi ab} = \frac{4a}{3\pi}$$

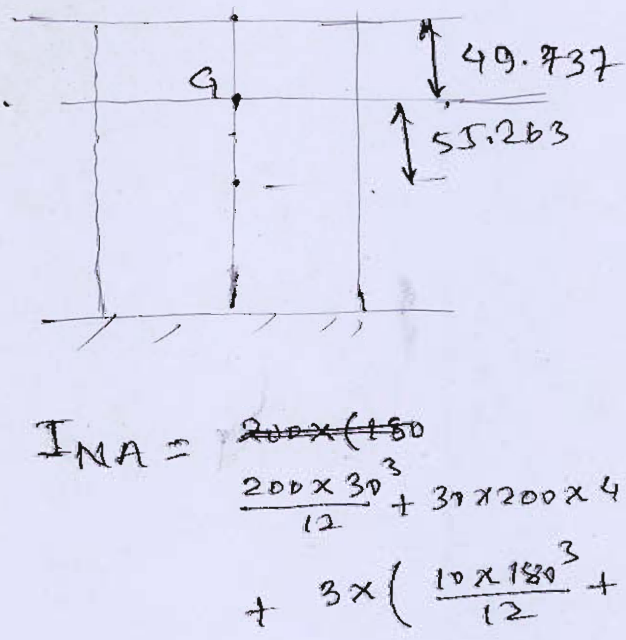
Q.5 (d) The extruded beam as shown below is made of aluminium having an allowable working stress in either tension or compression of 90 MPa. The beam is a cantilever, subjected to a uniform vertical load. Determine the allowable intensity of uniform loading.



[12 marks]

$$\bar{y} = \frac{\Sigma Ay}{\Sigma A} = \frac{3\times10\times180\times90 + 30\times200\times\left(180+\frac{30}{2}\right)}{3\times10\times180 + 30\times200}$$

$= 145.263$ mm



$I_{NA} =$ ~~200×(180~~

$$\frac{200\times30^3}{12} + 30\times200\times49.737^2$$

$$+ 3\times\left(\frac{10\times180^3}{12} + 10\times180\times55.263^2\right)$$

$= 46364210.53$ mm^4

$M_{max} = M = \frac{wL^2}{2}$

$= \frac{w \times 3^2}{2} \times 10^6$ N-mm

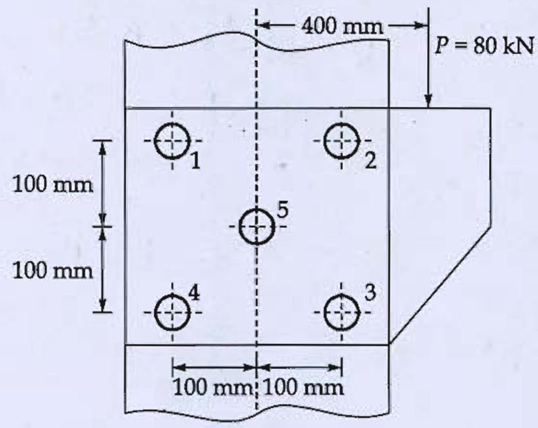
$\sigma_{per} \geq \frac{M}{Z_{NA}} y_{max}$

$90 \geq \frac{\left(\frac{w \times 3^2 \times 10^6}{2}\right)}{46364210.53} \times 145.263$

$w \leq 6.38$ kN/m. Ans

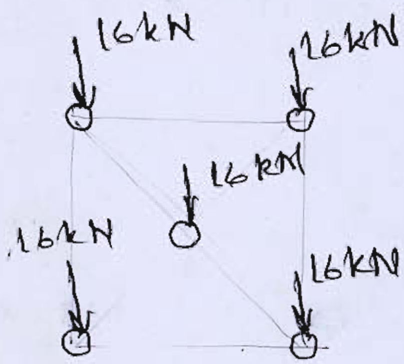
12

Q.5 (e) A bracket is attached to a steel channel by means five identical rivets as shown in figure. Determine the diameter of rivets, if the permissible shear stress is 100 N/mm^2.



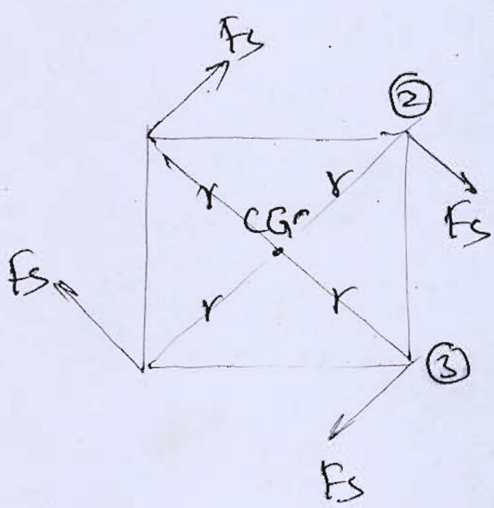
[12 marks]

Primary load



$F_p = \frac{80}{5} = 16\,kN$

Secondary load



F_s secondary shear load will be same for all outer rivets

∵ they are at same distance form CG

$Pe = 80 \times 400$

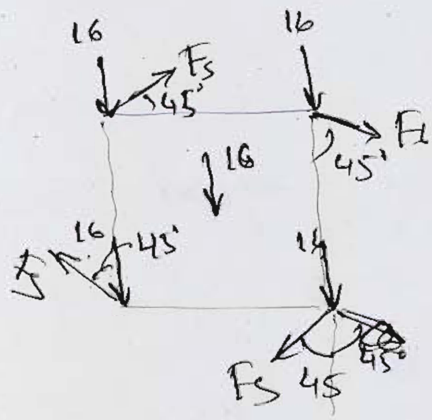
$= 32000\ kN\text{-}mm$

$r = \frac{200\sqrt{2}}{2} = 100\sqrt{2}\ mm$

$2 \times F_s \times 200\sqrt{2} = 32000$

$F_s = 56.568\ kN$

combineing



$R = \sqrt{16^2 + 56.56^2 + 2 \times 16 \times 56.56 \times \cos 45}$

$= 68.81$ kN

(12)

$\tau_{per} \geq \frac{R}{\frac{\pi}{4} d^2}$

$100 \geq \frac{68.81 \times 10^3}{\frac{\pi}{4} \times d^2} \Rightarrow d \geq 29.6$ mm

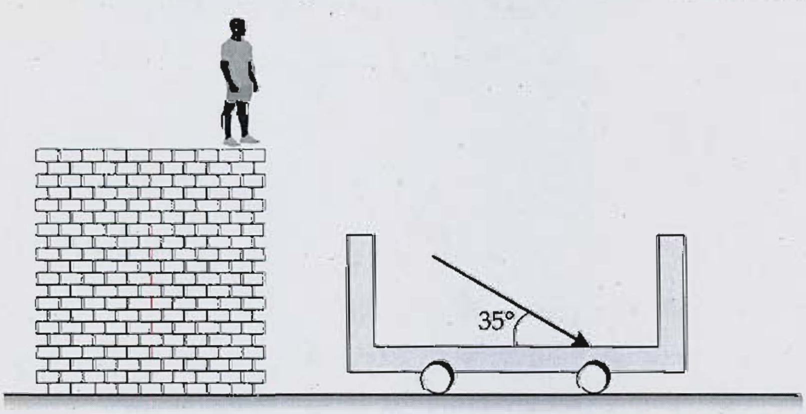
Q.6 (a) A man of 60 kg mass standing on a bridge jumps on to a cart below him such that he lands with a velocity of 5 m/s at an angle of 35° to the horizontal direction. If the cart is free to move, determine its velocity after he has jumped in for the following cases : the cart is initially

(i) at rest

(ii) moving with a velocity of 1 m/s away from the bridge.

(iii) moving with a velocity of 1 m/s towards the bridge.

Take the mass of the cart as 130 kg. Also determine the loss in kinetic energy in each case.



[20 marks]

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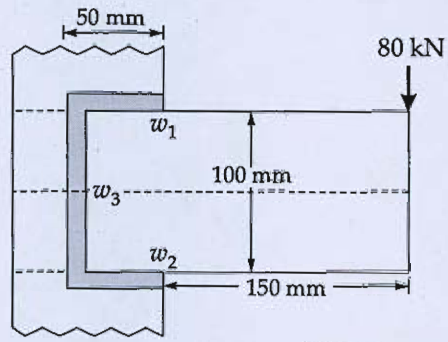
Q.6 (b) A welded connection, as shown in the figure is subjected to an eccentric force of 80 kN in the plane of the welds. Determine the size of the welds, if the permissible shear stress for the weld is 410 N/mm^2. Assume static condition.



[20 marks]

Q.6 (c) A cylindrical tank is 1.6 m diameter, 2.4 m long and 10 mm thick. Its ends are flat and are joined by nine tie bars, each 35 mm diameter equally spaced. If the tie bars are initially stressed to 45 N/mm^2 and the tank is filled with water. Determine

(i) the increase in capacity when the pressure is raised to 2 N/mm^2.

(ii) the final stress in the tie bars.

Taking $E = 2 \times 10^5\ N/mm^2$ and $\mu = 0.3$

[20 marks]

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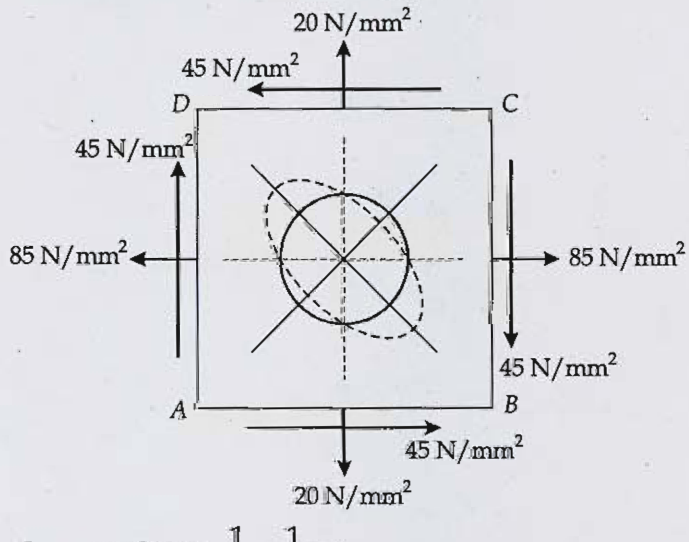
Q.7 (a) On a mild steel plate, a circle of diameter 60 mm is drawn before the plate is stressed as shown in the figure. Find the lengths of the major and minor axes of an ellipse formed as a result of the deformation of the circle marked.



Take $E = 2 \times 10^5$ N/mm² and $\frac{1}{m} = \frac{1}{4} = \mu$ **[20 marks]**

$$\sigma_{1,2} = \frac{\sigma_x + \sigma_y}{2} \pm \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + \tau_{xy}^2}$$

$$= \frac{85+20}{2} \pm \sqrt{\left(\frac{85-20}{2}\right)^2 + 45^2}$$

$$= 52.5 \pm 55.51$$

$$= 108 \text{ MPa}, -3 \text{ MPa}.$$

$$\varepsilon_1 = \frac{\sigma_1}{E} - \mu\frac{\sigma_2}{E}$$

$$= \frac{1}{2\times10^5}\left(108 + \frac{1}{4}\times3\right) = \frac{87}{16\times10^4} = 5.4375\times10^{-4}$$

major dia $= (d\cdot\varepsilon_1 + d) = 60.0326$ mm Ans

$$\varepsilon_2 = \frac{\sigma_2}{E} - \mu\frac{\sigma_1}{E}$$

$$= \frac{1}{2\times10^5}\left[-3 - \frac{1}{4}\times108\right]$$

$$= -1.5\times10^{-4}$$

minor dia $= d(1+\varepsilon_2)$

$= 60(1 - 1.5\times10^{-4})$

$= 59.991$ mm Ans

(20)

Q.7 (b) Following data is given for a full hydrodynamic bearing used for electric motor.
Radial load = 1250 N; Journal speed = 1500 rpm; Journal diameter = 50 mm
Static load on the bearing = 400 N; Start up bearing pressure = 2 N/mm^2
Permissible bearing pressure in application of elastic motor is 1 N/mm^2

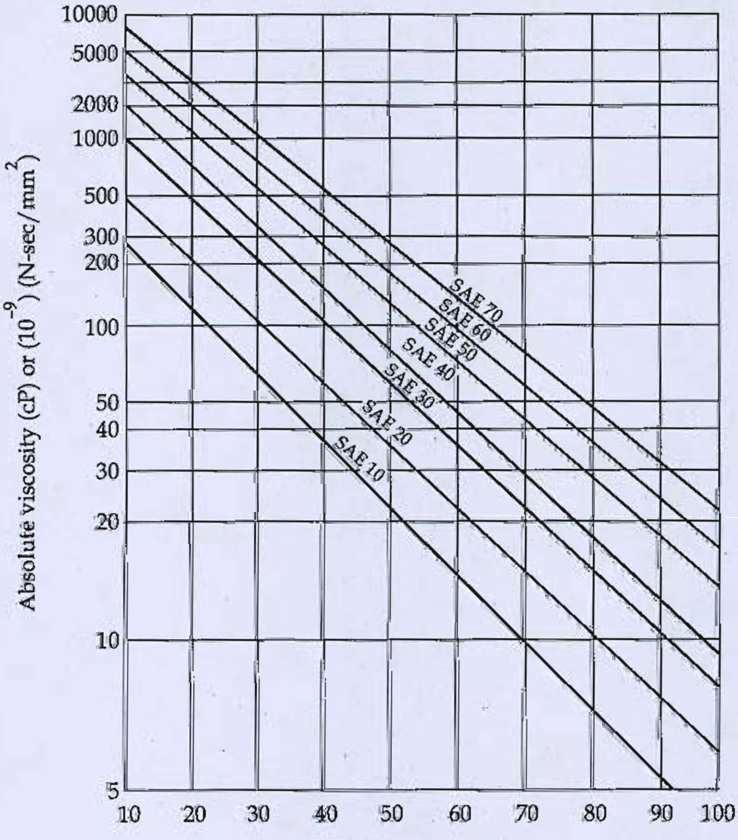
The value of surface roughness (CLA) of the journal and the bearing are 2 and 1 micron respectively. The minimum oil film thickness should be five times the sum of surface roughness of the journal and the bearings. Determine

(i) length of the bearing (ii) radial clearance
(iii) minimum oil film thickness (iv) viscosity of lubricant
(v) flow of lubricant

Select suitable oil for this application assuming the operating temperature as 65°C.

$\left(\frac{l}{d}\right)$	ε	$\left(\frac{h_0}{c}\right)$	S	ϕ	$\left(\frac{r}{c}\right)f$	$\left(\frac{Q}{rcn_sl}\right)$	$\left(\frac{Q_s}{Q}\right)$	$\left(\frac{p}{p_{max}}\right)$
$\left(\frac{1}{2}\right)$	0	1.0	∞	88.5	∞	π	0	–
	0.1	0.9	4.31	81.62	85.6	3.43	0.173	0.523
	0.2	0.8	2.03	74.94	40.9	3.72	0.318	0.506
	0.4	0.6	0.779	61.45	17.0	4.29	0.552	0.441
	0.6	0.4	0.319	48.14	8.10	4.85	0.730	0.365
	0.8	0.2	0.0923	33.31	3.26	5.41	0.874	0.267
	0.9	0.1	0.0313	23.66	1.60	5.69	0.939	0.206
	0.97	0.03	0.00609	13.75	0.610	5.88	0.980	0.126
	1.0	0	0	0	0	–	1.0	0

Table : Dimensionless performance parameters for full journal bearing with side flow



Viscosity-Temperature Relationship

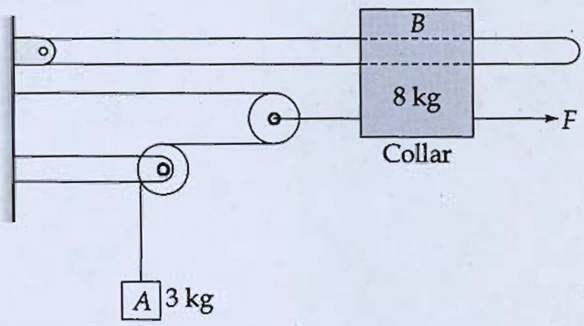
[20 marks]

Q.7 (c) (i) A lift is operated by four ropes each having 30 wires of 1.6 mm diameter. The cage weighs 1.5 kN and the weight of the rope is 4.6 N/m. Determine the maximum load carried by the lift if each wire is of 40 m length and the lift operates

1. without any drop
2. with a drop of 100 mm during operation.

[Take E_{rope} = 70 GPa and allowable stress = 120 MPa]

(ii) System shown in the figure is initially at rest. Neglecting friction determine the force F required if velocity of collar B becomes 8 m/s in 3 seconds after the start.



[10 + 10 marks]

(i) 4 ropes

30 wires | rope

total no of wire = 30 × 4 = 120

d = 1.6 mm W_c = 1.5 kN,

ρ = 4.6 N/m , L = 40 mm

6

(i) without any drop

F_{max} = σ_{per} · × 120 × $\frac{\pi}{4} d^2$ − 4.6 × 40

= $120 \times 120 \times \frac{\pi}{4} \times 1.6^2 \times 10^{-3} - 4.6 \times 40 \times 4 \times 10^{-3}$

= ~~28.973 kN~~ = 28.2 kN

max load carrying capacity. = ~~27.45 kN~~

~~27.27 kN~~

26.71 kN

(2)

~~σ_{static}~~

$$\delta_{static} = \frac{PL}{AE} + \frac{WL}{2AE}$$

$$= \frac{(P+1.5)\times 10^3 \times 40 \times 10^3}{120 \times \frac{\pi}{4} \times 1.6^2 \times 70 \times 10^3} + \frac{4.6 \times 40 \times 4 \times 4 \times 10^4}{2 \times \frac{\pi}{4} \times 1.6^2 \times 70 \times 10^3}$$

$$= 2.3684(P+1.5) + 104.58 \text{ mm}$$

$$IF = \frac{\sigma_{per}}{\sigma_{static}}$$

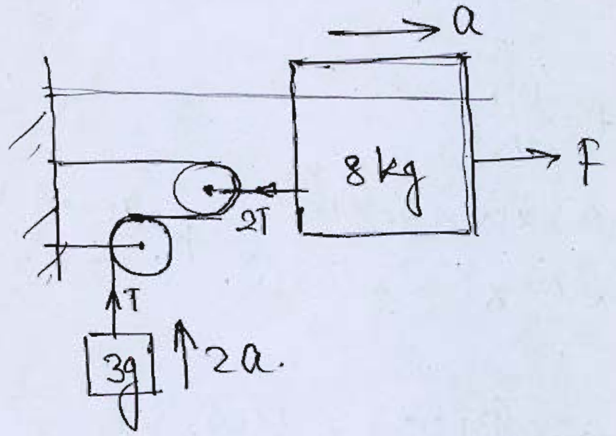
$$\sigma_{static} = \frac{(P+1.5)10^3 + 4.6 \times 40 \times 4}{\frac{\pi}{4}(1.6)^2}$$

Now,

$$\frac{120}{\frac{(P+1.5)\times 10^3 + 4.6 \times 40 \times 4}{\frac{\pi}{4} \times 1.6^2}} = 1 + \sqrt{1 + \frac{2 \times 100}{2.3684(P+1.5) + 104.58}}$$

$P =$

2(ii)



$u = 0$
$v = 8 m/s$
$t = 3 sec$

for 8 kg block

$F - 2T = 8a$ — ①

for 3 kg block

$T - 3g = 3 \times 2a$ — ②

from, given.

$v = u + at$

$8 = 0 + a \times 3$

$a = \frac{8}{3} m/s$ — ③

putting ③ in ②

$T = 45.43 N$

Putting the value of T and a in eqn ①

$F = 112.19 N$

10

Q.8 (a) (i) Discuss the five important parameters involved in the selection and design of journal bearings. Explain in detail how each parameter effects the performance and reliability of the bearing.

(ii) The torque developed by an engine is given by following equation:

$T = 15000 + 2000 \sin 2\theta - 1500 \cos 2\theta$

where T is the torque in N-m and θ is the crank angle from inner dead centre position. The resisting torque of the machine is constant throughout the work cycle. The coefficient of speed fluctuations is 0.02. The engine speed is 200 rpm. A circular solid steel disc, 60 mm thick, is used as flywheel. The mass density of steel is 7800 kg/m^3. Calculate the radius of the flywheel disk.

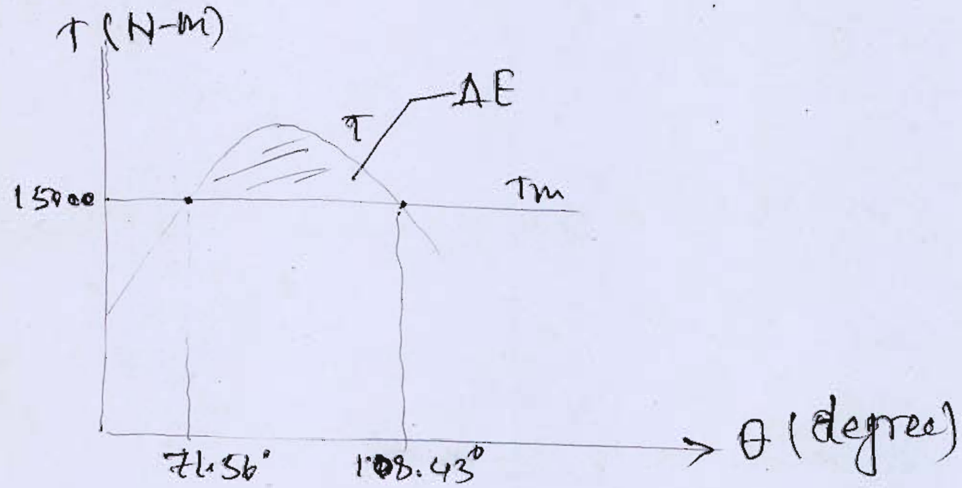
[10 + 10 marks]

(ii)

$$W = \int_0^{\pi} T\, d\theta = 15000\pi \text{ J}$$

$$T_m = \frac{W}{\pi} = 15000 \text{ N-m}$$

2



at $T = T_m$

$$0 = 2000 \sin 2\theta - 1500 \cos 2\theta$$

$$\theta = 108.43°, 71.56°$$

$$\Delta E = \int_{71.56}^{108.43} (T - T_m)\, d\theta = 5158.32 \text{ N-m}$$

$$\Delta E = m k^2 \omega^2 C_s$$

$$= \frac{mR^2}{2} \omega^2 C_s$$

$$= \rho \cdot \frac{\pi R^2 t}{2} R^2 \omega^2 C_s$$

$$51578.32 = 7800 \times \frac{\pi \times R^2 \times 0.06}{2} \times R^2 \times \left(\frac{\pi \times 200}{30} \right)^2 \times 0.02$$

$$R = 1.6817 \text{ m}$$

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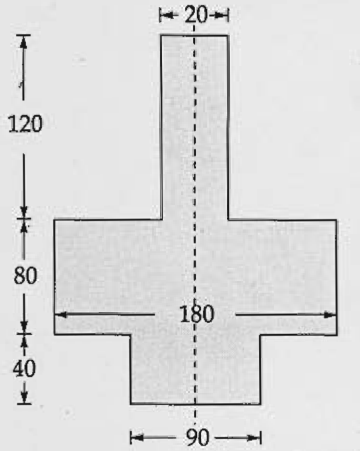
Q.8 (b) The cross-section of a conveyor beam is shown in the figure. The beam is subjected to a bending moment in the plane *y-y*. Determine the maximum permissible bending moment.

(i) for the bottom flange to be in tension.

(ii) for the bottom flange to be in compression.

The safe bending stress in tension and compression are 40 N/mm² and 140 N/mm² respectively.

[20 marks]

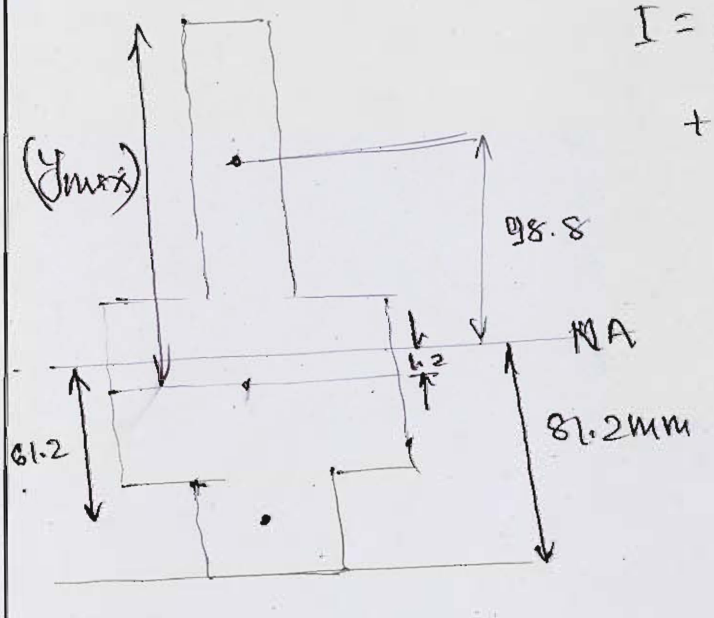


(All dimensions are in mm)

$$\bar{y} = \frac{90\times40\times20 + 180\times80\times(40+40) + 20\times120\times(60+80+40)}{90\times40 + 180\times80 + 20\times120}$$

$= 81.1765$ mm

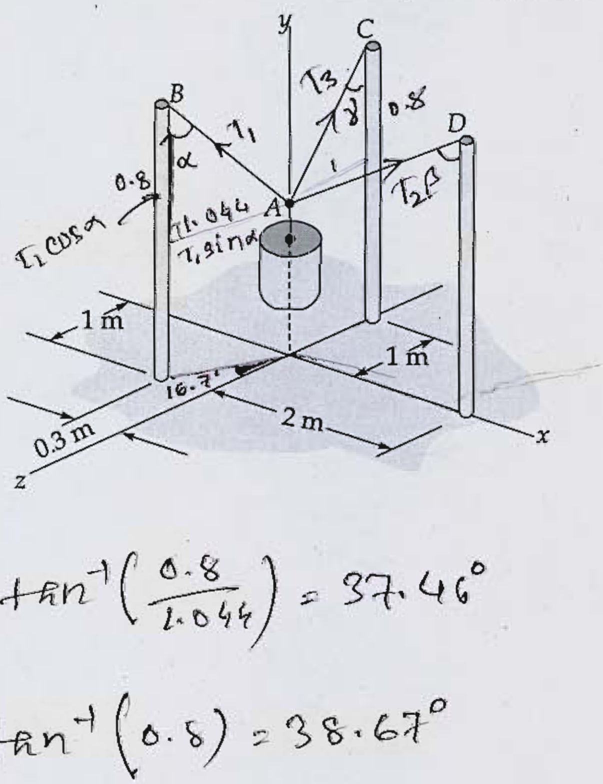
5



$$I = \frac{1}{12}\times20\times120^3 + 20\times120\times98.8^2 + \frac{1}{12}\times80^3\times180 + 80\times180\times1.2^2 + \frac{1}{12}\times40^3\times90 + 40\times90\times61.2^2$$

$= 47968320$ mm⁴

Q.8 (c) The 20 kg mass is suspended by cables attached to three vertical 2 m posts. Point A is at (0, 1.2, 0) m. Determine the tensions in cables AB, AC and AD.



[20 marks]

2

$$\alpha = \tan^{-1}\left(\frac{0.8}{1.044}\right) = 37.46^\circ$$

$$\gamma = \tan^{-1}(0.8) = 38.67^\circ$$

$$\beta = \tan^{-1}\left(\frac{0.8}{2}\right) = 21.8^\circ$$

$T_{1,z} = T_1 \sin\alpha \cdot \cos 16.7$

$= 0.583T_1$

$T_{1,x} = T_1 \sin\alpha \sin 16.7$

$= 0.175 T_1$

$\Sigma F_x = 0$

$T_2 \sin\beta = 0.175 T_1$

$T_2 = 0.471 T_1$

$\Sigma F_z = 0$

$0.583T_1 = T_3 \sin 38.67$

$T_3 = 0.933 T_1$

$\Sigma F_y = 0$

$20 \times 9.81 = T_1 \cos\alpha + T_2 \cos\beta + T_3 \cos\gamma$

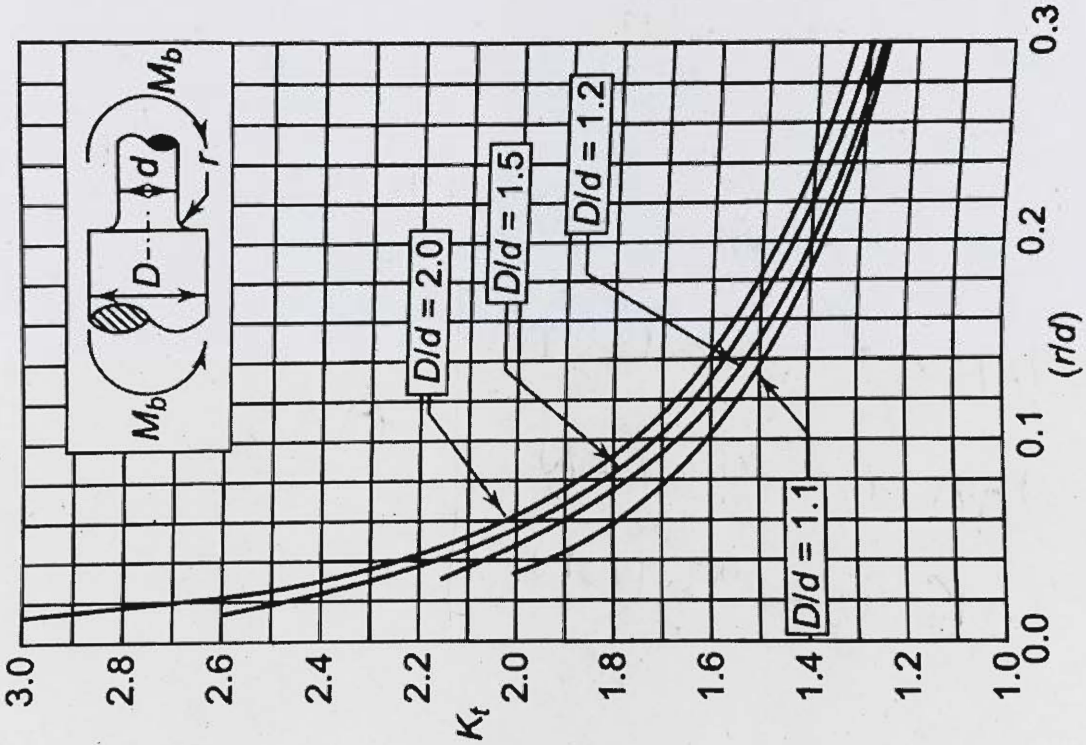
$T_{AB} = T_1 = 100.125$ N

$T_{AD} = T_2 = 47.16$ N

$T_{AC} = T_3 = 93.11$ N

Ans

oooo



Stress concentration factor

Space for Rough Work

Space for Rough Work

Space for Rough Work

Space for Rough Work