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ENGINEERING MATHEMATICS

ELECTRONICS ENGINEERING

Date of Test: 15/10/2025

ANSWER KEY >

1.	(c)	7.	(d)	13.	(b)	19.	(b)	25.	(a)
2.	(a)	8.	(a)	14.	(b)	20.	(c)	26.	(c)
3.	(b)	9.	(d)	15.	(d)	21.	(d)	27.	(c)
4.	(a)	10.	(b)	16.	(b)	22.	(d)	28.	(c)
5.	(c)	11.	(c)	17.	(d)	23.	(c)	29.	(b)
6.	(b)	12.	(c)	18.	(b)	24.	(a)	30.	(a)



DETAILED EXPLANATIONS

1. (c)

 \Rightarrow

The characteristic equation $[A - \lambda I] = 0$

i.e.
$$\begin{bmatrix} 4-\lambda & 6 \\ 2 & 8-\lambda \end{bmatrix} = 0$$
or
$$(4-\lambda)(8-\lambda)-12 = 0$$
or
$$32-8\lambda-4\lambda+\lambda^2-12 = 0$$

$$\Rightarrow \qquad \lambda^2-12\lambda+20 = 0$$

$$\Rightarrow \qquad \lambda^2-10\lambda-2\lambda+20 = 0$$

$$\Rightarrow \qquad (\lambda-10)(\lambda-2) = 0$$

Corresponding to $\lambda = 10$, we have

$$[A - \lambda I]x = \begin{bmatrix} -6 & 6 \\ 2 & -2 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$
Which gives,
$$-6x + 6y = 0$$

$$\Rightarrow \qquad x = y$$

$$2x - 2y = 0$$

$$\Rightarrow \qquad x = y$$

i.e. eigen vector
$$\begin{bmatrix} 1\\1 \end{bmatrix}$$

Corresponding to $\lambda = 2$, we have

$$[A - \lambda I]x = \begin{bmatrix} 2 & 6 \\ 2 & 6 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

 $\lambda = 10.2$

Which gives, 2x + 6y = 0i.e. eigen vector $\begin{bmatrix} -3\\1 \end{bmatrix}$

2. (a)

The product of eigen values is always equal to the determinant value of the matrix.

$$\begin{array}{lll} \lambda_1 &=& 5, & & \lambda_2 &=& \text{Unknown} \\ |A| &=& 30 & & \\ \lambda_1 \lambda_2 &=& 30 & & \\ 5(\lambda_2) &=& 30 & & \\ \lambda_2 &=& 6 & & & \end{array}$$

3. (b)

 \Rightarrow

$$\lim_{x \to 0} \left(\frac{3\cos^2 x - 2\sin^2 x}{2\sin x + 3\cos x} \right) = \lim_{x \to 0} \left(\frac{3-0}{0+3} \right) = \frac{3}{3} = 1$$

4. (a)

Probability of atleast one meeting the specification

=
$$1 - (\overline{A} \cap \overline{B} \cap \overline{C} \cap \overline{D})$$

= $1 - (0.4 \times 0.3 \times 0.2 \times 0.1)$
= $1 - (0.0024) = 0.9976$

5. (c)

Case-I: White ball is transferred from urn A to urn B

Probability of drawing white ball from $B = \frac{2}{2+4} \times \frac{6}{13} = \frac{2}{13}$

Case-II: Black ball is transferred from A to B

Probability of drawing black ball from $B = \frac{4}{2+4} \times \frac{5}{13} = \frac{10}{39}$

Required probability = $\frac{2}{13} + \frac{10}{39} = \frac{16}{39}$

6. (b)

$$\frac{\partial M}{\partial y} = \frac{x}{xy} = \frac{1}{y}$$

$$\frac{\partial N}{\partial x} = \frac{m}{y}$$

$$\frac{\partial M}{\partial y} = \frac{\partial N}{\partial x}$$

$$m = 1$$

\Rightarrow

$$\frac{e^x}{(1-e^x)}dx + \frac{\sec^2 y}{\tan y}dy = 0$$

Integrating on both sides, we get,

$$-\ln(1 - e^{x}) + \ln(\tan y) = C_{1}$$

$$\ln\left(\frac{\tan y}{(1 - e^{x})}\right) = C_{1}$$

$$\frac{\tan y}{(1 - e^{x})} = e^{C_{1}} = C$$

$$\tan y = C(1 - e^{x})$$

8. (a)

$$(D^2 + D)y = x^2 + 2x + 8$$

The particular integral is,

$$PI = \frac{x^2 + 2x + 8}{D(1+D)}$$

$$= \frac{1}{D}(1+D)^{-1}(x^2 + 2x + 8) = \frac{1}{D}(1-D+D^2-D^3+...)(x^2 + 2x + 8)$$

$$= \frac{1}{D}(x^2 + 2x + 8 - 2x - 2 + 2) = \frac{1}{D}(x^2 + 8) = \frac{x^3}{3} + 8x$$

9. (d)

Probability of showing even number = $\frac{2}{1+2} = \frac{2}{3}$

Probability of showing odd number = $\frac{1}{1+2} = \frac{1}{3}$



For sum to be odd = (Even + Even + odd)/(Even + Odd + Even)/(Odd + Even + Even)/(odd + odd + odd)

Required probability =
$$\frac{2}{3} \times \frac{2}{3} \times \frac{1}{3} \times 3 + \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} = \frac{12+1}{27} = \frac{13}{27}$$

10. (b)

$$y = e^x \cos x$$

In series $e^x \cos x$, coefficient of x^2 is $\frac{1}{2} \left(\frac{d^2 e^x \cos x}{dx^2} \right)_{x=0}$

$$y' = \frac{de^x \cos x}{dx} = e^x \cos x - e^x \sin x = y - e^x \sin x$$

$$\frac{d^2e^x\cos x}{dx^2} = y' - e^x\sin x - e^x\cos x = y - e^x\sin x - e^x\sin x - e^x\cos x$$

At
$$x = 0$$
,
$$\left. \left(\frac{d^2 e^x \cos x}{dx^2} \right) \right|_{x=0} = \left. \left(e^x \cos x - 2e^x \sin x - e^x \cos x \right) \right|_{x=0}$$
$$= \left. \left(-2e^{-x} \sin x \right) \right|_{x=0} = 0$$

So, The coefficient of $x^2 = \frac{1}{2}(0) = 0$

11. (c)

Given matrix is
$$M = \begin{bmatrix} 12+9i & -i \\ i & 12-9i \end{bmatrix}$$

Determinant of
$$M = \begin{vmatrix} 12+9i & -i \\ i & 12-9i \end{vmatrix} = (12+9i)(12-9i) + i^2$$

$$= (12^2-9^2i^2) + i^2$$

$$= 225-1$$

$$= 224$$

:. Inverse of
$$M = M^{-1} = \frac{1}{|M|} (adjM) = \frac{1}{224} \begin{bmatrix} 12 - 9i & i \\ -i & 12 + 9i \end{bmatrix}$$

12. (c)

$$\begin{vmatrix} 1 - \lambda & 2 \\ p & 5 - \lambda \end{vmatrix} = 0$$

$$(1 - \lambda)(5 - \lambda) - 2p = 0$$

$$\lambda^2 - 6\lambda + 5 - 2p = 0$$

Let the roots are λ_1 and λ_2 .

From the characteristic equation,

$$\lambda_1 + \lambda_2 = 6$$

$$\lambda_1 \lambda_2 = 5 - 2p \ge 0$$
 [For roots to be positive]
$$p \le \frac{5}{2}$$
 ... (i)

For roots to be real.

$$6^{2} - 4(5 - 2p) \ge 0$$

 $36 - 20 + 8p \ge 0$
 $p \ge -2$... (ii)

From equations (i) and (ii),

$$-2 \le p \le \frac{5}{2}$$

13. (b)

For non-trivial solution to exist,

$$\begin{vmatrix} 1 & -2 & 1 \\ k & -1 & 2 \\ 2 & -1 & 1 \end{vmatrix} = 0$$

$$-1 - 8 - k + 2 + 2 + 2k = 0$$

 $k = 5$

For
$$k = 5$$
,

$$x - 2y + z = 0$$

$$5x - y + 2z = 0$$

$$\frac{x}{-4+1} = \frac{y}{5-2} = \frac{z}{-1+10}$$

$$\frac{x}{-3} = \frac{y}{3} = \frac{z}{9}$$

$$x : y : z = -1 : 1 : 3$$

14. (b)

At extremum value $\frac{dy}{dx} = 0$

So,
$$\frac{dy}{dx} = \frac{p}{(x-4)(x-1)} - \frac{(px+q)[(x-4)+(x-1)]}{(x-4)^2(x-1)^2} = 0$$

 $x \neq 4, x \neq 1$

$$\frac{p(x-4)(x-1)-(px+q)[(x-4)+(x-1)]}{(x-4)^2(x-1)^2}=0$$

At x = 2,

$$p(2-4)(2-1)-(2p+q)\left[2-4+2-1\right]=0$$

$$-2p + 2p + q = 0$$

$$\Rightarrow$$
 $q = 0$

$$y(2) = \frac{2p}{(2-4)(2-1)} = -1$$

$$p = 1$$

 \Rightarrow The value of p & q are 1 and 0 respectively.

15. (d)

$$f(x) = 2x^{3} - 3x^{2} - 12x + 5$$

$$f'(x) = 6x^{2} - 6x - 12$$
For minima/maxima, $f'(x) = 0$

$$6x^{2} - 6x - 12 = 0$$

$$x^{2} - x - 2 = 0$$

$$(x + 1)(x - 2) = 0$$

$$x = -1, 2$$

$$f''(x) = 12x - 6$$

$$f''(-1) = -12 - 6 = -18 < 0 \implies \text{maxima}$$

$$f''(2) = 24 - 6 = 18 > 0 \implies \text{minima}$$

The function has maxima at x = -1 and minima at x = 2.

The function is decreasing between –1 and 2.

16. (b)

$$f(x) = \frac{\log_{\theta}(1+ax) - \log_{\theta}(1-bx)}{x}$$

For function to be continuous

$$f(0) = \lim_{x \to 0} f(x)$$

$$= \lim_{x \to 0} \frac{\log_e (1 + ax) - \log(1 - bx)}{x} = \lim_{x \to 0} \frac{\log_e (1 + ax) \times a}{ax} + \frac{\log(1 - bx) \times b}{-bx}$$

$$= a + b$$

17. (d)

$$u(x, y) = x^3 - 3xy^2 + 3x^2 - 3y^2$$

$$\frac{\partial u}{\partial x} = \frac{\partial v}{\partial y} = 3x^2 - 3y^2 + 6x$$

$$\frac{\partial u}{\partial y} = -\frac{\partial v}{\partial x} = -6xy - 6y$$

$$dv = \frac{\partial v}{\partial x} \cdot dx + \frac{\partial v}{\partial y} \cdot dy = -\frac{\partial u}{\partial y} dx + \frac{\partial u}{\partial x} dy$$

$$= (6xy + 6y)dx + (3x^2 - 3y^2 + 6x)dy$$

$$v = 3x^2y + 6xy - y^3 + C$$

18. (b)

$$\phi_{1} = ax^{2} - byz - (a + 2)x$$

$$\nabla \phi_{1} = [2ax - (a + 2)]\hat{i} - bz\hat{j} - by\hat{k}$$

$$\nabla \phi_{1}(1, -1, 2) = (a - 2)\hat{i} - 2b\hat{j} + b\hat{k}$$

$$\phi_{2} = 4x^{2}y + z^{3} - 4$$

$$\nabla \phi_{2} = 8xy\hat{i} + 4x^{2}\hat{j} + 3z^{2}\hat{k}$$

$$\nabla \phi_{2}(1, -1, 2) = -8\hat{i} + 4\hat{j} + 12\hat{k}$$

Since surfaces are orthogonal to each other at (1, -1, 2)

$$\nabla \phi_1 \cdot \nabla \phi_2 = 0$$

$$[(a-2)\hat{i} - 2b\hat{j} + b\hat{k}] \cdot [-8\hat{i} + 4\hat{j} + 12\hat{k}] = 0$$

$$-8(a-2)-8b+12b=0$$
 ... (i)

Also point (1, -1, 2) lies on the surface.

$$\Rightarrow$$

$$a \times 1 + 2b = (a+2)1$$

Putting this in equation 1, we get,

$$-8(a-2)-8+12=0$$

$$a-2 = -\frac{1}{8} \times (-4) = 0.5$$

19. (b)

z varies from 0 to $\frac{x^2 + y^2}{4}$; y varies from 0 to $\sqrt{16 - x^2}$; x varies from 0 to 4.

Volume =
$$\iiint dx dy dz = \int_{0}^{4} \int_{0}^{\sqrt{16-x^2}} \int_{0}^{\frac{x^2+y^2}{4}} dz dy dx$$
$$= \frac{1}{4} \int_{0}^{4} \int_{0}^{\sqrt{16-x^2}} (x^2 + y^2) dy dx = \frac{1}{4} \int_{0}^{4} \left(x^2 y + \frac{y^3}{3} \right) \Big|_{0}^{\sqrt{16-x^2}} dx$$
$$= \frac{1}{4} \int_{0}^{4} \left(x^2 \sqrt{16-x^2} + \frac{\left(\sqrt{16-x^2}\right)^3}{3} \right) dx$$

Let,

$$x = 4 \sin \theta$$
 $x \rightarrow 0$

$$dx = 4\cos\theta d\theta$$

$$\theta \rightarrow 0 \text{ to } \frac{\pi}{2}$$

Volume =
$$\frac{1}{4} \left[4^4 \int_0^{\pi/2} \sin^2 \theta \cos^2 \theta d\theta + \frac{4^4}{3} \int_0^{\pi/2} \cos^4 \theta d\theta \right]$$

= $\frac{1}{4} \left[4^4 \times \frac{\frac{3}{2} \times \frac{3}{2}}{2 \frac{6}{2}} + \frac{4^4}{3} \times \frac{\frac{5}{2} \times \frac{3}{2}}{2 \frac{6}{2}} \right]$
= $\frac{1}{4} \left[4^4 \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2!} \pi + \frac{4^4}{3} \times \frac{3}{2} \times \frac{1}{2} \times \frac{1}{2!} \times \pi \right]$
= $\frac{1}{4} \left[16\pi + 16\pi \right] = 8\pi = 25.13 \text{ unit}^3$

20. (c)

$$\frac{dT}{dt} = k(T-25)$$

T = Temperature of the body in °C and t = time in minutes.

$$\frac{dT}{T - 25} = kdt$$

$$\log (T - 25) = kt + C_1$$

$$T - 25 = Ce^{kt}$$

At t = 0, T = 100°C and at t = 1 minute, T = 75°C.

$$(100-25) = Ce^0$$

$$\Rightarrow$$
 $C = 75^{\circ}C$

$$50 = 75 e^k \quad \Rightarrow \qquad \qquad e^k = \frac{2}{3}$$

At t = 5 minutes, $T - 25 = 75 e^{k \times 5}$

$$T = 25 + 75 \times \left(\frac{2}{3}\right)^5 \approx 34.88^{\circ}C$$

21. (d)

$$AX = B$$

Augmented matrix, $[A:B] = \begin{bmatrix} -2 & 1 & 1 & : & l \\ 1 & -2 & 1 & : & m \\ 1 & 1 & -2 & : & n \end{bmatrix}$

$$R_3 \to R_3 + R_2 + R_1$$
:

$$|A:B| = \begin{vmatrix} -2 & 1 & 1 & : & l \\ 1 & -2 & 1 & : & m \\ 0 & 0 & 0 & : l+m+n \end{vmatrix}$$

Since,

$$l + m + n = 0$$

Rank of
$$[A:B] = 2$$

Rank of [A] = Rank of [A:B] = 2 < 3 (Number of variables)

 \Rightarrow Infinitely many solutions are possible.

22. (d)

$$c(y+c)^2 = x^3$$
 ...(i)

Differentiating, we get

$$2c(y+c)\frac{dy}{dx} = 3x^2$$

$$\Rightarrow \frac{2x^3}{(y+c)^2}(y+c)\frac{dy}{dx} = 3x^2$$
 \left(\tau \cdot c = \frac{x^3}{(y+c)^2}\right)

$$\Rightarrow \frac{2x^2}{V+C}\frac{dy}{dx} = 3x^2$$

$$\Rightarrow \frac{2x}{3} \left(\frac{dy}{dx} \right) = y + c$$

$$\Rightarrow \qquad c = \frac{2x}{3} \left(\frac{dy}{dx} \right) - y$$

Putting this value of 'c' in equation (i)

$$\left[\frac{2x}{3}\left(\frac{dy}{dx}\right) - y\right] \left[\frac{2x}{3}\frac{dy}{dx}\right]^2 = x^3$$

23. (c)

Suppose
$$y = \lim_{x \to \infty} \left(\frac{x+6}{x+1} \right)^{x+4}$$

$$\Rightarrow \qquad y = \lim_{x \to \infty} \left[\left(1 + \frac{5}{x+1} \right)^{\frac{x+1}{5}} \right]^{\frac{5(x+4)}{x+1}}$$

$$\Rightarrow ln y = \lim_{x \to \infty} \frac{5(x+4)}{(x+1)} ln \left(1 + \frac{5}{x+1}\right)^{\frac{x+1}{5}}$$
 ...(i)

 $\lim_{x\to\infty}\frac{5(x+4)}{(x+1)} \text{ is in the form of } \frac{\infty}{\infty} \text{ and } \lim_{x\to\infty}\ln\left(1+\frac{5}{x+1}\right)^{\frac{x+1}{5}} \text{ is in the form of } 0^{0}.$

Calculating the limits of both terms separately

$$\lim_{x \to \infty} 5 \frac{(x+4)}{(x+1)} = \lim_{x \to \infty} 5 \frac{\left(1 + \frac{4}{x}\right)}{\left(1 + \frac{1}{x}\right)} = 5 \frac{(1+0)}{(1+0)}$$

$$= 5$$

We can use direct result of $\lim_{t\to 0} (1+t)^{1/t} = e$...(ii)

$$\Rightarrow \lim_{x \to \infty} \ln \left[1 + \frac{5}{x+1} \right]^{\frac{x+1}{5}} = \ln(e)$$

$$= 1$$

$$\therefore \qquad \qquad \ln y = 5(1)$$

$$\Rightarrow \qquad \qquad y = e^{5}$$
...(iii)

24. (a)

Required probability = Chosen a defective bolt from Machine A + Chosen a defective bolt from Machine B + Chosen a defective bolt from Machine C

$$= \frac{1}{2} \times \frac{2}{100} + \frac{1}{4} \times \frac{2}{100} + \frac{1}{4} \times \frac{4}{100} = 0.25 \times 10^{-1} = 0.025$$

25. (a)

Probability =
$$\int_{2}^{\infty} f(x)dx$$
=
$$\int_{2}^{\infty} \left[\frac{1}{2} e^{-\frac{x}{2}} \right] dx$$
=
$$\left[-e^{-\frac{x}{2}} \right]_{2}^{\infty} = e^{-1} = 0.368$$

26. (c)

$$\sin y \, \frac{dy}{dx} = \cos y \, (1 - x \cos y)$$

$$\Rightarrow \qquad \sin y \frac{dy}{dx} - \cos y = -x \cos^2 y$$

$$\Rightarrow \frac{\sin y}{\cos^2 y} \frac{dy}{dx} - \frac{\cos y}{\cos^2 y} = -x$$

$$\Rightarrow \tan y \sec y \frac{dy}{dx} - \sec y = -x \qquad \dots (i)$$

 $\sec y = t$ Let

$$\Rightarrow \qquad \sec y \tan y \frac{dy}{dx} = \frac{dt}{dx} \qquad \dots (ii)$$

From equation (i) and (ii), we get

$$\frac{dt}{dx} - t = -x$$

Integrating factor =
$$e^{\int -dx} = e^{-x}$$

Multiplying the equation by the integrating factor

$$\Rightarrow \qquad e^{-x} \frac{dt}{dx} - e^{-x}t = -xe^{-x}$$

$$\Rightarrow \qquad te^{-x} = \int -xe^{-x}dx = xe^{-x} + e^{-x} + C$$

$$\therefore \qquad \qquad \sec y = (x+1) + ce^x$$

27. (c)

$$f(t) = (t+1)^{2}$$

$$\Rightarrow \text{Laplace} \{f(t)\} = L(t^{2}) + L(2t) + L(1)$$

$$= \frac{2}{s^{3}} + \frac{2}{s^{2}} + \frac{1}{s}$$

28. (c)

The matrix formed by the coefficients is $\begin{bmatrix} a & 1 & 2 \\ 1 & 2 & 1 \\ 2 & 1 & a \end{bmatrix}$

Determinant =
$$2a^2 - 2a - 4$$

$$D = 0 \text{ for } a = 2 \text{ or } a = -1$$

(A) If $D \neq 0$, then the system will have unique solution.

(B) If
$$a = 2$$
, the matrix formed by the coefficients is
$$\begin{bmatrix} 2 & 1 & 2 \\ 1 & 2 & 1 \\ 2 & 1 & 2 \end{bmatrix}$$



The rank of matrix is 2.

Considering 'z' as side unknown.

The characteristic determinant will be
$$\begin{bmatrix} 2 & 1 & 0 \\ 1 & 2 & b \\ 2 & 1 & 0 \end{bmatrix}$$

The determinant of this is 0.

The system will have infinite solutions when a = 2.

(C) If
$$a = -1$$
, the matrix formed by the coefficients is
$$\begin{bmatrix} -1 & 1 & 2 \\ 1 & 2 & 1 \\ 2 & 1 & -1 \end{bmatrix}$$

Its rank is 2.

Considering 'z' as side unknown.

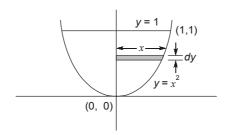
The characteristic matrix is
$$\begin{bmatrix} -1 & 1 & 0 \\ 1 & 2 & b \\ 2 & 1 & 0 \end{bmatrix}$$

The determinant of this matrix is 3b.

The system will have no solution if $b \neq 0$

 \therefore For a = -1 and $b \neq 0$, the system will have no solution.

29. (b)



$$y = x^2$$
 and $y = 1$ intesect at $(1, 1)$

Small disk of radius 'x' and depth 'dy' are integrated to compute the volume

Volume =
$$\int_{0}^{1} \pi x^{2} dy$$

$$= \int_{0}^{1} \pi y dy = \pi \left[\frac{y^{2}}{2} \right]_{0}^{1} = \frac{\pi}{2}$$

$$(\because y = x^{2})$$

30. (a)

Required probability =
$$\frac{\text{Favorable outcomes}}{\text{Total possible outcomes}}$$

Probability of selecting a false coin =
$$\frac{1}{4}$$

Probability of getting a tail on every flip of false coin = 1.

$$\therefore \qquad \text{Favorable outcomes} = \frac{1}{4} \times 1 = \frac{1}{4}$$

Probability of selecting a fair coin
$$=$$
 $\frac{3}{4}$

Probability of flipping a fair coin 4 times and getting

tails every time =
$$\left(\frac{1}{2}\right)^4 = \frac{1}{16}$$

$$\therefore \qquad \text{Unfavourable outcomes} = \frac{3}{4} \times \frac{1}{16} = \frac{3}{64}$$

Total possible outcomes =
$$\frac{1}{4} + \frac{3}{64} = \frac{19}{64}$$

$$\therefore \qquad \text{Required probability} = \frac{\frac{1}{4}}{\frac{19}{64}} = \frac{16}{19} \approx 0.84$$