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# **FLUID MECHANICS**

# CIVIL ENGINEERING

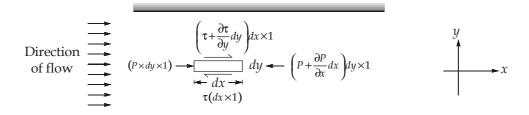
Date of Test: 14/09/2025

# **ANSWER KEY** ➤

1.	(b)	7.	(a)	13.	(b)	19.	(c)	25.	(c)
2.	(d)	8.	(b)	14.	(b)	20.	(d)	26.	(d)
3.	(d)	9.	(b)	15.	(a)	21.	(a)	27.	(d)
4.	(a)	10.	(a)	16.	(d)	22.	(a)	28.	(d)
5.	(c)	11.	(d)	17.	(c)	23.	(b)	29.	(a)
6.	(d)	12.	(b)	18.	(b)	24.	(c)	30.	(c)

# **DETAILED EXPLANATIONS**

## 1. (b)



For steady and uniform flow, there is no acceleration and hence ressultant force in the direction of flow is zero

$$P \times (dy \times 1) - \left(P + \frac{\partial P}{\partial x} dx\right) dy \times 1 - \tau (dx \times 1) + \left(\tau + \frac{\partial \tau}{\partial y} dy\right) dx \times 1 = 0$$

$$\frac{\partial P}{\partial x} = \frac{\partial \tau}{\partial y}$$

The pressure gradient in the direction of flow is equal to the shear gradient normal to the direction of flow.

# 2. (d)

Given:  $D_1$  = 200 mm,  $D_2$  = 400 mm Velocity in smaller diameter pipe,

$$V_1 = \frac{Q}{A_1} = \frac{0.250 \text{ m}^3/\text{s}}{\frac{\pi}{4} \times (0.2)^2} = 7.96 \text{ m/s}$$

Velocity in larger diameter pipe,

$$V_2 = \frac{Q}{A_2} = \frac{0.250 \text{ m}^3/\text{s}}{\frac{\pi}{4} \times (0.4)^2} = 1.99 \text{ m/s}$$

Loss of head due to sudden enlargement is given by,

$$h_L = \frac{(V_1 - V_2)^2}{2g} = \frac{(7.96 - 1.99)^2}{2g} = 1.817 \text{ m of water}$$

## 3. (d)

Since  $\overline{GM}_{\text{rolling}} \ll \overline{GM}_{\text{pitching}}$ 

Hence the stability of ship in rolling is more critical compared to pitching. Higher the period of oscillation, more comfort the passengers will feel.

## 4. (a)

$$dQ = |d\psi| = |\psi_2 - \psi_1|$$
At (1, 1); 
$$\psi_1 = 3 \times 1^2 \times 1 - 1^3 = 2 \text{ units}$$
At  $(\sqrt{3}, 1)$ ; 
$$\psi_2 = 3 \times (\sqrt{3})^2 \times 1 - 1^3 = 8 \text{ units}$$
So, 
$$dQ = |8 - 2| = 6 \text{ units}$$

### 5. (c)

When  $\frac{dh}{dx} > 0$ , it means that depth of water increases in the direction of flow. The profile of water so obtained is called back water curve.

When  $\frac{dh}{dx} < 0$ , it means that the depth of water decrease in the direction of flow. The profile of the water so obtained is called drop down curve.

### 6. (d)

Momentum thickness,  $\theta$  is given by

$$\theta = \int_{0}^{\delta} \frac{u}{U} \left( 1 - \frac{u}{U} \right) dy$$

$$\theta = \int_{0}^{\delta} \left\{ \left( \frac{2y}{\delta} \right) - \frac{y^{2}}{\delta^{2}} \right\} \left\{ 1 - \frac{2y}{\delta} + \frac{y^{2}}{\delta^{2}} \right\} dy$$

$$= \int_{0}^{\delta} \left[ \frac{2y}{\delta} - \frac{4y^{2}}{\delta^{2}} + \frac{2y^{3}}{\delta^{3}} - \frac{y^{2}}{\delta^{2}} + \frac{2y^{3}}{\delta^{3}} - \frac{y^{4}}{\delta^{4}} \right] dy$$

$$= \int_{0}^{\delta} \left[ \frac{2y}{\delta} - \frac{5y^{2}}{\delta^{2}} + \frac{4y^{3}}{\delta^{3}} - \frac{y^{4}}{\delta^{4}} \right] dy$$

$$= \left[ \frac{2y^{2}}{2\delta} - \frac{5y^{3}}{3\delta^{2}} + \frac{4y^{4}}{4\delta^{3}} - \frac{y^{5}}{5\delta^{4}} \right]_{0}^{\delta}$$

$$= \left[ \delta - \frac{5\delta}{3} + \delta - \frac{\delta}{5} \right] = \frac{2\delta}{15}$$

# 7.

Equating pressure at interface level,

$$P_A + \rho_0 g(0.15) = \rho_{Hg} g(0.1)$$

where  $\rho_0$  is density of oil and  $\rho_{\textit{Hg}}$  is density of mercury

$$\Rightarrow P_A + (0.85 \times 10^3) \times g \times 0.15 = (13.6 \times 10^3) \times g \times 0.10$$

$$\Rightarrow P_A = 12090.825 \text{ N/m}^2$$

$$= 12.09 \text{ kN/m}^2$$

$$P_A = 12090.825 \text{ N/n}$$
= 12.09 kN/m<sup>2</sup>

# 8.

Since the pipes are connected in series

$$\frac{L}{d^5} = \frac{L_1}{d_1^5} + \frac{L_2}{d_2^5}$$

$$\Rightarrow \frac{800}{d^5} = \frac{300}{400^5} + \frac{500}{300^5}$$

$$d^{3} = 400^{3} = 300^{4}$$

$$\Rightarrow d^{5} = 3.403 \times 10^{12}$$

$$\Rightarrow$$
  $d = 320.91 \text{ mm}$ 

# 9. (b)

Buoyancy force acts through center of gravity of displaced liquid.

A large metacentric height in a vessel improves stability and makes time period of oscillation shorter.

# 10. (a)

Consider an annular ring with thickness dr at radius r. Velocity variation in the gap is given as linear

Hence the velocity at radius r from centre = v = wr

:. Shear stress on the ring,

$$\tau = \mu \frac{du}{dy} = \mu \left( \frac{wr}{h} \right)$$

Force on the ring,

$$dF = \tau \times dA$$

$$= \left(\frac{\mu w r}{h}\right) \times 2\pi r dr = \left(\frac{2\pi \mu w}{h}\right) r^2 dr$$

Torque on the ring,  $dT = F \times r = r\tau dA = \left(\frac{2\pi\mu w}{h}\right)r^2 \cdot rdr$ 

$$= \left(\frac{2\pi\mu w}{h}\right) r^3 dr$$

 $\therefore \quad \text{Total torque on disc} = \int_{0}^{R} dT = \frac{2\pi\mu w}{h} \int_{0}^{R} r^{3} dr$ 

$$T = \frac{2\pi\mu w}{h} \left[ \frac{r^4}{4} \right]_0^R = \frac{\pi\mu w R^4}{2h}$$

## 11. (d)

Given,  $\theta = 60^{\circ}$ 

Distance, 
$$AC = \frac{h}{\sin 60^{\circ}} = \frac{2h}{\sqrt{3}}$$

The gate will start tipping about hinge B if the resultant pressure force acts at B. If the resultant pressure force passes through a point which is lying from B to C anywhere on the gate, the gate will tip over the hinge. Hence for the given position, point B becomes the centre of pressure.

Depth of centre of pressure,

$$h^* = (h - 3) \text{ m}$$
 ...(i)

But  $h^*$  is also given by,  $h^* = \frac{I_G \sin^2 \theta}{A\overline{h}} + \overline{h}$ 

Taking width of gate unity, then

Area, 
$$A = AC \times 1 = \frac{2h}{\sqrt{3}} \times 1; \ \overline{h} = \frac{h}{2}$$

$$I_G = \frac{bd^3}{12} = \frac{1 \times AC^3}{12} = \frac{1 \times \left(\frac{2h}{\sqrt{3}}\right)^3}{12} = \frac{8h^3}{12 \times 3 \times \sqrt{3}} = \frac{2h^3}{9 \times \sqrt{3}}$$

...(ii)

$$h^* = \frac{2h^3}{9\sqrt{3}} \times \frac{\sin^2 60}{\frac{2h}{\sqrt{3}}} \times \frac{h}{2} + \frac{h}{2}$$

$$\rightarrow$$

$$h^* = \frac{2h^3 \times \frac{3}{4}}{9h^2} + \frac{h}{2} = \frac{2h}{3}$$

From (i) and (ii)

$$h - 3 = \frac{2h}{3}$$
$$h = 9 \text{ m}$$

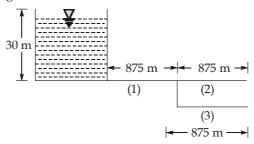
 $\Rightarrow$ 

: Height of water required for tipping the gate = 9 m

# 12.

Let Q be the initial discharge.

Diameter, d = 0.55 m, Length, l = 1.75 km = 1750 m



Before addition of pipe,
$$h_f = \frac{8flQ^2}{\pi^2 gD^5}$$
 ... (i)

 $\Rightarrow$ 

$$30 = \frac{8(0.04) \times (1750)Q^2}{\pi^2 (9.81) \times (0.55)^5}$$

$$Q = 0.51 \,\text{m}^3/\text{sec}$$

After addition of pipe,  $h_f = h_{f1} + h_{f2}$ 

... (ii)

Where,  $h_{f2}$  is Head loss in pipe 2,  $h_{f3}$  is Head loss in pipe 3

Also,

$$h_{f2} = h_{f3}$$

*:*.

$$\frac{f l_2 v_2^2}{2g D_2} = \frac{f l_3 v_3^2}{2g D_3}$$

$$v_2 = v_3$$

Also, let Q' be the final discharge

Now,

$$Q' = Q_2 + Q_3$$

$$Q_2 = Q_3$$

[∵ Continuity equation]

::

$$Q_2 = Q_3$$

$$[:: V_2 = V_{3}, A_2 = A_3]$$

 $\Rightarrow$ 

$$Q_2 = Q_3 = \frac{Q'}{2}$$

Substituting values in (ii)

$$h_f = \frac{8fl_1Q'^2}{\pi^2gD_1^5} + \frac{8fl_2(Q'/2)^2}{\pi^2gD_2^5}$$

$$30 = \frac{8 \times 0.04 \times 875}{\pi^2 \times 9.81 \times 0.55^5} \left( Q'^2 + \frac{Q'^2}{4} \right)$$

Solving,

$$Q' = 0.65 \,\mathrm{m}^3/\mathrm{s}$$

% increase = 
$$\frac{Q'-Q}{Q} \times 100 = \frac{0.65-0.51}{0.51} \times 100 = 27.45\%$$

13. (b)

Given, 
$$b = 10 \text{ m} , \qquad y = 3 \text{ m}$$
 
$$V = 1 \text{ m/s}$$
 Bed slope, 
$$S_0 = \frac{1}{4000}$$

Slope of energy line,  $S_f = 0.00004$ 

Change of depth flow of flow along the channel,

Now, 
$$\frac{dy}{dx} = \frac{S_0 - S_f}{1 - F_r^2}$$

$$\Rightarrow \frac{dy}{dx} = \frac{S_0 - S_f}{1 - \frac{V^2}{gy}} = \frac{0.00025 - 0.00004}{1 - \frac{(1)^2}{9.81 \times 3}} = \frac{0.00021}{0.966} = 2.17 \times 10^{-4}$$

14. (b)

Velocity before expansion,  $V_1 = 2.65 \text{ m/s}$ 

Velocity after expansion  $V_2 = 1.18 \text{ m/s}$ 

Loss of load at sudden expansion

$$H_L = \frac{(V_1 - V_2)^2}{2 \times g} = \frac{(2.65 - 1.18)^2}{2 \times 9.81} = 0.11$$

By energy equation

$$\frac{p_1}{\rho g} + \frac{V_1^2}{2g} + z = \frac{p_2}{\rho g} + \frac{V_2^2}{2g} + z + H_L$$

$$\Rightarrow \frac{p_2}{\rho g} = \frac{p_1}{\rho g} + \frac{V_1^2}{2g} - \frac{V_2^2}{2g} - H_L$$

$$\Rightarrow \frac{p_2}{1000 \times 9.81} = \frac{20 \times 1000}{9.81 \times 1000} + \frac{2.65^2}{2 \times 9.81} - \frac{1.18^2}{2 \times 9.81} - 0.11$$

$$p_2 = 21.735 \text{ kN/m}^2$$

$$\approx 21.74 \text{ kN/m}^2$$
Increase in pressure =  $(21.74 - 20) \text{ kN/m}^2$ 

$$= 1.74 \text{ kN/m}^2$$

15. (a)

Given, H = 6 m, x = 2 m and y = 0.18 m

Now, Coefficient of velocity, 
$$C_V = \frac{x}{2\sqrt{y.H}} = \frac{2}{2\sqrt{0.18 \times 6}} = 0.962$$

Discharge,  $Q = C_d \times A \times \sqrt{2gH}$ Now,

where 'Q' is  $4 \times 10^{-3}$  m<sup>3</sup>/s

$$\Rightarrow \qquad 4 \times 10^{-3} = C_d \times \frac{\pi \times 0.03^2}{4} \times \sqrt{2 \times 9.81 \times 6}$$

$$\Rightarrow$$
  $C_d = 0.52$ 

$$C_d = 0.522$$
Now,
$$C_d = C_V \times C_C$$

where  $C_C$  is coefficient of contraction

$$\Rightarrow C_C = \frac{C_d}{C_v} = \frac{0.522}{0.962} = 0.543$$

#### 16. (d)

On the quadrant part,

Horizontal component of hydrostatic force,

$$F_H = \gamma \text{ (Projected area)} \times \overline{h} = 9.81 \times 10^3 \times 1.2 \times 2.5 \times \left(1.5 + \frac{1.2}{2}\right)$$
  
= 61803 N = 61.8 kN

Vertical component of hydrostatic force,

 $F_V = \gamma$  [Volume of water above the curved surface upto free surface of water level]

= 
$$9.81 \times 10^3 \left[ 1.2(2.7) - \frac{\pi (1.2)^2}{4} \right] \times 2.5$$
  
=  $51723.88 = 51.72 \text{ kN}$ 

$$\theta = \tan^{-1} \left( \frac{F_H}{F_V} \right) = \tan^{-1} \left( \frac{61.8}{51.72} \right)$$

$$\theta = 50.07^{\circ}$$



$$u = V_0 \sin \frac{\pi}{2} \left( \frac{y}{\delta} \right)$$

$$\frac{du}{dy} = V_0 \cos \frac{\pi}{2} \left( \frac{y}{\delta} \right) \times \frac{\pi}{2\delta}$$

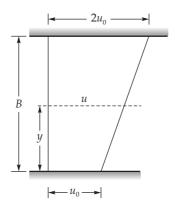
Local shear stress, 
$$\tau_0 = \mu \left(\frac{du}{dy}\right)_{y=0} = \mu \times \frac{V_0 \pi}{2\delta} = 1.02 \times 10^{-3} \times \frac{0.20 \times \pi}{2 \times 8 \times 10^{-3}}$$
$$= 0.04 \text{ N/m}^2$$

For rough pipe, 
$$\frac{1}{\sqrt{f}} = 2\log_{10}\left(\frac{R}{k_s}\right) + 1.74 = 2\log_{10}\left(\frac{0.30}{0.20 \times 10^{-3}}\right) + 1.74 = 8.09$$
 
$$f = 0.015$$
 
$$\tau_{\text{wall}} = \rho \frac{f V^2}{8}$$

where, 
$$V = V_{\text{avg}} = \frac{Q}{A} = \frac{0.64}{\frac{\pi}{4} \times 0.6^2} = 2.264 \text{ m/s}$$

$$\tau_{wall} = \frac{1000 \times 0.015 \times 2.264^{2}}{8} = 9.61 \text{ N/m}^{2}$$

19. (c)



Velocity profile is given by:  $u = u_0 \left( 1 + \frac{y}{B} \right)$ 

$$u_{\text{avg}} = \frac{\int u dA}{A} = \frac{\int_0^B u_0 \left(1 + \frac{y}{B}\right) (dy \times 1)}{(B \times 1)}$$

Let, 
$$\left(1 + \frac{y}{B}\right) = t$$

$$\therefore \qquad dy = Bdt$$

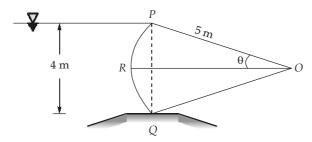
At 
$$y = 0 \Rightarrow t = 1$$
  
At,  $y = B \Rightarrow t = 2$ 

$$u_{\text{avg}} = \frac{u_0}{B} \times B \int_1^2 t dt = \frac{3u_0}{2} = 1.5u_0$$

 $\therefore \text{ Kinetic energy correction factor,} \alpha = \frac{\int u^3 dA}{u_{avo}^3 A} = \frac{\int_0^B u_0^3 \left(1 + \frac{y}{B}\right)^3 \left(dy \times 1\right)}{\left(1.5u_0\right)^3 \times (B \times 1)}$  $= \frac{u_0^3 B}{(1.5u_0)^3 \times B} \int_1^2 t^3 dt = \frac{1}{(1.5)^3} \times \frac{15}{4} = \frac{10}{9} = 1.11$ 

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# 20. (d)



Consider the gate width as 1 m

$$\sin \theta = \frac{2}{5}$$
,  $\theta = 23.57^{\circ}$ 

$$F_{H} = \gamma \times (\text{Projected area}) \times \overline{h} = 9.81 \times (4 \times 1) \times \frac{4}{2} = 78.48 \text{ kN}$$

$$F_{V} = \gamma \times \Psi = \gamma \times \text{Area}[\text{Sector POQR - Triangle POQ}]$$

$$= 9.81 \times \left[\pi \times 5^{2} \times \left(\frac{2 \times 23.57}{360}\right) - \frac{1}{2} \times 4 \times 5 \cos 23.57^{\circ}\right] = 10.97 \text{ kN}$$

$$F_{V} = \sqrt{F_{H}^{2} + F_{V}^{2}} = \sqrt{(78.48)^{2} + (10.97)^{2}} = 79.24 \text{ kN}$$

# 21. (a)

Total head loss,  $h_L = \frac{\left(V_1 - V_2\right)^2}{2g}$ 

Also 
$$Q = A_1 V_1 = A_2 V_2$$
;

$$d_1^2V_1 = d_2^2V_2$$

$$10^2V_1 = 20^2V_2$$

$$V_1 = 4V_2$$

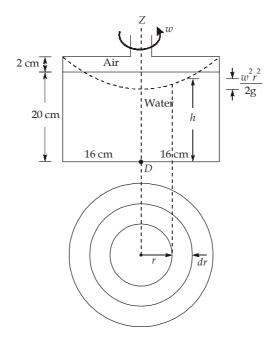
$$Q_1 = Q_2 = Q = 0.1 \text{ m}^3/\text{sec}$$

$$Q = A_1V_1 = A_2V_2$$

$$\Rightarrow 0.1 = \frac{\pi}{4}(0.1)^2V_1 \Rightarrow V_1 = 12.73 \text{ m/s}$$
And,
$$0.1 = \frac{\pi}{4}(0.2)^2V_2 \Rightarrow V_2 = 3.18 \text{ m/s}$$

$$h_L = \frac{(12.73 - 3.18)^2}{2 \times 9.81} = 4.65 \text{ m}$$

# 22. (a)



 $\therefore$  Water just touches point *A* 

$$\therefore 0.04 = \frac{w^2(0.16)^2}{2g}$$

 $dF = Pressure \times Area = \rho gh \times 2\pi r dr$ 

$$F = \int dF = \int \rho g \left( 0.18 + \frac{w^2 r^2}{2g} \right) \times 2\pi r dr$$

$$\Rightarrow F = 2\pi\rho g \int_{0}^{0.16} \left( 0.18 + \frac{w^{2}r^{2}}{2g} \right) r dr$$

$$= 2\pi\rho g \left[ \frac{0.18r^{2}}{2} + \frac{w^{2}}{2g} \times \frac{r^{4}}{4} \right]_{0}^{0.16}$$

$$= 2\pi\rho g \left[ 0.09(0.16)^{2} + \frac{w^{2}(0.16)^{2}}{2g} + \frac{(0.16)^{2}}{4} \right] = 157.8 \text{ N}$$

# 23. (b)

Let x be the distance from the leading edge such that the drag force in distance x is one-third of the total drag force.

$$F_{Dx} = \frac{1}{3} F_{DL} = C_{D_{fx}} (Bx) \left( \frac{\rho U^2}{2} \right)$$
$$F_{DL} = C_{D_{fL}} (BL) \left( \frac{\rho U^2}{2} \right)$$

$$\frac{C_{Dfx}}{C_{DfL}} \frac{x}{L} = \frac{F_{Dx}}{F_{DL}} = \frac{1}{3}$$
But from  $C_{Dfx} = \frac{1.328}{\sqrt{Ux/V}}$ 

$$C_{DfL} = \frac{1.328}{\sqrt{UL/V}}$$

$$\therefore \left(\frac{L}{x}\right)^{1/2} \frac{x}{L} = \frac{1}{3}$$

$$\Rightarrow \left(\frac{x}{L}\right)^{1/2} = \frac{1}{3}$$

# 24. (c)

For a function to be a valid potential function for incompressible flow, it must satisfy laplace equation i.e.,  $\nabla^2 \phi = 0$ .

# Checking for option (a):

$$\phi = A \log_{e} xy = A[\log_{e} x + \log_{e} y]$$

$$\frac{\partial \phi}{\partial x} = \frac{A}{x}; \quad \frac{\partial^{2} \phi}{\partial x^{2}} = -\frac{A}{x^{2}}$$

$$\frac{\partial \phi}{\partial y} = \frac{A}{y}; \quad \frac{\partial^{2} \phi}{\partial^{2} x} = -\frac{A}{y^{2}}$$

$$\nabla^{2} \phi = \frac{\partial^{2} \phi}{\partial x^{2}} + \frac{\partial^{2} \phi}{\partial y^{2}} = \left(-\frac{A}{x^{2}}\right) + \left(-\frac{A}{y^{2}}\right) \neq 0 \quad \text{(Not OK)}$$

 $x = \frac{L}{\Omega}$ 

Checking for option (b):

$$\phi = A(\cos x + \sin y)$$

$$\therefore \frac{\partial \phi}{\partial x} = A(-\sin x); \quad \frac{\partial^2 \phi}{\partial x^2} = -A\cos x$$

$$\therefore \frac{\partial \phi}{\partial y} = A\cos y; \quad \frac{\partial^2 \phi}{\partial y^2} = -A\sin y$$

$$\therefore \nabla^2 \phi = \frac{\partial^2 \phi}{\partial x^2} + \frac{\partial^2 \phi}{\partial y^2} = -A(\cos x + \sin y) \neq 0 \text{ (Not OK)}$$

Checking for option (c):

$$\phi = \frac{A}{2}(x^2 - y^2)$$

$$\frac{\partial \phi}{\partial x} = Ax; \qquad \frac{\partial^2 \phi}{\partial x^2} = A$$

:.

$$\frac{\partial \phi}{\partial y} = -Ay;$$
  $\frac{\partial^2 \phi}{\partial y^2} = -A$ 

$$\nabla^2 \phi \ = \ \frac{\partial^2 \phi}{\partial x^2} + \frac{\partial^2 \phi}{\partial y^2} = A + (-A) = 0 \ \ (OK)$$

Correct option is (c).

#### 25. (c)

$$Re_L = \frac{v \times L}{v} = \frac{12 \times 0.8}{1.47 \times 10^{-5}} = 653061.2245 > 5 \times 10^5$$

:. Turbulent flow

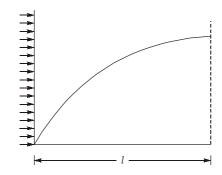
So, for turbulent flow, boundary layer thickness,

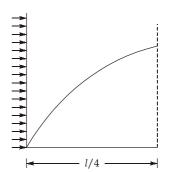
$$\delta = \frac{0.376x}{(\text{Re}_x)^{1/5}} = \frac{0.376 \times L}{(\text{Re}_L)^{1/5}}$$

$$\Rightarrow \qquad \delta = \frac{0.376 \times 0.8}{(653061.2245)^{1/5}} = 0.02067 \,\mathrm{m}$$

$$\delta = 2.067 \, \text{cm}$$

### 26. (d)





For laminar flow,

$$C_{\rm D} = \frac{0.664}{\sqrt{\text{Re}}}$$

where,

$$Re = \frac{Ul}{v}$$

$$C_D = \frac{0.664}{\sqrt{\frac{Ul}{v}}}$$

$$C_D \propto \frac{1}{\sqrt{l}}$$

$$C_D \sqrt{l}$$
 = Constant

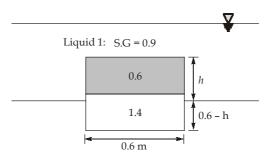
$$C_{D,1}\sqrt{l_1} = C_{D,2}\sqrt{l_2}$$

$$\frac{C_{D,1}}{C_{D,2}} = \sqrt{\frac{l_2}{l_1}}$$

$$\frac{C_{D,1}}{C_{D,2}} = \sqrt{\frac{l/4}{l}}$$

$$\frac{C_{D,1}}{C_{D,2}} = \sqrt{\frac{l}{4}} = 0.5$$

# 27. (d)



Liquid 2: S.G = 1.2

Buoyant force, 
$$F_B = \text{Weight of fluid displaced}$$
  
 $\Rightarrow F_B = [(0.9 \times 9.81) \times 0.6 \times 0.6 \times h] + [(1.2 \times 9.81) \times 0.6 \times 0.6 \times (0.6 - h)]$   
Now,  $F_B = (-1.0595h + 2.5428) \text{ kN}$ 

Weight of block = 
$$(1.4 \times 9.81 \times 0.6 \times 0.6 \times 0.3) + (0.6 \times 9.81 \times 0.6 \times 0.6 \times 0.3)$$
  
=  $2.11896 \text{ kN}$ 

For stable equilibrium,

Weight of block = Buoyant force  
⇒ 
$$2.11896 = -1.0595h + 2.5428$$
  
⇒  $h = \frac{2.5428 - 2.1189}{1.0595}$   
⇒  $h = 0.4 \text{ m} = 40 \text{ cm}$ 

28. (d)

Given: 
$$L_r = \frac{L_m}{L_p} = \frac{1}{3}, V_p = 900 \text{ kmph,}$$
 
$$\rho_p = 1.582 \text{ kg/m}^3$$
 
$$\mu_p = 1.474 \times 10^{-5} \text{ kg/m.s}$$
 
$$\rho_m = 999.7 \text{ kg/m}^3, \mu_m = 1.307 \times 10^{-3} \text{ kg/m.s}$$

Since, in the given condition viscous forces are predominant.

$$\therefore \text{ For dynamic similarity,} (\text{Re})_{\text{m}} = (\text{Re})_{p}$$

$$\Rightarrow \frac{\rho_{m}V_{m}L_{m}}{\mu_{m}} = \frac{\rho_{p}V_{p}L_{p}}{\mu_{p}}$$

$$\Rightarrow V_{m} = \frac{\mu_{r} \cdot V_{p}}{L_{r} \cdot \rho_{r}} = \left(\frac{\rho_{p}V_{p}L_{p}}{\mu_{p}}\right) \times \left(\frac{\mu_{m}}{L_{m}\rho_{m}}\right)$$

$$V_{m} = \left(\frac{1.582 \times 900 \times 3L_{m}}{1.474 \times 10^{-5}}\right) \times \left(\frac{1.307 \times 10^{-3}}{999.7 \times L_{m}}\right)$$

$$\Rightarrow V_{m} = 378.86 \text{ kmph} \approx 379 \text{ kmph}$$

#### 29. (a)

According to principle of manometry,

$$\begin{array}{lll} P_1 + \rho_1 g(2+0.5) - \rho_{\rm Hg} & \times g \times 0.5 - \rho_1 g(2) = P_2 \\ \Rightarrow & P_1 - P_2 = \rho_{\rm Hg} \times g \times 0.5 - \rho_1 g(0.5) \\ \Rightarrow & P_1 - P_2 = 0.5 \times g \; (\rho_{\rm Hg} - \rho_1) = 0.5 \times g \times (S_{Hg} - S_1) \rho_w \\ \Rightarrow & P_1 - P_2 = 0.5 \times 9.81 \; (13.6 - 0.8) \times 1000 \; {\rm Pa} \\ \Rightarrow & P_1 - P_2 = 62784 \; {\rm Pa} \simeq 62.78 \; {\rm kPa} \end{array}$$

#### 30. (c)

Applying Bernoulli's equation between 1 and 2

$$\frac{p_1}{\rho g} + \frac{V_1^2}{2g} + Z_1 = \frac{p_2}{\rho g} + \frac{V_2^2}{2g} + Z_2$$
As
$$p_1 = p_2 = P_{\text{atm}}$$

$$V_1 = 0 \quad \text{(Free surface of reservoir)}$$

$$Z_1 = \frac{V_2^2}{2g} + Z_2$$

$$\Rightarrow \frac{V_2^2}{2g} = Z_1 - Z_2 = 0.6 - (-0.25) = 0.85$$

 $V_2^2 = 2g \times 0.85$ 

 $V_2 = \sqrt{2 \times 9.81 \times 0.85}$ 

 $V_2 = 4.08 \text{ m/s} \simeq 4.1 \text{ m/s}$