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## **OPEN CHANNEL FLOW**

## **CIVIL ENGINEERING**

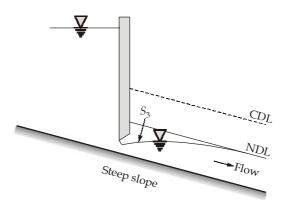
Date of Test: 06/09/2025

#### ANSWER KEY >

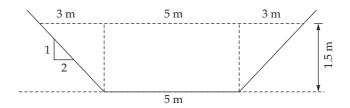
1.	(d)	6.	(b)	11.	(a)	16.	(d)	21.	(a)	
2.	(d)	7.	(c)	12.	(d)	17.	(b)	22.	(c)	
3.	(c)	8.	(b)	13.	(a)	18.	(a)	23.	(c)	
4.	(b)	9.	(b)	14.	(b)	19.	(a)	24.	(c)	
5.	(b)	10.	(a)	15.	(c)	20.	(b)	25.	(d)	

## **DETAILED EXPLANATIONS**

#### 1. (d)



- 2. (d)
- 3. (c)



Froude Number,

$$Fr = \frac{V}{\sqrt{gD}}$$

$$m = 2$$
,  $b = 5$  m,  $y = 1.5$  m

Cross-sectional area of the flow,

$$A = (b + my) y$$

$$\Rightarrow$$
  $A =$ 

$$A = (5 + 2 \times 1.5) \times 1.5$$

$$= 12 \text{ m}^2$$

Top width of flow,

$$T = 5 + 3 + 3 = 11 \text{ m}$$

Hydraulic depth,

$$D = \frac{A}{T} = \frac{12}{11} = 1.09 \text{ m}$$

$$Q = VA$$

 $\Rightarrow$ 

$$V = \frac{15}{12} = 1.25 \text{ m/s}$$

*:*.

$$Fr = \frac{1.25}{\sqrt{9.81 \times 1.09}} = 0.382 < 1$$

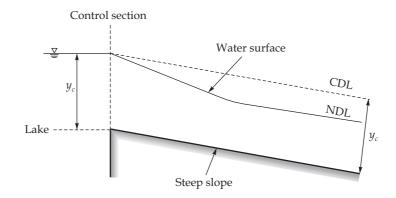
:. The flow is subcritical or tranquil flow.

#### 4. (b)

At the entrance to the steep channel, a control section exists i.e., the flow into the channel takes place at the critical depth,  $y_c$ . The water surface then joins the normal depth line as shown in figure.

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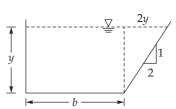
Critical depth, 
$$y_c = \left(\frac{q^2}{g}\right)^{1/3}$$

Given data: 
$$Q = 35 \text{ m}^3/\text{s}, b = 4 \text{ m}, g = 9.81 \text{ m/s}^2$$

$$Q = \frac{Q}{B} = \frac{35}{4} = 8.75 \text{ m}^3/\text{s/m}$$

$$y_{c} = \left[ \frac{(8.75)^{2}}{9.81} \right]^{1/3} = 1.9836 \text{ m} \approx 1.98 \text{ m}$$

#### 5. (b)



Given data: 
$$Q = 20 \text{ m}^3/\text{s}$$

$$V = 2 \,\mathrm{m/s}$$

$$n = 0.015$$

Manning's formula,  $V = \frac{1}{n}R^{2/3}S_0$ 

$$\Rightarrow S_0^{1/2} = \frac{nV}{R^{2/3}}$$

$$R = \frac{A}{P}$$

For minimum bed slope  $(S_0)$ , since V is constant at 2 m/s, it is the hydraulic radius R which has to be maximum. As the area of flow (A) is fixed at  $10 \text{ m}^2$ , the condition of minimum bed slope boils down to minimum wetted perimeter

$$S_0 \propto \frac{1}{R} \propto \frac{P}{A}$$

Cross-sectional area,  $A = \frac{Q}{V} = \frac{20}{2} = 10 \text{ m}^2$ 

$$A = b \times y + \frac{1}{2} \times y \times 2y = by + y^2 \dots (i)$$

Perimeter, 
$$P = b + y + \sqrt{y^2 + (2y)^2} = b + y + \sqrt{5}y$$
 ...(ii)

Using eq. (i),  $b = \frac{A - y^2}{y} = \frac{A}{y} - y$ 

Substituting *b* in eq. (ii)  $P = \frac{A}{y} - y + y + \sqrt{5}y$ 

$$\Rightarrow \qquad P = \frac{A}{y} + \sqrt{5} y$$

For *P* to be minimum,  $\frac{dP}{dy} = 0$ 

$$\Rightarrow \frac{A}{y^2} = \sqrt{5}$$

$$\Rightarrow \qquad y = \sqrt{\frac{A}{\sqrt{5}}} = \sqrt{\frac{10}{\sqrt{5}}}$$

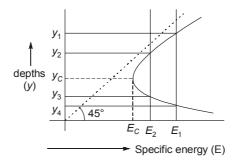
$$\Rightarrow$$
  $y = 2.115 \text{ m}$ 

$$b = \frac{A}{y} - y = \frac{10}{2.115} - 2.115$$

$$\Rightarrow \qquad b = 2.613 \text{ m} \simeq 2.61 \text{ m}$$

Energy loss, 
$$E_L = \frac{(y_2 - y_1)^3}{4y_1y_2}$$
  
=  $\frac{(1.8 - 0.6)^3}{4 \times 0.6 \times 1.8} = 0.4 \text{ m}$ 

8. (b)



$$E_2 < E_1 y_4 < y_3$$

where  $y_1$ ,  $y_2$  are subcritical depths and  $y_3$ ,  $y_4$  are supercritical depths.

Thus for supercritical flow, if specific energy decreases than corresponding depth increases.

#### 9. (b)

Length of GVF profile is more than the length of hydraulic jump.

- **10.** (a)
- 11. (a)

### Types of Jump

- A. Undular jump
- B. Weak jump
- C. Oscillating jump
- D. Steady jump
- E. Strong jump

### Pre-Jump Froude Number (Fr<sub>1</sub>)

- **1.** 1 to 1.7
- **2.** 1.7 to 2.5
- 3. 2.5 to 4.5
- **4.** 4.5 to 9
- 5. Greater than 9

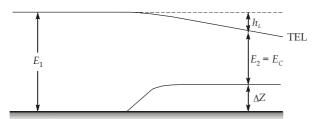
12. (d)

$$Q = 12 \,\mathrm{m}^3/\mathrm{s}$$

$$B = 5 \text{ m}$$

$$y_1 = 1.5 \text{ m}$$

$$h_L$$
 = Upstream velocity head =  $\frac{V_1^2}{2g}$ 



$$\Rightarrow$$

$$E_{1} = \Delta Z + E_{C} + h_{L}$$

$$\Delta Z = E_{1} - E_{C} - h_{L}$$

$$= y_{1} + \frac{V_{1}^{2}}{2g} - \frac{3}{2}y_{c} - \frac{V_{1}^{2}}{2g} = y_{1} - \frac{3}{2}y_{c}$$

$$y_c = \left(\frac{q^2}{g}\right)^{1/3} = \left[\left(\frac{12}{5}\right)^2 \times \frac{1}{9.81}\right]^{1/3}$$

$$\Rightarrow$$

$$y_c = 0.8374 \text{ m}$$

$$\Delta Z = 1.5 - \frac{3}{2} \times 0.8374 = 0.244 \,\mathrm{m}$$

$$\Delta Z = 0.244 \text{ m} = 24.4 \text{ cm}$$

#### 13. (a)

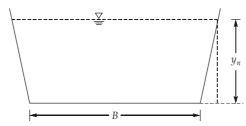
Given,

$$Q = 20 \,\mathrm{m}^3/\mathrm{s}$$

$$S_0 = 0.004 \,\text{m/m}$$

$$n = 0.030$$

It is half hexagonal channel, so it is most the efficient trapezoidal channel.



For the most efficient trapezoidal channel

$$A = \sqrt{3}y_n^2$$

and

$$R = \text{Hydraulic radius} = \frac{y_n}{2}$$

$$Q = AV = A\frac{1}{n}R^{2/3}S_0^{1/2}$$

$$\Rightarrow$$

$$20 = \sqrt{3}y_n^2 \times \frac{1}{0.030} \times \left(\frac{y_n}{2}\right)^{2/3} \times \sqrt{0.004}$$

$$\Rightarrow$$

$$y_n = 2.25 \text{ m}$$

14. (b)

 $y_1$  = upstream flow depth = 2 m

 $y_2$  = downstream flow depth = 1 m

Head loss or energy loss = 10% of kinetic head at downstream =  $0.1\frac{V_2^2}{2\sigma}$ 

Applying energy equation between upstream (1) and downstream (2) of sluice gate

$$E_1 = E_2 + E_L$$

$$\Rightarrow y_1 + \frac{V_1^2}{2g} = y_2 + \frac{V_2^2}{2g} + 0.1 \frac{V_2^2}{2g}$$

$$\Rightarrow \qquad 2 + \frac{Q^2}{B^2 y_1^2 2g} = y_2 + 1.1 \frac{V_2^2}{2g} = y_2 + 1.1 \frac{Q^2}{B^2 y_2^2 2g}$$

$$\Rightarrow 2 + \frac{Q^2}{4^2 \times 2^2 \times 2 \times 10} = 1 + \frac{1.1 \times Q^2}{4^2 \times 1^2 \times 2 \times 10}$$

$$\Rightarrow$$
 1 =  $\frac{1}{4^2 \times 2 \times 10} Q^2 \left( 1.1 - \frac{1}{4} \right)$ 

$$\Rightarrow$$
  $Q^2 = 376.47$ 

$$\Rightarrow$$
  $Q = 19.40 \text{ m}^3/\text{s}$ 

Now 
$$F_{r2}^2 = \frac{Q^2 T}{g A_2^3} = \frac{376.47 \times 4}{10 \times (4 \times 1)^3}$$

$$\therefore \qquad F_{r2} = 1.5$$

15. (c)

Given:

$$Q = 4 \,\mathrm{m}^3/\mathrm{s}$$

For flow to be critical,

we know that

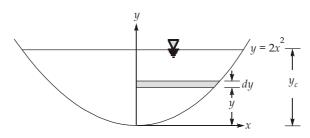
$$\frac{Q^2T}{gA^3} = 1$$

$$Q^2T = A^3g$$

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...(i)





$$y = y_c$$

$$y_c = 2x_c^2$$

$$x_c = \sqrt{\frac{y_c}{2}}$$

Top width (T) = 
$$2x_c = 2\sqrt{\frac{y_c}{2}}$$
  
 $dA = xdy$   
 $dA = \sqrt{\frac{y}{2}}dy$   

$$A = 2\int dA = 2\int_0^{y_c} \sqrt{\frac{y}{2}}dy$$

$$= \sqrt{2} \cdot \left[\frac{y^{3/2}}{3/2}\right]_0^{y_c} = \sqrt{2} \times \frac{2}{3}(y_c)^{3/2}$$

Now, using (i)

$$(4)^{2} \times 2\sqrt{\frac{y_{c}}{2}} = g \times \left[\sqrt{2} \times \frac{2}{3}(y_{c})^{3/2}\right]^{3}$$

$$(4)^{2} \times 2\sqrt{\frac{y_{c}}{2}} = 9.81 \times \left[\sqrt{2} \times \frac{2}{3}(y_{c})^{3/2}\right]^{3}$$

$$y_{c} = 1.288 \text{ m}$$

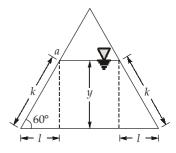
$$R = \frac{\text{Wetted area}}{\text{Wetted perimeter}} = \frac{A}{P}$$

$$A = \left(\frac{1}{2} \times \frac{y}{\sqrt{3}} \times y\right) \times 2 + \left(a - \frac{2y}{\sqrt{3}}\right) y$$

$$P = a + 2 \times \frac{2y}{\sqrt{3}}$$

$$A = \frac{y^2}{\sqrt{3}} + ay - \frac{2y^2}{\sqrt{3}} = ay - \frac{y^2}{\sqrt{3}}$$

$$R = \frac{ay - \frac{y^2}{\sqrt{3}}}{a + \frac{4y}{\sqrt{3}}}$$



$$\tan 60^\circ = \frac{y}{l} \Longrightarrow l = \frac{y}{\sqrt{3}}$$

$$\sin 60^\circ = \frac{y}{k} \Longrightarrow k = \frac{2y}{\sqrt{3}}$$

:.

For *R* to be maximum,  $\frac{dR}{dy} = 0$ 

$$\frac{dR}{dy} = \frac{\left(a + \frac{4y}{\sqrt{3}}\right)\left(a - \frac{2y}{\sqrt{3}}\right) - \left(ay - \frac{y^2}{\sqrt{3}}\right)\left(\frac{4}{\sqrt{3}}\right)}{\left(a + \frac{4y}{\sqrt{3}}\right)^2} = 0$$

$$\Rightarrow 4y^2 + 2\sqrt{3}ya - 3a^2 = 0$$

$$y = 0.535a \simeq 0.54a$$

17. (b)

$$q_1 = \frac{Q}{B_1} = \frac{2.75}{2.5} = 1.1 \,\text{m}^3/\text{s/m}$$

Upstream conditions:  $V_1 = \frac{q_1}{v_1} = \frac{1.1}{0.9} = 1.222 \text{ m/s}$ 

$$F_1 = \frac{V_1}{\sqrt{gy_1}} = \frac{1.222}{\sqrt{10 \times 0.9}} = 0.4073 < 1$$
 (: Subcritical flow)

$$E_1 = y_1 + \frac{V_1^2}{2g} = 0.9 + \frac{(1.222)^2}{2 \times 10} = 0.975 \text{ m}$$

At the maximum contraction, critical depth will occur at the contracted section. Thus,  $y_2 = y_{c2}$  $E_1 = E_2 = E_c = 0.975 \text{ m}$ Thus,

$$E_c = \frac{3}{2}y_c \Rightarrow y_{c_2} = \frac{2}{3} \times 0.975 = 0.65 \text{ m}$$

 $y_{c_2} = \left(\frac{q^2}{q}\right)^{1/3}$ We know that,

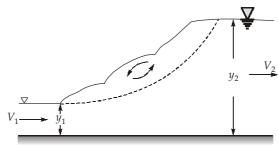
$$\Rightarrow \qquad q = \left[ (0.65)^3 \times 10 \right]^{1/2} = 1.657 \text{ m}^3/\text{s/m}$$

$$\Rightarrow \frac{Q}{B} = 1.657$$

$$\Rightarrow$$
  $B = B_{\min} = \frac{2.75}{1.657} = 1.66 \text{ m}$ 

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#### 18. (a)



Given data: Depth of flow = 0.6 m,  $E_i = 10 \text{ m}$ 

$$E = y + \frac{V^2}{2g}$$

$$\Rightarrow 10 = 0.6 + \frac{V^2}{2 \times 9.81}$$

$$\Rightarrow$$
  $V = 13.58 \text{ m/s}$ 

$$F_1 = \frac{V}{\sqrt{gy}} = \frac{13.58}{\sqrt{9.81 \times 0.6}} = 5.597 > 1$$
 (Super critical flow)

Using the relation, 
$$\frac{y_2}{y_1} = \frac{1}{2} \left( -1 + \sqrt{1 + 8F_1^2} \right)$$

$$\Rightarrow \frac{y_2}{0.6} = \frac{1}{2} \left( -1 + \sqrt{1 + 8 \times (5.597)^2} \right)$$

$$\Rightarrow \qquad y_2 = 4.459 \text{ m} \simeq 4.46 \text{ m}$$

#### 20. (b)

$$y_c = \left(\frac{q^2}{g}\right)^{1/3} = 1.54 \text{ m}$$

As per manning's formula

$$Q = A \frac{1}{n} R^{2/3} \sqrt{s_0}$$

For wide rectangular channel R = y, A = By

$$q = \frac{1}{n} y^{5/3} \sqrt{s_0}$$

$$y_0^{5/3} = \frac{qn}{\sqrt{s_0}}$$

$$y_0 = \left[\frac{6 \times 0.013}{\sqrt{0.006}}\right]^{3/5} = 1 \text{ m}$$

 $y_0$  = normal depth

Now as  $y_0 < y_c$  (slope is steep) and local depth y = 1.2 which is  $y_0 < y < y_c$  hence flow profile is  $S_2$ .

#### 21. (a)

Given data,

$$Q = 50 \text{ m}^3/\text{s}$$
  
 $S = 0.004$ 

We know that under free fall condition depth of flow at free fall location will be critical flow.

Hence,

$$\frac{Q^2T}{A^3g} = 1$$

$$\frac{(50)^2 \times 5}{(5y)^3 \times 9.81} = 1$$

$$\frac{50 \times 50 \times 5}{125 \times y^3 \times 9.81} = 1$$

 $\Rightarrow$ 

$$y = 2.168 \text{ m} \simeq 2.17 \text{ m}$$

#### 22. (c)

23. (c)

$$\frac{V}{\sqrt{gy}} = Fr_1$$

$$\Rightarrow$$

$$Fr_1 = \frac{V_1}{\sqrt{gy_1}} = \frac{12}{\sqrt{9.81 \times 1}} = 3.83$$

$$y_1 = 1 \text{ m}$$

$$\frac{y_2}{y_1} = \frac{1}{2} \left[ -1 + \sqrt{1 + 8Fr_1^2} \right]$$

$$y_2 = 4.94 \text{ m}$$

#### 24. (c)

25. (d)

> When a  $S_2$  profile ends with a sudden drop of bed, the surface drops suddenly and it is called hydraulic drop. This can happen with any profile except  $A_2$ .

There can be no hydraulic jump in  $S_2$  profile.