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POWER SYSTEM-2

ELECTRICAL ENGINEERING

Date of Test : 04/09/2025

ANSWER KEY ➤

1. (b)	7. (d)	13. (d)	19. (c)	25. (b)
2. (c)	8. (d)	14. (a)	20. (a)	26. (a)
3. (c)	9. (b)	15. (a)	21. (a)	27. (b)
4. (a)	10. (a)	16. (b)	22. (d)	28. (a)
5. (b)	11. (d)	17. (d)	23. (b)	29. (d)
6. (c)	12. (a)	18. (c)	24. (b)	30. (c)

DETAILED EXPLANATIONS

1. (b)

We know that, $RRRV = \frac{V_m}{\sqrt{LC}} \sin\left(\frac{t}{\sqrt{LC}}\right)$

For short line, L and C decreases

So, $\frac{V_m}{\sqrt{LC}}$ increases

2. (c)

In LLG fault,

$$I_{\text{positive}} + I_{\text{negative}} + I_{\text{zero}} = 0$$

Here, $j1.653 - j0.5 - j1.153 = 0$

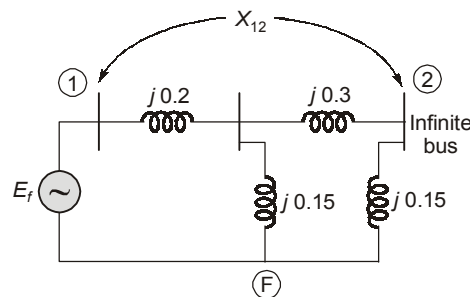
3. (c)

$$\text{SLG fault current } I_f = \frac{3E}{X_1 + X_2 + X_0 + 3X_n} = 1$$

or, $3X_n = 3 - (0.75)$

or, $X_n = 0.75 \text{ pu}$

4. (a)



$$X_{12} = \frac{j(0.2 \times 0.15 + 0.3 \times 0.15 + 0.2 \times 0.3)}{0.15} \quad (\text{Using star to delta transformation})$$

$$= j\left(0.2 + 0.3 + \frac{0.2 \times 0.3}{0.15}\right) = j0.9 \text{ p.u.}$$

5. (b)

$$\text{Synchronizing power coefficient} = P_{\max} \cos \delta_0 = \frac{dP_e}{d\delta}$$

Here, $P_{\max} = 2,$
 $\delta = 30^\circ$

$$\therefore S_p = 2 \cos 30^\circ$$

$$= 2 \times \frac{\sqrt{3}}{2} = \sqrt{3}$$

6. (c)

For a solid LG fault,

$$\text{Fault current is: } (I_F)_{LG} = \frac{3E}{(2X_1 + X_0 + 3X_n)} \quad (\text{Here, } X_1 \approx X_2 \text{ for synchronous generator})$$

Similarly, for a solid 3- ϕ fault

$$(I_F)_{3-\phi} = \frac{E}{X_1}$$

For LG fault current to be less than 3- ϕ fault current,

$$\frac{3E}{2X_1 + X_0 + 3X_n} < \frac{E}{X_1}$$

$$\text{or, } 2X_1 + X_0 + 3X_n > 3X_1$$

$$\text{or, } X_n > \frac{1}{3}(X_1 - X_0)$$

Hence, option (c) is correct.

7. (d)

Voltage drop in each phase of generator is

$$\begin{bmatrix} \Delta V_a \\ \Delta V_b \\ \Delta V_c \end{bmatrix} = \begin{bmatrix} j2 & j1 & j1 \\ j1 & j2 & j1 \\ j1 & j1 & j2 \end{bmatrix} \begin{bmatrix} I_a \\ I_b \\ I_c \end{bmatrix}$$

or we can write in sequence components,

$$\begin{bmatrix} \Delta V_{a0} \\ \Delta V_{b0} \\ \Delta V_{c0} \end{bmatrix} = \begin{bmatrix} X_0 & 0 & 0 \\ 0 & X_1 & 0 \\ 0 & 0 & X_2 \end{bmatrix} \begin{bmatrix} I_{a0} \\ I_{a1} \\ I_{a2} \end{bmatrix}$$

$$X_0 = X_s + 2X_m = j2 + 2(j1) = j4 \text{ p.u.}$$

$$X_1 = X_s - X_m = j2 - j1 = j1 \text{ p.u.}$$

$$X_2 = X_s - X_m = j2 - j1 = j1 \text{ p.u.}$$

$$I_f = I_a = \frac{3E_a}{X_1 + X_2 + X_0} = \frac{3 \times 1}{j(4 + 1 + 1)} = -j0.5 \text{ p.u.}$$

$$\begin{bmatrix} \Delta V_a \\ \Delta V_b \\ \Delta V_c \end{bmatrix} = \begin{bmatrix} j2 & j1 & j1 \\ j1 & j2 & j1 \\ j1 & j1 & j2 \end{bmatrix} \begin{bmatrix} -j0.5 \\ 0 \\ 0 \end{bmatrix} = \begin{bmatrix} 1 \\ 0.5 \\ 0.5 \end{bmatrix}$$

$$\begin{bmatrix} V_{an} \\ V_{bn} \\ V_{cn} \end{bmatrix} = \begin{bmatrix} E_{an} \\ E_{bn} \\ E_{cn} \end{bmatrix} - \begin{bmatrix} \Delta V_a \\ \Delta V_b \\ \Delta V_c \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} - \begin{bmatrix} 1 \\ 0.5 \\ 0.5 \end{bmatrix} = \begin{bmatrix} 0 \\ 0.5 \\ 0.5 \end{bmatrix}$$

8. (d)

We know that, $(Z_{p.u.})_{new} = (Z_{p.u.})_{old} \times \frac{(MVA)_{new}}{(MVA)_{old}} \times \frac{(kV)_{old}^2}{(kV)_{new}^2}$

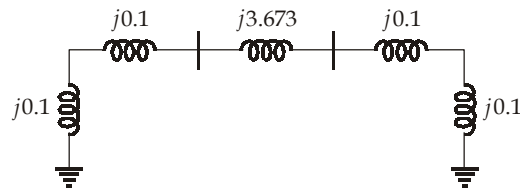
For G_1 and M_1 :

$$(X_{p.u.})_{new} = 0.05 \times \frac{80}{40} \times \left(\frac{11}{11}\right)^2 = j 0.1 \text{ p.u.}$$

For line:

$$(X_{\Omega})_{base} = \frac{(kV)^2}{MVA} = \frac{33^2}{80} = 13.6125 \Omega$$

$$(X_{p.u.})_{line} = \frac{\text{Actual value}}{\text{Base value}} = \frac{50}{13.6125} = j 3.673 \text{ p.u.}$$



9. (b)

3- ϕ fault current:

Let system is under no load condition before fault,

$$\therefore E = 1 \angle 0^\circ \text{ p.u.}$$

$$3\text{-}\phi \text{ fault current, } I_f = \frac{E}{X_1}$$

$$\Rightarrow X_1 = \frac{1}{-j5} = j0.2 \text{ p.u.}$$

Line-line fault current:

$$I_f = \frac{\sqrt{3}E}{X_1 + X_2}$$

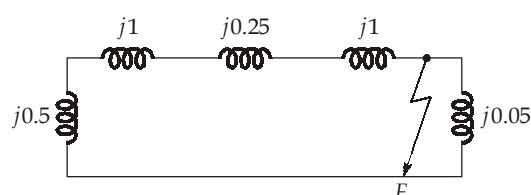
$$\Rightarrow X_1 + X_2 = \frac{\sqrt{3}}{-j2.5}$$

$$\Rightarrow j 0.2 + X_2 = j 0.69 \text{ p.u.}$$

$$\Rightarrow X_2 = j 0.49 \text{ p.u.}$$

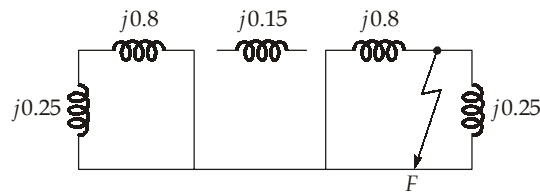
10. (a)

Positive and negative sequence reactance diagram:



$$\begin{aligned} Z_1 &= Z_2 \\ &= j 2.75 \parallel j 0.5 = j 0.423 \text{ p.u.} \end{aligned}$$

Zero sequence reactance diagram:



$$Z_0 = j 0.8 \parallel j 0.25 = j 0.19 \text{ p.u.}$$

Considering system at no load before fault

i.e.

$$E = 1.0 \angle 0^\circ \text{ p.u.}$$

$$(I_F) = 3 \left(\frac{E}{Z_1 + Z_2 + Z_0} \right) = 3 \left(\frac{1}{j0.423 + j0.423 + j0.19} \right)$$

$$I_f = -j2.896 \text{ p.u.}$$

11. (d)

Let us choose a base of 15 MVA, 11 kV on LV side of transformer.

We know that:

$$Z_{(\text{pu})\text{new}} = Z_{p(\text{old})} \times \frac{(MVA)_{b,\text{new}}}{(MVA)_{b,\text{old}}} \times \frac{(kV)_{b,\text{old}}^2}{(kV)_{b,\text{new}}^2}$$

$$\therefore X_{g1} = 0.2 \times \frac{15}{10} = 0.3 \text{ p.u.}$$

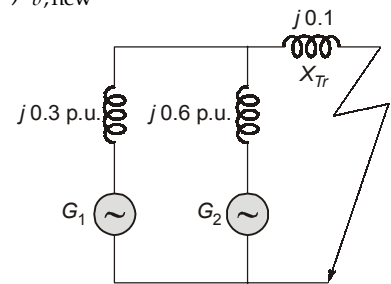
$$X_{g2} = 0.2 \times \frac{15}{5} = 0.6 \text{ p.u.}$$

$$X_{Tr} = 0.1 \text{ p.u.}$$

$$\begin{aligned} \therefore I_F'' &= \frac{E_g}{Z_1} = \frac{1.0}{(j0.3 \parallel j0.6) + j0.1} \\ &= -j 3.333 \text{ p.u.} \end{aligned}$$

Thus,

$$I_{G1}'' = \text{Subtransient current of generator-1} = -j 3.333 \text{ pu}$$



12. (a)

Since the generators are in parallel, they will operate at the same frequency at steady load.

Let load on generator 1 (200 MW) = x MW

load on generator 2 (400 MW) = $(600 - x)$ MW

and reduction in frequency = Δf

$$\therefore \frac{\Delta f}{x} = \frac{0.04 \times 50}{200} \quad \dots (i)$$

$$\text{and } \frac{\Delta f}{600 - x} = \frac{0.05 \times 50}{400} \quad \dots (ii)$$

Equating Δf in (i) and (ii),

$$x = 230.769 \approx 231 \text{ MW (load on generator-1)}$$

$$600 - x = 369 \text{ MW (load on generator-2)}$$

$$\therefore \text{System frequency} = 50 - \frac{0.04 \times 50}{200} \times 231 = 47.69 \text{ Hz.}$$

13. (d)

Since the new branch is connected between bus-2 and reference bus, therefore

$$Z_{\text{bus, new}} = Z_{\text{bus, old}} - \frac{1}{(Z_{kk} + Z_s)} [2^{\text{nd}} \text{ column}] [2^{\text{nd}} \text{ row}]$$

$$\begin{aligned} \text{or, } Z_{22, \text{ new}} &= Z_{22, \text{ old}} - \frac{1}{(Z_{22} + Z_s)} (Z_{22})(Z_{22}) = 0.34 - \frac{1(0.34)(0.34)}{(0.34 + 0.1)} \\ &= 0.0772 \text{ pu} \end{aligned}$$

$$\begin{aligned} \text{Also, } Z_{23, \text{ new}} &= Z_{23, \text{ old}} - \frac{1}{(Z_{22} + Z_s)} (Z_{22})(Z_{23}) \\ &= 0.25 - \frac{1}{(0.34 + 0.1)} (0.34)(0.25) \\ &= 0.0568 \text{ pu} \end{aligned}$$

14. (a)

From coordination equation,

$$\frac{dF_n}{dP_{Gn}} \cdot \frac{1}{1 - \frac{\partial P_L}{\partial P_{Gn}}} = \lambda$$

$$\text{Given, } P_L = 0.5 P_{G1}^2$$

$$\text{So, } \frac{dF_1}{dP_{G1}} \cdot \frac{1}{1 - P_{G1}} = \frac{dF_2}{dP_{G2}} \cdot \frac{1}{1 - 0}$$

$$\Rightarrow 10000 \times \frac{1}{1 - P_{G1}} = 12500$$

$$P_{G1} = \frac{1}{5} \text{ p.u.}$$

as the base value of 100 MVA

$$P_{G1} = \frac{1}{5} \times 100 = 20 \text{ MVA}$$

$$\begin{aligned} P_L &= 0.5 P_{G1}^2 = 0.5 \times \left(\frac{1}{5}\right)^2 = 0.02 \text{ p.u.} \\ &= 0.02 \times 100 = 2 \text{ MVA} \end{aligned}$$

$$P_D = P_{G1} + P_{G2} - P_L$$

$$40 = 20 + P_{G2} - 2$$

$$\Rightarrow P_{G2} = 22 \text{ MVA}$$

15. (a)

We use switch diagram to draw the zero-sequence network.

16. (b)

We know that, $RRRV = \frac{V_m}{\sqrt{LC}} \sin\left(\frac{t}{\sqrt{LC}}\right)$

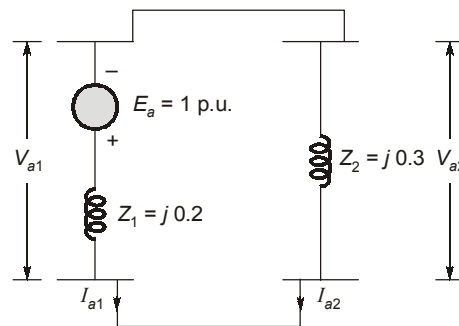
For short line, L and C decreases

So, $\frac{V_m}{\sqrt{LC}}$ increases

17. (d)

$$\begin{bmatrix} V_a \\ V_b \\ V_c \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ \alpha^2 & \alpha & 1 \\ \alpha & \alpha^2 & 1 \end{bmatrix} \begin{bmatrix} V_{a1} \\ V_{a2} \\ V_{a0} \end{bmatrix}$$

Sequence network representing L-L fault on phases b and c ,



$$I_{a1} = -I_{a2} = \frac{1}{j0.5} = -j2 \text{ p.u.}$$

from the above network

$$\begin{aligned} V_{a1} &= V_{a2} \\ V_{a1} &= E_a - I_{a1} X_1 \\ &= 1 - (-j2)(j0.2) = 0.6 \text{ p.u.} \end{aligned}$$

$\therefore$

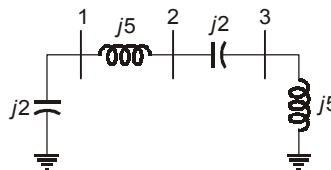
$$V_{a1} = V_{a2} = 0.6 \text{ p.u.}$$

$$\begin{aligned} V_{ab} &= V_a - V_b \\ &= (V_{a1} + V_{a2} + V_{a0}) - (\alpha^2 V_{a1} + \alpha V_{a2} + V_{a0}) \\ &= 2 V_{a1} - (\alpha^2 + \alpha) V_{a1} = (2 - \alpha^2 - \alpha) 0.6 \end{aligned}$$

$$\begin{aligned} V_{ab} \text{ p.u.} &= 1.8 \text{ p.u.} \\ V_{ab} &= 1.8 \times 11 = 19.8 \text{ kV} \end{aligned}$$

18. (c)

In the question the values given at capacitors are admittance values and at inductors are impedance values.



$$Y = \begin{bmatrix} j2 - j0.2 & j0.2 & 0 \\ j0.2 & j2 - j0.2 & -j2 \\ 0 & -j2 & j2 - j0.2 \end{bmatrix}$$

$$[Y]_{\text{bus}} = j \begin{bmatrix} 1.8 & 0.2 & 0 \\ 0.2 & 1.8 & -2 \\ 0 & -2 & 1.8 \end{bmatrix}$$

19. (c)

$$V_R = V_m (1 - \cos \omega t)$$

$$\omega = \frac{1}{\sqrt{LC}},$$

 V_m = per phase peak voltage

$$\omega = \frac{1}{\sqrt{0.5 \times 10^{-3} \times 8 \times 10^{-3}}} = 500 \text{ rad/sec}$$

$$V_m = \left(\frac{33}{\sqrt{3}} \right) \times \sqrt{2} \text{ kV} = 26.94 \text{ kV}$$

at

$$V_R = 26.94 (1 - \cos (500 \times 1.57 \times 10^{-3}))$$

$$V_R = 7.88 \text{ kV} \quad [\text{Keep the capacitor in radians mode}]$$

20. (a)

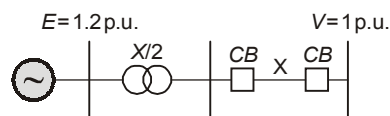
At healthy condition

$$\text{Total impedance} = \frac{X}{2} + \frac{X}{2} = X$$

$$P = \frac{EV}{X} = \frac{1.2 \times 1}{X} = 5 \text{ p.u.}$$

$$X = \frac{1.2}{5} = 0.24 \text{ p.u.}$$

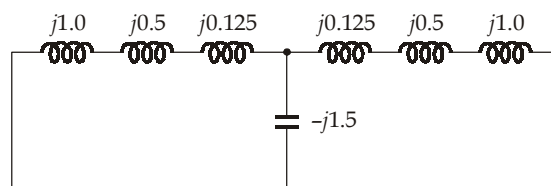
at faulty condition after CB open



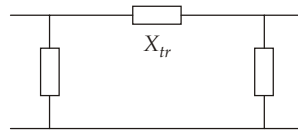
$$P = \frac{EV}{X_{\text{Total}}} = \frac{1.2 \times 1}{X + \frac{X}{2}} = \frac{2 \times 1.2}{3 \times 0.24}$$

$$P = 3.33 \text{ p.u.}$$

21. (a)



Converting star into delta:



The transfer reactance,
$$X_{tr} = j1.625 + j1.625 + \frac{j1.625 \times j1.625}{-j1.5}$$
$$= 1.48 \text{ p.u.}$$

22. (d)

$$Z_{\text{Bus (new)}} = \begin{bmatrix} 0.3 & 0.3 \\ 0.3 & 0.3 + 0.5 \end{bmatrix} = \begin{bmatrix} 0.3 & 0.3 \\ 0.3 & 0.8 \end{bmatrix}$$

23. (b)

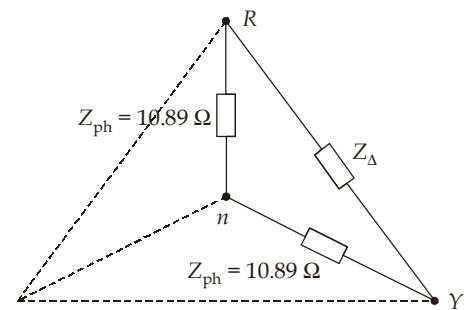
The reactance in p.u. = $Z_{\text{p.u.}} = Z_{\Omega} \times \frac{\text{MVA}_{(b)}}{(\text{kV})_b^2}$

$$Z_{\Omega} = Z_{\text{p.u.}} \times \frac{(kV_b)^2}{(\text{MVA})_b}$$
$$= 0.10 \times \frac{(33)^2}{10} = 10.89 \Omega$$

So reactance per phase = $Z_{ph} = 10.89 \Omega$

$$Z_{\Delta} = 3 \times Z_{ph} = 3 \times 10.89$$

$$Z_{\Delta} = 32.67 \Omega$$



24. (b)

$$S_{D2} = (0.8 + j0) \text{ p.u.}$$

This 0.8 p.u. active power is supplied by the generator G_1

$$\therefore 0.8 = \frac{1 \times 1}{0.5} \sin \delta$$

$$\delta = \sin^{-1} \left(\frac{0.8}{2} \right) = 23.58^\circ$$

$$Q_R = \frac{|V_1| \times |V_2|}{X} \cos \delta - \frac{|V_1|^2}{X}$$

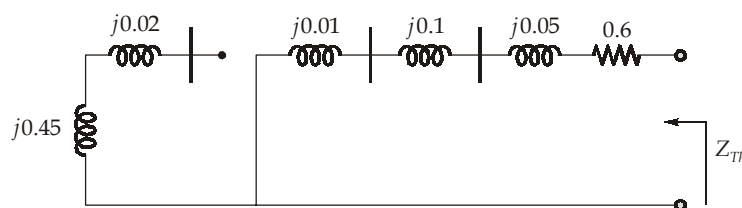
$$= \frac{1}{0.5} \cos(23.58^\circ) - \frac{1}{0.5}$$

$$Q_R = -0.167 \text{ p.u.}$$

The VAR rating of the capacitor = 0.167 p.u.

25. (b)

The zero sequence impedance network from point P and ground



The Thevenin's equivalent zero sequence impedance

$$Z_{Th} = (0.6 + j 0.16) \text{ p.u.}$$

26. (a)

$$|I''| = \frac{E}{|X_d''|} = \frac{1}{0.22} = 4.54 \text{ p.u.}$$

$$I_{\text{base}} = \frac{\text{MVA}_b}{\sqrt{3}(\text{kV}_b)} = \frac{100 \times 10^6}{\sqrt{3} \times 11 \times 10^3} = 5248.6 \text{ A} = 5.248 \text{ kA}$$

The magnitude of initial symmetrical rms current

$$= 4.54 \times 5.248 = 23.82 \text{ kA}$$

27. (b)

Kinetic energy $\propto$ frequency²

$$W \propto f^2$$

$$\frac{W_1}{W_2} = \frac{f_1^2}{f_2^2}$$

$$f_2 = f_1 \sqrt{\frac{W_2}{W_1}} = 50 \times \sqrt{\frac{500 - (0.5 \times 50)}{500}} \quad [\because W = GH = 100 \times 5 \text{ MJ}]$$

$$= 48.734 \text{ Hz}$$

Percentage deviation in frequency,

$$= \frac{50 - 48.734}{50} \times 100 = 2.532\%$$

Thus we can say that I_1 and I_3 currents are going into bus thus they are PQ bus and I_2 is going away from bus

$\therefore$ Bus-2 is generator bus (PV bus).

28. (a)

Fault current at bus 3 is,

$$I_{f3} = \frac{V_3(0)}{Z_{33} + Z_f} = \frac{1}{j0.2780 + j0.15}$$

$$I_{f3} = -j 2.336 \text{ p.u.}$$

$$|I_{f3}| = 2.336 \text{ p.u.}$$

29. (d)

Zero sequence current in R line is

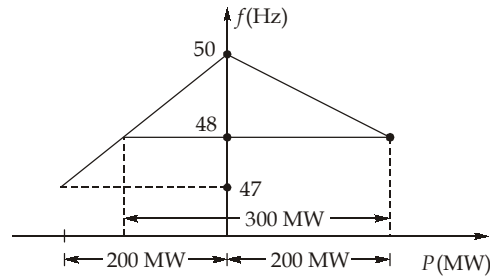
$$\vec{I}_{R0} = \frac{1}{3} \times \text{Current in neutral wire}$$

$$= \frac{1}{3} \times 300 \angle 300^\circ = 100 \angle 300^\circ \text{ A}$$

$$\begin{aligned} \text{Current in Y-line} \quad \vec{I}_Y &= \vec{I}_{R0} + a^2 \vec{I}_{R1} + a \vec{I}_{R2} \\ &= (100 \angle 300^\circ) + (1 \angle 120^\circ)^2 (200 \angle 0^\circ) + (1 \angle 120^\circ) (100 \angle 60^\circ) \\ &= (100 \angle 300^\circ) + (200 \angle -120^\circ) + (100 \angle 180^\circ) \end{aligned}$$

$$\vec{I}_Y = (300 \angle -120^\circ) \text{ A}$$

30. (c)



New frequency of operation of 200 MW alternator,

$$f_1 = 50 - \frac{2}{200} P_1$$

and, $f_2 = 50 - \frac{3}{200} P_2$

Total load, $P_1 + P_2 = 300 \text{ MW}$

...(i)

Units operated in parallel so,

$$f_1 = f_2 = f$$

$$50 - \frac{2}{200} P_1 = 50 - \frac{3}{200} P_2$$

$$2P_1 - 3P_2 = 0$$

...(ii)

From equations (i) and (ii), we get

$$P_1 = 180 \text{ MW}$$

$$P_2 = 120 \text{ MW}$$

Machine (1) which has better speed regulation will be loaded first to its full load rating, so it will operate on maximum load of 200 MW.

$$2P_1 - 3P_2 = 0$$

...(iii)

$$2 \times 200 - 3P_2 = 0$$

$$P_2 = \frac{400}{3} = 133.33 \text{ MW}$$

Total power delivered by two machine without overloading

$$\therefore P_1 + P_2 = 200 + 133.33 = 333.33 \text{ MW}$$

