

**MADE EASY**

Leading Institute for IES, GATE & PSUs

Delhi | Bhopal | Hyderabad | Jaipur | Pune | Kolkata

Web: www.madeeasy.in | E-mail: info@madeeasy.in | Ph: 011-45124612

MACHINE

(DC + TRANSFORMER + INDUCTION)

ELECTRICAL ENGINEERING

Date of Test : 26/06/2025

ANSWER KEY >

1. (c)	7. (c)	13. (d)	19. (a)	25. (b)
2. (a)	8. (d)	14. (a)	20. (b)	26. (c)
3. (b)	9. (d)	15. (b)	21. (d)	27. (b)
4. (c)	10. (c)	16. (b)	22. (c)	28. (d)
5. (a)	11. (d)	17. (c)	23. (d)	29. (b)
6. (b)	12. (a)	18. (b)	24. (a)	30. (c)

DETAILED EXPLANATIONS

1. (c)

For maximum torque (T_{\max})

$$s_{\max, T} = \frac{R_2}{X_2}$$

$$s_{\max, T} = \frac{1}{4}$$

$$\text{Synchronous speed, } N_s = \frac{120 \times 50}{6} = 1000 \text{ rpm}$$

Now at T_{\max} speed of motor,

$$N_r = (1 - s) N_s = (1 - 0.25) \times 1000$$

$$N_r = 750 \text{ rpm}$$

2. (a)

In a wave winding the armature current get equally divided between two parallel paths but in lap winding there can be a problem of circulating currents between two parallel paths and hence causing unequal currents in both paths.

3. (b)

$$\text{Time constant} = \frac{L}{r} = 0.2; \quad I^2 r = 400 \text{ W}$$

$$\begin{aligned} \text{Energy stored in Joules} &= \frac{1}{2} L I^2 = \frac{1}{2} \times I^2 r \times \frac{L}{r} \\ &= \frac{1}{2} \times 400 \times 0.2 = 40 \text{ Joules} \end{aligned}$$

4. (c)

$$\begin{aligned} V &= 240 \text{ V}, & I_a &= 40 \text{ A} \\ N_1 &= 1500 \text{ rpm}, & R_a &= 0.3 \Omega \end{aligned}$$

$T \propto I_a^2$, since the torque is constant.

$$\begin{aligned} \therefore I_{a1}^2 &= I_{a2}^2 \\ \Rightarrow I_{a1} &= I_{a2} = 40 \text{ A} \end{aligned}$$

During starting the induced emf is zero, hence the current is limited only by the resistance in the armature circuit.

$$\therefore \text{Total resistance} = \frac{240}{40} = 6 \Omega$$

$$\text{Extra resistance to be added in series with armature} = 6 - 0.3 = 5.7 \Omega$$

5. (a)

Impedance under block rotor condition,

$$Z_b = \frac{V_b}{I_b} = \frac{82.5}{9.3} = 8.87 \Omega$$

Resistance under block rotor condition,

$$R_b = \frac{W_b}{I_b^2} = \frac{500}{(9.3)^2} = 5.78 \, \Omega$$

Rotor resistance referred to stator,

$$\begin{aligned} R'_2 &= R_b - R_1 \\ &= 5.78 - 2.5 = 3.28 \, \Omega \end{aligned}$$

6. (b)

Rotor input (or) air gap power

$$= 45 - 1.5 = 43.5 \, \text{kW}$$

$$s = 0.04$$

Internal mechanical power developed is

$$= 43.5 (1 - 0.04) = 43.5 \times 0.96 = 41.76 \, \text{kW}$$

7. (c)

$$T_{st} = 0.8 T_{\max}$$

$$0.8 = \frac{2s_{\max}}{s_{\min}^2 + 1}$$

$$s_{\max}^2 - \frac{2}{0.8} s_{\max} + 1 = 0$$

$$s_{\max}^2 - 2.5 s_{\max} + 1 = 0$$

$$s_{\max} = 0.5$$

$$\therefore 0.5 = \frac{0.03 + R_{\text{ext}}}{0.18}$$

$$0.09 = 0.03 + R_{\text{ext}}$$

$$R_{\text{ext}} = 0.09 - 0.03 = 0.06 \, \Omega$$

8. (d)

We know, $\frac{N_{\Delta(P)}}{N_{Y(P)}} = 5$

Also, $\frac{N_{\Delta(P)}}{N_{Y(P)}} = \frac{V_{\Delta(P)}}{V_{Y(P)}}$

$$V_{Y(P)} = \frac{400}{\sqrt{3}} \, \text{V}$$

$$V_{\Delta(P)} = \frac{N_{\Delta(P)}}{N_{Y(P)}} V_{Y(P)} = 5 \times \frac{400}{\sqrt{3}} = \frac{2000}{\sqrt{3}} \, \text{V}$$

For delta side, $V_{\Delta(L)} = V_{\Delta(P)} = \frac{2000}{\sqrt{3}} \, \text{V}$

9. (d)

For maximum efficiency at unity power factor using condition,

$$\text{kVA}_m = (\text{kVA})_f \sqrt{\frac{P_i}{P_{cu}}} = 400 \sqrt{\frac{700}{2800}} = 400 \sqrt{\frac{1}{4}} = 200 \text{ kVA}$$

At maximum efficiency,

$$P_c = P_i$$

$$\% \eta_{\max} = \frac{200}{200 + \frac{700}{1000} + \frac{700}{1000}} = 99.30\%$$

10. (c)

For a 3-phase induction motor, spatial displacement,

$$\delta = 90^\circ + \phi_2$$

where ' ϕ_2 ' is power factor angle,

$$\cos \phi_2 = 0.707$$

$$\phi_2 = 45^\circ$$

$$\delta = 90^\circ + 45^\circ = 135^\circ$$

11. (d)

For dc series motor;

Given,

$$V_t = 220 \text{ V},$$

$$N_r = 1500 \text{ rpm}$$

$$I_a = 25 \text{ A},$$

$$R_a = 0.4 \text{ } \Omega,$$

$$R_{se} = 0.6 \text{ } \Omega$$

Torque;

$$T \propto I_a^2$$

back emf at 1500 rpm,

$$\begin{aligned} E_{b1} &= V_t - I_{a1} (R_a + R_{se}) \\ &= 220 - 25 (0.4 + 0.6) \end{aligned}$$

$$E_{b1} = 195 \text{ V}$$

We know that,

$$E_b \propto N$$

Back emf at 1200 rpm;

$$\frac{E_{b2}}{195} = \frac{1200}{1500}$$

$$E_{b2} = \frac{12}{15} \times 195 = 156 \text{ V}$$

Let us assume R_{ext} to be connected in series:

$$E_{b2} = V_t - I_{a2} (R_a + R_{se} + R_{\text{ext}})$$

To obtain rated torque at 1200 rpm, armature current must be same;

i.e.

$$I_{a2} = 25 \text{ A}$$

Now,

$$156 = 220 - 25 (0.4 + 0.6 + R_{\text{ext}})$$

$$220 - 156 = 25 (1 + R_{\text{ext}})$$

$$R_{\text{ext}} = 1.56 \text{ } \Omega$$

12. (a)

At no load;

$$\begin{aligned}\text{Back emf, } E_{b0} &= V_t - I_{a0} (R_a) \\ E_{b0} &= 220 - 3(0.5) \\ E_{b0} &= 218.5 \text{ V}\end{aligned}$$

At full load;

$$\begin{aligned}\text{Back emf, } E_{bfl} &= V_t - I_{afl} (R_a) \\ &= 220 - 45(0.5) \\ E_{bfl} &= 197.5 \text{ V}\end{aligned}$$

As flux is given constant;

then, we can write; $E_b \propto N$

$$\text{or, } \frac{E_{bfl}}{E_{b0}} = \frac{N_{fl}}{N_0}$$

$$\begin{aligned}N_{fl} &= \left(\frac{197.5}{218.5} \right) \times 1500 \\ &= 1355.83 \approx 1356 \text{ rpm}\end{aligned}$$

13. (d)

Given:

S.C. Test (H.V): 57.5 V, 8.34 A, 284 W

$$Z_{eq} = \frac{57.5}{8.34} = 6.894 \Omega$$

$$R_{eq} = \frac{284}{(8.34)^2} = 4.083 \Omega$$

$$X_{eq} = \sqrt{Z_{eq}^2 - R_{eq}^2} = 5.555 \Omega$$

For voltage regulation to be zero;

$$\text{Power factor; } \cos \phi = \cos \tan^{-1} \left(\frac{R_{eq}}{X_{eq}} \right) = \cos (36.32^\circ)$$

$$\cos \phi = 0.805 \text{ leading}$$

14. (a)

Primary is star connected and secondary is delta connected.

$$(V_L)_{\text{primary}} = 11000 \text{ V}$$

$$(V_{ph})_{\text{primary}} = \frac{11000}{\sqrt{3}} \text{ V}$$

$$\frac{(V_{ph})_{\text{sec}}}{(V_{ph})_{\text{prim}}} = \frac{1}{5}$$

$$\therefore \text{ Turns ratio} = \left(\frac{\text{High voltage}}{\text{Low voltage}} \right)_{\text{phase}}$$

$$\therefore (V_{ph})_{\text{sec}} = \frac{11000}{5\sqrt{3}} \text{ V}$$

$$(V_{ph})_{\Delta} = (V_L)_{\Delta}$$

$$\text{Output kVA} = \sqrt{3} V_L I_L$$

$$= \sqrt{3} \times \frac{11000}{5\sqrt{3}} \times 423 = 930.6 \text{ kVA}$$

15. (b)

Given that,

$$V_{OC} = 230 \text{ V},$$

$$I_{OC} = 1.3 \text{ A},$$

$$P_{OC} = 100 \text{ W}$$

$$R_C = \frac{V_{OC}^2}{P_{OC}} = \frac{230^2}{100} = 529 \Omega$$

Power factor angle,

$$\phi_{OC} = \cos^{-1} \left(\frac{P_{OC}}{V_{OC} I_{OC}} \right) = \cos^{-1} \left(\frac{100}{230 \times 1.3} \right) = 70.46^\circ$$

$$X_\phi = \frac{R_C}{\tan \phi_{OC}} = \frac{529}{\tan 70.46^\circ} = 187.73 \Omega$$

Referred to high voltage side,

$$R_C = 529 \times \left(\frac{400}{230} \right)^2 = 1600 \Omega$$

$$X_\phi = 187.73 \times \left(\frac{400}{230} \right)^2 = 567.8 \Omega$$

16. (b)

Load characteristic is

$$T_L \propto N^2$$

For dc series motor, torque-current relation is given by

$$T_d \propto I_a^2$$

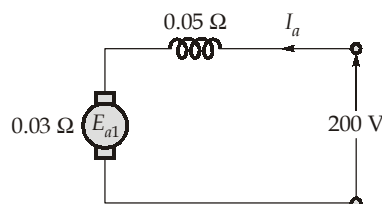
\therefore

$$\frac{I_{a2}}{I_{a1}} = \frac{N_2}{N_1}$$

$$\frac{I_{a2}}{15} = \frac{750}{1500}$$

$$I_{a2} = 7.5 \text{ A}$$

Case-I:



$$E_{a1} = 200 - 15 \times (0.03 + 0.05)$$

$$E_{a1} = 198.8 \text{ V}$$

Case-II:

When additional resistance added in series with the armature circuit,

$$I_{a2} = 7.5 \text{ A,}$$

$$N_2 = 750 \text{ rpm}$$

Now,

$$E_a \propto \phi \omega_m$$

$$\frac{E_{a2}}{E_{a1}} = \frac{N_2 I_{a2}}{N_1 I_{a1}} \quad (\text{In dc series motor } \phi \propto I_a)$$

$$\frac{E_{a2}}{198.8} = \frac{750 \times 7.5}{1500 \times 15}$$

$$E_{a2} = 49.7 \text{ V}$$

$$E_{a2} = 200 - 7.5(0.08 + R_{\text{ext}}) = 49.7$$

$$0.08 + R_{\text{ext}} = \frac{200 - 49.7}{7.5}$$

$$R_{\text{ext}} = 20.04 - 0.08 \\ = 19.96 \Omega$$

17. (c)

Armature power developed,

$$= \text{shaft power} + \text{rotational losses}$$

$$= 1.5 \text{ kW} + 0.1 \text{ kW}$$

$$E_b I_a = 1.6 \text{ kW}$$

Back emf is given by,

$$E_b = \frac{NP\phi Z}{A \times 60} = \frac{N \times 0.035 \times 500}{60}$$

and armature current, $I_a = \frac{230 - E_b}{0.06}$

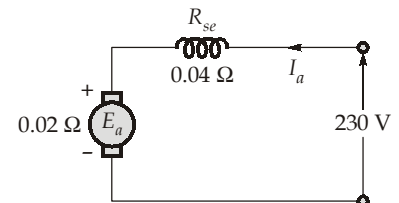
$$E_b \left(\frac{230 - E_b}{0.06} \right) = 1600$$

$$230 E_b - E_b^2 - 96 = 0$$

$$E_b = 229.58 \text{ V}$$

$$\text{Speed, } N = \frac{60 E_b}{\phi Z} = \frac{60 \times 229.58}{0.035 \times 500}$$

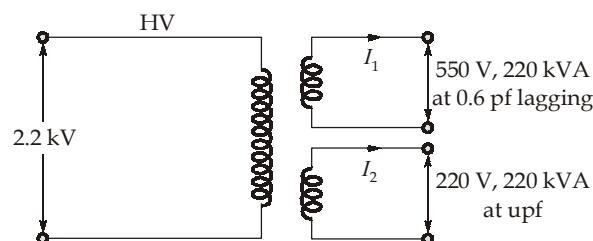
$$N = 787.13 \text{ rpm}$$



(For lap $A = P$)

18. (b)

Consider the below circuit:



Rated current in winding - 1

$$I_1 = \frac{220 \times 1000}{550} = 400 \angle -53.13^\circ \text{ A}$$

Rated current in winding - 2

$$I_2 = \frac{220 \times 1000}{220} = 1000 \angle 0^\circ \text{ A}$$

Current in HV side due to rated current in winding - 1

$$I_1' = \frac{(400 \angle -53.13) \times 0.55}{2.2} = 100 \angle -53.13^\circ \text{ A}$$

Current in HV side due to rated current in winding - 2

$$I_2' = \frac{(1000 \angle 0^\circ) \times 0.22}{2.2} = 100 \angle 0^\circ \text{ A}$$

$$\text{HV side current} = 100 \angle -53.13^\circ + 100 \angle 0^\circ$$

$$I = 178.885 \angle -26.565^\circ \text{ A}$$

$$|I| = 178.885 \text{ A}$$

19. (a)

$$\begin{aligned} V_{t1} &= 400 \text{ V}; & I_{a1} &= 150 \text{ A} \\ R_a &= 0.12 \Omega; & N_1 &= 1500 \text{ rpm} \end{aligned}$$

The value of load resistance,

$$R_L = \frac{400}{150} = 2.67 \Omega$$

Load current 100 A, the terminal voltage,

$$V_{t2} = 100 \times R_L = 100 \times 2.67 = 267 \text{ V}$$

$$I_{a2} = 100 \text{ A}; \quad R_a = 0.12 \Omega$$

$$E_g = \frac{\phi NZ}{60} \times \left(\frac{P}{A} \right) \Rightarrow E_g \propto N$$

$$\frac{E_{g1}}{E_{g2}} = \frac{N_1}{N_2} = \frac{V_{t1} + I_{a1}R_a}{V_{t2} + I_{a2}R_a}$$

$$\Rightarrow \frac{400 + 150 \times 0.12}{267 + 100 \times 0.12} = \frac{1500}{N_2}$$

$$N_2 = 1001.19 \text{ rpm}$$

20. (b)

There is a change of flux/pole due to armature reaction,

$$E_G \propto \phi_1 N_1$$

$$\Rightarrow I_f = \frac{230}{200} = 1.15 \text{ A}$$

$$(V - IR) \propto \phi_1 N_1$$

$$[230 - (10 - 1.15)(0.1)] \propto 1400\phi_1 \quad \dots(1)$$

$$[230 - (200 - 1.15)(0.1)] \propto N_2\phi_2 \quad \dots(2)$$

Equation (2) divided by (1),

$$\frac{210.1}{229.1} = \frac{N_2}{1400} \times 0.96$$

$$\Rightarrow N_2 = 1337 \text{ rpm}$$

$$\therefore \text{Torque developed } (T_d) = \frac{210.115 \times (200 - 1.15)}{\left(\frac{2\pi \times 1337}{60} \right)} = 298.4 \text{ N-m}$$

21. (d)

$$V_{sc} = 120 \text{ V}, I_{sc} = 9.6 \text{ A}, P_{sc} = 460 \text{ W}$$

$$Z_e = \frac{V_{sc}}{I_{sc}} = \frac{120}{9.6} = 12.5 \Omega$$

$$R_e = \frac{P_{sc}}{I_{sc}^2} = \frac{460}{(9.6)^2} = 4.99 \Omega$$

$$R_{lm} = 1.5 \Omega$$

$$R'_2 = R_e - R_{lm} = 4.99 - 1.5 = 3.49 \Omega$$

$$\text{Given, } V_0 = 220 \text{ V}, I_0 = 4.6 \text{ A}, P_0 = 125 \text{ W}$$

Core, friction and windage losses

$$= 125 - (4.6)^2 \left(1.5 + \frac{3.49}{4} \right) = 74.8 \text{ W}$$

22. (c)

$$\text{Synchronous speed, } N_s = \frac{120f}{P} = \frac{120 \times 50}{4} = 1500 \text{ rpm}$$

$$\text{Forward slip, } s_f = \frac{N_s - N_r}{N_s} = \frac{1500 - 1420}{1500} = 0.053$$

$$\text{Backward slip, } s_b = (2 - s) = (2 - 0.053) = 1.947$$

The effective rotor resistance in backward branch

$$= \frac{R_2}{2(2 - s)} = \frac{7.5}{2(2 - 0.053)}$$

$$= 1.926 \Omega \approx 1.93 \Omega$$

23. (d)

Given transformer rating 50 kVA, 22 kV/220 V percent resistance = 1% percent reactance = 8%.

Taking hv side voltage as base voltage is 22 kV.

$$\text{Base apparent power, } S_B = 50 \text{ kVA}$$

As primary is Δ connected.

$$\text{Phase voltage, } V_P = \text{line voltage, } V_L$$

$$\therefore \text{Base impedance, } Z_{\text{base}} = \frac{3(V_{\phi, \text{base}})^2}{S_{\text{base}}} = \frac{3 \times (22000)^2}{50 \times 10^3} = 29040 \Omega$$

The per unit impedance of transformer,

$$Z_{\text{eq pu}} = 0.01 + j0.08 \text{ pu}$$

∴ High voltage side impedance,

$$\begin{aligned} Z_{ph\ hv} &= Z_{eq\ pu} \times Z_{base} \\ &= (0.01j + j0.08) \times 29040 \\ &= 290.40 + j2323.2\ \Omega \end{aligned}$$

24. (a)

We know, Field current, $I_f = \frac{400}{200} = 2\text{ A}$

At no load, $I_{a0} = 5.6 - 2 = 3.6\text{ A}$

$$E_{a0} = 400 - (0.18 \times 3.6) - 2 = 397.35\text{ V}$$

At full load, $I_a(fl) = 60.3 - 2 = 58.3\text{ A}$

$$E_a(fl) = 400 - 0.18 \times 58.3 - 2 = 387.506\text{ V}$$

Assuming initial flux be ϕ ,

New flux value due to weakening,

$$\phi' = (1 - 0.04)\phi = 0.96\phi$$

$$\frac{n(fl)}{n(nl)} = \frac{387.506}{397.35} \times \frac{1}{0.96} = 1.016$$

25. (b)

We know, flux/pole = $\frac{\pi D l}{p} \times \text{pole pitch}$

$$= \frac{\pi \times 30 \times 10^{-2}}{4} \times 20 \times 10^{-2} \times 0.4 = 0.0188\text{ Wb}$$

Induced emf, $E = \frac{P\phi n Z}{60 A} = \frac{0.0188 \times 1500 \times 400}{60} = 188\text{ V}$

Gross mechanical power developed

$$= \frac{188 \times 30}{1000} = 5.64\text{ kW}$$

$$\text{Torque developed} = \frac{5.64 \times 1000}{\frac{2\pi \times 1500}{60}} = 35.905\text{ N-m}$$

26. (c)

Armature resistance is assumed negligible,

Also field current is ignored in comparison to armature current

$$\begin{aligned} I_L &= I_a \\ 200 &= K_e \times 600 \end{aligned} \quad \dots(i)$$

$$T = K_t \times 20 = K_L \times (600)^2 \quad \dots(ii)$$

When $20\ \Omega$ resistor added in armature circuit

$$(200 - 20I_a) = K_e \times n \quad \dots(iii)$$

$$K_t I_a = K_L n^2 \quad \dots(iv)$$

Dividing equation (iii) by (i) and (iv) by (ii),

$$\frac{200 - 20I_a}{200} = \frac{n}{600}$$

$$\frac{I_a}{20} = \frac{n^2}{(600)^2}$$

$$I_a = \frac{20n^2}{(600)^2}$$

$$1 - \frac{1}{10} \left[\frac{20n^2}{(600)^2} \right] = \frac{n}{600}$$

$$(600)^2 - 2n^2 = 600n$$

$$2n^2 + 600n - (600)^2 = 0$$

$$n = 300, -600$$

practical value, $n = 300 \text{ rpm}$

$$\frac{I_a}{20} = \frac{n^2}{(600)^2} = \frac{(300)^2}{(600)^2} = \frac{1}{4}$$

$$I_a = \frac{20}{4} = 5 \text{ A}$$

27. (b)

- As torque remain rated at 1500 rpm and 1000 rpm, so armature current and flux will be same.
- At 1500 rpm, using motor equation

$$V = E_b + I_a R_a$$

$$240 = E_b + 50 \times 0.2$$

$$E_b = 230 \text{ V}$$

$$E_{b2} = \frac{N_2}{N_1} E_{b1} \quad (\text{as } \phi \text{ is constant})$$

$$E_{b2} = \frac{1000}{1500} \times 230 = 153.33 \text{ V}$$

At 1000 rpm, R_{ext} is introduced

Applying motor equation, $V = E_{b2} + I_a(R_a + R_{\text{ext}})$

$$240 = 153.33 + 50(0.2 + R_{\text{ext}})$$

$$240 = 153.33 + 10 + 50R_{\text{ext}}$$

$$R_{\text{ext}} = 1.5334 \Omega$$

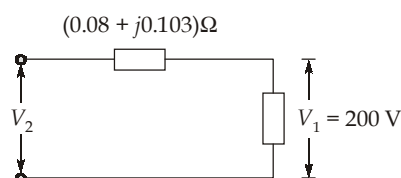
28. (d)

By referring the transformer impedance to LV side,

$$R_{LV} = 0.05 + \frac{3}{(10)^2} = 0.08 \Omega$$

$$X_{LV} = 0.05 + \frac{5.3}{(10)^2} = 0.103 \Omega$$

Drawing circuit representation,



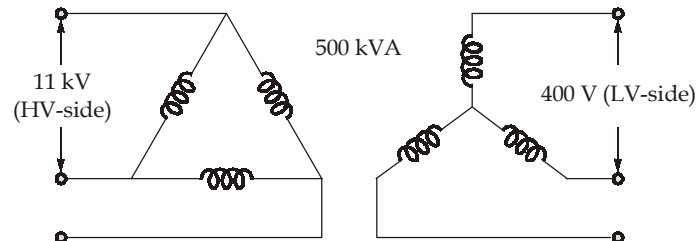
$$\text{Current, } I_2 = \frac{20 \times 1000}{200} = 100 \text{ A}$$

$$\text{Voltage drop} = 100(0.08 \times 0.8 + 0.103 \times 0.6) = 12.58 \text{ V}$$

$$\text{Voltage regulation} = \frac{12.58}{200} \times 100 = 6.29\%$$

29. (b)

For given transformer configuration,



Phase current at star side,

$$I_{PY(\text{rated})} = \frac{500}{\sqrt{3} \times 0.40} = 721.687 \text{ A}$$

Phase current at delta side,

$$I_{P\Delta(\text{rated})} = \frac{500}{3 \times 11} = 15.151 \text{ A}$$

$$\text{At lv side, resistance } R_{LV} = \frac{2000}{3 \times (721.687)^2} = 1.28 \times 10^{-3} \Omega$$

$$\text{At hv side, resistance } R_{HV} = \frac{2500}{3 \times (15.15)^2} = 3.63 \Omega$$

Turn ratio,

$$\frac{\text{Phase voltage (hv side)}}{\text{Phase voltage (lv side)}} = \frac{11}{0.40 / \sqrt{3}} = 47.63$$

Referred values on delta side (Δ side)

$$R_{eq}(\text{HV}) = 3.63 + 1.28 \times 10^{-3} (47.63)^2 = 6.53 \Omega \text{ (per phase)}$$

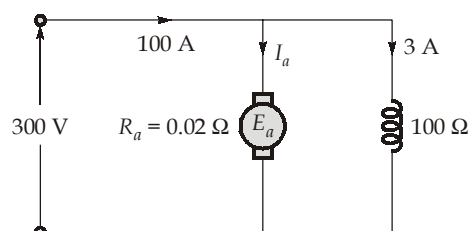
$$X(\text{p.u.}) = 0.05$$

$$Z_{\text{base}}(\text{HV}) = \frac{11000}{15.15} = 726.024 \Omega$$

$$X_{eq \text{ HV}} = 0.05 \times 726.024 = 36.30 \Omega \text{ (per phase)}$$

30. (c)

Case-I:



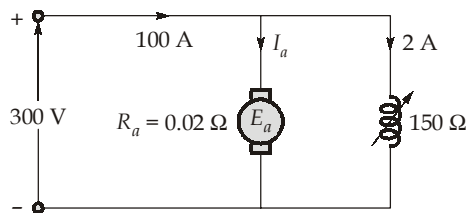
$$\text{Armature current, } I_{a1} = 100 - 3 = 97 \text{ A}$$

$$\text{Back emf, } E_{a1} = 300 - 97 \times 0.02$$

$$E_{a1} = 298.06 \text{ V}$$

Case-II:

When $50\ \Omega$ external resistance added in field circuit,



Load torque is constant

$$T \propto \phi I_a$$

$$\phi_2 I_{a2} = \phi_1 I_{a1}$$

$$\phi \propto I_f$$

$$I_{a2} = I_{a1} \frac{\phi_1}{\phi_2} = 97 \times \frac{3}{2} = 145.5\text{ A}$$

$$E_{a2} = 300 - 145.5 \times 0.02$$

$$E_{a2} = 297.09\text{ V}$$

We know that,

$$E_a \propto \phi \omega_m$$

$$\frac{E_{a2}}{E_{a1}} = \frac{\phi_2}{\phi_1} \times \frac{N_2}{N_1}$$

$$\frac{297.09}{298.06} = \frac{2}{3} \times \frac{N_2}{1600}$$

$$N_2 = 2392.18\text{ rpm}$$

