

## DETAILED EXPLANATIONS

1. (c)
$F_{1}$ covers $F_{2}$ : True
$F_{2}$ covers $F_{1}$ : True
2. (b)

$$
\begin{gathered}
\pi_{A, B}(R) \bowtie_{R . B<S . B} \rho_{S(A, B)}\left(\pi_{B . C}(R)\right) \\
\begin{array}{|ll|}
\hline \boldsymbol{A} & \boldsymbol{B} \\
\hline 1 & 2 \\
3 & 2
\end{array} \left\lvert\, \begin{array}{|ll|}
\hline \boldsymbol{A} & \boldsymbol{B} \\
\hline 2 & 3 \\
2 & 1 \\
\hline
\end{array}\right.
\end{gathered} \Rightarrow \begin{array}{|llll|}
\hline \boldsymbol{A} & \boldsymbol{B} & \boldsymbol{A} & \boldsymbol{B} \\
\hline 1 & 2 & 2 & 3 \\
3 & 2 & 2 & 3 \\
\hline
\end{array}
$$

3. (a)


So, ER-diagram represents many student can enroll many courses.

- In ER-diagram Relationship set can have own attribute.
- Many to one relation can be represented the relation between non-weak entity set.

4. (b)
$\mathrm{B}^{+}$tree index has more levels than B-tree index for large number of keys. Since in B-tree every key appears at only single level but which is not the case for $\mathrm{B}^{+}$tree.
5. (c)

$$
\frac{(3+2+1)!}{3!\cdot 2!}=\frac{6!}{3!\cdot 2!}=60
$$

6. (d)

Both the statements are incorrect.
The select operation is commutative i.e. $\sigma_{\mathcal{C}_{1}}\left(\sigma_{c_{2}}(R)\right) \Leftrightarrow \sigma_{C_{2}}\left(\sigma_{G_{1}}(R)\right)$.
Ultimately only those tupples will be selected which satisfy both $C_{1}$ and $C_{2}$. Hence order does not matter. But $\Pi$ (projection) operation is not commutative.
$\left.\Pi_{a_{1}}\left(\Pi_{a_{2}}(R)\right)=\Pi_{a_{1}}(R)\right)$ if and only if $a_{1}$ is substring (or subset) of $a_{2}$, otherwise operation would be incorrect.
7. (d)

The given locking protocol follows the properties of strict 2 PL which is conflict serializable, recoverable and avoid cascading rollbacks.
8. (c)

Candidate keys for the relation are: $P Q, Q S$ and $Q R$
$S \rightarrow P$, prime attribute $\rightarrow$ prime attribute (not allowed in BCNF but allowed in 3NF).
$\Rightarrow$ Relation $R$ is in 3NF but not in BCNF since $S \rightarrow P$ does have a superkey on the left hand side.
9. (c)

The precedence graph of the given schedule is


Therefore schedule is equivalent to $\left(T_{1}, T_{4}, T_{3}, T_{2}\right),\left(T_{1}, T_{3}, T_{4}, T_{2}\right)$ and $\left(T_{4}, T_{3}, T_{1}, T_{2}\right)$.
10. (d)

$$
\begin{aligned}
\text { Disk block size } & =5000 \text { records } \\
\text { Block size } & =10 \text { records or } 15 \text { (keys }+ \text { Pointers) }
\end{aligned}
$$

Sparse index at $1^{\text {st }}$ level. So number of disk block at $1^{\text {st }}$ level is number of block in database.

$$
\begin{aligned}
\text { Data base } & =\frac{5000}{10}=500 \text { blocks } \\
1^{\text {st }} \text { level } & =\left\lceil\frac{500}{15}\right\rceil=\lceil 33.33\rceil=34 \text { blocks } \\
2^{\text {nd }} \text { level } & =\left\lceil\frac{34}{15}\right\rceil=\lceil 2.26\rceil=3 \text { blocks } \\
3^{\text {rd }} \text { level } & =1 \text { block } \\
\text { Total } & =[500+34+3+1] \text { blocks } \\
& =538 \text { blocks }
\end{aligned}
$$

11. (b)

| $T_{1}$ | $T_{2}$ | $T_{3}$ |
| :--- | :---: | :---: |
|  | $S(A)$ |  |
|  | $R_{2}(A)$ |  |
| $X(B)$ |  |  |
| $W_{1}(B)$ |  |  |
| $X(C)$ |  |  |
| $W(C)$ |  | $S(B)$ |
| $S(A)$ |  | $R_{3}(B)$ |
| $U(A)$ |  |  |
|  |  |  |
|  | $S(B)$ |  |
|  | $R_{2}(B)$ |  |
| $S(B)$ |  |  |
| $R(A)$ |  |  |
| $U(B)$ |  |  |
| $C_{1}$ | $R_{2}(C)$ |  |
|  | $U(A) U(B)$ |  |
|  | $C_{2}$ | $X(A)$ |
|  |  | $W_{3}(A)$ |
|  |  | $U(B) U(A)$ |
|  |  | $C_{3}$ |

(i) Conflict serializable

(ii) Allowed by 2PL.
(iii) Not strict recoverable.
(iv) No allowed by strict 2PL.
12. (c)

If relation $R$ in 3NF but not BCNF then atleast two compound keys must exists where non-trivial FD with determinant not superkey.
13. (c)

The given relation with functional dependencies is in 3NF i.e., no transitive and partial function dependency exist but $C \rightarrow A$, violets BCNF i.e., super key $\rightarrow$ any attributes. So, relation $R$ in 3NF but not BCNF.
(d) $\{A B \rightarrow C, C \rightarrow A, B C \rightarrow D, B E \rightarrow C, E C \rightarrow A, C F \rightarrow B, D \rightarrow E\}$
14. (b)

| $[A B \rightarrow C$ |  | $[A B \rightarrow C$ |  | $[A B \rightarrow C$ |
| :---: | :---: | :---: | :---: | :---: |
| $C \rightarrow A$ |  | $C \rightarrow A$ |  | $C \rightarrow A$ |
| $B C \rightarrow D$ |  | $B C \rightarrow D$ |  | $B C \rightarrow D$ |
| $A C D \rightarrow B$ | $\xrightarrow{\text { After }}$ | $C D \rightarrow B$ | After | $B E \rightarrow C$ |
| $B E \rightarrow C$ | removal of | $B E \rightarrow C$ | removal of | $E C \rightarrow F$ |
| $E C \rightarrow F$ | extraneous | $E C \rightarrow F$ | redundant | $C F \rightarrow B$ |
| $E C \rightarrow A$ | attributes | $E C \rightarrow A$ | FD's | $D \rightarrow E]$ |
| $C F \rightarrow B$ |  | $C F \rightarrow B$ |  | Minimal |
| $C F \rightarrow D$ |  | $C F \rightarrow D$ |  | cover |
| $D \rightarrow E]$ |  | $D \rightarrow E]$ |  |  |

15. (a)

Condition $X=X_{1}$ and $Y \neq Y_{1}$ says that vertices whose starting vertex is same but end vertices is different, which returns vertices whose out degree is atleast 2.
16. (a)
$Q_{1}$ :Retrieves $A$ which are more than some $C$.
$Q_{2}$ :Retrieves $A$ which are more than some $C$.
$Q_{3}$ :Retrieves $A$ which are more than every $C$.
17. (b)

18. (a)

Order $P$ :

$$
\begin{aligned}
P \times \text { Pointer }+(P-1) \times \text { Key } & \leq \text { Block } \\
P \times 8+(P-1) 12 & \leq 1000 \\
20 P & \leq 1012 \\
P & =\left\lfloor\frac{1012}{20}\right\rfloor=50
\end{aligned}
$$

| Level | Min nodes | Min $B_{P}$ | Min keys |
| :---: | :---: | :---: | :---: |
| 1 | 1 | 2 | 1 |
| 2 | 2 | $2 \times 25$ | 24 |
| 3 | 50 | - | $50 \times 24$ |
| 1200 |  |  |  |

19. (a)

\# of serial schedules conflict equal to schedule $(S)$ is \# of topological orders

$$
\left.T_{1}<\begin{array}{l}
T_{2}-T_{4}-T_{5} \\
T_{4}-T_{2}-T_{5}
\end{array}\right\} 2 \text { sequences for } T_{1} T_{2} T_{4} T_{5}
$$

$T_{3}$ can be any where in both sequences. Total 10 topological order.
20. (b)

Order $P \Rightarrow P \times B_{P}+(P-1)$ Key $\leq$ Block

$$
P \times 12+(P-1) 20 \leq 512
$$

$$
32 P \leq 532
$$

$$
P=\left\lfloor\frac{532}{32}\right\rfloor=16
$$

Maximum index nodes in index mean min fill factor

21. (d)


Emp (ssn, Ename, rating)
Dept_manages (did, dname, address, ssn)
Works (ssn did)
Childs belongs to (ssn name, age, gender)
22. (a)

- Only serial schedules $T_{1} \rightarrow T_{2}, T_{2} \rightarrow T_{1}$ are conflict serializable.
- None of non serial schedules are conflict serializable.

23. (b)

$$
{ }^{5} C_{2}+{ }^{5} C_{3}+{ }^{5} C_{4}+{ }^{5} C_{5}=26
$$

24. (b)

The output Table will be

| Dealer-No. | Color-id |
| :---: | :---: |
| $D_{2}$ | $C_{2}$ |
| $D_{7}$ | $C_{3}$ |
| $D_{2}$ | $C_{5}$ |
| $D_{7}$ | $C_{6}$ |

25. (a)

$$
\begin{aligned}
\text { Content of index <key, BP> } & =6+10=16 \\
\text { Block factor of database } & =\frac{512}{16}=32 \\
\text { Number of block in database } & =\frac{8192}{32}=256
\end{aligned}
$$

In first level entry for each record,

$$
\text { Number of blocks in first level }=\frac{\text { Number of Database Block }}{\text { Entry size of 1st level }}=\left\lfloor\frac{256}{32}\right\rfloor=8
$$

In second level

$$
\text { Number of blocks in second level }=\frac{\text { Number of 1st level Block }}{\text { Entry size of 2nd level }}=\left\lceil\frac{8}{32}\right\rceil=1
$$

26. (b)


Null value of $B$ column record not references to any record of $S$. Remaining records of $R$ references to atmost one record of $S$.
27. (c)
$\left\{t \mid \exists r \in\right.$ student $(r[$ ID $]=t[I D]) \wedge\left(\forall u \in\right.$ course $\left(u\left[d e p t \_n a m e\right]=" C S " \Rightarrow \exists s \in\right.$ takes $(t[I D]=s[I D] \wedge$ $s[$ course_id] $=u[$ course_id])) $\}$ will results all students who have taken all courses offered in the CS department. Since we know that $P \Rightarrow Q \equiv$ not $P \vee Q$, so option (b) is also true.
28. (a)

In wait-die scheme, when transaction $T_{i}$ request a data items currently held by $T_{j}$, $T_{i}$ is allowed to wait only if it has a time stamp smaller then that of $T_{j}$ otherwise $T_{i}$ is rolled back (die). Here process $P$ is running so it has time stamp less than process $Q$ now if process $P$ need a resource held by process $Q$ then process $P$ has to wait.
29. (d)

Checking for conflict serializable:


Cycle is present
So not conflict serialiazable

Since their is blind write between $W_{2}(a)$ to $W_{3}(a)$, so it may be view serializable.
Checking for view serializability:

1. Final write:

$$
\begin{equation*}
a=T_{1}, b=T_{3} \tag{1}
\end{equation*}
$$

2. Initial read: $\quad a=T_{1}, T_{2} b=T_{3}, c=T_{1}$
3. Write read: No write read

$$
\begin{align*}
\left(T_{2}, T_{3}\right) & \rightarrow T_{1} \\
T_{1} & \rightarrow T_{2}, T_{3} \tag{2}
\end{align*}
$$

from (1)

Both at a time not possible, so not view serializable.
30. (b)

If we insert keys $45,48,55$ in same order, then on insertion of key 55 , root will be overflow and new level will be created.

