

ESE | GATE | PSUs

State Engg. Exams

MADE EASY
WORKBOOK 2025



**Detailed Explanations of
Try Yourself Questions**

Electronics Engineering
Electromagnetics



1

Vector Analysis

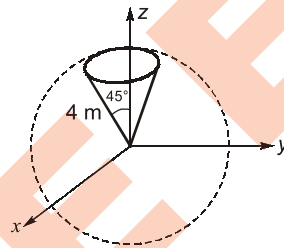
T1. Sol.

$$\bar{A} = \nabla f = 4xyz\hat{a}_x + 2x^2z\hat{a}_y + 2x^2y\hat{a}_z$$

$$(0, 0, 0) \xrightarrow{dx \hat{a}_x} (2, 0, 0) \xrightarrow{dy \hat{a}_y} (2, 7, 0) \xrightarrow{dz \hat{a}_z} (2, 7, 4)$$

$$\therefore \int \bar{A} \cdot d\bar{l} = \int_{z=0}^4 4xyz dx @_{y=0}^{y=7} + \int_{x=2}^4 2x^2 z dy @_{z=0}^{z=4} + \int_{y=7}^4 2x^2 y dz @_{x=2}^{x=2} = 224$$

T2. Sol.



$$\oint \bar{D} \cdot d\bar{s} :$$

Spherical co-ordinate system : $\hat{a}_r, \hat{a}_\theta, \hat{a}_\phi / dr d\theta d\phi / r \sin\theta$

$$\int \frac{5r^2}{4} \cdot r^2 \sin\theta d\theta d\phi @_{\theta=0, \frac{\pi}{4}} @_{\phi=0, 2\pi}$$

$$= 589.1 \text{ C}$$

$$\int (\nabla \cdot \bar{F}) dV :$$

$$\nabla \cdot \bar{D} = 5r$$

$$dV = r^2 \sin\theta d\theta d\phi dr$$

T3. Sol.

$$\nabla \cdot \bar{F} = \frac{1}{\rho} \frac{\partial}{\partial \rho} (\rho\rho) + \frac{1}{\rho} \frac{\partial}{\partial \phi} [\rho(\sin^2 \phi)] + \frac{\partial}{\partial z} (-z)$$

$$= 2 + 2\sin\phi \cos\phi - 1 = 1 + \sin 2\phi$$

$$\text{If } \phi = 0,$$

$$\text{If } \phi = \frac{\pi}{2},$$

$$\nabla \cdot \bar{F} = 1 + \sin 2\phi$$

$$\nabla \cdot \bar{F} = 1$$

$$\nabla \cdot \bar{F} = 1$$

If $\phi = \frac{\pi}{4}$,

$\nabla \cdot F = 2$

Hence, option (d) satisfied.

T4. Sol.

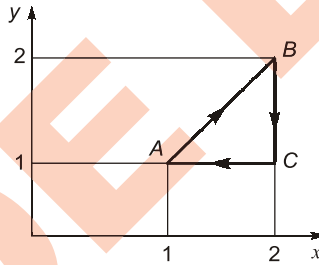
$$\begin{aligned} \nabla \cdot \vec{A} &= \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \cdot \frac{1}{r} \right) + \frac{1}{r \sin \theta} \frac{\partial}{\partial \theta} (-r^2 \sin \theta \sin \theta) + \frac{1}{r \sin \theta} \frac{\partial}{\partial \phi} (10 \cos \phi) \\ \nabla \cdot \vec{A} &= \frac{1}{r^2} - 2r \cos \theta - \frac{10 \sin \phi}{r \sin \theta} \\ \nabla \cdot \vec{A} \Big|_{\left(2, \frac{\pi}{4}, \frac{\pi}{2} \right)} &= \frac{1}{4} - \frac{4}{\sqrt{2}} - \frac{10}{2 \times \frac{1}{\sqrt{2}}} = \frac{1}{4} - 7\sqrt{2} = -9.65 \end{aligned}$$

T5. Sol.

$$\begin{aligned} \nabla \cdot A &= \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 \cdot Kr^n) = \frac{1}{r^2} K(n+2) r^{n+2} \\ \nabla \times A &= 0 \end{aligned}$$

Hence, option (b) is correct.

T6. Sol.



$$\begin{aligned} \oint \vec{A} \cdot d\vec{l} &= \left[\int_{A \rightarrow B} + \int_{B \rightarrow C} + \int_{C \rightarrow A} \right] \vec{A} \cdot d\vec{l} \\ \left. \begin{aligned} \vec{A} &= 3x^2y^3\hat{a}_x - x^3y^2\hat{a}_y \\ d\vec{l} &= dx\hat{a}_x + dy\hat{a}_y \end{aligned} \right\} \vec{A} \cdot d\vec{l} = 3x^2y^3dx - x^3y^2dy \end{aligned}$$

Path AB : $y = x \Rightarrow dy = dx$

$$\int \vec{A} \cdot d\vec{l} = \int 3x^2y^3dx - x^3y^2dy = \int 3x^5 - x^5 dx = \int_{x=1}^2 2x^5 dx = 2 \cdot \frac{x^6}{6} \Big|_1^2 = 21$$

Path BC : $x = 2 \Rightarrow dx = 0$

$$\int \vec{A} \cdot d\vec{l} = -\int x^3y^2dy = -x^3 \int_{y=2}^1 y^2 dy @ x=2 = -8 \times \frac{y^3}{3} \Big|_2^1 = +\frac{56}{3}$$

Path CA : $y = 1 \Rightarrow dy = 0$

$$\int \bar{A} \cdot d\bar{l} = \int 3x^2 y^3 dx = 3y^3 \int_{x=2}^1 x^2 dx @ y=1 = 3 \cdot \frac{x^3}{3} \Big|_2^1 = -7$$

$$\therefore \oint \bar{A} \cdot d\bar{l} = 21 + \frac{56}{3} - 7 = \frac{98}{3}$$

$\int (\nabla \times \bar{A}) \cdot d\bar{s}$:

$$\nabla \times \bar{A} = \begin{vmatrix} \hat{a}_x & \hat{a}_y & \hat{a}_z \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ 3x^2 y^3 & -x^3 y^2 & 0 \end{vmatrix} = -12x^2 y^2 \hat{a}_z$$

$$d\bar{s} = dx dy (-\hat{a}_z)$$

$$\begin{aligned} \therefore \int \nabla \times \bar{A} \cdot d\bar{s} &= 12 \int_{x=1}^2 x^2 dx \int_{y=1}^x y^2 dy = 12 \int_{x=1}^2 x^2 dx \frac{y^3}{3} \Big|_{y=1}^x = \frac{12}{3} \int_{x=1}^2 x^2 dx (x^3 - 1) \\ &= 4 \left[\int_1^2 x^5 dx - \int_1^2 x^2 dx \right] = \frac{98}{3} \end{aligned}$$

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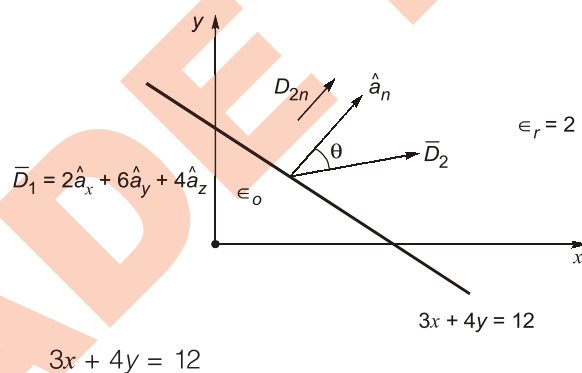
2

Maxwell's Equations and Boundary Conditions

T1. Sol.

$$\begin{aligned} \phi &= Q_{\text{enc}} = \int \rho_v dV = \int (\nabla \cdot \bar{D}) dV \\ \Rightarrow \phi &= \int_V (y + x + z) \cdot dx dy dz = \int_{y=-2}^2 y dy \int_{x=1}^4 dx \int_{z=-1}^2 dz + \int_{x=1}^4 x dx \int_{y=-2}^2 dy \int_{z=-1}^2 dz + \int_{z=-1}^2 z dz \int_{x=1}^4 dx \int_{y=-2}^2 dy \\ \Rightarrow \phi &= \frac{y^2}{2} \Big|_{-2}^2 \cdot x \Big|_1^4 \cdot z \Big|_{-1}^2 + \frac{x^2}{2} \Big|_1^4 \cdot y \Big|_{-2}^2 \cdot z \Big|_{-1}^2 + \frac{z^2}{2} \Big|_{-1}^2 \cdot x \Big|_1^4 \cdot y \Big|_{-2}^2 \\ \Rightarrow \phi &= 0 + \frac{15}{2} \cdot 4 \cdot 3 + \frac{3}{2} \cdot 3 \cdot 4 = 90 + 18 = 108 \text{ C} \end{aligned}$$

T2. Sol.



@ $x = 0 ; y = 3$

@ $y = 0 ; x = 4$

$$\hat{a}_n = \frac{\nabla f}{|\nabla f|} = \frac{3\hat{a}_x + 4\hat{a}_y}{5}$$

Normal component :

$$\therefore D_{1n} = \bar{D}_1 \cdot \hat{a}_n = 2\hat{a}_x + 6\hat{a}_y + 4\hat{a}_z \cdot \frac{3\hat{a}_x + 4\hat{a}_y}{5} = \frac{6 + 24}{5} = 6$$

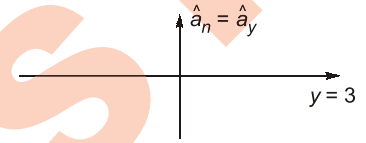
$$\therefore \bar{D}_{1n} = D_{1n} \cdot \hat{a}_n$$

$$\Rightarrow D_{1n} = 6 \left\{ \frac{3\hat{a}_x + 4\hat{a}_y}{5} \right\} = \boxed{3.6\hat{a}_x + 4.8\hat{a}_y = \bar{D}_{2n}}$$

$$\begin{aligned} \therefore \bar{H}_{1t} &= \bar{H}_1 - H_{1n} = (6, 8, 4) - (6, 8, 0) = 4\hat{a}_z \\ \text{Now, @ } \bar{K} = 0, \bar{H}_{1t} = \bar{H}_{2t} &\Rightarrow \bar{H}_{2t} = 4\hat{a}_z \\ \text{Also, } \bar{B}_{1n} &= B_{2n} \\ \Rightarrow \mu_1 \bar{H}_{1n} &= \mu_2 \bar{H}_{2n} \\ \Rightarrow \bar{H}_{2n} &= \frac{\mu_1}{\mu_2} \bar{H}_{1n} = \frac{2}{5} \{6\hat{a}_x + 2\hat{a}_y\} = 2.4\hat{a}_x + 0.8\hat{a}_y \\ \therefore \bar{H}_2 &= \bar{H}_{2t} + \bar{H}_{2n} = 2.4\hat{a}_x + 0.8\hat{a}_y + 4\hat{a}_z \end{aligned}$$

T5. Sol.

$$\begin{aligned} (\bar{H}_{1t} - \bar{H}_{2t}) \times \hat{a}_{n12} &= \bar{K} \\ \therefore [(4\hat{a}_x + 7\hat{a}_y - 5\hat{a}_z) - (8\hat{a}_x + 14\hat{a}_y - 5\hat{a}_z)] \times \hat{a}_y &= \bar{K} \\ \Rightarrow [-4\hat{a}_x - 7\hat{a}_y] \times \hat{a}_y &= \bar{K} \\ \therefore -4\hat{a}_z &= \bar{K} \end{aligned}$$



T6. (c)

Relative motion always causes induced emf which is absent in option (c).

T7. Sol.

Source free space, $\rho_v = 0, \bar{J} = 0, \sigma = 0$

(a) $\nabla \cdot \bar{D} = \rho_v = 0 \Rightarrow \nabla \cdot \bar{E} = 0$

(b) $\nabla \cdot \bar{B} = 0$

(c) $\nabla \times \bar{E} = -\frac{\partial \bar{B}}{\partial t}$

(d) $\nabla \times \bar{H} = \bar{J} + \frac{\partial \bar{D}}{\partial t} = \sigma \bar{E} + \epsilon \frac{\partial \bar{E}}{\partial t}$

$\Rightarrow \nabla \times \bar{H} = \epsilon \frac{\partial \bar{E}}{\partial t}$

$\Rightarrow \nabla \times \bar{B} = \mu_o \epsilon_o \frac{\partial \bar{E}}{\partial t}$

$\Rightarrow \nabla \times \bar{B} - \frac{1}{c^2} \frac{\partial \bar{E}}{\partial t} = 0$



3

Electromagnetic Waves

T1. Sol.

- (a) Attenuation in Y-direction and propagation in ZX-direction. (Invalid)
- (b) Valid
- (c) Valid
- (d) Invalid- $\frac{\omega}{\beta} = 2 \times 10^8$ m/s not 3×10^8 m/s
- (e) Invalid- E or H having phase shift
- (f) Invalid- H is not orthogonal to propagation.

T2. (c)

Heaviest attenuation in case-3 and highest loss tangent.

T3. (c)

$$\gamma = \sqrt{j\omega\mu(\sigma + j\omega\epsilon)} = \sqrt{j\omega\mu \cdot j\omega\epsilon \left(1 + \frac{\sigma}{j\omega\epsilon}\right)} = j\omega\sqrt{\mu\epsilon} \left(\sqrt{1 + \frac{j\sigma}{\omega\epsilon}}\right)$$

T4. Sol.

$$V_p \text{ of the wave} = \frac{0.6}{5 \times 10^{-9}} = 1.20 \times 10^8 \text{ m/s}$$

$$\lambda = \frac{1.20 \times 10^8}{1} = 120 \text{ MHz}$$

T5. (b)

$$\delta = \frac{1}{\alpha} \quad \text{where } \alpha \text{ is zero (attenuation constant)}$$

$$\delta = \infty \text{ for } \sigma = 0$$

T6. Sol.

(i) $\beta = 250 \text{ rad/m}$

(ii) $v_p = \frac{\omega}{\beta} \quad \omega = 3 \times 10^8 \times 250 \quad ; \quad \omega = 75 \times 10^9 \text{ rad/sec}$

$$\begin{aligned} \text{(iii)} \quad & \beta = 250 = \frac{2\pi}{\lambda} \\ & \lambda = \frac{\pi}{125} \text{ m} \\ \text{(iv)} \quad & \eta = 120 \Omega \\ \text{(v)} \quad & H_s = \frac{200 \angle 30^\circ}{120\pi} e^{-j250z} a_y \text{ A/m} \end{aligned}$$

T7. (d)

For a good conducting medium

$$\alpha = \beta = \sqrt{\frac{\omega\mu\sigma}{2}} = \sqrt{\pi f\mu\sigma}$$

\therefore Phase velocity

$$v_p = \left(\frac{\omega}{\beta} \right) = \frac{\omega}{\sqrt{\frac{\omega\mu\sigma}{2}}} = \sqrt{\frac{2\omega}{\mu\sigma}} = \sqrt{\frac{4\pi f}{\mu\sigma}} = 2\sqrt{\frac{\pi f}{\mu\sigma}}$$

T8. Sol.

$\frac{\sigma}{\omega\epsilon}$ decides type of material

$$\frac{12 \times 10^2}{2\pi \times 10^7 \times \frac{1}{36\pi \times 10^9}} \gg 1$$

T9. Sol.

$$\frac{J_c}{J_d} = 1 \quad ; \quad \frac{\sigma}{\omega\epsilon} = 1$$

$$n\text{'s phase} = E_x \text{ to } H_y \text{ phase} = \frac{\tan^{-1}(\sigma/\omega\epsilon)}{2} = 22.5^\circ$$

T10. Sol.

$$\begin{aligned} P_{\text{avg}} &= \frac{1}{2} (E \times H^*) \\ &= \frac{100}{2} \begin{vmatrix} \hat{a}_x & \hat{a}_y & \hat{a}_z \\ j & 2 & -j \\ -1 & -j & 1 \end{vmatrix} \\ &= 50(3\hat{a}_x + 3\hat{a}_z) = 150(\hat{a}_x + \hat{a}_z) \end{aligned}$$

T11. (a)

Linear: In phase components.

T12. Sol.

$$\eta = \frac{25}{1.2} \angle 35^\circ = \frac{E_x}{H_y}$$

T13. Sol.

(0, 0, 0) to (1, 1, 1) - propagation directions

$$\beta_x = \beta_y = \beta_z = \frac{\beta}{\sqrt{3}}$$

Wave polarized in YZ plane

$$E \text{ direction} = K_1 \hat{a}_y + K_2 \hat{a}_z$$

$$K_1 = K_2 \text{ as } \beta_y = \beta_z$$

$$\beta_y \cdot K_1 + \beta_z K_2 = 0$$

$$E(x, y, z, t)_{(y,z)} = E_o e^{j(\omega t - \beta/\sqrt{3}(x+y+z))} \frac{(\hat{a}_y - \hat{a}_z)}{\sqrt{2}} \text{ or } \frac{(-\hat{a}_y + \hat{a}_z)}{\sqrt{2}}$$

T14. Sol.

$E(y, z, t)_{(y,z)}$ - E direction and propagation direction in same plane.

T15. Sol.

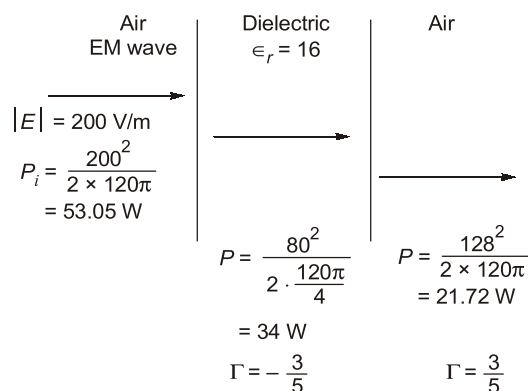
(i) $V_p = \frac{2\pi \times 10^7}{0.8} \neq 3 \times 10^8$ Wrong

(ii) Wave has $\alpha = 0$

So, lossless medium but not conductor. As conductor has heavy loss.

(iii) $V_p = \frac{2\pi \times 10^7}{0.8} = 0.78 \times 10^8 \text{ m/s}$

(iv) Power density = $\frac{1}{2} \times \frac{4^2}{120\pi} \times \sqrt{\epsilon_R} = 21\sqrt{\epsilon_R} \frac{\text{mW}}{\text{m}^2}$

T16. Sol.

$$\tau_E = \frac{2\eta_2}{\eta_1 + \eta_2} = \frac{2 \times \frac{1}{4}}{\frac{1}{4} + 1} = \frac{\frac{2}{4}}{\frac{5}{4}} = \frac{2}{5}$$

$$\therefore \frac{E_t}{E_i} = \tau_E \Rightarrow E_t = \frac{2}{5} \times 200 = 80 \text{ V/m}$$

$$\tau_E = \frac{2\eta_2}{\eta_1 + \eta_2} = \frac{2}{\frac{1}{4} + 1} = \frac{2}{5} \times 4 = \frac{8}{5}$$

$$\therefore E_t = \tau_E \times E_i = \frac{8}{5} \times 80 = 128 \text{ V/m}$$

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4

Transmission Lines

T1. Sol.

25 dB per 25 km

1 dB/km is the attenuation rate

2.5 dB corresponds to 2.5 km

$$D = 2.5 \text{ km}$$

T2. (d)

$$\Gamma \text{ in first case} = \frac{2Z - Z}{2Z + Z} = \frac{1}{3}$$

$$\Gamma \text{ in second case} = \frac{Z/2 - Z}{Z/2 + Z} = -\frac{1}{3}$$

$$\text{Power reflection coefficient} = \frac{1}{9}$$

Same power in both case.

T3. (c)

$$\frac{\beta}{\omega L} = \frac{\omega \sqrt{LC}}{\omega L} = \sqrt{\frac{C}{L}} = \frac{1}{Z_0}$$

T4. (b)

Distortionless line has $\frac{L}{R} = \frac{C}{G}$

$$\alpha = \sqrt{RG} = \sqrt{RG} = \sqrt{R \cdot \frac{RC}{L}} = R \sqrt{\frac{C}{L}}$$

T5. (a)

$$I(x) = I_L \cosh(rx) + \frac{V_L}{Z_0} \sinh(rx)$$

with $V_L = 0$ at short circuit, $I(x) = I_L \cosh(rx)$

T6. (c)

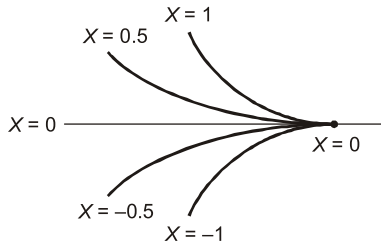
Z_0 depends on physical dimensions but never on the length of the line.

T7. (a)

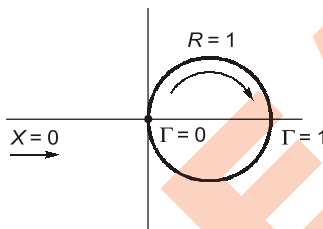
$$\Gamma = \frac{j20 - 50}{j20 + 50} = 1 \angle 180^\circ - \tan^{-1}\left(\frac{2}{5}\right) = 1 \angle 136^\circ$$

T8. (a, b, c)

Symmetry of lines are clearly as shown below



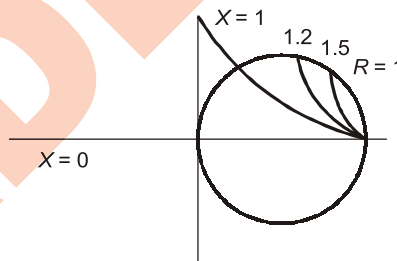
(b) and (c) True



Hence, a, b and c are correct.

T9. (a)

$$\frac{Z_L}{Z_o} = R + jX \text{ with } R > 1$$



T10. (a)

$$\lambda = \frac{3 \times 10^8}{2 \times 10^9} = 0.15 \text{ m} = 15 \text{ cm}$$

$$\frac{\lambda}{2} = 7.5 \text{ cm} \Rightarrow 1^{\text{st}} \text{ minimum is at the load}$$

Z_L is resistive and less than Z_o .

T11. Sol.

$$Z_{SC} = jZ_o \tan \beta l = j25$$

Inductive reactance to cancel the load reactance

$$j50 \tan \beta l = j25$$

$$\tan \beta l = \frac{1}{2}$$

$$\beta l = 0.46 \text{ radians}$$

$$l = \frac{0.46}{2 \times 3.14} \times \frac{3 \times 10^8}{10 \times 10^9} = 0.22 \text{ cm}$$

T12. Sol.

$$\Gamma = \frac{Z_L - Z_o}{Z_L + Z_o} = \frac{75 - 50}{75 + 50} = \frac{25}{125} = \frac{1}{5}$$

$$\therefore S = \frac{1 + 1/5}{1 - 1/5} = \frac{6}{4} = \frac{3}{2}$$

$$\therefore Z_{\max} = Z_o \cdot S = 75$$

$$Z_{\min} = \frac{Z_o}{S} = \frac{100}{3}$$

$$\frac{Z_{\max}}{Z_{\min}} = 2.25$$

T13. (b)At the input when $t = 0$,

$$V_{\text{in}} = \frac{120}{300} \times 300 = 120 \text{ V}$$

$$\Gamma \text{ at load} = \frac{100 - 120}{100 + 120} = \frac{-1}{11}$$

The reflected voltage cancels to 120 V and reduces to less than 120 V.

T14. Sol.

$$2\beta Z_{\max} = 2n\pi + \theta$$

$$\Rightarrow 2 \cdot \frac{2\pi}{150} \cdot 500 = 2n\pi - 150$$

$$\Rightarrow \frac{40\pi}{3} = 2n\pi - \frac{6\pi}{6}$$

$$\Rightarrow \frac{40}{3} = 2n - \frac{5}{6}$$

$$\Rightarrow n = 7.08 \simeq 7$$

$$2\beta Z_{\max} = 2\pi - 150$$

$$Z_{\max} = 43 \text{ m}$$

$$\Rightarrow 1^{\text{st}} \text{ max} = 43$$

$$\Rightarrow 2^{\text{nd}} \text{ max} = 43 + \{\text{distortion between two successive max}\}$$

$$= 43 + \frac{\lambda}{2} = 43 + \frac{159}{2} = 43 + 75 = 118$$

Number of maximas on the line, $n = 7$ 

5

Waveguides

T1. Sol.

$$V_g = \frac{d\omega}{d\beta} = \sqrt{A\omega}$$

$$\frac{d\omega}{\sqrt{\omega}} = \sqrt{A} d\beta$$

Integrate on both sides, $\frac{(\omega)^{1/2}}{1/2} = \sqrt{A}\beta$

$$2\sqrt{\omega} = \sqrt{A}\beta$$

Divide with ω on both sides, $\frac{2\sqrt{\omega}}{\omega} = \sqrt{A} \frac{\beta}{\omega}$

$$\frac{\omega}{\beta} = V_p = \sqrt{\frac{A\omega}{2}} = \frac{V_g}{2} \quad \text{As } \beta \propto \omega^{1/2}$$

T2. Sol.

$$\sin\theta = \frac{f_c}{f}$$

$$\text{First mode } f_c = \frac{c}{2a} = \frac{3 \times 10^8}{\sqrt{9} \times 2 \times 3 \times 10^{-2}}$$

$$f_c = \frac{5}{3} \text{ GHz} = 1.67 \text{ GHz}$$

$$\sin\theta = \frac{1.67}{2}$$

$$\theta = 56^\circ$$

T3. Sol.

$$f_c \text{ for dominant mode TE}_{10} \quad f_c = \frac{c}{2a} = \frac{3 \times 10^8}{2 \times 7 \times 10^{-2}} = 2.14 \text{ GHz}$$

$$\text{TE}_{20} f_c = 4.28 \text{ GHz}$$

$$\text{TE}_{01} f_c = \frac{c}{2b} = \frac{3 \times 10^8}{2 \times 4 \times 10^{-2}} = 3.75 \text{ GHz}$$

$$\frac{\text{TE}_{11}}{\text{TM}_{11}} f_c = 4.3 \text{ GHz}$$

Total 5 modes $\text{TE}_{10} - \text{TE}_{20} - \text{TE}_{01} - \text{TE}_{11} - \text{TM}_{11}$.

T4. (b)**T5. (c, d)**

Maximum single mode operational bandwidth when $a \leq 2b$.

T6. (c)

TM₁₂,

T7. Sol.

$$TE_1 f_c = \frac{c}{2a} = \frac{3 \times 10^8}{2 \times 3 \times 10^{-2}} = 5 \text{ GHz}$$

7 modes: TE₁, TM₁, TE₂, TM₂, TE₃, TM₃ and TEM

T8. Sol.

$$\begin{aligned} \text{Power dissipated} &= \frac{1}{2} \frac{E_0^2}{n} a \cdot b = \frac{E_0^2}{120\pi} \cos\theta a \cdot b \\ &= \frac{1}{4} \times \frac{4 \times 4 \times 10^6}{377} \sqrt{1 - \frac{1}{4}} \times 2 \times 10^{-4} = 1.8 \text{ W} \end{aligned}$$

T9. Sol.

Least possible TM mode is TM₁₁

$$f_c = \left(\sqrt{\left(\frac{1}{a}\right)^2 + \left(\frac{1}{a}\right)^2} \right) \frac{c}{2} = \frac{c}{\sqrt{2} a} = 21.2 \text{ GHz}$$

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6

Antennas

T1. (d)

A small loop has an approximate gain of 1.5.

$$\text{Gain} = \frac{4\pi}{\lambda^2} \cdot Ae$$

$$\lambda = \sqrt{\frac{4\pi \cdot 3}{1.5 \cdot 32\pi}} = 0.5 \text{ m} = 500 \text{ mm}$$

T2. (c)

$$W_r = \frac{W_t \cdot G_t \cdot G_r}{\left(\frac{4\pi d}{\lambda}\right)^2}$$

$$d = 1000 \text{ m}; \quad f = 300 \text{ kHz}; \quad \lambda = \frac{3 \times 10^8}{300 \times 10^6} = 1 \text{ m}; \quad G_t = 10; \quad G_r = 10^{0.8}$$

$$\therefore W_r = \frac{25 \times 10 \times 10^{0.8}}{\left(\frac{4\pi \times 10 \times 10^3}{1}\right)^2} = 99.8 \text{ nW}$$

T3. (a)

$$\text{Gain} = \frac{4\pi V_o \sin\theta \sin^2\phi}{\int_{\theta=0}^{\pi} \int_{\phi=0}^{\pi} V_o \sin\theta \sin^2\phi \sin\theta d\theta d\phi}$$

$$\int_{\theta=0}^{\pi} \sin^2\theta d\theta = \int_{\theta=0}^{\pi} \left(\frac{1 - \cos 2\theta}{2}\right) d\theta = \frac{\pi}{2}$$

$$D = \frac{4\pi}{\frac{\pi}{2} \times \frac{\pi}{2}} = 5.1$$

T4. (c)

$\lambda/2$ dipole open circuit at one end and other end is also open. It is a shunt LC circuit with radiation resistance of 73Ω .

T5. (d)

Most monopoles are used to produce vertical polarized waves suitable for ground waves.

T6. (c)

E and H fields in a dipole antenna exists as induction and radiation terms.

H or E depending as $1/r$ is radiation field.

E_θ has single $1/r$ term.

H or E depending as $1/r^2$ and $1/r^3$ and induction.

E_r , E_θ and H_ϕ have such fields.

T7. Sol.

$$\text{Gain} = 5 \sin 2\theta \quad \text{Directivity} = 5$$

In half power direction gain = 2.5

$$\text{Power density} = \frac{E_{\text{rms}}^2}{120\pi} = \frac{W_t G_t}{4\pi d^2}$$

$$E_{\text{rms}} = \frac{\sqrt{30 \times 1 \times 10^3 \times 2.5}}{5 \times 10^3} = 0.054 \text{ V/m}$$

T8. Sol.

Any antenna is a resonant device under oscillations of V and I .

Marconi antenna is a $\lambda/4$ monopole and resonant at any length and any side.

T9. Sol.

Broadside array means $\alpha = 0$

$$\frac{\sin(N\psi/2)}{\sin(\psi/2)} = \text{Array pattern}$$

For null directions $\frac{N\psi}{2} = 2n\pi$ with $\frac{\psi}{2} \neq 2n\pi$ as denominator $\sin\left(\frac{\psi}{2}\right) \neq 0$

$$\psi \neq 4n\pi$$

$$\psi = \frac{4n\pi}{N} = \frac{4n\pi}{6} = \frac{2n\pi}{3}$$

$$\psi = \beta d \cos\theta = \frac{2n\pi}{3}$$

$$\frac{2\pi}{\lambda} \cdot \frac{\lambda}{2} \cos\theta = \frac{2\pi}{3} \quad \text{when } n = 1$$

$$\cos\theta = \frac{2}{3} \Rightarrow \theta_{NP} = 42^\circ$$

$$\text{Beam width first Nulls} = \frac{\text{HPBW}}{2} = 84^\circ$$

T10. (b)

$$\psi = 0 + \frac{2\pi}{\lambda} \cdot \frac{\lambda}{4} \cos\theta = \frac{\pi}{2} \cos\theta$$

For maximas $\frac{\pi}{2} \cos \theta = 0$ $\theta_{\max} = 90^\circ$ or 270°

For minimas, $\psi = \pi$ $\frac{\pi}{2} \cos \theta = \pi$ this is not possible

For half power points $\frac{\pi}{2} \cos \theta = \frac{\pi}{2}$ $\theta = 0^\circ$ or 180°

T11. Sol.

As per multiplication of patterns

$$\sin \theta \cos(\psi/2) = 0 \text{ towards } 45^\circ \text{ direction}$$

$$\frac{\psi}{2} = \frac{\pi}{2} \text{ or } (2n+1) \frac{\pi}{2}$$

$$\alpha + \beta d \cos \theta = \pi \text{ with } \alpha = \pi \text{ due to image}$$

The next solution $\pi + \frac{2\pi}{\lambda} d \frac{1}{\sqrt{2}} = 3\pi$

$$d = \lambda\sqrt{2} \text{ is possible when } \theta = 45^\circ$$

For maxima direction

$$\pi + \frac{2\pi}{\lambda} \sqrt{2\lambda} \cdot \cos \theta = 2\pi$$

$$\cos \theta = \frac{1}{2\sqrt{2}}$$

$$\theta = 70^\circ$$

T12. (a)

$$E_{\text{rms}} = \frac{\sqrt{30W_t}}{d} = \frac{\sqrt{30 \times 3 \times 10^3}}{3 \times 10^3} = 0.1 \text{ V/m}$$

T13. (a)

$$\text{Gain} = \frac{4\pi}{\Omega_A} = \frac{4\pi}{(\text{HPBW})^2} = \frac{4\pi}{\lambda^2} \cdot \pi R^2$$

$$\text{HPBW} \propto \frac{\lambda}{D}$$

T14. Sol.

$$\text{Gain} = 6 \text{ dB over isotropic} = 4$$

250 mW with gain 4

With isotropic antenna, $\text{Power} = \frac{250}{4} = 62.5 \text{ mW}$

T15. (a)

