

**ESE | GATE | PSUs**

**State Engg. Exams**

**MADE EASY**  
**WORKBOOK 2025**



**Detailed Explanations of  
Try Yourself *Questions***

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**Mechanical Engineering**  
Design of Machine Elements



# 1

## Static & Fluctuating Stresses



### Detailed Explanation of Try Yourself Questions

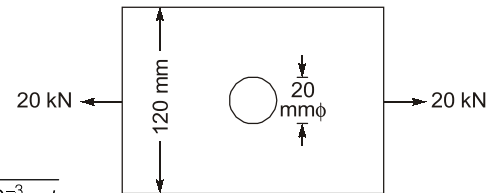
#### T1 : Solution

⇒

⇒

$$\sigma = \frac{P}{A}$$
$$\frac{600 \times 10^6}{3 \times 5} = \frac{20 \times 10^3}{(120 - 20) \times 10^{-3} \times t}$$

$$t = \frac{2 \times 10^5}{4 \times 10^7} = 5 \times 10^{-3} \text{ m} = 5 \text{ mm}$$



#### T2 : Solution

Mean stress,

$$\sigma_m = \frac{200 + (-100)}{2} = 50 \text{ MPa}$$

Variable stress,

$$\sigma_v = \frac{200 - (-100)}{2} = 150 \text{ MPa}$$

Soderberg's formula,

$$\frac{1}{N} = \frac{\sigma_m}{\sigma_y} + \frac{\sigma_v}{\sigma_e}$$

$$\frac{1}{2} = \frac{50}{0.55 \times \sigma_u} + \frac{150}{0.5 \times \sigma_u} = \frac{1}{\sigma_u} \left[ \frac{50}{0.55} + \frac{150}{0.5} \right]$$

⇒

$$\sigma_u = 781.818 \text{ MPa} \approx 781.82 \text{ MPa}$$

#### T3 : Solution

$$\sigma_{\max} = \frac{32M_{\max}}{\pi d^3} = \frac{32 \times 500}{\pi d^3} = \frac{5092.96 \times 10^3}{d^3} \text{ MPa}$$

$$\sigma_{\min} = \frac{32M_{\min}}{\pi d^3} = \frac{32 \times -200}{\pi d^3} = \frac{-2037.18 \times 10^3}{d^3} \text{ MPa}$$

$$\sigma_{\text{mean}} = \frac{\sigma_{\max} + \sigma_{\min}}{2} = \frac{1527.89 \times 10^3}{d^3} \text{ MPa}$$

$$\sigma_v = \frac{\sigma_{\max} - \sigma_{\min}}{2} = \frac{3565.07 \times 10^3}{d^3} \text{ MPa}$$

For ductile material-using Soderberg equation

$$\frac{1}{N} = \frac{\sigma_m}{\sigma_y} + \frac{\sigma_v}{\sigma_e} \quad [\sigma_e = 0.5 \sigma_u]$$

$$\frac{1}{2.5} = \frac{1527.89 \times 10^3}{400d^3} + \frac{3565.07 \times 10^3}{\frac{540}{2} \times d^3}$$

$$\Rightarrow d^3 = 2.5 \times 10^3 \times \left[ \frac{1527.89}{400} + \frac{3565.07 \times 2}{540} \right] = 34.91 \text{ mm}$$

$$\Rightarrow d \simeq 35 \text{ mm}$$



# 2

## Welded, Riveted and Bolted Joint



### Detailed Explanation of Try Yourself Questions

#### T1 : Solution

Pitch of rivets,

$$\rho = \frac{\pi(D+t)}{\text{No. of rivets/row}} = \frac{\pi(1600+30)}{45}$$
$$= 113.8 \text{ mm} \approx 115 \text{ mm}$$

Efficiency,

$$\eta_c = 1 - \frac{d}{\rho} = 1 - \frac{35}{115} = 69.56 \% \approx 70\%$$

#### T2 : Solution

Permissible tensile stress,

$$(\sigma_t)_{\max} = \frac{\sigma_y}{N} = \frac{380}{2.5} = 152 \text{ MPa}$$

$$\text{Stiffness in the bolt, } K_b = \frac{W}{\delta} = \frac{AE}{L} = \left(\frac{\pi d^2}{4}\right) \frac{E}{L} = \frac{\pi d^2}{4} \times \frac{207000}{100}$$
$$= 1625.77 d^2 \text{ N/mm}$$

The area  $A_c$  of the two plates (which is in compression),

$$A_c = \frac{\pi}{4}(2d)^2 - \frac{\pi}{4}d^2 = 2.356 d^2$$

Combined stiffness of the two plates

$$K_c = \frac{A_c E_c}{L} = \frac{2.356 d^2 \times 71000}{100} = 1672.9 d^2 \text{ N/mm}$$

$$\Delta P = P \left[ \frac{K_b}{K_b + K_c} \right] = 20 \times 10^3 \left[ \frac{1625.77 d^2}{1625.77 d^2 + 1672.9 d^2} \right]$$
$$= 9857.12 \text{ N}$$

Resultant load on bolt

$$P_b = P_i + \Delta P = 10000 + 9857.12 = 19857.12 \text{ N}$$

$$(\sigma_t)_{\max} = \frac{P_b}{A}$$

$$152 = \frac{19857.12}{\frac{\pi}{4} d_c^2}$$

⇒

$$d_c = 12.897 \text{ mm}$$

$$d = \frac{d_c}{0.8} = 16.12125 \text{ mm}$$

Corresponding bolt is M 20.

**T3 : Solution**

Area of two welds,

$$A = 2(100 \times t) = (200 t) \text{ mm}^2$$

Primary shear stress

$$\tau_1 = \frac{P}{A} = \frac{20 \times 10^3}{200t} = \left( \frac{100}{t} \right) \text{ MPa}$$

Moment of inertia of two welds,

$$I = 2 I_{xx}$$

$$I_{xx} = \frac{100t^3}{12} + Ay_1^2 = \frac{100t^3}{12} + (100t)(100)^2 \text{ mm}^4$$

Since dimension  $t$  is very small compared with 100, so term  $t^3$  can be neglected.

Therefore,

$$I_{xx} = (100^3 t) \text{ mm}^4$$

$$I = 2I_{xx} = t \times \left( \frac{bd^2}{2} \right) = t \times \left( \frac{100 \times 200^2}{2} \right) = 2 \times 10^6 t \text{ mm}^4$$

Bending stress in the top weld

$$= 2 \times (10^6 t) \text{ mm}^4$$

$$\sigma_b = \frac{M_b y}{I} = \frac{(20 \times 10^3 \times 200) \times 100}{2 \times 10^6 t} = \frac{200}{t} \text{ MPa}$$

Maximum shear stress

$$\tau = \sqrt{\left( \frac{\sigma_b}{2} \right)^2 + \tau_1^2} = \sqrt{\left( \frac{200}{2t} \right)^2 + \left( \frac{100}{t} \right)^2}$$

⇒

$$\tau = \frac{141.42}{t} \text{ MPa}$$

⇒

$$100 = \frac{141.42}{t}$$

⇒

$$t = 1.4142 \text{ mm}$$

⇒

$$h = \frac{t}{0.707} = 2 \text{ mm}$$



# 3

## Bearings



### Detailed Explanation of Try Yourself Questions

#### T1 : Solution

Life of bearing in millions of revolutions

$$= \left(\frac{C}{W}\right)^3 = \left(\frac{35}{45}\right)^3 = 0.4705$$
$$L = 60 NL_H$$

$$\Rightarrow \text{Life in hours, } L_H = \frac{L}{60N} = \frac{0.4705 \times 10^6}{60 \times 1800} = 4.356 \text{ hrs}$$

This the life expected for 90% of the bearings.

The average life expectancy is 5 times of the above life.

i.e. Average life =  $5 \times 4.356 = 21.78 \text{ hrs}$

#### T2 : Solution

Heat generated,  $H_g = \mu VW = 0.003 \times 30 \times 10^3 \times \frac{\pi \times 0.1 \times 1200}{60} = 565.5 \text{ watts}$

Heat dissipation rate =  $96 \text{ J/m}^2/\text{sec.}/^\circ\text{C}$

$$= 96 \times \left[ \frac{100}{1000} \times \frac{100}{1000} \times 20 \right] \text{ J/sec/}^\circ\text{C} = 19.2 \text{ J/sec/}^\circ\text{C}$$

Heat dissipated,  $H_d = 19.2 \times \Delta t \text{ J/sec.}$

Equating,  $H_g = H_d$

$$\Rightarrow 565.5 = 19.2 \Delta t$$

$$\Rightarrow \Delta t = 29.45^\circ\text{C}$$

Surface temperature =  $29.45 + \text{room temperature}$

$$= 29.45 + 35 = 64.45^\circ\text{C}$$

**T3 : Solution**

$$L = 60 NL_H = 60 \times 900 \times 2000 = 108 \times 10^6 \text{ revolutions}$$

$$L = \left(\frac{C}{W}\right)^3 \times 10^6$$

$$108 \times 10^6 = \left(\frac{C}{2.0}\right)^3 \times 10^6$$

$$C = 9.5 \text{ kN} = 9500 \text{ N}$$

∴ 6204 bearing is suitable

**T4 : Solution**

Given,  $W = 6 \text{ kN} = 6000 \text{ N}$ ,  $N = 1500 \text{ rpm}$ ,  $D = 0.05 \text{ m}$ ,  $L = 0.05 \text{ m}$ ,  $S = 0.121$ ,  $C = 50 \times 10^{-6} \text{ m}$

$$P = \frac{W}{LD} = \frac{6000}{50 \times 10^{-3} \times 50 \times 10^{-3}} = 2.4 \times 10^6 \text{ Pa}$$

Sommerfeld number,

$$S = \left(\frac{D}{C}\right)^2 \times \frac{ZN}{P}$$

⇒

$$0.121 = \left(\frac{50 \times 10^{-3}}{50 \times 10^{-6}}\right)^2 \times \frac{Z \times 1500}{60 \times 2.4 \times 10^6}$$

⇒

$$Z = 0.011616 \text{ Ns/m}^2 = 0.11616 \text{ Poise} = 11.62 \text{ cP}$$



# 4

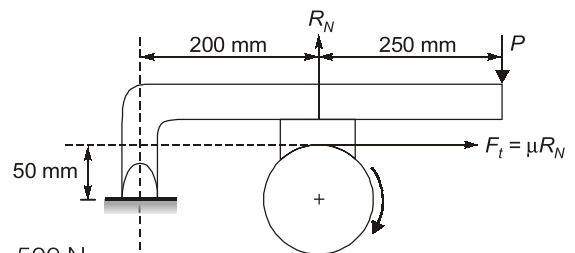
## Brakes



### Detailed Explanation of Try Yourself Questions

#### T1 : Solution

$$\begin{aligned}
 D &= 300 \text{ mm} = 0.3 \text{ m} \\
 T &= 75 \text{ N-m} \\
 T &= F_t \times r = \mu R_N \times r \\
 \Rightarrow 75 &= 0.35 \times R_N \times 0.15 \\
 \Rightarrow R_N &= 1428.57 \text{ N} \\
 F_T &= \mu R_N = 0.35 \times 1428.57 = 500 \text{ N} \\
 P \times (250 + 200) + F_T \times 50 &= R_N \times 200 \\
 \Rightarrow P \times 450 + 500 \times 50 &= 1428.57 \times 200 \\
 \Rightarrow P &= 579.365 \text{ N}
 \end{aligned}$$



#### T2 : Solution

Tension ratio,

$$\frac{T_1}{T_2} = e^{\mu\theta}$$

$$= e^{\frac{\pi \times 270}{180} \times 0.2} = 2.566 \quad \dots(i)$$

Torque equation

$$T = (T_1 - T_2)$$

$$\Rightarrow \frac{P \times 60}{2\pi N} = T_1 - T_2$$

$$\Rightarrow \frac{30 \times 10^3 \times 60}{2\pi \times 400} = (T_1 - T_2) \times r \quad \Rightarrow r = 1 \text{ m}$$

$$\Rightarrow (T_1 - T_2) = 716.197 \text{ N} \quad \dots(ii)$$

From Eq (i) and (ii) we get

$$T_1 = 1173.54 \text{ N}$$

$$T_2 = 457.34$$

So, maximum tension =  $T_1 = 1173.54 \text{ N}$



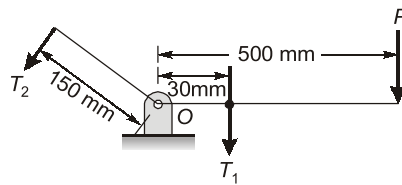
**T3 : Solution**

Drum diameter = 850 mm  
 Thickness of block = 75 mm  
 $\mu = 0.4$

$$\frac{T_1}{T_2} = \left( \frac{1 + \mu \tan 7.5^\circ}{1 - \mu \tan 7.5^\circ} \right)^{12}$$

$$\frac{T_1}{T_2} = \left( \frac{1 + 0.4 \tan 7.5^\circ}{1 - 0.4 \tan 7.5^\circ} \right)^{12}$$

$$\frac{T_1}{T_2} = 3.5432$$



By taking moment about 'O'

$$P \times 500 + T_1 \times 30 = T_2 \times 150$$

$$P \times 500 + 3.5432 \times 30 T_2 = T_2 \times 150$$

$$P \times 500 = 43.704 T_2$$

Power absorbed by blocks

$$P = (T_1 - T_2) \omega \times \frac{d}{2}$$

$$d = 850 + 2 \times 75 = 1000$$

$$225 \times 10^3 \times 10^3 = (T_2 \times 3.5432 - T_2) \times \frac{2\pi \times 240}{60} \times \frac{1000}{2}$$

$$T_2 = 7040.27 \text{ N}$$

$$P \times 500 = 43.704 \times 7040.27$$

$$P = 615.35 \text{ N}$$



# 5

## Friction Clutches



### Detailed Explanation of Try Yourself Questions

#### T1 : Solution

Pressure variation for uniform wear is given by

$$P = \frac{W}{2\pi(r_0 - r_i)r}$$

Maximum pressure occurs at smallest radius,

$$P_{\max} = \frac{W}{2\pi(r_0 - r_i)r_i} = \frac{8000}{2\pi(0.2 - 0.1)0.1} = 127323.9 \text{ N/m}^2 \\ = 127.3 \text{ kN/m}^2$$

Minimum pressure occurs at largest radius,

$$P_{\min} = \frac{W}{2\pi(r_0 - r_i)r_0} = \frac{8000}{2\pi(0.2 - 0.1)0.2} = 63.66 \text{ kN/m}^2$$

#### T2 : Solution

Design torque,

$$T = 2 \times 50 = 100 \text{ N-m}$$

For uniform wear conditions, pressure variation is given by

$$P = \frac{C}{r} = \frac{W}{2\pi(r_0 - r_i)r}$$

Maximum pressure occurs at inner radius i.e. at  $r = r_i$

So, 
$$P_{\max} = \frac{W}{2\pi(r_0 - r_i)r_i}$$

$$\Rightarrow 1 \times 10^6 = \frac{W}{2\pi\left(\frac{0.1}{2} - \frac{0.065}{2}\right) \times \frac{0.065}{2}}$$

$$\Rightarrow W = 3573.56 \text{ N} \\ T = \mu WR_m \cdot n$$

$$100 = 0.08 \times 3573.56 \times \left( \frac{\frac{0.1}{2} + \frac{0.065}{2}}{2} \right) \times n$$

⇒

$$n = 8.479 \approx 9 \text{ pair of contact surface}$$

Generally we take friction disk in such a way so that total number of contact pair are even, so answer should be 10.

**T3 : Solution**

$$P = T \cdot \omega$$

$$873.8 = T \times \frac{2\pi \times 900}{60}$$

$$T = 9.272$$

Also,

$$T = I \alpha$$

$$T = (mk^2) \alpha$$

$$9.272 = 14 \times (160)^2 \times \alpha$$

$$\alpha = 25.87 \text{ rad/se c}^2$$

Also,

$$\omega_F = \omega_i + \alpha t$$

$$t = \frac{2\pi \times 900}{60 \times 25.87} = 3.64 \text{ sec}$$

**T4 : Solution**

$$T = \frac{P \times 60}{2\pi N} = \frac{20 \times 10^3 \times 60}{2\pi \times 4000} = 47.746 = \mu WR_m$$

⇒

$$R_m = \frac{T}{\mu W}$$

⇒

$$\frac{2}{3} \left( \frac{r_0^3 - r_i^3}{r_0^2 - r_i^2} \right) = \frac{T}{\mu \times P \times \pi (r_0^2 - r_i^2)}$$

⇒

$$\begin{aligned} (r_0^3 - r_i^3) &= \frac{3T}{2\mu P\pi} \Rightarrow r_0^3 = r_i^3 + \frac{3T}{2\mu P\pi} \\ &= (50 \times 10^{-3})^3 + \frac{3 \times 47.746}{2 \times 0.3 \times 1.2 \times 10^6 \times \pi} \\ r_i &= 0.0395 \text{ m} = 39.5 \text{ mm} \end{aligned}$$

**T5 : Solution**

$$r_i = r_o - b \sin \alpha = 350 - 130 \sin 12.5 = 321.863 \text{ mm}$$

$$r_m = \frac{350 + 321.863}{2} = 335.93 \text{ mm}$$

Torque,

$$T = \frac{\mu W}{\sin \alpha} \times r_m$$

$$\begin{aligned} W &= \frac{T \sin \alpha}{\mu r_m} = \frac{400 \times 1000 \times 0.21644}{0.4 \times 335.93} \\ &= 644.298 \text{ N} \approx 644.3 \text{ N} \end{aligned}$$



# 6

## Gears



### Detailed Explanation of Try Yourself Questions

#### T1 : Solution

Wear strength,

$$\frac{N_p}{N_g} = 2 = \frac{T_g}{T_p}$$

$$S_w(\text{or}) P_w = kQwd_p$$
$$k = 1.5 \text{ N/mm}^2$$

$$Q = \frac{2T_g}{T_p + T_g} = \frac{2}{1 + \frac{T_p}{T_g}} = \frac{2}{1 + \frac{1}{2}} = \frac{4}{3}$$

Now,

$$w = 100 \text{ mm}$$

$$d_p = 400 \text{ mm}$$

$$P_w = kQwd_p$$

$$= 1.5 \times \frac{4}{3} \times 100 \times 400 = 80000 \text{ N} = 80 \text{ kN}$$

#### T2 : Solution

$$\phi = 20^\circ$$

$$\text{Power} = 20 \text{ kW} = 20 \times 10^3 \text{ W}$$

$$N_p = 300 \text{ rpm}$$

$$\text{Velocity ratio} = \frac{T_g}{T_p} = 3$$

$$\sigma_{OG} = 100 \text{ MPa} = 100 \times 10^6 \text{ N/m}^2$$
$$= 100 \text{ N/mm}^2$$

$$\sigma_{OP} = 120 \text{ MPa} = 120 \times 10^6 \text{ N/m}^2$$

$$T_P = 15$$

$$T_G = 3 T_P = 3 \times 15 = 45$$

$$b = 14 \text{ m}$$

$$\sigma_{es} = 600 \text{ MPa} = 600 \text{ N/mm}^2$$

$$E_p = 200 \text{ GPa} = 200 \times 10^3 \text{ N/mm}^2$$

$$E_s = 100 \text{ GPa} = 100 \times 10^3 \text{ N/mm}^2$$

Module:

let

$m$  = Module in mm and

$D_p$  = Pitch circle diameter of the pinion in mm

Pitch line velocity,

$$V = \frac{\pi D_p N_p}{60} = \frac{\pi m T_P N_p}{60} = \frac{\pi \times m \times 15 \times 300}{60}$$

$$= 0.235 \text{ m/s}$$

Assuming steady load condition and 8-10 hours of service per day, the service factor  $C_s$  is taken as 1, i.e.  $C_s = 1$ .

We know that the design tangential tooth load,

$$W_T = \frac{P}{V} \times C_s = \frac{20 \times 10^3}{0.235m} \times 1 = \frac{85.10 \times 10^3}{m} \text{ N}$$

and Velocity factor,

$$C_v = \frac{3}{3+v} = \frac{3}{3+0.235m}$$

Tooth form factor for pinion

$$y_p = 0.154 - \frac{0.912}{T_P} = 0.154 - \frac{0.912}{15} = 0.0932$$

And tooth form factor for gear

$$y_g = 0.154 - \frac{0.912}{T_g} = 0.154 - \frac{0.912}{45} = 0.133$$

$\therefore$

$$\sigma_{PO} \times y_p = 120 \times 0.0932 = 11.184$$

$$\sigma_{OG} \times y_G = 100 \times 0.133 = 13.3$$

Since  $(\sigma_{OP} \times y_p)$  is less than  $(\sigma_{OG} \times y_G)$  therefore the pinion is weaker. Now using the Lewis equation to the pinion, we have

$$W_T = \sigma_{wp} \times b \pi m y_p = \sigma_{OP} \times C_v b \pi m y_p \quad [\because \sigma_{wp} = \sigma_{OP} \times C_v]$$

$$\frac{85.1 \times 10^3}{m} = 120 \times \left( \frac{3}{3+0.235m} \right) \times (14m \times \pi m \times 0.0932)$$

$$\frac{85.1 \times 10^3}{m} = \frac{1475.69}{(3+0.235m)}$$

$$\Rightarrow \frac{57.66}{m} = \frac{m^2}{3+0.235m} = 172.98 + 13.55 m = m^3$$

$$\Rightarrow m^3 - 13.55 m - 172.98 = 0$$

$$m = 6.37 \text{ mm} \approx 7 \text{ mm}$$

Face width:

$$b = 14 m = 14 \times 7 = 98 \text{ mm}$$

Pitch diameter of gears,

$$D_p = m T_P = 7 \times 15 = 105 \text{ mm}$$

$$D_g = m T_g = 7 \times 45 = 315 \text{ mm}$$

Checking the gears for wear:-

Ratio factor,

$$Q = \frac{2 \times VR}{VR + 1} = \frac{2 \times 3}{3 + 1} = 1.5$$

Load stress factor =  $\frac{(\sigma_{es})^2 \sin \phi}{1.4} \left[ \frac{1}{E_p} + \frac{1}{E_g} \right]$

$$= \frac{600^2 \times \sin 20^\circ}{1.4} \left[ \frac{1}{200 \times 10^3} + \frac{1}{100 \times 10^3} \right]$$

$$= 1.3192 \text{ N/mm}^2$$

The maximum or limiting load for wear

$$W_w = D_p \times b Q K$$

$$= 105 \times 98 \times 1.5 \times 1.319$$

$$= 20358.765 \text{ N} = 20.358 \text{ kN}$$

Tangential load on tooth,

$$W_T = \frac{85.1 \times 10^3}{m} = \frac{85.1 \times 10^3}{7}$$

$$= 12157 \text{ N} = 12.157 \text{ kN}$$

Since maximum wear load (20.358 kN) is more than the tangential load (12.157 kN) on the tooth, the design is satisfactory from the wear point of view.



# 7

## Shaft



### Detailed Explanation of Try Yourself Questions

#### T1 : Solution

$$T = 50 \text{ Nm}$$

$$\tau = 140 \text{ MPa} \quad N = 2$$

$$\tau_{\text{permissible}} = \frac{140}{N} = 70 \text{ MPa}$$

$\therefore$

$$\tau_{\text{per}} = \frac{16T}{\pi d^3}$$

$$d \geq \left( \frac{16T}{\pi \tau_{\text{per}}} \right)^{1/3}$$

$$d \geq \left( \frac{16 \times 50}{\pi \times 70 \times 10^6} \right)^{1/3}$$

$$d \geq 0.015379 \text{ m}$$

$$d \geq 15.379 \text{ mm}$$

$$d \approx 16 \text{ mm}$$

#### T2 : Solution

Given;

Torsional rigidity,

$$d_s = 100 \text{ mm}, \quad d_o = 2 d_i; \quad G_s = G_h, \quad \tau_s = \tau_h, \quad L_s = L_h$$

$$k = \frac{T}{\theta} = \frac{GJ}{L}$$

$$k \propto J$$

(As per given data)

$$J_s = \frac{\pi d_s^4}{32}$$

$$J_h = \frac{\pi}{32} (d_o^4 - d_i^4) = \frac{\pi}{32} d_o^4 \left[ 1 - \left( \frac{1}{2} \right)^4 \right] = \frac{15}{16} \times \frac{\pi}{32} d_o^4$$

and

$$\tau_s = \frac{16T}{\pi d_s^3}$$

$$\tau_h = \frac{16T}{\pi d_o^3 \times 15/16} = \frac{256T}{15 \times \pi d_o^3}$$

∴

$$\tau_s = \tau_h \quad (\text{as given})$$

or

$$\frac{16T}{\pi d_s^3} = \frac{256T}{15 \times \pi d_o^3}$$

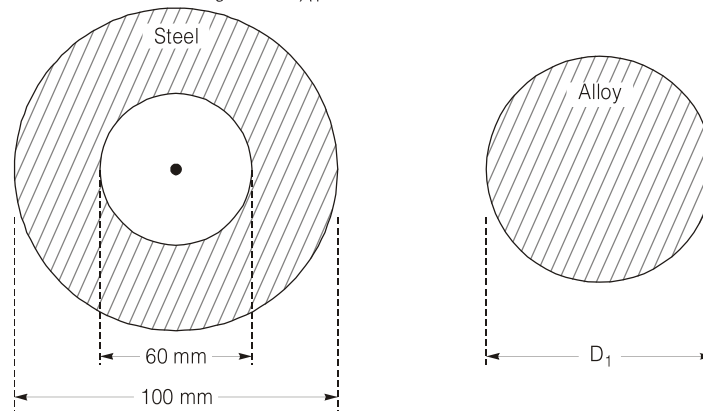
or

$$d_o^3 = d_s^3 \left( \frac{16}{15} \right)$$

⇒

$$d_o = \left( \frac{16}{15} \right)^{1/3} \times d_s = 1.0217 \times 100 = 102.175 \text{ mm}$$

$$\frac{k_s}{k_h} = \frac{J_s}{J_h} = \left( \frac{d_s}{d_o} \right)^4 \times \frac{16}{15} = \left( \frac{100}{102.17} \right)^4 \times \frac{16}{15} = 0.9787$$

**T3 : Solution**Given,  $d = 60 \text{ mm}$ ,  $D = 100 \text{ mm}$ ,  $G_s = 2 G_{A1}$ 

$$(Z_p)_{\text{Hollow shaft}} = \frac{J_{\text{Hollow}}}{D/2} = \frac{\pi (D^4 - d^4)}{16 D}$$

$$(Z_p)_{\text{Solid shaft}} = \frac{J_{\text{solid}}}{D_1/2} = \frac{\pi D_1^3}{16}$$

From the given condition,

$$\frac{D^4 - d^4}{D} = D_1^3$$

∴

$$D_1^3 = \frac{100^4 - 60^4}{100}$$

⇒

$$D_1 = 95.4786 \text{ mm} \approx 95.5 \text{ mm} \quad \text{Ans.}$$

Ratio of torsional rigidity

$$= \frac{(GJ)_{\text{Steel}}}{(GJ)_{\text{Alloy}}} = 2 \frac{J_{\text{Steel}}}{J_{\text{Alloy}}} \quad \text{Assume } L \text{ same for both}$$

or

$$\text{Ratio} = \frac{2(D^4 - d^4)}{D_1^3 \cdot D} = \frac{2(100^4 - 60^4)}{100 \times (95.4)^3} = 2.005 \approx 2 \quad \text{Ans.}$$

